

# Solution of question 1.2.2

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Question: We are given a triangle and the mid-points D, E, F of the sides AB, BC, AC respectively. We have to find the normal form of equation of lines AD, BE, CF.

**Solution:**

$$\mathbf{A} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad (1)$$

$$\mathbf{B} = \begin{pmatrix} -4 \\ 6 \end{pmatrix} \quad (2)$$

$$\mathbf{C} = \begin{pmatrix} -3 \\ -5 \end{pmatrix} \quad (3)$$

The equation of line AD is :

$$\mathbf{n}^T(\mathbf{x} - \mathbf{A}) = 0 \quad (12)$$

$$\Rightarrow \mathbf{n}^T \mathbf{x} = \mathbf{n}^T \mathbf{A} \quad (13)$$

$$\Rightarrow \begin{pmatrix} \frac{3}{2} & \frac{9}{2} \end{pmatrix} \mathbf{x} = \begin{pmatrix} \frac{3}{2} & \frac{9}{2} \end{pmatrix} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad (14)$$

$$\Rightarrow \frac{3}{2} \begin{pmatrix} 1 & 3 \end{pmatrix} \mathbf{x} = \frac{3}{2} \begin{pmatrix} 1 & 3 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad (15)$$

$$\Rightarrow \begin{pmatrix} 1 & 3 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 1 & 3 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad (16)$$

$$= -2 \quad (17)$$

The mid points D, E, F of sides AB, BC, AC are :-

$$\mathbf{D} = \begin{pmatrix} \frac{-7}{2} \\ \frac{1}{2} \end{pmatrix} \quad (4)$$

$$\mathbf{E} = \begin{pmatrix} -1 \\ -3 \end{pmatrix} \quad (5)$$

$$\mathbf{F} = \begin{pmatrix} \frac{-3}{2} \\ \frac{5}{2} \end{pmatrix} \quad (6)$$

Now, the direction vector of line,  $\mathbf{m}$  is :

$$\mathbf{m} = \mathbf{D} - \mathbf{A} \quad (7)$$

$$= \begin{pmatrix} \frac{-9}{2} \\ \frac{3}{2} \end{pmatrix} \quad (8)$$

$\mathbf{n}$  can be written in the form :-

$$\mathbf{n} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \mathbf{m} \quad (9)$$

$$= \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} \frac{-9}{2} \\ \frac{3}{2} \end{pmatrix} \quad (10)$$

$$= \begin{pmatrix} \frac{3}{2} \\ \frac{9}{2} \end{pmatrix} \quad (11)$$

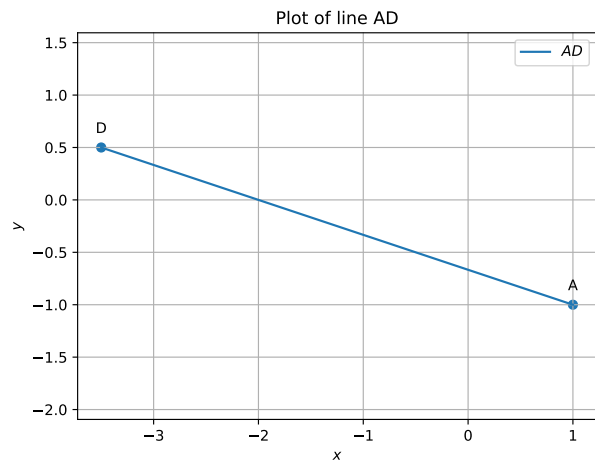


Fig. 0. Line AD