



# USACO Bronze Level Practice Sheet 1

## Problem 1: Cow Coolers

### Problem Description

Bessie the cow is hosting a summer party and wants to keep her drinks cool by placing them in coolers. She has  $N$  coolers labeled from 1 to  $N$  and  $M$  drinks labeled from 1 to  $M$ .

Each cooler can hold at most one drink, and each drink can be placed in at most one cooler. Bessie wants to minimize the maximum distance between any two drinks and asks for your help.

The distance between two drinks  $i$  and  $j$ , where  $i \neq j$ , is defined as  $|P_i - P_j|$ , where  $P_i$  and  $P_j$  are the positions of the coolers containing drinks  $i$  and  $j$ , respectively.

Given the positions of the coolers and drinks, determine the minimum possible maximum distance between any two drinks.

### Input Specifications

The first line contains two space-separated integers,  $N$  and  $M$  ( $1 \leq N, M \leq 100$ ). The next line contains  $N$  space-separated integers, denoting the positions of the coolers. The next line contains  $M$  space-separated integers, denoting the positions of the drinks.

### Output Specifications

Output a single integer, the minimum possible maximum distance between any two drinks.

## Example

### Input

```
5 3
2 4 6 8 10
1 7 9
```

### Output

```
2
```

### Explanation

Bessie can place drink 1 in cooler 2, drink 2 in cooler 6, and drink 3 in cooler 9. The maximum distance between any two drinks is then  $|2-6| = |6-9| = 2$ .

## Problem 2: Cow's Winter

### Problem Description

Bessie the cow is trying to figure out how much food she needs to buy for the upcoming winter. She has  $N$  types of food, labeled from 1 to  $N$ , and each type of food has a price and a nutritional value. Bessie has a budget of  $B$  dollars and wants to maximize the total nutritional value of the food she buys while staying within her budget. Each type of food can be bought any number of times. Given the budget, the prices, and the nutritional values of the  $N$  types of food, determine the maximum possible total nutritional value of the food Bessie can buy.

### Input Specifications

The first line contains two space-separated integers,  $N$  and  $B$  ( $1 \leq N, B \leq 100$ ). The next  $N$  lines each contain two space-separated integers, the price and the nutritional value of the  $i$ -th type of food,  $P_i$  and  $V_i$  ( $1 \leq P_i, V_i \leq 100$ ).

### Output Specifications

Output a single integer, the maximum possible total nutritional value of the food Bessie can buy.

## Example

### Input

```
3 8
3 5
4 6
5 7
```

### Output

```
13
```

### Explanation

Bessie can buy two units of the first type of food and one unit of the second type of food for a total cost of  $3 * 2 + 4 = 10$  dollars, which is within her budget of 8 dollars. The total nutritional value of the food she buys is  $2 * 5 + 6 = 16$ , but she can only consume a maximum of 13 units of nutritional value, which is the maximum possible total nutritional value of the food she can buy.

## Problem 3: Hay Warehouse

### Problem Description

Bessie the cow is storing her hay bales in a warehouse. The warehouse is a rectangular prism of dimensions  $L \times W \times H$ , and she has stacked  $N$  hay bales in the warehouse. Each hay bale has a length of  $L_i$ , a width of  $W_i$ , and a height of  $H_i$ . Bessie wants to know the minimum height she needs to set the roof of the warehouse at in order to fit all of the hay bales.

Assume that the hay bales are stacked without any gaps and without overlapping.

### Input Specifications

The input consists of three lines. The first line contains three space-separated integers:  $L$ ,  $W$ , and  $H$  ( $1 \leq L, W, H \leq 100$ ), representing the dimensions of the warehouse. The second line contains a single integer  $N$  ( $1 \leq N \leq 100$ ), representing the number of hay bales. The following  $N$  lines each contain three space-separated integers:  $L_i$ ,  $W_i$ , and  $H_i$  ( $1 \leq L_i, W_i, H_i \leq 100$ ), representing the dimensions of each hay bale.

### Output Specifications

Output a single integer, the minimum height Bessie needs to set the roof of the warehouse at in order to fit all of the hay bales.

## Example

### Input

```
10 10 10
3
7 7 7
6 6 6
5 5 5
```

### Output

```
18
```

### Explanation

The warehouse has dimensions  $10 \times 10 \times 10$ . Bessie has stacked three hay bales of dimensions  $7 \times 7 \times 7$ ,  $6 \times 6 \times 6$ , and  $5 \times 5 \times 5$ . The minimum height Bessie needs to set the roof of the warehouse at in order to fit all of the hay bales is 18.