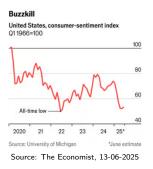
Subjective expectations in life-cycle models

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History of subjective expectations (Bruine de Bruin et al., 2023)



1940s: University of Michigan's Surveys of Consumers and Survey of Consumer Finances by George Katona and others

- Idea: past behavior not always good guide for future
- Subjective expectations incorporated in aggregate measures relevant for research and policy

Why measure subjective expectations?

Household expectations valuable to (Katona and Klein, 1952; Manski, 2004)

- Predict choices
- Understand how those choices are made (preferences, expectations, constraints)
- Understand formation of expectations

Economic theory models decision making based on **probabilistic expectations** (Manski, 2004)

- Inter-personal comparability
- Internal (logical) consistency
- Different moments (location, dispersion)

Popularity grew since early 1990s

Empirical evidence in favor of subjective expectations

- Survival expectations predict actual survival (Hurd and McGarry, 2002)
- Adolescents' expectation of life events predict those events (Fischhoff et al., 2000)

Additional drivers

- Subjective measures (e.g., Michigan Survey of Consumers) predict changes in consumption and inflation (Carroll et al., 1994; Ludvigson, 2004; Ang et al., 2007)
- Doubts about rationality of expectations (Tversky and Kahneman, 1974)

Currently many (most?) major household surveys include expectations questions

• 6 in U.S., multiple in Europe (U.K.) and Canada

Roadmap

- Introduction
- 2 Life-cycle models
- 3 Literature overview
- Measurement models
- 6 Heterogeneous survival expectations in a life-cycle model (de Bresser, 2024)

Life-cycle models

Decisions with long-term consequences

- Saving and retirement
- Health investments
- Education, marriage, ...

Applications

- Understand observed behavior (why save?)
- Predict behavior under counterfactual institutions (pension reform)

Basic ingredients

- Choices
- Preferences
- Expectations (Manski, 2004; Koşar and O'Dea, 2023)
 - States of nature (health, survival, wage)
 - Future choices
- Budget constraint (institutions)

A sketch of a life-cycle model (based on Koşar and O'Dea, 2023, and

Van der Klaauw and Wolpin, 2008)

Structure: discrete time (age) t in years, certain death at age T

Choices

- Consumption c_t (continuous)
- Labor supply h_t (discrete, up to age T^R)

Utility function (consumption c_t and leisure l_t)

$$U\left(c_{t}, I_{t}\right) = \frac{\left(c_{t}^{\nu} I_{t}^{1-\nu}\right)^{1-\gamma}}{1-\gamma}$$

Budget constraint

$$\begin{cases} a_{t+1} &= \left(a_t + y_t \mathbb{1}\left\{h_t = 1\right\} - c_t\right) \left(1 + r\right) \text{ if } t < T^R\\ a_{t+1} &= \left(a_t + \kappa \times \text{pension}\left(\mathbf{h}_{T^R}, \mathbf{y}_{T^R}\right) - c_t\right) \left(1 + r\right) \text{ if } t \geq T^R\\ l_t &= 1 - \eta \mathbb{1}\left\{h_t = 1\right\} \end{cases}$$

A sketch of a life-cycle model (based on Koşar and O'Dea, 2023, and

Van der Klaauw and Wolpin, 2008)

Risk (expectations)

- Personal or demographic states: longevity
- Features of economic environment: wage y_t
- Future policy: pension $(\mathbf{h}_{T^R}, \mathbf{y}_{T^R})$

E.g., $s_{i,t+1}$ is one-year survival probability conditional on survival to age t

Recursive specification

$$V_{t}\left(\chi_{t}\right) = \max_{c_{t},h_{t}} U\left(c_{t},I_{t}\right) + \beta s_{i,t+1} \mathbb{E}_{i,t}\left[V_{t+1}\left(\chi_{t+1}\right)\right]$$

subject to the budget constraint

state
$$\chi_t = \{a_t, \mathbf{y}_t, \mathbf{h}_t\}; \ \mathbf{y}_t = (y_1, ..., y_t)$$

Solving the model

Collect unknown model features in heta

• Preference parameters $\{\beta,\gamma,\nu\}$, expectations κ

If θ were known: backward induction to obtain decision rules

$$\widetilde{c}_t\left(\chi_t,\boldsymbol{\theta}\right) \qquad \widetilde{h}_t\left(\chi_t,\boldsymbol{\theta}\right)$$

Model solution implies trajectories of choices and of **expectations of future choices**

$$\mathbb{P}\left[\widetilde{h}_{t+\tau} = 1 | t; \chi_t, \theta\right] \qquad \mathbb{P}\left[\widetilde{a}_{t+\tau} > a | t; \chi_t, \theta\right]$$

Identification: different θ lead to different distributions of observables under the model

- Binary property of model + joint distribution of observables
- More data allow less restrictive model

Estimation

Step 1: Estimate processes outside the model if possible (exogenous)

- ullet All objects that do not depend on decision rules \widetilde{c}_t and \widetilde{h}_t
- E.g., interest rate r

Step 2: Estimate remaining unknown model features in θ by matching model implications to observed data

- Preference parameters $\{\beta, \gamma, \nu\}$ and endogenous aspects of expectations (formation, learning)
- Maximum Likelihood or Method of Moments

Rational expectations

Rational expectations: expectations equal to our estimates

$$s_{i,t+1}\mathbb{E}_{i,t}\left[V_{t+1}|\chi_{t}\right] = \widehat{s}_{t+1}\widehat{\mathbb{E}}_{t}\left[V_{t+1}|\chi_{t}\right] \ \forall i$$

e.g., $s_{i,t+1} = \text{actuarial forecast}$

Requires only data on choices and state variables

Expectations equal estimated processes for state variables

Good approximation if

- Decision makers have the same information as econometrician
- Decision makers process that information as econometrician (inference)

Subjective expectations

Subjective expectations

$$s_{i,t+1}\mathbb{E}_{i,t}\left[V_{t+1}|\chi_t\right] = \widetilde{s}_{i,t+1}\widetilde{\mathbb{E}}_{i,t}\left[V_{t+1}|\chi_t\right]$$

 $\widetilde{s}_{i,t+1}$ and/or $\widetilde{\mathbb{E}}_{i,t}\left[V_{t+1}|\chi_{t}
ight]$ are based on survey data from individual i

Good approximation if

- We know how respondent *i* understands the survey questions
 - ▶ Tries to report $s_{i,t+1}$ (meta-data: time stamps, self-evaluations)
- We know how respondent *i* uses the response format
 - ▶ Transformation $s_{i,t+1} \rightarrow \widetilde{s}_{i,t+1}$ (peculiarities in responses)
- Face/construct/predictive validity

Best practice in survey design (Bruine de Bruin et al., 2023, see also Dillman, 2011; Bergman et al., 2020):

- Cognitive interviews
- Simple language

Subjective vs rational expectations

More data allow less restrictive model

- Identification problem: observed choices compatible with multiple combinations of preferences and expectations (Manski et al., 1991; Manski, 2004)
- Observing expectations directly allows greater flexibility:
 "...it is enough to assume that elicited expectations faithfully describe persons' perceptions of their environments"
 - Manski (2004)
 - Expectations may not follow observed realization of states
 - Processes may be non-stationary
 - Level and heterogeneity
 - Important question of measurement
- More data, not degrees of freedom

Expectation formation in status quo and in counterfactual

Considerations for survey design

Probabilistic survey items that elicit direct analogues of model objects

- Inter-personal comparability (Manski, 2004; Bruine de Bruin et al., 2023)
- Choice probabilities are more informative than discrete choice (Manski, 1999)
 - ▶ Resolvable uncertainty in stated preferences for incomplete scenarios
 - Ranking of alternatives

Example: three questions on future pension claiming

- "Agreement with the following statement: I will collect pension benefits by age 65.
 - 1. completely agree, ..., 5. completely disagree"
- "At what age do you expect to start collecting pension benefits? ... years old"
- (a) "What is the chance that you will collect pension benefits by age 65? 0, ..., 100%"

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Two types of subjective expectations (Manski, 2004)

Over states of nature

- Economic/policy environment
 - ▶ Replacement rate income at retirement
 - Income (wage) next year
- Personal characteristics
 - Survival: "What is the percent chance that you will live to be age 75 or more?"

Over choices

- Labor supply: "What are the chances that you will be working full-time after you reach age 62?"
- Bequests: "Including property and other valuables, what are the changes that you (and your [partner]) will leave an inheritance totaling \$10,000 or more?"

Subjective expectations in life-cycle models: states of the nature

Expectation formation not modeled

- Survival
 - Saving and bequests: Gan et al. (2015), Bissonnette et al. (2017), Heimer et al. (2019), de Bresser (2024)
 - ► Annuity demand: O'Dea and Sturrock (2023), Pang (2025)
 - Annuity supply: Hosseini (2015)
- Income shocks: Pistaferri (2001), Attanasio et al. (2020), Arellano et al. (2024)
- Policy environment: Van der Klaauw and Wolpin (2008)

Models with expectation formation

- Survival: Groneck et al. (2016), Caliendo et al. (2020)
- Pension entitlements: Hentall-MacCuish (2019)

Subjective expectations in life-cycle models: choice expectations I

Features

- Actual choices not available (e.g., life-care annuities in NL)
- Conditional choices allow fully specified economic environment that maps into model
 - Choice set and characteristics
- Identification through experimental variation in attributes (e.g., price)
- Combination with actual choices: estimation efficiency or validation

Unconditional choice expectations (large HH surveys)

$$\widetilde{\mathbb{P}}_i\left(\widetilde{h}_{i,t+ au}=1
ight)$$

- Expected behavior given current information set of respondent
- Labor supply/retirement: Wolpin and Gonul (1985), Van der Klaauw and Wolpin (2008)
- Bequests: McGee (2021), Erdenesuren (2023)

Subjective expectations in life-cycle models: choice expectations II

Conditional choice expectations (bespoke surveys)

$$\widetilde{\mathbb{P}}_{i}\left(\widetilde{h}_{i,t+\tau}=1|\chi_{t+\tau}=\chi_{t+\tau}^{j}\right)$$

- Expected behavior in hypothetical scenario(-s)
 - ▶ E.g., labor supply given health: Giustinelli and Shapiro (2024)
- Behavior in multiple states of the world: no selection
- Conditions that may never prevail
- Multiple scenarios create within-individual variation

Examples (discrete and/or probabilistic)

- Retirement: Van Soest and Vonkova (2014), Ameriks et al. (2020)
- Long-term care insurance: Boyer et al. (2020), Michaud and St. Amour (2023)

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Complications of working with subjective expectations

Complex mapping expectations \rightarrow survey reports

- Logically inconsistent probabilities (monotonicity)
- Choice probabilities inconsistent with our model (recall error)
- Reported probabilities a-priori implausible (e.g., 100% certain to survive past future age)

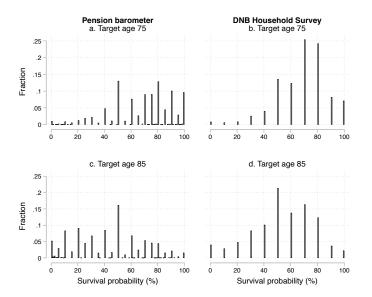
Rounding

- Bunching of reported probabilities at multiples of 10%
- Latent construct (40% multiple of 1 and 10)
- Survey-induced or not (scale 0-10 or 0-100%)

Focal answers

- Excess bunching at 0, 50, 100%
- Epistemic uncertainty rather than subjective risk (Fischhoff and Bruine De Bruin, 1999; De Bruin et al., 2000)

Example: bunching in survival probabilities



Stated probability to live to age 75/85 (de Bresser, 2019)

How to model subjective expectations?

Partial identification (Manski and Molinari, 2010; Bissonnette and de Bresser, 2018)

- For continuous variable: limited number of grid points
- Rounding:
 - Inferred from all reported probabilities
 - Inferred from probabilities one-by-one (worst case)

Non-linear least squares and spline interpolation (Dominitz and Manski, 1997; Bellemare et al., 2012)

- NLLS with suitable distribution (log-normal for income)
- Linear or higher order splines

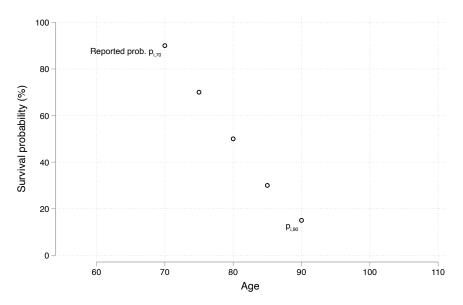
Parametric mixing model (Kleinjans and Soest, 2014; de Bresser, 2019, 2024)

- Handles both focal answers and rounding
- Conditional means provide partial pooling for individual-specific parameters

Classification different modeling approaches

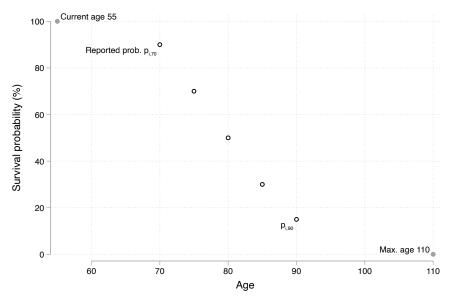
	Point identification	Partial identification
Expectations constructed individual-by-individual	Parametric distr. by NLLS Spline interpolation	No rounding, no smoothing Rounding, no smoothing Rounding, smoothing
Partial pooling of expectations	Parametric mixing model	

Different modeling approaches – data for respondent i

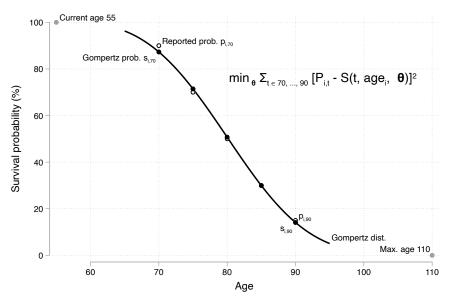


100 ¬ Current age 55

One-by-one expectations – partial identification



One-by-one expectations – point identification



100 7 Current age 55 26 / 58

Partial pooling - parametric mixing model I

Data (DNB Household Survey):

"Please indicate your answer on a scale of 0 thru 10, where 0 means 'no chance at all' and 10 means 'absolutely certain'.

How likely is it that you will attain (at least) the age of [65]?"

- Answers can be interpreted as probabilities (de Bresser, 2019)
- Rounding enforced by response scale

Model:

- Expectations follow Gompertz distribution
- Common baseline hazard, multiplied by health and individual effects
- Ordinal rounding model
- Conditional means for individual effects capture variation in expectations

Partial pooling - parametric mixing model II

True expectations follow Gompertz distribution:

$$S_{i,t_{i}+\tau_{k}} = \mathbb{P}\left(T \geq t_{i} + \tau_{k} | T \geq t_{i}\right) = g\left(t_{i}, \tau_{k}; \gamma_{i}, \alpha\right)$$
$$\gamma_{i} = \exp\left(\mathbf{x}_{i}'\boldsymbol{\beta} + \zeta_{i} + \eta_{it}\right); \zeta_{i} \sim \mathcal{N}\left(0, \sigma_{\zeta}^{2}\right), \eta_{it} \sim \mathcal{N}\left(0, \sigma_{\eta}^{2}\right)$$

 $S_{i,t_i+ au_k}$ for individual i with age t_i , target age $t_i+ au_k$

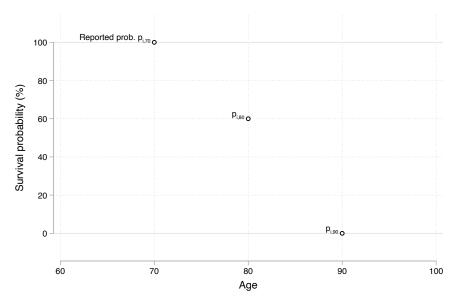
Two steps from true $S_{i,t_i+\tau_k}$ to reported $P_{i,t_i+\tau_k}$:

1. Add recall error $\varepsilon_{i,t_i+\tau_k}$

$$P_{i,t_i+\tau_k}^* = S_{i,t_i+\tau_k} + \varepsilon_{i,t_i+\tau_k} ; \varepsilon_{i,t_i+\tau_k} \sim \mathcal{N}\left(0,\sigma_i^2\right)$$

2. $P_{i,t_i+ au_k}^*$ rounded (10, 50, 100) and censored between 0 and min $\left[100,P_{i,t_i+ au_{k-1}}\right]$

Partial pooling - parametric mixing model III

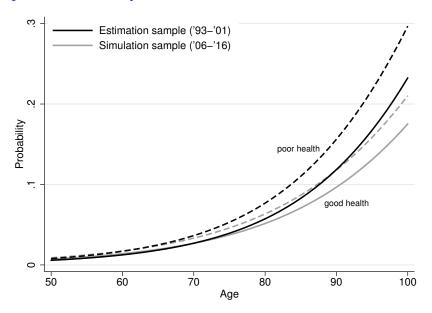


Parameter estimates for subjective survival

	a. Pre-reform (1993-2001)			b. Post-reform (2006-2016)				
Poor health Educ. middle ^a Educ high ^a Constant	Expectations – hazard rates		Heteroskedasticity recall error		Expectations – hazard rates		Heteroskedasticity recall error	
	1.363*** 1.005 1.058 0.00875***	(0.0443) (0.0423) (0.0423) (6.56e-4)	0.00979 -0.161*** -0.162*** 2.355***	(0.0509) (0.0536) (0.0456) (0.0391)	1.244*** 0.927*** 1.104*** 0.0185***	(0.0187) (0.0249) (0.0320) (4.01e-4)	0.155*** -0.133*** -0.0993*** 2.485***	(0.0201) (0.0215) (0.0192) (0.0161)
$\begin{aligned} & Var\left[\zeta_{i}\right] \text{ (ind. effects)} \\ & Var\left[\eta_{it}\right] \text{ (seq. effects)} \\ & Var\left[\zeta_{i}\right] / Var\left[\zeta_{i}\right] + Var\left[\eta_{it}\right] \end{aligned}$	0.406*** 0.0626*** 0.866***	(0.0181) (0.00476) (0.0103)			0.503*** 0.0203*** 0.961***	(0.0687) (0.00159) (0.00606)		
Baseline hazard	7.788***	(0.100)			6.693***	(0.0280)		
	Rounding				Rounding			
μ_1 μ_2	1.461*** 3.326***	(0.0895) (0.179)			2.478*** 3.996***	(0.110) (0.141)		
$\begin{array}{l} Var\left[\zeta_i^r\right] \text{ (ind. effects)} \\ Var\left[\eta_{it}^r\right] \text{ (seq. effects)} \\ Var\left[\zeta_i^r\right]/Var\left[\zeta_i^r\right] + Var\left[\eta_{it}^r\right] \end{array}$	0.821*** 0.114 0.878***	(0.184) (0.0917) (0.0883)			2.729*** 0.00863 0.997***	(0.320) (0.00962) (0.00348)		
$\begin{array}{l} Corr\left[\zeta_{i};\zeta_{i}^{r}\right] \\ Corr\left[\eta_{it};\eta_{it}^{r}\right] \end{array}$	0.0909 0.264	(0.0740) (0.231)			0.149*** -0.397	(0.0438) (0.488)		
Number of individuals Number of probabilities Log-likelihood	1,371 4,858 -8,393.77				1,557 15,789 -25,947.56			

^a Baseline: low education level (lower secondary education). Educ. middle: intermediate vocational. Educ. high: (applied) university. Standard errors in parentheses. ***p < 0.01, **p < 0.05, *p < 0.1

Subjective mortality estimates – level



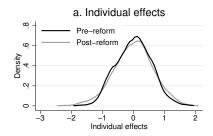
Individual-level coefficients: conditional means

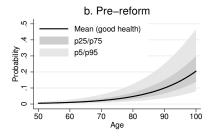
Mixing distribution: distribution of subjective survival in population

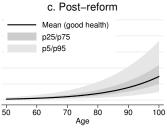
Conditional means: approximations of individual-specific subjective survival

- Mixing distribution (prior) + probabilities reported by individual $i \Rightarrow$ posterior distribution for individual and sequence effect i
- ullet Means of posterior distributions as approximation of ζ_i and η_{it}

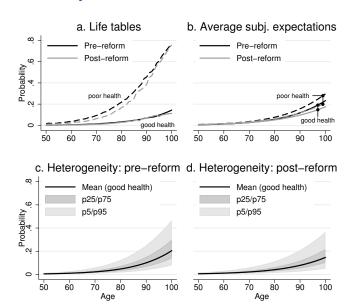
Conditional means of unobserved heterogeneity







Different mortality estimates – levels and variation



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- Introduction
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Can subjective survival expectations improve performance of structural retirement model? (de Bresser, 2024)

Population aging necessitates pension reform

In the Netherlands:

- Statutory retirement age public pension increases with life expectancy
- Occupational pensions are adjusted for claiming age

Long-running panels allow validation of counterfactual predictions

Can subjective survival expectations improve performance of structural retirement model? (de Bresser, 2024)

Different combinations of preferences and expectations may...

- ... imply similar retirement in one policy regime
- ... yet different retirement in counterfactual regime

Three types of survival expectations

- Rational expectations (life tables)
- Average subjective survival
- 4 Heterogeneous subjective survival

Measurement model of subjective survival

• Heterogeneity captured through single parameter

Validation of counterfactual model predictions is important

Model outline

Unitary model for men aged 50-100 (yearly)

Choices: labor supply, consumption, claiming benefits (occ. pension, DI, UI) Details

Preferences: consumption, leisure, bequests

Risk: longevity, health, wage

Pre-reform pension regime (1993-2001) and post-reform regime (2006-2016)

Instantaneous utility from consumption and leisure

- CRRA utility
- Time costs of
 - Work (fixed cost) (French, 2005)
 - Poor health
 - Claiming DI or UI (stigma/lack of knowledge)

Utility from leaving **bequests** (French, 2005)

Weight allowed to depend on household size





Sources of income:

- Earnings
- Disability and unemployment benefits (up to age 65)
- Public pension (automatic at age 65)
- Occupational pension
 - Replacement rate of final earnings, function of years worked
- Exogenous income of spouse

Cash-on-hand = wealth + net income - medical expenditures

• Government transfers guarantee $c_{\min} = n_t \times 7,000$

Policy reform: actuarial adjustments to pensions **Perfect**



Pre-reform (1993-2001)

- Early retirement age 59-64; regular benefits afterwards
- Early retirement replacement rate 85%: no actuarial adjustment
- Continued accrual of pension entitlements while on early retirement
- Cohorts: born before 1950.

Post-reform (2006-2016)

- Unified system: claiming may start at any age from age 60
- Actuarial adjustments: benefits lowered by 6% per year for claiming before age 65; raised by 7% for delayed claiming
- No continued accrual of pension entitlements
- Cohorts: born from 1950 onwards

Estimation

Method of Simulated Moments estimation algorithm (French, 2005; De Nardi et al., 2010; French and Jones, 2011):

- Estimate all processes that do not require model (mortality etc.)
- Take initial conditions (state variables) from data
- Simulate life cycles for 5,000 workers
- Compare target moments and simulations (MM objective function)
- MSM estimator maximizes fit of simulations to data (simulated annealing)

Target moments: age profiles for

- Labor supply (hrs/participation) by health
- DI, UI and occ. pension claiming
- Quartiles of wealth

Data

Data taken from **DNB Household Survey (DHS)**

- Administered by CentERdata at Tilburg University
- 5,000 individuals in 3,000 households
- Sampled from address registry

Sample selection:

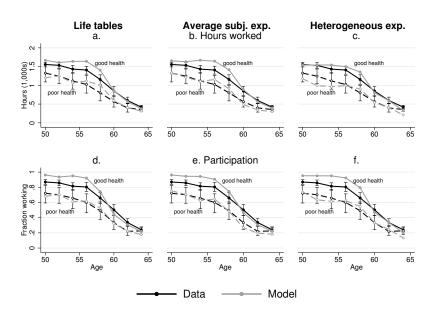
- Auxiliary processes
 - ▶ Men aged 50+ during relevant waves (1993-2001 and 2006-2016)
- Target moments
 - ► Sample for auxiliary processes, but never self-employed; 15+ years work experience; relevant cohort (before 1950/1950 and later)

Parameter estimates

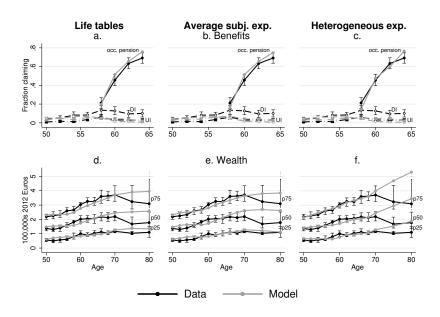
	(1)	(2)	(3)
	Life tables	Average subj. exp.	Heterogeneous exp
Utility function			
Concavity (σ)	4.64	4.64	5.18
	(0.000023)	(0.000028)	(0.000038)
Consumption weight (κ)	0.68	0.65	0.42
	(0.000061)	(0.000063)	(0.000065)
Discount factor (β)	1.04	1.04	0.98
	(0.000026)	(0.000035)	(0.000028)
Fixed cost of work; hrs/yr (γ)	1085	1013	1101
. ,, (,,	(27.5)	(4.5)	(8.0)
Time cost of bad health; hrs/yr (δ)	131	249	251
, ,,,	(13.9)	(34.6)	(6.9)
Stigma cost DI; hrs/yr (ϕ)	1681	2029	2140
	(441.9)	(345.5)	(145.4)
Stigma cost UI; hrs/yr (ξ)	3620	3509	3568
	(8.9)	(1.9)	(5.9)
Bequests			
Intercept bequest weight (θ_0)	-2.45	-3.91	-9.27
	(0.00014)	(0.00015)	(0.00010)
Slope bequest weight (θ_1)	4.73	5.56	2.51
	(0.00012)	(0.00014)	(0.000082)
Concavity bequests (K)	675,282	913,915	441,061
	(29.0)	(34.3)	(6.0)
Function value	473.27	473.21	483.89

a $u\left(c_{t}, l_{t}\right) = \frac{n_{t}}{1-\sigma}\left[\left(\frac{c_{t}}{n_{t}}\right)^{\kappa} l_{t}^{1-\kappa}\right]^{1-\sigma} - 1\right]; \ b\left(w_{t}, n_{t}\right) = \exp\left[\theta_{0} + \theta_{1} n_{t}\right] \times \frac{\left(w_{t} + K\right)^{\left(1-\sigma\right)\kappa}}{1-\sigma} \\ l_{t} = 4,000 - h_{t} - \gamma \mathbb{I}\left\{h_{t} > 0\right\} - \delta \mathbb{I}\left\{\text{health} = \text{bad}\right\} - \phi \mathbb{I}\left\{\text{claim DI}\right\} - \xi \mathbb{I}\left\{\text{claim UI}\right\}$

Model fit I



Model fit II

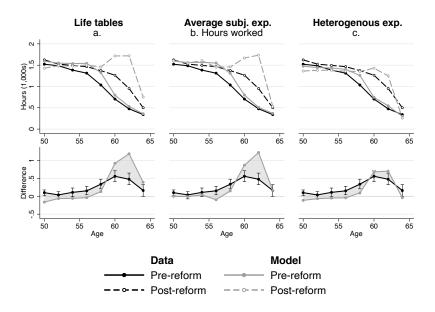


Counterfactual predictions – average retirement age

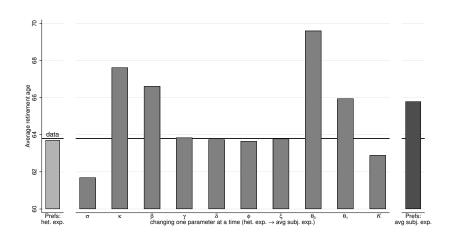
reform sample ('93-'01)	Post-reform sample ('06-'16)	Difference (yrs)
61.2 (60.97 – 61.41)	63.8 (63.49 – 64.03)	2.6 (2.23 – 2.92)
756	467	1223
reform sample ('93-'01)	Post-reform sample ('06-'16)	Difference (yrs)
60.7 60.9	65.9 65.1	5.2 4.2
	(60.97 – 61.41) 756 reform sample ('93-'01) 60.7	61.2 63.8 (60.97 – 61.41) (63.49 – 64.03) 756 467 reform sample ('93-'01) Post-reform sample ('06-'16) 60.7 65.9

^{95%} confidence intervals based on robust standard errors in parentheses.

Counterfactual predictions – average hours worked



Influence of estimates on out-of-sample predictions: average retirement age



Can subjective survival expectations improve performance of structural retirement model?

The level of expectations affects preference estimates

- Actuarial and subjective mortality yield different preference estimates
- Similar model fit.
- Poor counterfactual predictions
 - ► Retirement age increases by 4-5 yrs (data: 2.6 yrs)

Heterogeneity affects preferences and improves predictions

- Model fit similar to homogeneous survival expectations
- Accurate counterfactual predictions
 - ▶ Retirement age increases by 2.7 yrs
 - Key preference estimates: risk aversion, patience, consumption weight and bequest weight

No improvement from limited heterogeneity based on health behaviors

Moving forward

Elicitation of conditional probabilities

- Perceptions of causal effects (e.g., Giustinelli and Shapiro, 2024)
- Joint distributions
- Updating of expectations in cross-sectional data

Elicitation of uncertainty in addition to perceived risk

Intervals for reported probabilities (e.g., Giustinelli et al., 2019)

Together with PhDs we will work on:

- Model of life-care annuities with subjective expectations on both states and choices
- Income processes estimated on subj. probabilities, survey measure of income, and admin income

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Maximum Likelihood estimation Plack

Add error ε_t with CDF $F(\varepsilon)$ to single-period utility

$$U(c_t, I_t, \varepsilon_t) = U(c_t, I_t) + \varepsilon_t$$

Data: N individuals for T^d periods

- Choices (e.g., wealth, labor supply) and/or expectations (e.g., prob. of working at future ages)
- $\mathcal{D} = \{a_{i,t}; \mathbb{P}_{i,t} [h_{i\tau} = 1]; i = 1, ..., N; t = 1, ..., T^d\}$

 $\widehat{\boldsymbol{\theta}}_{\mathsf{ML}}$ maximizes the likelihood function $\mathcal{L}\left(\boldsymbol{\mathcal{D}},\boldsymbol{\theta}\right) = \prod_{i=1}^{N} L\left(\mathcal{D}_{i},\boldsymbol{\theta}\right)$:

$$\widehat{\boldsymbol{\theta}}_{\mathsf{ML}} = \arg\max_{\boldsymbol{\theta}} \prod_{i=1}^{N} L\left(\mathcal{D}_{i}, \boldsymbol{\theta}\right)$$

Maximum Likelihood estimation Plack

$$\widehat{ heta}_{\mathsf{ML}}$$
 maximizes the likelihood function $\mathcal{L}\left(\mathcal{D}, heta
ight) = \prod_{i=1}^{N} L\left(\mathcal{D}_{i}, heta
ight)$:

$$\widehat{\boldsymbol{\theta}}_{\mathsf{ML}} = \arg\max_{\boldsymbol{\theta}} \prod_{i=1}^{N} L\left(\mathcal{D}_{i}, \boldsymbol{\theta}\right)$$

If agent's problem does not have analytical solution and/or there are missing state variables: **Maximum Simulated Likelihood**

- ullet Solve model at $oldsymbol{ heta}$ to obtain optimal decisions $reve{ ilde{a}}_t\left(\chi_t,oldsymbol{ heta}
 ight)$ and $reve{ ilde{\mathbb{P}}}_t\left(\chi_t,oldsymbol{ heta}
 ight)$
- Simulate behavior using those decision rules

$$\widehat{\boldsymbol{\theta}}_{\mathsf{MSL}} = \arg\max_{\boldsymbol{\theta}} \prod_{i=1}^{N} L\left(\check{\mathcal{D}}_{i}, \boldsymbol{\theta}\right)$$

Method of Simulated Moments Phack

Moments $\check{\mathbf{m}}$ ($\boldsymbol{\theta}$) summarize behavior simulated from the model

- Should be informative about parameters to be estimated
 - E.g., (expected) labor supply moments to estimate relative weights on consumption and leisure
- Mean / quantiles
- Conditional / unconditional

Estimate θ bringing simulated behavior as close as possible to the data \mathbf{m} :

$$\widehat{\boldsymbol{\theta}} = \arg\min_{\boldsymbol{\theta}} \left(\mathbf{m} - \check{\mathbf{m}} \left(\boldsymbol{\theta} \right) \right)' \mathbf{W} \left(\mathbf{m} - \check{\mathbf{m}} \left(\boldsymbol{\theta} \right) \right)$$

W is symmetric positive definite weighting matrix

Generalization: Indirect Inference (Gourieroux et al., 1993; Smith Jr, 1993)

Indirect Inference Plack

Specify auxiliary model of observables

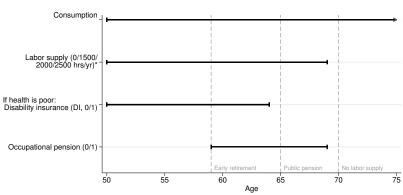
- Easy to compute
- ullet Estimator when applied to data: $\widehat{oldsymbol{eta}}_{\mathcal{A}}$
- Constant-only model equivalent to MSM

Estimate parameters by minimizing distance between auxiliary parameters from observed and simulated data

$$\widehat{oldsymbol{ heta}} = rg \min_{oldsymbol{ heta}} \left(\widehat{oldsymbol{eta}}_{A} - \widehat{oldsymbol{eta}}_{S} \left(oldsymbol{ heta}
ight)
ight)' \mathbf{W} \left(\widehat{oldsymbol{eta}}_{A} - \widehat{oldsymbol{eta}}_{S} \left(oldsymbol{ heta}
ight)
ight)$$

W is symmetric positive definite weighting matrix

Decisions at different ages Pack



[&]quot;If labor supply equals zero, individual does not claim DI or occupational pension and labor market history entitles individual to unemployment insurance (UI), UI benefits are received automatically. UI benefits stop in case the agent chooses to work or claim DI or occupational pensions; when the entitlement is exhausted; or at age 65.

Life cycle model: state variables •Back

Variable	Values	
Wealth ^a	0 - 1,000,000	
Wage ^a	5 – 100	
Health	Good/bad	
Occupational pension	$\{1=no\ occupational\ pension\ scheme,$	
	2 = occupational pension scheme - not claimed,	
	3 = occupational pension scheme - claimed}	
Benefit level occ. pension		
Years worked	15 – 50 years	
Final earnings ^a	0 - 250,000	
DI eligibility	not eligible/eligible	
UI eligibility	$\{1=not\;eligible\;(0\;years),$	
	4 = fully eligible (3 years)	

^a All monetary amounts in 2012 Euros

Utility:

$$u\left(c_{t}, l_{t}\right) = \frac{n_{t}}{1 - \sigma} \left[\left(\left(\frac{c_{t}}{n_{t}}\right)^{\kappa} l_{t}^{1 - \kappa} \right)^{1 - \sigma} - 1 \right]$$

- c_t consumption; l_t leisure; n_t equivalence scale for the number of individuals in the household
- \bullet σ concavity of utility function; κ relative weight of consumption in utility function

Leisure:

$$\mathit{I}_{t} = 4,000 - \mathit{h}_{t} - \gamma \mathbb{I}\left\{\mathit{h}_{t} > 0\right\} - \delta \mathbb{I}\left\{\mathrm{health} = \mathrm{bad}\right\} - \mathrm{stigma} \ \mathrm{costs}$$

- 4,000 hours time endowment
- h_t hours worked (0/1500/2000/2500 hours per year)
- ullet γ fixed leisure cost of work; δ leisure cost of being in bad health
- Stigma costs for DI and UI expressed in hours of leisure

Bequest motive (adapted from French, 2005) Model Stimates



$$b(w_t, n_t) = \exp \left[\theta_0 + \theta_1 n_t\right] \times \frac{(w_t + K)^{(1-\sigma)\kappa}}{1-\sigma}$$

- w_t wealth; n_t equivalence scale (HH size)
- θ_1 : weight of bequests in utility depends on survival of spouse
- K determines curvature of bequest utility

Expectations Pack

Survival

① Actuarial tables, use Bayes' rule to condition on health m_t :

$$\Pr(T = t + 1 | m_t = 2) = \frac{\Pr(m_t = 2 | T = t + 1) \times \Pr(T = t + 1)}{\Pr(m_t = 2)}$$

- Subjective expectations no heterogeneity
- Subjective expectations heterogeneity
- Life tables conditional on smoking and drinking

Health

• AR(1) logit estimated on observed health m_t :

$$\Pr\left(m_{t+1} = 2 \middle| m_t, t\right) = \frac{\exp\left[\mu_0 + \mu_1 t + \mu_2 \mathbb{I}\left\{m_t = 2\right\}\right]}{1 + \exp\left[\mu_0 + \mu_1 t + \mu_2 \mathbb{I}\left\{m_t = 2\right\}\right]}$$

Wage

AR(1) estimated on observed wages (Gourinchas and Parker, 2002)

Budget constraint Back

Consumption cannot exceed cash-on-hand x_t :

$$x_t = w_t + netinc_t + inc_t^{sp} - OOP_t$$

 w_t is wealth; $netinc_t$ is net income; inc_t^{sp} is (exogenous) net income of the spouse; OOP_t are out-of-pocket medical expenditures

- $netinc_t = \tau (earn_t, Dlinc_t, Ulinc_t, pubpens_t, occpens_t, w_t, t)$
- 20% wage penalty for working part time (1500 hrs/yr)
- DI and UI replace 70% of earnings (capped at 50,400 Euros)
- Automatic transfer from UI/DI to public pension at age 65
- Government transfers guarantee minimum consumption c_{\min} : $x_t = \max\{x_t, n_t c_{\min}\}$ (Hubbard et al., 1995)

Pensions Back

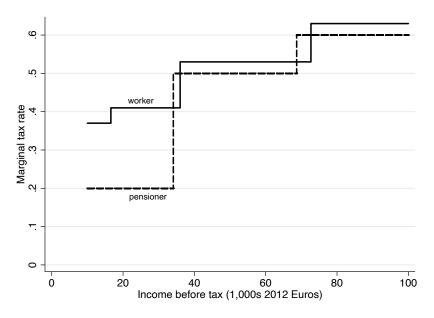
Public pension

- Flat rate subsistence income
- Automatic onset at age 65
- 9,000 Euros/year for individual in couple

Occupational pension

- 90% of employees covered
- Mandatory participation with fixed contribution rate
- Two phases (pre-reform):
 - 4 Age 59-65: early retirement pension (VUT)
 - 85% replacement rate; no actuarial adjustment; continued accumulation of entitlements
 - * Phased out around year 2000 for cohorts 1950 and later
 - 2 Age 65 and older: regular occupational pension
 - ★ Replacement rate is function of contribution years (1.75pp per year)
 - ⋆ occpens_t = 0.0175 × yrswrk_t × (prevearn_t − 19,000)

Tax function Pack



Effect of abolishment early retirement (VUT) • Back

