

Trade-Offs Between Ranking Objectives: Reduced-Form Evidence and Structural Estimation


DSE2025: Expectations and Learning in Dynamic Structural Models

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University College London, School of Management

Ranked Product Lists


Introduction



Hotel Cornelisz
Museum Quarter

4.2/5 Very Good (988 reviews)


Member Price available
per night ~~\$91~~ **\$67**
\$85 total
Includes taxes & fees



Hotel Mercier
Jordaan

4.6/5 Wonderful (668 reviews)


\$81
per night
\$101 total
Includes taxes & fees



Monet Garden Hotel Amsterdam
Amsterdam

4.6/5 Wonderful (1,050 reviews)

We have 5 left at
per night ~~\$127~~ **\$88**
\$109 total
Includes taxes & fees




Room Mate Aitana
Amsterdam

Free Cancellation
Reserve now, pay later

4.6/5 Wonderful (997 reviews)

Member Price available
per night ~~\$152~~ **\$137**
\$166 total
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Hotel The Exchange
Red Light District

We have 2 left at 10% off at

- Ranking algorithms can serve different objectives.
 - Maximize **platform revenues/profits** (=share of total revenues across products).
 - Maximize **consumer welfare**.
- 1. What determines the trade-offs between objectives?
- 2. How can we quantify these trade-offs?
- Focus: revenue and consumer welfare effects through influencing consumers' choices.
 - Relatively involved model of consumer search.
 - Taking supply side as given (other than ranking).

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- Large literature empirically studying various aspects of rankings:
 - Ursu (2018); Choi and Mela (2019); Donnelly, Kanodia, and Morozov (2023); Compiani et al. (2024)
 - And more...
- So what exactly is new here?
 1. Reduced-form evidence for **heterogeneous position effects** (= key factor shaping trade-offs).
 - Position effect: increase in searches/purchases for an alternative moving up.
 2. Novel structural model with **product discovery** as mechanism for position effects.
 - Matters for model fit and quantifying trade-offs.
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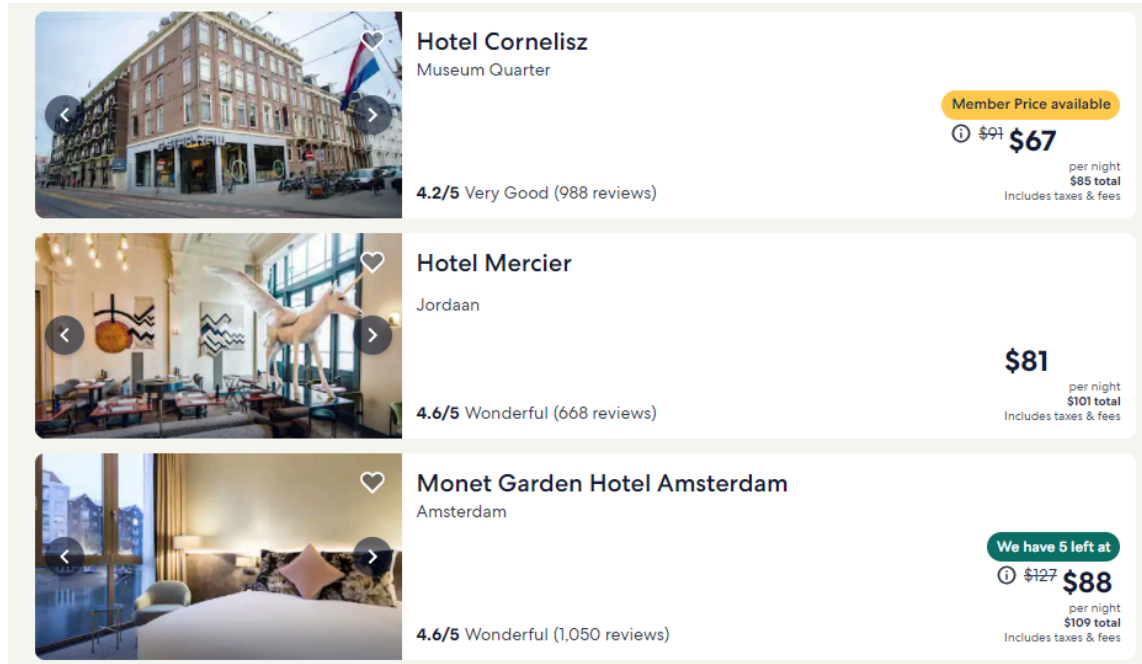
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- Background: competition on Kaggle.com, first used by Ursu (2018).
- Click-stream data of hotel search sessions on Expedia.com.
 - 166,039 search sessions, 788 (overlapping) destinations, 55 countries.
- Main feature: subsample of $\approx 30\%$ sessions with a **randomized ranking**.
 - \Rightarrow Allows identifying position effects separately from consumers' preferences.
- Data contains information on:
 - Clicks and bookings (but not search order).
 - Positions.
 - Hotel & query characteristics.
- Only sessions that did not sort results.

- Quantifying the effects of different (counterfactual) rankings requires a model that captures how consumers interact with a ranked product list.
- I develop an empirical implementation of the **search and discovery** model of Greninger (2022).

Model: Decision Process

Search and Discovery Model



Click & inspect


Click & inspect

Click & inspect

Scroll & discover

Model: Decision Process


Search and Discovery Model



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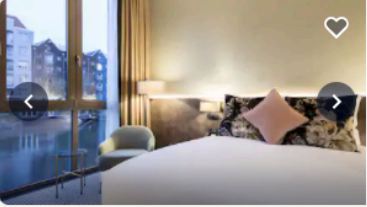
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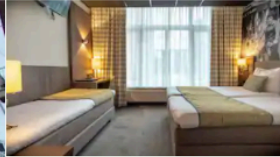

Scroll & discover

Model: Decision Process

Search and Discovery Model

COVID-19 alert: Travel requirements are changing rapidly, including need for pre-travel COVID-19 testing and quarantine on arrival.
[Check restrictions for your trip.](#) [Dismiss](#)

[← See all properties](#)



Overview

Rooms

Location

Amenities

Policies

Reviews

Reserve a room

Hotel Cornelisz


☆☆☆


4.2/5 Very Good


Guests rated this property 4.3/5 for cleanliness.

978 reviews >

Popular amenities


 Free WiFi


 Breakfast available

 Business services


See all >


Cleaning and safety practices


 Cleaned with disinfectant


 Contactless check-in


See all >

 Laundry

 Housekeeping

 24/7 front desk

 24-hour vacancy between guest room stays


 Hand sanitizer provided

AMSTERDAM-WEST
DE BAARSJES
400FOWEG
OMGEVING
AMSTERDAM
OUD-WEST
GRACHTENGORDEL
WILLEMSPIJK
AMSTERDAM
OUD-ZUID


AMSTERDAM
DE WALLEN
Rijksmuseum
Vondelpark
Albert Cuypmarkt

PC Hooftstraat 24-28, Amsterdam, 1071 BX
[View in a map >](#)


Explore the area

 Rijksmuseum


3 min walk

 Van Gogh Museum

5 min walk

 Leidseplein

6 min walk

 Amsterdam (AMS-Schiphol)

19 min drive

Greminger | Trade-Offs Between Ranking Objectives

- Utility of consumer i when booking hotel j :

$$u_{ij} = \underbrace{x_j^l \beta + \nu_{ij}}_{u_{ij}^l: \text{list page}} + \underbrace{x_j^d \kappa + \delta_j + \varepsilon_{ij}}_{u_{ij}^d: \text{detail page}}$$

- x_j^l, x_j^d : observed hotel attributes.
- δ_j : fixed effect for hotel j (estimated only for frequent hotels).
- $\varepsilon_{ij} \sim \text{Normal}(0, 1)$
- $\nu_{ij} \sim \text{Normal}(0, 1)$
- Utility of outside option : $u_{i0} = \beta_0 + \eta_i, \eta_i \sim \text{Uniform}(0, 1)$.

- Actions are costly:
 - Discovery costs: c^d
 - Search costs (product-specific): c_j^s
- Free recall: no cost to go back.
- Precedence constraints:
 - Searching a hotel requires it to have been revealed.
 - Choosing a hotel requires it to have been searched.

Model: Beliefs About Detail Page Utility

Search and Discovery Model

- Initially, consumers only observe list page utility u_{ij}^l of first alternative j on list.
- Based on x_j^l , consumers have belief about the utility of the detail page U_{ij}^d .
 - $E[U_{ij}^d | x_j^l] = x_j^l \gamma$.
 - (unconditional) U_{ij}^d follows empirical distribution.
 - γ is estimated (captures perceived correlation between x_j^l and U_{ij}^d).

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- Consumers believe they are randomly sampling from the joint distribution of $(x_j^l, x_j^d, c_j^s, \nu_{ij}, \varepsilon_{ij})$.
- Equivalent to consumers believing that they sample from a distribution of *effective values*.
 - Expected benefit of revealing alternative depends only on distribution of effective values (Greminger (2022)).
 - Effective value combines $(x_j^l, x_j^d, c_j^s, \nu_{ij}, \varepsilon_{ij})$ in a way that accounts for search behavior.

- Belief about ranking: changes distribution of effective values across positions h .
 - To simplify, assume only mean $\mu(h)$ of the distribution changes and specify functional form.

$$\mu(h) = \bar{\mu} + \rho \log(h + 1)$$

- ρ is estimated and captures beliefs about ranking algorithm.
- $\rho < 0$ means consumers expect alternatives further down to be worse *on average*.
- $\bar{\mu}$ is determined by assumption that consumers know the overall distribution across positions.
- Agnostic as to why distribution changes across positions.

- Rational consumers sequentially choose one of the available actions.
- Greninger (2022): the optimal policy is based on reservation values.
 \Rightarrow Always optimal to choose the action with the highest reservation value.
- Three reservation values:
 1. Purchasing: $z_{ij}^p = u_{ij}$
 2. Searching / clicking: $z_{ij}^s = x_j^l \beta + \nu_{ij} + x_j^l \gamma + \xi(c_j^s)$
 3. Discovering / scrolling: $z^d(h) = \mu(h) + \Xi(c^d)$
- $\xi(c_j^s)$ and $\Xi(c^d)$ capture respective net benefits.

- Simulated maximum likelihood estimation approach:
 - Parameters to estimate: $\theta = (\beta_0, \beta, \kappa, \gamma, c^d, c_j^s, \delta_j, \rho)$.
 - Optimal policy implies inequalities for reservation values given observed actions.
 - Maximize likelihood of all inequalities holding given observed actions.
 - Example: i searching but not choosing hotel j requires $z_{ij}^s \geq u_{i0}$ and $u_{ij} \leq u_{i0}$ (and more).
- Resulting likelihood function can be difficult to compute, even in simpler search models.
 - High-dimensional integral over shocks of many alternatives.
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- New result simplifying simulating the likelihood function.
- Main idea: inequalities can be expressed relative to the effective value \tilde{w}_{ij} of the chosen option j .

$$\tilde{w}_{ij} = x_j^l \beta + \nu_{ij} + \min\{x_j^l \gamma + \xi(c_j^s), x_j^d \kappa + \varepsilon_{ij}\}$$

$$\tilde{w}_{i0} = u_{i0}$$

- Probability of all inequalities holding given \tilde{w}_{ij} has closed form (after another result).
- Only requires numerically integrating over \tilde{w}_{ij} .

1. Partition probability space to obtain likelihood function that is smooth in all parameters.
 - Depending on \tilde{w}_{ij} , consumers discover different number of alternatives and inequalities change.
 - \tilde{w}_{ij} has kink at $x_j^l \gamma + \xi(c_j^s) = x_j^d \kappa + \varepsilon_{ij}$.
 2. Estimate $\xi(c_j^s)$ and $\Xi(c_d)$ and back out costs (c_j^s, c^d) post-estimation.
 - Works because only these values enter consumer decisions through reservation values.
 - Avoids costly computation of $\xi(c_j^s)$ and $\Xi(c^d)$ during estimation.
 - Allows demand predictions with few assumptions on beliefs.
- Julia and Python packages coming in the near future!

- Standard arguments for identification of parameters governing search (conditional on discovery).
- Discovery process is latent, but position effects only explained through discovery.
 - Ranking is randomized.
 - Only change in discovery value $z^d(h) = \mu(h) + \Xi(c^d)$ across positions h explains position effects.
 - $z^d(h)$ and consequently stopping probabilities are identified from the data.

- Search and discovery model: **product discovery** explains position effects.
 - Consumers leave list page before reaching the end.
- Classic Weitzman model: **position-specific search costs** explain position effects.
 - Consumers observe the entire list page (all x_j^l and ν_{ij}).
 - It is more costly to search products in lower positions ($c_j^s(h)$ depends on position h).
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- A Weitzman model predicts the following:
 - Searches in lower positions are more likely to convert to a purchase.
 - (except without position effects).
- Rationale:
 - Searching in a lower position is more costly.
- ⇒ Only happens when list utility $x_j^l \beta + \nu_{ij}$ is already large.
- No similar prediction from search and discovery model (costs do not depend on position).
- Prediction is not supported by the Expedia data ⇒ suggests product discovery mechanism.
 - Ursu (2018): conditional on search, the purchase probability is constant across positions.

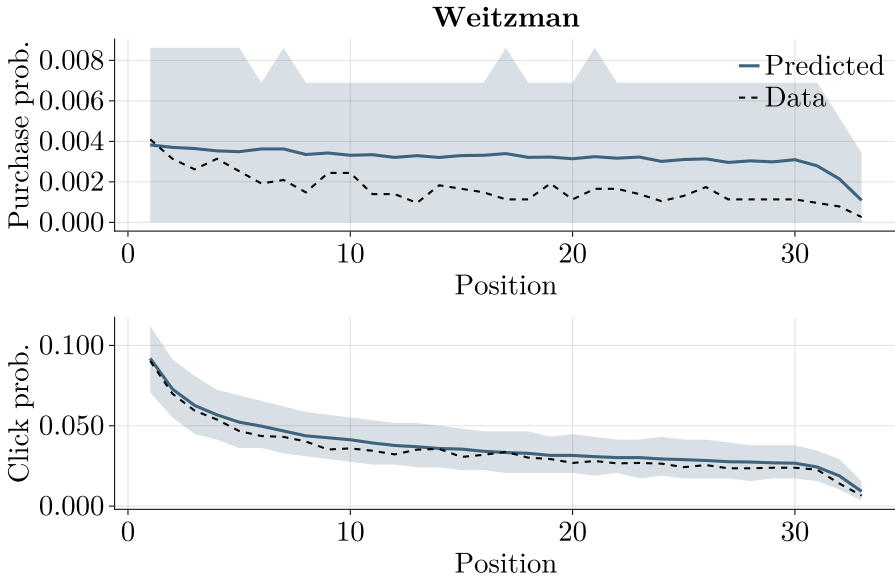
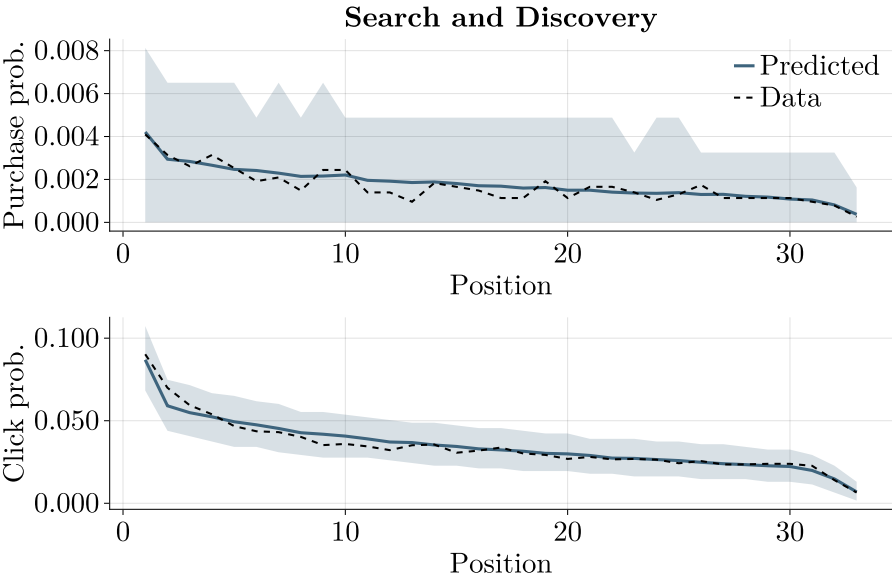
[Details](#)

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Model Fit Comparison

Search and Discovery Model



- Quantifying trade-offs between ranking objectives requires optimal rankings for each objective.
 - Difficult combinatorial optimization problem.
- 1. New heuristic for maximizing revenues: **Bottom Up Ranking**.
 - Rationale: ordering of alternatives on top does not matter for demand at bottom.
- 2. New heuristic for maximizing consumer welfare: **Effective Value Ranking**.
 - Rationale: alternatives on top should be sufficiently good to be searched and chosen.
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Counterfactual Results

Counterfactuals

Changes relative to Expedia Ranking

	Eff. Value	Bottom Up Ranking
Expedia		
Total revenues (%)	10.99	12.93
Number of transactions (%)	17.08	11.06
Avg. price of booking (%)	−5.20	1.67
Consumers		
Consumer welfare (\$, per consumer)	0.06	0.04
Consumer welfare (\$, per booking)	13.58	7.73
Discovery costs (\$, per booking)	−0.14	−0.10

- Trade-offs are smaller than prior work suggests:
 - Ursu (2018) and Compiani et al. (2024) also use Expedia data and find larger trade-offs.
 - Main difference: modeling position effects through product discovery.

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Reduced-Form Evidence: Summary

Reduced-Form Evidence

- Heterogeneity in position effects shapes trade-offs between ranking objectives.
 - Ranking products with large position effect higher increases transactions.

$$\Delta_{\text{Switch}} \text{ Demand} = \Delta_{\text{Up}} \text{ Demand}_B + \Delta_{\text{Down}} \text{ Demand}_A$$

⇒ Heterogeneity in position effects determines transactions and revenues under different rankings.

- Using simple reduced-form model (LPM), I find that:
 1. Cheaper hotels tend to have larger positions effects (conditional on other attributes).
 2. “Desirable” hotels tend to have larger position effects (desirable = more clicks/bookings).
- ⇒ Moving cheaper/desirable hotels up can increase revenues through more transactions.

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- Novel structural model with product discovery mechanism for position effects.
 - Mechanism matters for model fit and counterfactual results.
- Trade-offs between ranking objectives are limited.

Thank You!

Working paper: <https://arxiv.org/abs/2210.16408>

Email: r.greminger@ucl.ac.uk

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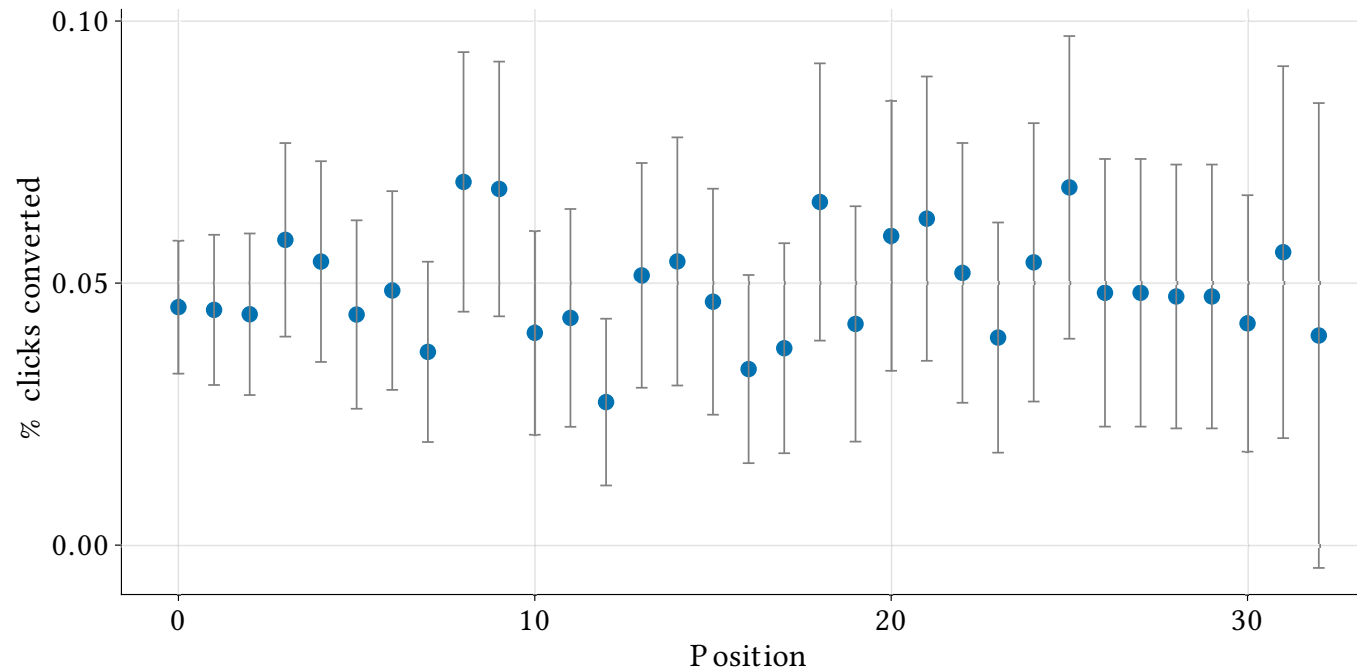
- Probability to book a hotel conditional on having clicked on it:

$$P(\text{choose } j \mid \text{search } j) = P(U_{ij}^l + U_{ij}^d \geq \bar{w}_{-j} \mid U_{ij}^l + \xi(h) \geq \bar{w}_{-j})$$

- U_{ij}^l : part of utility from list page.
- U_{ij}^d : part of utility from detail page.
- $\xi(h)$: part of search value that is not part of utility.
- \bar{w}_{-j} : maximum effective value of alternatives other than j .

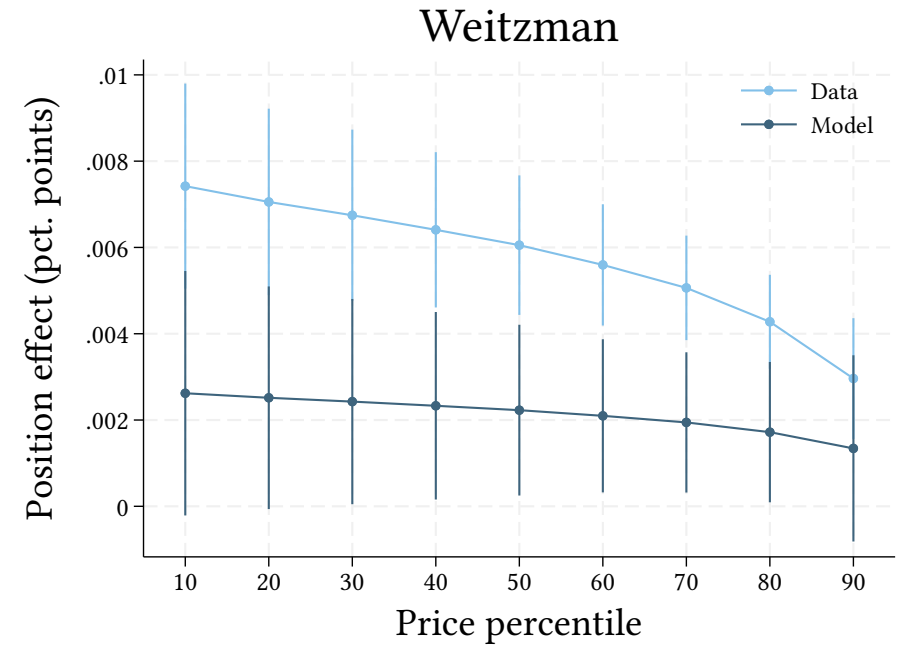
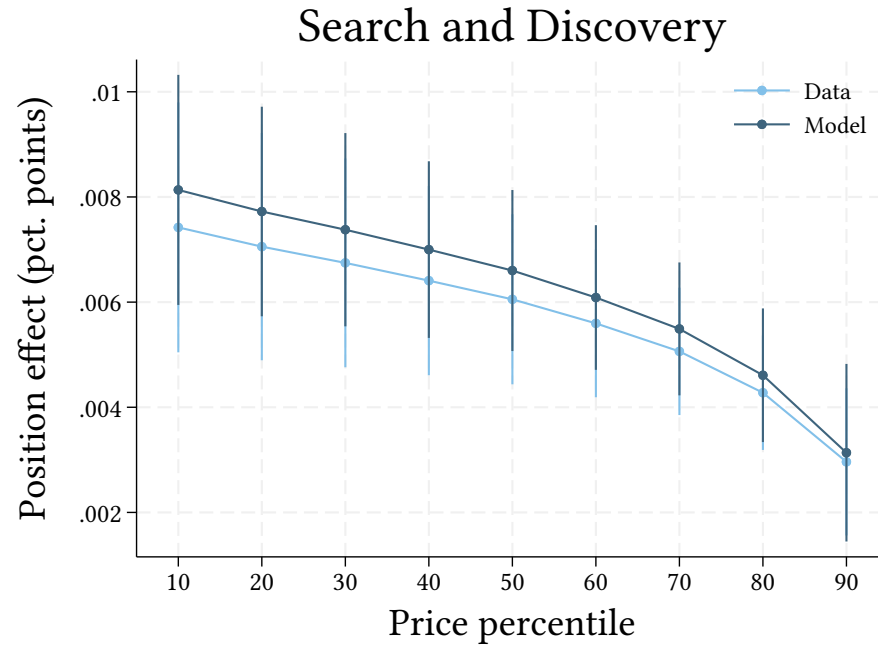
Position Effect Mechanism

- Pattern first highlighted by Ursu (2018): conditional on search, the purchase probability is constant across positions.



Model Fit Comparison

Appendix



Position effect in booking probability at different prices.

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