

## Problem Set #2 (Algorithms)

Department: \_\_\_\_\_

Student ID: \_\_\_\_\_

Student Name: \_\_\_\_\_

For the following problems, consider the merge sort for an input sequence of  $n$  distinct numbers.

1. For each of the following cases, find the running time in  $\Theta$ -notation. Justify your answers mathematically.

- (a) The best case
- (b) The worst case
- (c) The average case

2. To draw the graphs in Problems 3 and 4, write a program which includes the comments.

3. For each of the following cases, show and explain the step-by-step results of the merge sort.

- (a) One sorted input
- (b) One reverse-sorted input
- (c) One random input

4. For each of the following cases, draw and explain the graph of the actual running time in your PC with varying  $n$ . Compare the graph with that of the insertion sort.

- (a) Sorted inputs
- (b) Reverse-sorted inputs
- (c) Average case using random inputs