

# Beyond Markovian Forgetfulness: Episodic Memory for Reasoning-Intensive Retrieval

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## Abstract

Reasoning-intensive information retrieval uses large language models to solve complex queries via multi-step reasoning. However, existing methods have critical limitations. Chain-of-Thought (CoT) approaches suffer from inefficiency, while state-based methods, despite better token efficiency, often fall into reasoning cycles that trap the query refinement process. To address these issues, we propose Episodic Memory for Retrieval (EMR), which enhances the state-based framework with an episodic memory. This module stores the full history of prior states for a query, allowing the model to avoid repetition of such cycles. Experiments on the BRIGHT benchmark show that EMR consistently outperforms both CoT and state-based baselines. Moreover, it is highly token-efficient, reducing token usage by 72% on average. Our work demonstrates that episodic memory is a robust and efficient solution for advanced reasoning-intensive retrieval. The code is available in the supplementary materials.

## 1 Introduction

Traditional Information Retrieval (IR) systems often struggle to answer complex queries that require multi-step reasoning (Yang et al., 2018; Feldman and El-Yaniv, 2019). Reasoning-intensive IR (Xiao et al., 2024; Das et al., 2025) leverages large language models (LLMs) to enhance retrieval performance through techniques such as iterative query refinement and document reranking.

Early approaches to reasoning-intensive IR, such as Rank1 (Weller et al., 2025) and Rank-R1 (Zhuang et al., 2025) leveraged the Chain-of-Thought (CoT) capabilities of LLMs. While effective in producing detailed reasoning traces, these approaches sacrifice token efficiency. As shown in Figure 1(a), the model generates a long and redundant reasoning chain within a single step. This process can lead to a *reasoning cycle* (e.g., AI safety

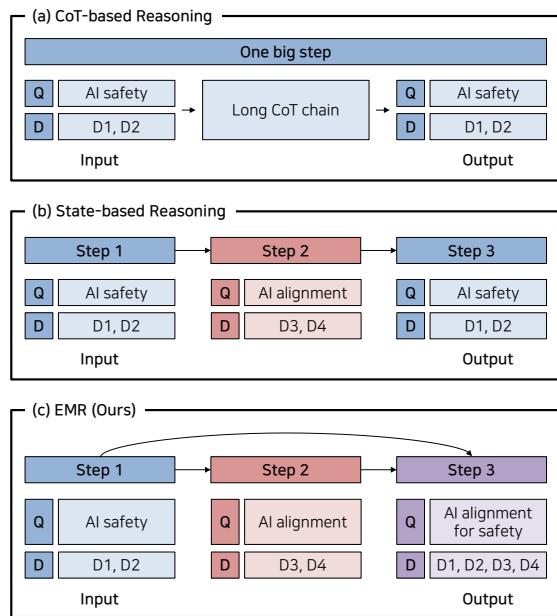


Figure 1: An illustration of different reasoning approaches for query refinement. (a) **CoT-based Reasoning** generates a single and long reasoning chain, which can be inefficient and may not result in a meaningful query update. (b) **State-based Reasoning** refines the query based solely on the immediate previous state, making it vulnerable to reasoning cycles. (c) **EMR** enhances state-based reasoning with an **episodic memory** that retains the history of all past states. This prevents cycles and enables progressive query refinement.

→ AI safety) that consumes substantial computation without yielding progress.

To improve efficiency, state-based methods such as SMR (Lee et al., 2025) decompose reasoning into iterative transitions. By design, each step is prompted to produce a new state, mitigating immediate self-loops and reducing token usage. However, this framework imposes a Markovian assumption, conditioning each new state only on the immediate predecessor. As a result, multi-step cycles can still emerge (e.g., AI safety → AI alignment → AI safety), as shown in Figure 1(b). In our exper-

054 iments, we observed that such loops occur in up to  
055 65% of queries, depending on the dataset.

056 We address these limitations with Episodic  
057 Memory for Retrieval (EMR), which augments  
058 the state-based paradigm with an explicit memory  
059 module to eliminate reasoning cycles. Inspired by  
060 *episodic memory* in agentic approaches (DeChant,  
061 2025; Nuxoll and Laird, 2012), which refers to  
062 the ability to recall past experiences, our method  
063 records the full history of states generated for a  
064 query. The model is then prompted to condition on  
065 this trajectory when producing the next state. This  
066 trajectory-aware mechanism prevents the revisiting  
067 of prior states and encourages the generation of  
068 progressively refined queries.

069 **Figure 1(c)** shows how a query progresses to  
070 refinement: For instance, by referencing its mem-  
071 ory of having already generated AI safety and AI  
072 alignment, the model is guided to produce a more  
073 advanced query like AI alignment for safety,  
074 rather than repeating previous steps. This episodic  
075 memory is implemented as a text-based log within  
076 the model’s system prompt, ensuring constant ac-  
077 cessibility during inference. Furthermore, through  
078 prompt compression, EMR achieves superior to-  
079 ken efficiency compared to the state-based method,  
080 despite the additional tokens to store past states.

081 To validate EMR, we conducted extensive ex-  
082 periments on BRIGHT, a widely-used benchmark  
083 for reasoning-intensive IR. The results demon-  
084 strate that EMR consistently outperforms existing CoT-  
085 based and state-based approaches across various  
086 settings, confirming its effectiveness. Furthermore,  
087 we show that our approach is token-efficient, re-  
088 ducing token consumption by 72% on average  
089 compared to the state-based approach. This re-  
090 sult suggests that the gains in token efficiency from  
091 episodic memory are larger than the cost introduced  
092 by maintaining it.

## 093 2 Related Work

### 094 2.1 CoT-based Reasoning for IR

095 The advent of LLMs has enabled new approaches  
096 for addressing complex information retrieval tasks  
097 that demand multi-step reasoning. Early ap-  
098 proaches in this domain, such as Rank1 (Weller  
099 et al., 2025) and Rank-R1 (Zhuang et al., 2025),  
100 leveraged CoT prompting to deconstruct intricate  
101 information needs.

102 However, the lengthy reasoning chains they  
103 generated are often redundant, which could mis-

104 guide the query refinement process. Subsequent  
105 CoT compression approaches, like O1-Pruner (Luo  
106 et al., 2025), aimed to mitigate this by shortening  
107 the CoT chain. Despite these efforts, the fundamen-  
108 tal limitation of the CoT paradigm is its single-pass  
109 generation process. This approach is vulnerable to  
110 reasoning cycles, motivating a shift toward more  
111 granular, state-based methods.

### 112 2.2 State-based Reasoning for IR

113 To address the inefficiencies of CoT, methods like  
114 SMR (Lee et al., 2025) reformulated the task as a  
115 sequence of state transitions. This approach signifi-  
116 cantly improved token efficiency by breaking down  
117 the reasoning process into discrete steps.

118 However, its reliance on a Markovian assump-  
119 tion makes it susceptible to multi-step reasoning  
120 cycles. This motivates a mechanism that can retain  
121 and leverage the history of past states to ensure  
122 consistent forward progress.

### 123 2.3 Memory in Agentic Approaches

124 The need for a history-aware mechanism has been  
125 explored in the field of agentic AI. In this do-  
126 main, episodic memory (DeChant, 2025; Nuxoll  
127 and Laird, 2012) refers to an agent’s ability to  
128 record and recall a sequence of past experiences,  
129 allowing it to engage in more complex planning.

130 Inspired by this approach, our primary contri-  
131 bution is the integration of this episodic memory  
132 concept into the state-based IR framework. Unlike  
133 previous methods conditioned only on the prior  
134 state, our approach conditions the policy on the en-  
135 tire history of previously generated queries. This al-  
136 lows our model to systematically prevent reasoning  
137 cycles while preserving the high token efficiency of  
138 the state-based paradigm, leading to a more robust  
139 and progressive query refinement process.

## 140 3 Method

141 Our approach enhances the state-based reasoning  
142 paradigm as a sequential state-transition problem,  
143 defining its core components: states, actions, and  
144 the policy model (§3.1). Building upon this foun-  
145 dation, we then introduce our core contribution,  
146 EMR, and describe how its episodic memory is  
147 constructed and applied to guide the reasoning pro-  
148 cess (§3.2).

### 149 3.1 Problem Setup: State-based Reasoning

150 Following the recent work (Lee et al., 2025), we  
151 formulate the reasoning-intensive IR task as a se-

152 sequential decision-making process. This process is  
153 characterized by three fundamental components: a  
154 state representing the current context, an action that  
155 modifies it, and a policy that selects the best action.  
156 This formulation can be viewed as a Markov Decision  
157 Process (MDP), where the policy guides the  
158 transitions between states to progressively refine  
159 the initial state.

160 **State.** We define the state  $s_t$  at step  $t$  as a tuple  
161 consisting of the current query and a set of retrieved  
162 documents. This represents a snapshot of the rea-  
163 soning process at a given moment. Formally, a  
164 state is defined as:

$$165 \quad s_t = (q_t, D_t) \quad (1)$$

166 where  $q_t \in \mathcal{Q}$  is the query at step  $t$ , with  $\mathcal{Q}$  being  
167 the list of all possible queries.  $D_t \subset \mathcal{D}$  is the list of  
168 documents retrieved using the query  $q_t$ , where  $\mathcal{D}$   
169 represents the entire document corpus. The goal is  
170 to transition from an initial state  $s_0$  to a final state  
171  $s_n$  where  $D_n$  is optimized for the user's informa-  
172 tion need.

173 **Action.** An action  $a_t$  represents a strategic opera-  
174 tion chosen by the policy to advance the search  
175 process. Our action space  $\mathcal{A}$  consists of three dis-  
176 tinct operations:

$$177 \quad \mathcal{A} = \{ \text{REFINE}, \text{RERANK}, \text{STOP} \} \quad (2)$$

178 The REFINE action is deployed to broaden the  
179 search space. It uses the LLM to generate a new  
180 query  $q_{t+1}$ , retrieves a new set of documents, and  
181 expands the current document list  $D_t$  by appending  
182 these new results. Conversely, the RERANK action  
183 is used to exploit the currently held information. It  
184 leverages the LLM to perform a listwise reranking  
185 of documents in  $D_t$ , prioritizing the most relevant  
186 items. For computational feasibility, this list is  
187 then truncated to the top- $k$  entries, creating a more  
188 focused document set  $D_{t+1}$  while the query  $q_t$  re-  
189 mains stable. Finally, the process terminates with  
190 the STOP action when the policy determines that  
191 the gathered documents in  $D_t$  are sufficient. This  
192 terminates the loop and returns  $D_t$  as the output.

193 **Policy.** The Policy  $\pi$  serves as the decision-  
194 making engine of our reasoning agent, strate-  
195 gically guiding the search process toward a res-  
196 olution. Embodied by an LLM, the policy as-  
197 sesses the current state  $s_t = (q_t, D_t)$  at each  
198 step  $t$  to determine the most promising action

199  $a_t \in \{\text{REFINE}, \text{RERANK}, \text{STOP}\}$  to execute. For effi-  
200 ciency, the LLM generates both the chosen action  
201 and its direct result within a single forward pass.  
202 For instance, if the policy chooses REFINE, it out-  
203 puts the action itself along with the newly refined  
204 query. This one-call-per-step architecture mini-  
205 mizes latency and computational cost. To ensure  
206 the reasoning process remains bounded, the pol-  
207 icy is also constrained by a predefined maximum  
208 number of steps,  $T_{\max}$ . If the current step count  
209 reaches this threshold, the policy issues a STOP ac-  
210 tion, preventing overly long or costly reasoning  
211 chains.

212 **Reasoning Cycle.** A significant drawback of the  
213 state-based formulation is its vulnerability to rea-  
214 soning cycles, where the agent becomes trapped  
215 in a loop by revisiting previously explored states.  
216 This issue is a direct consequence of the policy's  
217 Markovian nature: its decisions are conditioned  
218 solely on the current state  $s_t$ , with no memory of  
219 the path taken to reach it. Formally, the reasoning  
220 cycle is defined as follows:

$$221 \quad q_t = q_{t'} \quad (t' < t) \quad (3)$$

222 where equality denotes exact lexical identity. Such  
223 loops prevent meaningful progress, leading to re-  
224 dundant computation and suboptimal retrieval per-  
225 formance. This limitation highlights the need for  
226 a mechanism that can break the Markovian chain  
227 by incorporating a memory of its history into the  
228 agent.

## 229 3.2 Proposed: EMR

230 This section discusses how EMR introduces an  
231 episodic memory, by first describing the concep-  
232 tual role of episodic memory in state-based rea-  
233 soning (§3.2.1) and then detailing its implemen-  
234 tation for reading and writing states in textual form  
235 (§3.2.2). Finally, we introduce the memory com-  
236 pression mechanism designed to maintain high to-  
237 ken efficiency, even with the overhead of storing  
238 memory states (§3.2.3).

### 239 3.2.1 Role of Episodic Memory

240 The role of the episodic memory in EMR is to  
241 break the Markovian dependency inherent in the  
242 standard state-based approach. As defined in §3.1,  
243 the vanilla policy  $\pi$  makes decisions based solely  
244 on the current state  $s_t$ , rendering it blind to the path  
245 taken to arrive there.

246 To address this, we introduce an episodic mem-  
247 ory, denoted as  $M_t$ , which is the complete history

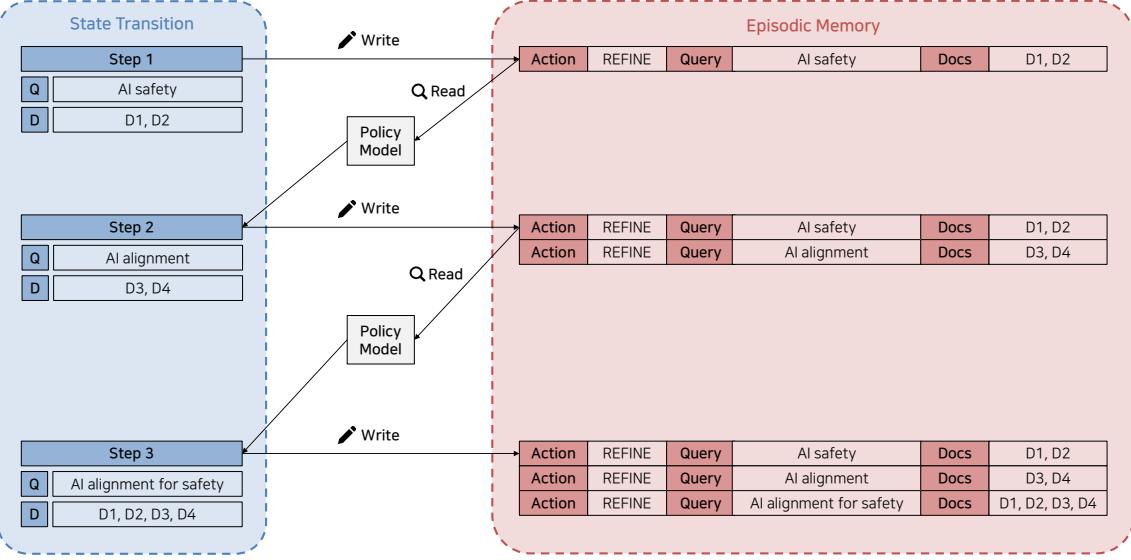


Figure 2: An illustration of the EMR architecture and the role of episodic memory. The figure shows the interplay between the iterative **State Transition** process (left) and the **Episodic Memory** (right). At each step, the policy model generates the next state based on the memory’s history, and then updates the memory with that newly generated state.

of all states visited up to step  $t$ . Formally, the memory is a sequence of past states:

$$M_t = (s_0, s_1, \dots, s_{t-1}) \quad (4)$$

where  $s_i = (q_i, D_i)$  is the state at step  $i$ .

By incorporating this memory, we redefine the policy function. The original policy  $\pi(s_t)$  is transformed into a memory-augmented policy,  $\pi'$ , which conditions its decisions on both the current state and the entire history stored in the memory. The action selection process is thus updated as follows:

$$a_t = \pi'(s_t, M_t) \quad (5)$$

This seemingly simple modification has two profound implications for the reasoning process, as illustrated in Figure 2.

First, the memory-augmented policy can explicitly prevent cycles. By having access to the set of all past queries  $\{q_0, q_1, \dots, q_{t-1}\}$  within  $M_t$ , the policy  $\pi'$  can be instructed to avoid generating any query that has been previously explored. This directly resolves the cyclic behavior defined in Equation 3.

Second, beyond cycle prevention, the memory provides a rich historical context to generate more targeted queries, rather than just reacting to the immediate present. The following sections will detail the practical implementation of how this conceptual memory is read and written as a textual log within the LLM’s prompt.

### 3.2.2 Memory Read and Write Operations

To utilize the conceptual memory  $M_t$  described in the previous section, we designed a token-efficient textual format that can be seamlessly integrated into the policy model’s prompt. This process involves two key operations: writing the historical states into a textual log and reading this log as context for the next decision. The entire memory structure is prepended to the main task prompt at each step  $t$ , ensuring the model has constant access to its history.

The memory is formatted as plain text and organized into two distinct sections as shown in Table 1: a history of actions and a repository of document contents.

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## History of Recent Actions
[1] Action: {a_1} Query: {q_1} Ranks: {IDs of D_1}
...
[t-1] Action: {a_{t-1}} Query: {q_{t-1}} Ranks: {IDs of D_{t-1}}

## Memory of Documents
[ID of d_1] {d_1}
[ID of d_2] {d_2}
...
[ID of d_n] {d_n}
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Table 1: Text format of the history of previous states in the system prompt of EMR.

The History of Recent Actions section

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292 serves as a log of the reasoning trajectory. A crucial  
293 design choice for token efficiency is that each  
294 entry stores only the identifiers (IDs) of the docu-  
295 ments retrieved at that step, rather than their full  
296 contents. This significantly reduces the token count  
297 that grows with each step, as document contents  
298 can be hundreds of tokens long while their IDs are  
299 just single tokens or short strings.

300 The Memory of Documents section acts as a  
301 deduplicated repository. It maps document IDs to  
302 their full textual content. This structure decouples  
303 the log from the voluminous document content, pre-  
304 venting redundant storage of the same document if  
305 it is retrieved multiple times across different steps.  
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307 We deliberately chose a simple plain text format  
308 over structured formats like JSON or XML. Our  
309 preliminary experiments indicated that while struc-  
310 tured formats offered no significant performance  
311 improvement, they consistently incurred a higher  
312 token overhead due to syntactic characters (e.g.,  
313 brackets, quotes, and tags). The plain text approach  
314 provides the best balance of performance and token  
economy for this task.

315 **Read Operation.** The read operation is per-  
316 formed implicitly at the beginning of each step  
317  $t$ . The entire two-part memory block, represent-  
318 ing  $M_t$ , is formatted as a single string and placed  
319 within the LLM’s prompt, typically following the  
320 system message. This provides the full historical  
321 context required for the memory-augmented policy  
322  $\pi'(s_t, M_t)$  to make its next decision.

323 **Write Operation.** The write operation occurs af-  
324 ter the policy executes an action  $a_t$  and a new state  
325  $s_t = (q_t, D_t)$  is generated. The process involves  
326 two updates:

- 327 • A new formatted string is appended to the  
328 History of Recent Actions.
- 329 • Each document in the retrieved set  $D_t$  is  
330 checked. If a document’s ID is not already  
331 present in the Memory of Documents, its ID  
332 and full content are appended to that section.

333 This read-write cycle continues until the STOP  
334 action is issued, ensuring that the memory is al-  
335 ways a complete and up-to-date record of the entire  
336 reasoning process.

### 337 3.2.3 Memory Compression

338 Despite deduplication, the cumulative length of  
339 unique document contents still poses a significant

challenge to token efficiency. As a result, as the  
reasoning process explores more documents, the  
memory’s token footprint can grow excessively,  
leading to increased computational costs and poten-  
tial context window limitations. To mitigate this  
issue, we introduce a memory compression mecha-  
nism that reduces each document to only its most  
query-relevant sentences.

This compression is performed via a three-step  
extractive summarization process whenever a new  
set of documents  $D_t$  is retrieved by a query  $q_t$ .

**Sentence Segmentation.** All documents in  $D_t$   
are split into sentences using spaCy<sup>1</sup>, creating a  
large pool of candidate sentences.

**Relevance Scoring.** Each sentence is scored for  
relevance to  $q_t$  using a pre-trained MiniLM cross-  
encoder<sup>2</sup>.

**Global Filtering and Composition.** Unlike per-  
document selection, we rank all sentences from  
the entire pool and keep only the top- $k$  overall.  
This global selection ensures that only the most  
relevant sentences enter the Memory of Documents,  
implicitly pruning irrelevant documents entirely.  
The resulting compressed summaries reduce token  
overhead while focusing the policy model on the  
most salient information for ongoing reasoning.

## 4 Results and Analysis

### 4.1 Experimental Setup

**Datasets.** We evaluate our method using the  
BRIGHT benchmark (Su et al., 2024), which is de-  
signed for reasoning-intensive IR tasks. The bench-  
mark is composed of 12 diverse datasets spanning  
domains such as mathematics, code, and scientific  
questions. To demonstrate the generalizability of  
our approach, we report performance across all of  
them.

**Evaluation Metrics.** Consistent with the base-  
line methods, we employ nDCG@10 as our pri-  
mary evaluation metric, a standard metric in IR.  
We also report other metrics such as Recall and  
MAP in the Appendix to further validate our ro-  
bustness.

**Baselines.** We compare EMR against the follow-  
ing baselines. See Appendix A.1 for more details.

<sup>1</sup><https://spacy.io/>

<sup>2</sup><https://huggingface.co/cross-encoder/ms-marco-MiniLM-L6-v2>

- 384 • **CoT-based Reasoning:** We include  
 385 Rank1 (Weller et al., 2025) and Rank-  
 386 R1 (Zhuang et al., 2025), which are strong  
 387 CoT-based models, and O1-Pruner (Luo et al.,  
 388 2025), a method for compressing reasoning  
 389 trajectories.
- 390 • **State-based Reasoning:** We use SMR (Lee  
 391 et al., 2025), which models the retrieval pro-  
 392 cess as transitions between states.
- 393 • **Retriever:** We include BM25 (Robertson  
 394 et al., 2009), a traditional sparse retriever, and  
 395 ReasonIR (Shao et al., 2025), a dense retriever  
 396 trained for reasoning tasks.

397 **Implementation Details.** All baselines follow  
 398 published implementations provided in official  
 399 repositories and papers. Hyperparameters not men-  
 400 tioned here follow those in the original publica-  
 401 tions. To ensure a comprehensive comparison  
 402 across LLMs with differing performance, we con-  
 403 duct our experiment on both Qwen2.5-32B and  
 404 Qwen3-32B. See Appendix A.2 for more details.

## 4.2 Analysis

We structure our analysis around three research questions to validate the effectiveness of EMR.

### 4.2.1 RQ1. Does Reducing Cycles with Episodic Memory Boost Performance?

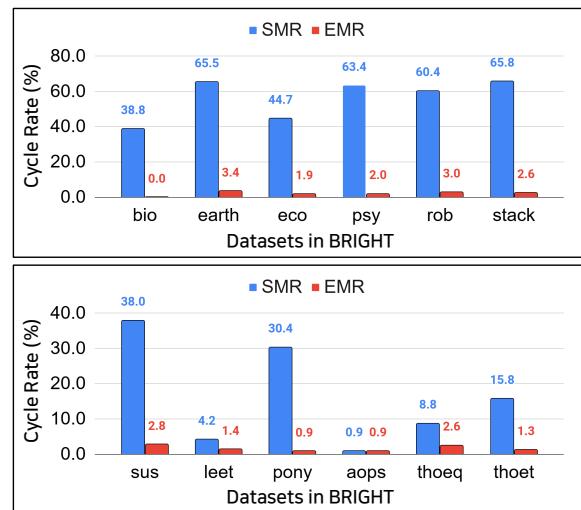


Figure 3: Comparison of the cycle ratio between EMR and SMR on the BRIGHT benchmark. The ratio indicates the percentage of queries that encounter one or more reasoning cycles during the refinement process.

Reducing Reasoning Cycles. To answer RQ1, we first measure the occurrence of reasoning cycles as defined in Eq. 3: any instance where a refined query revisits a previously generated one.

As illustrated in Figure 3, EMR (red) consistently suppresses reasoning cycles compared to SMR (blue) across all BRIGHT datasets. Aggregated over all datasets, the average cycle rate is reduced by 94%, from 38.75% for SMR to just 2.25% for EMR.

A closer analysis reveals that the baseline’s vulnerability to reasoning cycles is heterogeneous, varying with the type of the queries in each domain. On datasets like *Leetcode* and *AoPS*, SMR already exhibits few cycles. This is likely because their queries often contain code snippets or mathematical formulas, whose high lexical specificity makes exact repetition less probable. In contrast, on datasets with natural language queries such as *EarthScience*, *Psychology*, and *StackOverflow*, SMR is highly vulnerable to cyclic behavior, with cycle rates exceeding 60%. Across all datasets, EMR reduces the cycle rates to under 4%. This demonstrates that episodic memory provides a robust solution to the reasoning cycle problem inherent in state-based models.

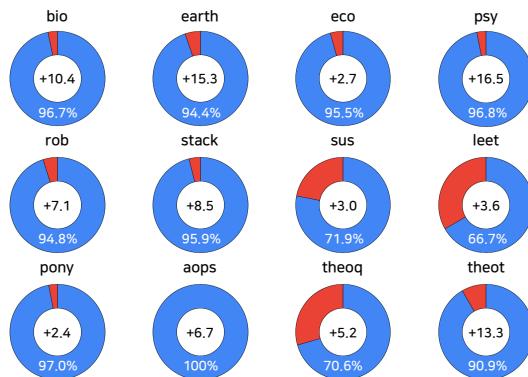


Figure 4: Analysis of queries that encounter cycles with SMR baseline. For each BRIGHT dataset, the donut chart displays the percentage of these queries for which EMR successfully resolves the cycle (blue). The central number indicates the average nDCG@10 point gain for these resolved queries.

**Performance Gain in Cycle Queries.** To further quantify the impact of cycle mitigation, we conducted a fine-grained analysis on queries where SMR encounters a reasoning cycle. We measure both the rate at which EMR resolves the cycle and the subsequent impact on retrieval performance.

	Bio	Earth	Econ	Psy	Rob	Stack	Sus	Leet	Pony	AoPS	TheoQ	TheoT	Avg
<b>Retriever</b>													
BM25	18.9	27.2	14.9	12.5	13.6	18.4	15.0	24.4	7.9	6.2	10.4	4.9	14.5
<b>Cot-based Reasoning</b>													
BM25 + Rank1	22.1	31.7	14.6	15.7	15.8	17.7	20.3	22.9	<b>9.7</b>	5.9	11.8	9.3	16.5
BM25 + Rank-R1	23.6	33.5	16.8	15.4	18.8	18.4	20.3	24.9	9.1	6.9	12.1	8.7	17.4
BM25 + O1-Pruner	23.6	31.9	17.7	18.0	17.2	20.0	19.8	24.2	8.4	6.6	10.7	7.0	17.1
<b>State-based Reasoning</b>													
BM25 + SMR (Qwen2.5)	28.7	34.9	20.4	20.7	20.9	20.8	19.2	22.1	6.3	6.3	18.0	20.3	19.9
BM25 + SMR (Qwen3)	44.0	42.1	22.9	23.3	18.3	21.1	29.5	14.5	7.8	3.1	6.9	6.4	20.0
<b>EMR: State-based Reasoning with Episodic Memory</b>													
BM25 + EMR (Qwen2.5)	41.2	42.1	<b>24.7</b>	33.1	19.2	23.8	26.1	<b>26.4</b>	8.3	6.8	<b>26.5</b>	<b>29.2</b>	26.4
BM25 + EMR (Qwen3)	<b>53.1</b>	<b>54.6</b>	23.2	<b>37.4</b>	<b>23.4</b>	<b>26.9</b>	<b>31.8</b>	15.8	9.0	<b>7.2</b>	20.9	17.3	<b>26.7</b>

Table 2: Retrieval performance (nDCG@10) on the **BRIGHT** benchmark using **BM25** as the underlying retriever. All methods differ only in their reasoning strategy. Best scores per dataset are bolded.

	Bio	Earth	Econ	Psy	Rob	Stack	Sus	Leet	Pony	AoPS	TheoQ	TheoT	Avg
<b>Retriever</b>													
ReasonIR	43.6	42.9	32.7	38.8	20.9	25.8	27.5	31.5	19.6	7.4	33.1	35.7	30.0
<b>Cot-based Reasoning</b>													
ReasonIR + Rank1	49.7	35.8	22.0	37.5	22.5	21.7	35.0	18.8	<b>32.5</b>	10.8	22.9	43.7	29.4
ReasonIR + Rank-R1	50.3	36.1	24.4	38.9	23.7	22.0	34.2	22.6	31.3	10.7	24.5	44.0	30.2
ReasonIR + O1-Pruner	48.6	37.4	24.4	38.8	24.0	21.6	35.3	22.5	31.1	11.2	24.0	<b>44.1</b>	30.3
<b>State-based Reasoning</b>													
ReasonIR + SMR (Qwen2.5)	52.2	51.1	27.5	45.1	22.8	29.4	30.9	27.9	18.1	7.4	36.4	32.6	31.8
ReasonIR + SMR (Qwen3)	53.7	52.3	29.5	46.9	24.5	30.6	32.5	29.0	19.8	9.2	38.0	34.2	33.4
<b>EMR: State-based Reasoning with Episodic Memory</b>													
ReasonIR + EMR (Qwen2.5)	55.9	55.4	33.3	49.4	26.7	33.6	35.1	31.2	22.6	11.1	39.0	35.6	35.7
ReasonIR + EMR (Qwen3)	<b>56.9</b>	<b>56.0</b>	<b>33.5</b>	<b>50.0</b>	<b>28.2</b>	<b>34.1</b>	<b>35.7</b>	<b>32.4</b>	23.1	<b>12.4</b>	<b>40.5</b>	37.2	<b>36.7</b>

Table 3: Retrieval performance (nDCG@10) on **GPT4-Reason queries** of the **BRIGHT** benchmark. Best scores per dataset are bolded.

Figure 4 shows that EMR successfully resolves the cycle in over 90% of these failure cases on average, as indicated by the blue portion of each chart. Moreover, this resolution translates into substantial gain. The number at the center of each chart represents the nDCG@10 gain for these queries, amounting to 8%p increase in average. Notably, the largest performance gains are observed in datasets with natural language queries, such as *EarthScience* (+15.3) and *Psychology* (+16.5). This observation aligns with our earlier findings, confirming that EMR effectively prevents cycles even in scenarios where the baseline is most prone to failure.

#### 4.2.2 RQ2. Is EMR More Effective and Efficient?

To answer RQ2, we designed a comprehensive evaluation to measure two key performance axes: re-

trieval effectiveness and token efficiency.

**Retrieval Effectiveness.** As shown in Table 2, which evaluates performance in nDCG@10 with the BM25 retriever, EMR consistently outperforms all CoT-based and state-based baselines. On average, EMR achieves a 6.7%p gain in nDCG@10 compared to SMR. See Appendix A.3 for a comprehensive evaluation across other metrics such as Recall and MAP.

This performance gain is not just the result of better initial query refinement of LLMs. To verify this, we conducted an experiment using strong initial queries refined by GPT-4, provided by the BRIGHT benchmark. As detailed in Table 3, EMR remains the top-performing method, still outperforming SMR by a 3.3%p margin in nDCG@10.

Furthermore, the superiority of EMR is not simply from using a more powerful LLM. Across both

	Bio	Earth	Econ	Psy	Rob	Stack	Sus	Leet	Pony	AoPS	TheoQ	TheoT	Avg
<b>Retriever</b>													
ReasonIR	26.3	31.5	23.3	30.3	17.8	24.0	20.6	35.0	10.3	14.3	31.6	27.2	24.4
<b>Cot-based Reasoning</b>													
ReasonIR + Rank1	32.0	30.0	22.3	31.1	16.7	25.8	22.4	31.4	15.5	12.1	27.8	26.3	24.5
ReasonIR + Rank-R1	33.0	34.1	24.2	33.5	20.2	25.4	22.8	33.5	14.1	10.7	30.3	27.8	25.8
ReasonIR + O1-Pruner	31.6	34.9	24.5	33.2	21.0	24.9	24.7	33.3	11.8	12.9	29.9	27.1	25.8
<b>State-based Reasoning</b>													
ReasonIR + SMR (Qwen2.5)	34.7	35.1	26.2	32.8	20.9	25.2	24.2	30.8	10.4	13.5	30.1	28.6	26.0
ReasonIR + SMR (Qwen3)	41.7	37.8	26.4	31.2	20.3	26.0	32.5	28.8	10.5	14.8	33.0	28.5	27.6
<b>EMR: State-based Reasoning with Episodic Memory</b>													
ReasonIR + EMR (Qwen2.5)	41.7	41.5	31.4	36.6	22.8	25.8	34.9	32.0	11.2	15.1	38.4	34.3	30.5
ReasonIR + EMR (Qwen3)	<b>52.4</b>	<b>46.8</b>	<b>32.2</b>	<b>39.9</b>	<b>24.7</b>	<b>30.2</b>	<b>35.3</b>	<b>36.1</b>	<b>12.2</b>	<b>15.3</b>	<b>40.7</b>	<b>34.6</b>	<b>33.4</b>

Table 4: Retrieval performance (nDCG@10) on the **BRIGHT** benchmark using **ReasonIR** as the underlying retriever. All methods differ only in their reasoning strategy. Best scores per dataset are bolded.

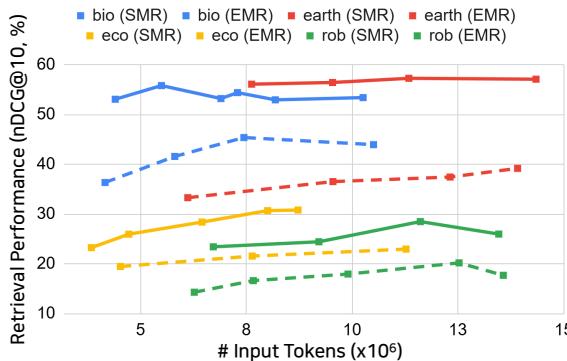


Figure 5: Retrieval performance versus cumulative input tokens for EMR (solid lines) and SMR (dashed lines) on selected BRIGHT datasets. Each color represents a different dataset.

**Table 2** and **Table 3**, while the Qwen3-based models generally outperform Qwen2.5-based models, EMR maintains the highest average score regardless of the underlying LLM. This indicates that episodic memory provides a robust advantage that is not dependent on initial query quality or biased towards a specific LLM.

**Token Efficiency.** Beyond performance, EMR demonstrates superior token efficiency. **Figure 5** shows retrieval performance against the number of tokens consumed for the representative four datasets of the BRIGHT benchmark. In this figure, each color represents a distinct dataset, while solid lines denote EMR and dashed lines indicate SMR. See Appendix A.4 for more details.

The figure shows that EMR dominates SMR across all token budget ranges. This confirms that the token overhead introduced by maintaining the

episodic memory is more than offset by the efficiency gains from avoiding redundant reasoning steps and our memory compression strategy.

### 4.2.3 RQ3. Is EMR Complementary to Stronger Retrievers?

To answer RQ3, we investigate whether the benefits of EMR are complementary to the gains from using more advanced retrieval components.

We test if the performance gains from EMR persist when using a more powerful retriever. We replaced the sparse retriever BM25 with ReasonIR, a strong dense retriever trained for reasoning tasks. **Table 4** shows that the advantage of EMR remains with a significant margin. Specifically, EMR with Qwen3 achieves an average nDCG@10 of 33.4, surpassing the strongest baseline (SMR with Qwen3) by 5.8%p. This demonstrates that the improvements from EMR’s trajectory-aware reasoning and ReasonIR’s stronger retrieval are orthogonal and additive.

## 5 Conclusion

In this work, we address reasoning cycles in state-based approaches for reasoning-intensive IR by introducing EMR, a framework that integrates an episodic memory module to guide the reasoning process. By conditioning the policy on its entire history of visited states, EMR reduces the cycle rate by about 94%. Experiments on the BRIGHT benchmark demonstrate that this approach consistently outperforms existing CoT-based and state-based baselines in both retrieval effectiveness and token efficiency.

## 527 6 Limitations

528 While EMR demonstrates robust performance, it  
529 has a modular design that allows for several promising  
530 extensions. For instance, the current action  
531 space is intentionally concise (Refine, Rerank,  
532 Stop). This set could easily be expanded to in-  
533 clude more specialized tools like external API calls  
534 and user feedback, transforming EMR into a more  
535 comprehensive information searcher. Such interac-  
536 tions would enhance our episodic memory with a  
537 more comprehensive history.

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## 610 A Appendix

### 611 A.1 Baseline Methods

612 To provide a comprehensive evaluation of EMR,  
613 we compare it against various baseline methods.  
614 All models described in this section are released  
615 under the MIT License.

616 **CoT-based Reasoning.** We include CoT-based  
617 baselines as they are standard approach in the liter-  
618 ature and represent a widely adopted methodology,  
619 ensuring our evaluation is grounded in established  
620 practices.

- **Rank1** (Weller et al., 2025) and **Rank-R1** (Zhuang et al., 2025) are strong CoT-based reasoning models. Rank1 is fine-tuned on reasoning traces, while Rank-R1 further enhances this capability through reinforcement learning. We select these models over earlier

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methods like ReAct (Yao et al., 2023) because  
they are specifically adapted for IR and rep-  
resent the leading CoT-based methods in this  
domain.

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• **O1-Pruner** (Luo et al., 2025) focuses on the  
efficiency of CoT. It employs reinforcement  
learning to compress the lengthy reasoning  
paths generated by CoT models, aiming to  
reduce computational overhead without sacri-  
ficing the final answer quality.

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**State-based Reasoning.** We include state-based  
baselines to compare EMR, aiming to demonstrate  
not only superior overall performance but also  
how our proposed episodic memory component  
enhances the efficiency of state transitions.

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• **SMR** (Lee et al., 2025) frames the multi-step  
retrieval process as a Markov Decision Pro-  
cess. At each step, a policy model observes  
the current state (e.g., the query and retrieved  
documents) and selects a discrete action to  
transition to the next state, finally building a  
set of relevant documents for the answer.

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**Retriever.** We include both a traditional sparse  
retriever and a strong dense retriever to investi-  
gate the synergy between the retrieval backbone  
and EMR. This comparison is crucial to demon-  
strate that the benefits of EMR are orthogonal to  
the retriever’s capabilities. Our method provides  
consistent improvements even when paired with a  
more powerful retriever.

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• **BM25** (Robertson et al., 2009) serves as our  
traditional sparse retrieval baseline. It is a  
keyword-based algorithm that has been a long-  
standing and robust baseline in IR for decades,  
relying on term frequency and inverse docu-  
ment frequency.

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• **ReasonIR** (Shao et al., 2025) represents  
a strong baseline in dense retrieval for  
reasoning-intensive IR. It is highly effective  
for tasks that require understanding context  
and intent beyond simple keyword match-  
ing. Its strong performance over other notable  
dense retrievers like Contriever (Izacard et al.,  
2021) and RankLLaMA (Ma et al., 2024)  
makes it a challenging and relevant baseline.

## 672 A.2 Implementation Details

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**Models and Adaptations.** The baseline mod-  
els used in our experiments are derived from var-  
ious LLMs. Rank1-32B utilizes Qwen2.5-32B<sup>1</sup>

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as its backbone, while Rank-R1-14B is built upon  
Qwen2.5-14B<sup>2</sup>. Due to the absence of a 32B ver-  
sion for Rank-R1, our experiments employ the 14B  
model. For O1-Pruner, which is not inherently a  
retrieval model, we implemented a custom prompt  
to enable query rewriting and document rerank-  
ing functionalities; its 32B version originates from  
QwQ-32B-preview<sup>3</sup>. To ensure a fair and compre-  
hensive evaluation, we also benchmark against the  
base LLMs, Qwen2.5-32B<sup>1</sup> and Qwen3-32B<sup>4</sup>.

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**Experimental Settings.** All experiments were  
performed on a single NVIDIA A6000 GPU. The  
hyperparameters for EMR were fixed across all  
datasets and models unless otherwise stated: we  
set the batch size to 8, LLM temperature to 0.1,  
top- $k$  for retrieval to 10, and the maximum number  
of reasoning steps to 16. For calculating computa-  
tional cost, we define token usage as the sum of all  
input tokens across the reasoning process.

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To ensure a fair comparison and isolate the im-  
provements of our method, we use the same system  
prompt as SMR for our policy model, as shown in  
**Table 5**. This approach mitigates potential perfor-  
mance differences due to prompt variations.

## 695 A.3 Evaluation on Other Metrics

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To further demonstrate the robustness of our pro-  
posed method, this section supplements the pri-  
mary nDCG@10 evaluation with results on ad-  
ditional metrics. We evaluated performance on  
the BRIGHT benchmark using BM25 as the re-  
triever, measuring results with two additional met-  
rics: MAP@10 (shown in **Table 6**) and Recall@10  
(shown in **Table 7**). Consistent with our main find-  
ings, EMR maintains a clear performance advan-  
tage over both CoT and compressed CoT baselines  
across these metrics.

## 712 A.4 Token Efficiency

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We assess the token efficiency of EMR by com-  
paring its token consumption to that of SMR under  
the same experimental setup (top- $k$ =10). **Ta-**  
**ble 8** shows that EMR is more efficient, requiring  
about 72% fewer tokens on average. This demon-  
strates that the episodic memory in EMR not only  
enhances retrieval performance but also achieves  
superior token efficiency.

<sup>1</sup>Qwen/Qwen2.5-32B-Instruct

<sup>2</sup>Qwen/Qwen2.5-14B-Instruct

<sup>3</sup>Qwen/QwQ-32B-Preview

<sup>4</sup>Qwen/Qwen3-32B-FP8

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You are a highly intelligent artificial agent responsible for managing a search system. Your role is to either refine the given query or re-rank retrieved search results, thereby enhancing both recall and precision of the search. You can output exactly one of the following operations, after which another agent will execute it and return the results to you.

## Input Format

The input provided to you will have the following structure:

```
```
{
  "query": "<current version of a query>",
  "ranks": [
    {"<docid>", "document contents"},
    {"<docid>", "document contents"},
    ...
  ]
}
````
```

### Decision policy (check in order):

1. Query Refinement

- Choose "action = refine" if any of the following are met:
- The query is ambiguous or generic
  - The retrieved search results are unsatisfactory
  - The query is short
  - Key domain terms are missing in the query

2. Re-ranking

- Choose "action = refine" only if the query already looks good and at least one retrieved document seems on-topic.

3. Stop

- Choose "action = stop" only when you are \*certain\* that no further improvement is possible.

## Possible Outputs (select exactly one)

### Query Refinement

You may refine the query by rewriting it into a clear, specific, and formal version that is better suited for retrieving relevant information from a list of passages. Only return the document IDs (`docid`) in the `reranked` list. Do not include document contents. Output format:

```
```
{
  "action": "refine",
  "query": "<refined version of a query>",
  "reason": "<reason for this action>"
}
````
```

### Re-ranking

You may reorder the retrieved documents (do not remove non-relevant ones). The results should be sorted in descending order of relevance. Output format:

```
```
{
  "action": "rerank",
  "ranks": ["<docid>", "<docid>", ...],
  "reason": "<reason for this action>"
}
````
```

### Stop

You may stop this iteration when the results are satisfactory. Output format:

```
```
{
  "action": "stop",
  "reason": "<reason for this action>"
}
````
```

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Table 5: System prompt used in EMR.

|  | Bio         | Earth       | Econ        | Psy         | Rob         | Stack       | Sus         | Leet        | Pony       | AoPS       | TheoQ       | TheoT       | Avg         |
|--|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|------------|------------|-------------|-------------|-------------|
| <b>Retriever</b>                                       |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25   | 13.1        | 18.1        | 8.9         | 7.0         | 8.5         | 13.4        | 10.0        | 19.7        | 1.6        | 6.2        | 10.4        | 4.9         | 10.2        |
| <b>Cot-based Reasoning</b>                             |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + Rank1   | 16.1        | 23.0        | 7.9         | 11.3        | 10.5        | 12.3        | 16.2        | 17.6        | <b>2.2</b> | 3.1        | 10.4        | 8.6         | 11.6        |
| BM25 + Rank-R1   | 17.7        | 25.0        | 10.3        | 10.7        | 14.1        | 13.1        | 16.1        | 20.2        | 2.1        | 4.9        | 10.8        | 7.7         | 12.7        |
| BM25 + O1-Pruner                                       | 17.2        | 22.6        | 10.7        | 12.9        | 12.7        | 14.9        | 15.5        | 19.5        | 1.8        | 3.7        | 8.9         | 5.6         | 12.2        |
| <b>State-based Reasoning</b>                           |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + SMR (Qwen2.5)                                   | 22.0        | 25.7        | 13.6        | 15.4        | 15.0        | 15.5        | 16.6        | 21.0        | 1.6        | 3.1        | 14.1        | 15.2        | 14.9        |
| BM25 + SMR (Qwen3)                                     | 23.1        | 24.4        | 14.0        | 15.7        | 15.3        | 16.2        | 17.0        | 21.8        | 1.9        | 3.4        | 16.2        | 15.4        | 15.4        |
| <b>EMR: State-based Reasoning with Episodic Memory</b> |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + EMR (Qwen2.5)                                   | 33.9        | 42.1        | <b>16.1</b> | 26.3        | 15.2        | 17.3        | 19.7        | <b>22.0</b> | 1.9        | 4.0        | <b>24.2</b> | <b>25.8</b> | <b>20.7</b> |
| BM25 + EMR (Qwen3)                                     | <b>44.3</b> | <b>44.5</b> | 15.4        | <b>28.2</b> | <b>17.3</b> | <b>20.5</b> | <b>24.6</b> | 10.4        | <b>2.2</b> | <b>4.2</b> | 19.1        | 15.2        | 20.5        |

Table 6: Retrieval performance (MAP@10) on the **BRIGHT** benchmark using **BM25** as the underlying retriever. All methods differ only in their reasoning strategy. Best scores per dataset are bolded.

|  | Bio         | Earth       | Econ        | Psy         | Rob         | Stack       | Sus         | Leet        | Pony       | AoPS       | TheoQ       | TheoT       | Avg         |
|--|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|------------|------------|-------------|-------------|-------------|
| <b>Retriever</b>                                       |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25   | 21.7        | 31.9        | 16.8        | 15.6        | 19.6        | 21.3        | 21.3        | 29.5        | 4.1        | 6.0        | 8.6         | 9.2         | 17.1        |
| <b>Cot-based Reasoning</b>                             |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + Rank1   | 21.7        | 31.9        | <b>16.8</b> | 15.6        | 19.6        | 21.3        | 21.3        | 29.5        | 4.1        | 6.0        | 8.6         | 9.2         | 17.1        |
| BM25 + Rank-R1   | 21.7        | 31.9        | 16.8        | 15.6        | 19.6        | 21.3        | 21.3        | 29.5        | 4.1        | 6.0        | 8.6         | 9.2         | 17.1        |
| BM25 + O1-Pruner                                       | 23.8        | 34.4        | 20.2        | 19.8        | 19.6        | 21.3        | 21.5        | 29.5        | 2.3        | 6.0        | 12.9        | 10.3        | 18.5        |
| <b>State-based Reasoning</b>                           |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + SMR (Qwen2.5)                                   | 25.3        | 33.0        | 19.5        | 21.7        | 21.4        | 24.6        | 21.6        | 26.6        | 3.6        | 6.1        | 20.9        | 24.8        | 20.8        |
| BM25 + SMR (Qwen3)                                     | 25.9        | 34.1        | 22.9        | 22.4        | 20.8        | 25.0        | 22.1        | 27.2        | 3.7        | 6.6        | 21.3        | 25.1        | 21.1        |
| <b>EMR: State-based Reasoning with Episodic Memory</b> |             |             |             |             |             |             |             |             |            |            |             |             |             |
| BM25 + EMR (Qwen2.5)                                   | 38.3        | 47.0        | <b>23.3</b> | 34.5        | 17.4        | 29.1        | 26.8        | <b>30.7</b> | <b>4.3</b> | 6.4        | <b>26.0</b> | <b>30.7</b> | 26.2        |
| BM25 + EMR (Qwen3)                                     | <b>52.8</b> | <b>53.7</b> | 23.2        | <b>38.3</b> | <b>24.3</b> | <b>32.5</b> | <b>31.2</b> | 25.6        | <b>4.3</b> | <b>6.9</b> | 21.0        | 17.9        | <b>27.6</b> |

Table 7: Retrieval performance (Recall@10) on the **BRIGHT** benchmark using **BM25** as the underlying retriever. All methods differ only in their reasoning strategy. Best scores per dataset are bolded.

| Dataset        | SMR  | EMR | Reduction |
|----------------|------|-----|-----------|
| bio            | 10.5 | 4.4 | -58.1%    |
| earth          | 40.7 | 5.0 | -87.7%    |
| econ           | 14.3 | 3.8 | -73.2%    |
| psy            | 22.7 | 3.4 | -85.1%    |
| rob            | 18.5 | 6.7 | -63.8%    |
| stack          | 30.2 | 5.1 | -83.0%    |
| sus            | 13.8 | 5.1 | -62.8%    |
| leet           | 6.5  | 5.0 | -22.6%    |
| pony           | 5.0  | 2.0 | -60.1%    |
| aops           | 3.3  | 2.9 | -11.0%    |
| theoq          | 6.2  | 4.3 | -31.0%    |
| theot          | 3.9  | 1.3 | -66.9%    |
| <b>Average</b> | 14.6 | 4.1 | -72.1%    |

Table 8: Comparison of token usage (in millions) between EMR and SMR across various datasets in the BRIGHT benchmark. The values represent the total number of input tokens required per task. The final column shows the average of all datasets.