

Summary Report

A Regression Model to predict the Market Value of Housing Units in Year 2013

Business question: What predicts 2013 market value of single family housing units?

Linear regression analysis was conducted to identify any relationship between variables within the Housing Affordability Data System dataset regarding factors that predict the current market value of single family housing units for 2013. The conclusion of the analysis was that there are many factors that predict the housing or current market value of single family units for 2013. Factors that have statistical significance and seem to contribute are:

- * BEDRMS 2011: number of bedrooms in the housing unit
- * LMED 2011: average median income for the area
- * FMR 2011: cost or fair market monthly rental rate of the housing unit
- * BUILT 2011: the year in which the housing unit was built
- * ROOMS 2011: number of rooms in the housing unit
- * REGION 2011: location in the United States of the housing unit; however, there is no statistical significance in market value of the housing unit and the housing unit being located in the midwest region of the US as compared to the southern region
- * METRO3: location to metropolitan city of the housing unit
- * ZINC2 2011: annual household income of the occupant of the housing unit
- * AGE 2011: Age of head of household of the housing unit
- * VALUE 2011: Market value of housing unit

Regression model listed below:

$$\ln(\text{VALUE}_{2013}) = \beta_0 + \beta_1 \text{AGE}_{2011} + \beta_2 \text{BEDRMS}_{2011} + \beta_3 \ln(\text{PER}_{2011}) + \beta_4 \text{REGION_WEST} + \beta_5 \text{REGION_MIDWEST} + \beta_6 \text{REGION_NORTHEAST} + \beta_7 \ln(\text{LMED}_{2011}) + \beta_8 \ln(\text{FMR}_{2011}) + \beta_9 \ln(\text{BUILT}_{2011}) + \beta_{10} \ln(\text{VALUE}_{2011}) + \beta_{11} \ln(\text{ZINC2}_{2011}) + \beta_{12} \text{ROOMS}_{2011} + \beta_{13} \text{ZADEQ_ADEQUACY} + \beta_{14} \text{ALL_OTHER_METROS} + \beta_{15} \ln(\text{LN_UTILITY}_{2011}) + \beta_{16} \ln(\text{OTHERCOST}_{2011})$$

Interpretation of regression model predictor variables and their coefficients in relation to outcome variable (VALUE 2013):

- * Intercept: has no practical managerial value
- * β_1 : a year increase in age for the head of household corresponds to 0.086% increase in market value of housing unit, all other variables held at their current level.
- * β_2 : an increase of one bedroom corresponds to 3.588% decrease in market value of the housing unit, all other variables held at their current level.
- * β_3 : there is no statistical significance for the market value of the housing unit and the number of people in the household, all other variables held at their current level.
- * β_4 : when the housing unit is located in the western region of the US the market value of the housing unit increases by 10.026% as compared to the southern region of the US, all other variables held at their current level.
- * β_5 : there is no statistical significance for the market value of the housing unit and the housing unit being located in the midwest.
- * β_6 : when the housing unit is located in the northeastern region of the US, the market value of the housing unit increases by 3.180% as compared to the southern region of the US all other variables held at their current level.
- * β_7 : each dollar increase in area median income corresponds to a 0.178% increase in market value of the housing unit all other variables held at their current level.
- * β_8 : a 1% change in fair market monthly rent corresponds to a 0.355% increase in market value of the housing unit all other variables held at their current level.
- * β_9 : a 1% change in the year the housing unit was built corresponds to a 3.708% increase in market value of housing unit all other variables held at their current level.
- * β_{10} : a 1% change in the current market value of the unit corresponds to a 0.587% change in current market value of the unit, all other variables held at their current level.
- * β_{11} : a 1% increase in annual household income is associated with a 0.0468% increase in market value of the housing unit, all other variables held at their current level.
- * β_{12} : one additional room in the housing unit corresponds to a 4.969% increase in market value of the housing unit all other variables held at their current level.
- * β_{13} : there is no statistical significance for the market value of the housing unit when the housing unit is in moderately inadequate condition or severely inadequate condition compared to adequate condition, all other variables held at their current level.
- * β_{14} : when the housing unit is located outside of the "Central City" metropolitan area, the market value of the housing unit increases by 4.256% as compared to the "Central City" metropolitan area, all other variables held at their current level.
- * β_{15} : there is no statistical significance for the market value and monthly utility costs for the housing unit, all other variables held at their current level.
- * β_{16} : there is no statistical significance for the market value and the sum of other monthly costs for the housing unit, all other variables held at their current level.

Prediction in the 'Hold-out' Data:

The regression model has a R-square of 0.59 since we added the Market Value for year 2011 as an additional 'X' variable, suggesting the linear regression model explains 59% of the market value variation. Using the coefficients from this regression model and using the set of 'X' variables in the hold out data we make predictions of the Market Value for the 1000 housing units held out. The MAD statistic (Mean Absolute Deviation) for the prediction turns out to be \$100,974.19 with the average Market Value is around \$251,403.08.

Please see the worksheet 'Statistical Tests' for various calculations

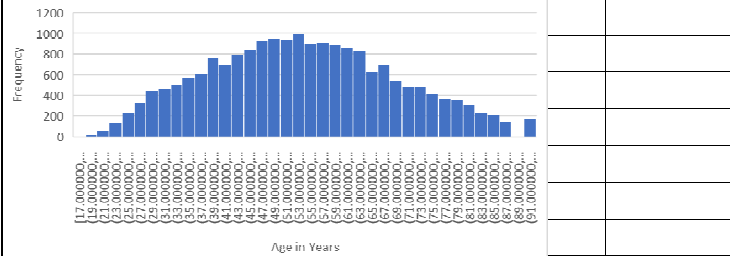
Descriptive Statistics			
AGE 2011		BEDRMS 2011	
Mean	55.22127875	Mean	3.249380844
Standard Error	0.109974	Standard Error	0.005888297
Median	55	Median	3
Mode	54	Mode	3
Standard Deviation	15.46885076	Standard Deviation	0.828242959
Sample Variance	239.2853438	Sample Variance	0.685986399
Kurtosis	-0.590702367	Kurtosis	1.004500518
Skewness	0.163535941	Skewness	0.460139258
Range	76	Range	8
Minimum	17	Minimum	0
Maximum	93	Maximum	8
Sum	1092553	Sum	64289
Count	19785	Count	19785
LN_BUILT_2011		LN_VALUE_2011	
Mean	7.585383202	Mean	12.11047694
Standard Error	9.52887E-05	Standard Error	0.00532507
Median	7.588323677	Median	12.08390501
Mode	7.575584652	Mode	12.20607265
Standard Deviation	0.013403228	Standard Deviation	0.749019879
Sample Variance	0.000179647	Sample Variance	0.561030779
Kurtosis	-0.849976792	Kurtosis	0.931277436
Skewness	-0.38962876	Skewness	0.092541652
Range	0.046827894	Range	7.293954882
Minimum	7.559559496	Minimum	8.006367568
Maximum	7.60638739	Maximum	15.30032245
Sum	150076.8066	Sum	239605.7862
Count	19785	Count	19785
REGION_MIDWEST		REGION_WEST	
Mean	0.2686884	Mean	0.197624463
Standard Error	0.00315151	Standard Error	0.00283108
Median	0	Median	0
Mode	0	Mode	0
Standard Deviation	0.443288705	Standard Deviation	0.39821734
Sample Variance	0.196504876	Sample Variance	0.15857705
Kurtosis	-0.910737423	Kurtosis	0.306782283
Skewness	1.043721539	Skewness	1.518799289
Range	1	Range	1
Minimum	0	Minimum	0
Maximum	1	Maximum	1
Sum	5316	Sum	3910
Count	19785	Count	19785
ZADEQ_ADEQUACY		LN_VALUE_2013	
Mean	0.02254233	Mean	12.11570431
Standard Error	0.001055337	Standard Error	0.005484881
Median	0	Median	12.10071213
Mode	0	Mode	11.91839057
Standard Deviation	0.148442875	Standard Deviation	0.771498698
Sample Variance	0.022035287	Sample Variance	0.595210241
Kurtosis	39.39430689	Kurtosis	0.881243026
Skewness	6.433531275	Skewness	0.022273443
Range	1	Range	5.529429088
Minimum	0	Minimum	9.210340372
Maximum	1	Maximum	14.73976946
Sum	446	Sum	239709.2098
Count	19785	Count	19785

Descriptive Statistics							
LN_PER 2011			LN_LMED_2011			LN_FMR_2011	
Mean	0.840226356		Mean	11.09115698		Mean	7.033712121
Standard Error	0.00377795		Standard Error	0.001208243		Standard Error	0.002212717
Median	0.693147181		Median	11.05888967		Median	6.98471632
Mode	0.693147181		Mode	11.04780589		Mode	6.873163834
Standard Deviation	0.531403295		Standard Deviation	0.169950414		Standard Deviation	0.311238944
Sample Variance	0.282389462		Sample Variance	0.028883143		Sample Variance	0.09686968
Kurtosis	-0.714695205		Kurtosis	0.76158575		Kurtosis	1.367973905
Skewness	-0.081619987		Skewness	0.555166688		Skewness	0.591471501
Range	2.63905733		Range	1.323534672		Range	4.980758223
Minimum	0		Minimum	10.42525312		Minimum	6.03787092
Maximum	2.63905733		Maximum	11.74878779		Maximum	11.01862914
Sum	16623.87846		Sum	219438.5409		Sum	139161.9943
Count	19785		Count	19785		Count	19785
LN_ZINC2_2011			ROOMS 2011			REGION_NORTHEAST	
Mean	10.97168439		Mean	6.626585797		Mean	0.172251706
Standard Error	0.006846798		Standard Error	0.011416061		Standard Error	0.002684565
Median	11.08214255		Median	6		Median	0
Mode	11.5125654		Mode	6		Mode	0
Standard Deviation	0.963064856		Standard Deviation	1.605773548		Standard Deviation	0.37760861
Sample Variance	0.927493917		Sample Variance	2.578508687		Sample Variance	0.142588263
Kurtosis	8.289383131		Kurtosis	1.017184133		Kurtosis	1.014113978
Skewness	-1.583833585		Skewness	0.768274335		Skewness	1.73609086
Range	13.13244637		Range	13		Range	1
Minimum	0		Minimum	1		Minimum	0
Maximum	13.13244637		Maximum	14		Maximum	1
Sum	217074.7757		Sum	131107		Sum	3408
Count	19785		Count	19785		Count	19785
ALL_OTHER_METROS			LN_UTILITY_2011			LN_OTHERCOST_2011	
Mean	0.783219611		Mean	5.90253816		Mean	4.23590979
Standard Error	0.002929508		Standard Error	0.371531275		Standard Error	0.005248702
Median	1		Median	5.537334267		Median	4.199705078
Mode	1		Mode	5.438079309		Mode	3.912023005
Standard Deviation	0.412062173		Standard Deviation	52.25927793		Standard Deviation	0.738278081
Sample Variance	0.169795234		Sample Variance	2731.03213		Sample Variance	0.545054525
Kurtosis	-0.109980048		Kurtosis	19782.01436		Kurtosis	1.06566732
Skewness	-1.374784012		Skewness	140.6432433		Skewness	0.080699969
Range	1		Range	7353.793559		Range	7.362116366
Minimum	0		Minimum	2.206441232		Minimum	0
Maximum	1		Maximum	7356		Maximum	7.362116366
Sum	15496		Sum	116781.7175		Sum	83807.47519
Count	19785		Count	19785		Count	19785
VALUE_2013							
Mean	249478.3927						
Standard Error	1866.826742						
Median	180000						
Mode	150000						
Standard Deviation	262586.2861						
Sample Variance	68951557674						
Kurtosis	36.20571861						
Skewness	4.941396009						
Range	2510000						
Minimum	10000						
Maximum	2520000						
Sum	4935930000						
Count	19785						

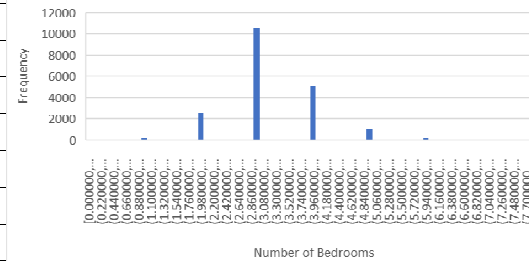
Graphs and Charts

Histograms

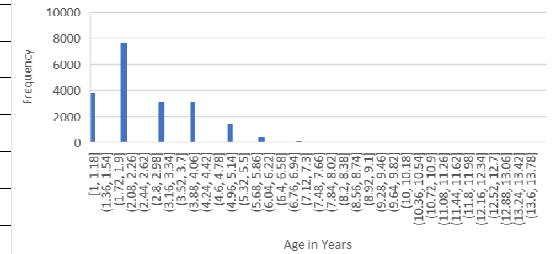
Age of Head of Household (AGE) 2011



Number of Bedrooms in Housing Unit (BEDRMS) 2011



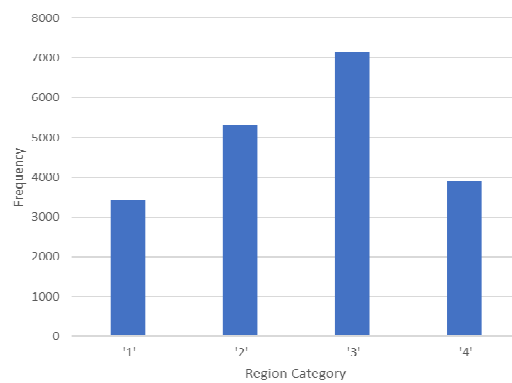
Persons Per Household (PER) 2011



Bar Graphs

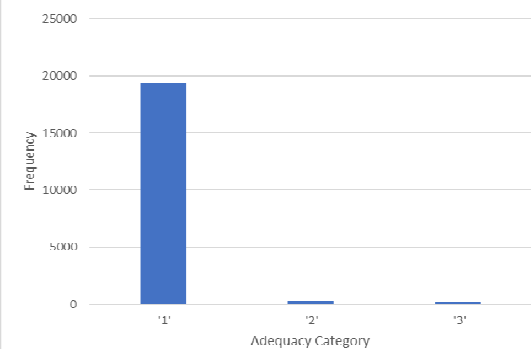
Category	Frequency
'1'	3408
'2'	5316
'3'	7151
'4'	3910

Region in US (REGION) 2011



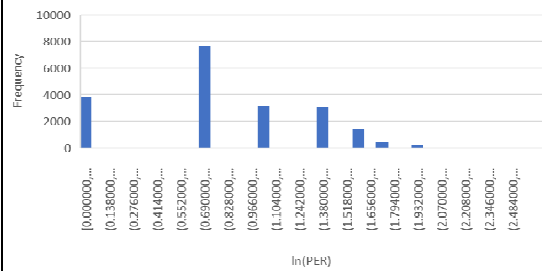
Category	Frequency
'1'	19339
'2'	284
'3'	162

Adequacy of Housing Unit (ZADEQ) 2011

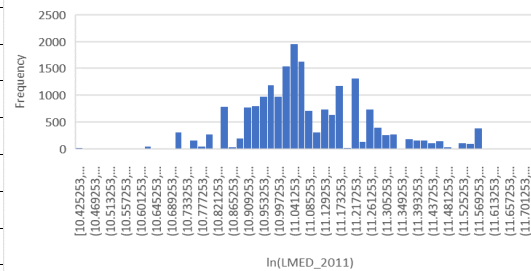


Transformed Variables: all natural log

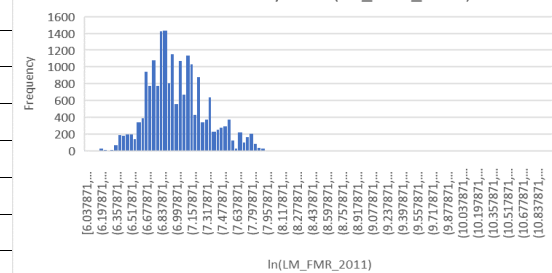
Persons Per Household (LN_PER_2011)



Area Median Income (LN_LMED_2011)

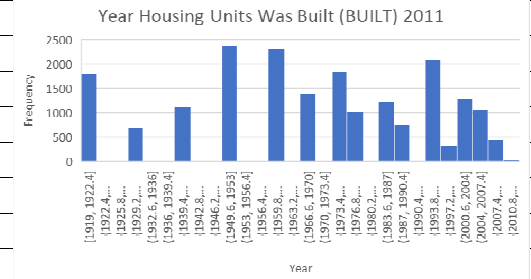
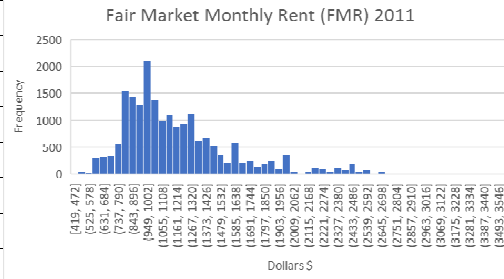
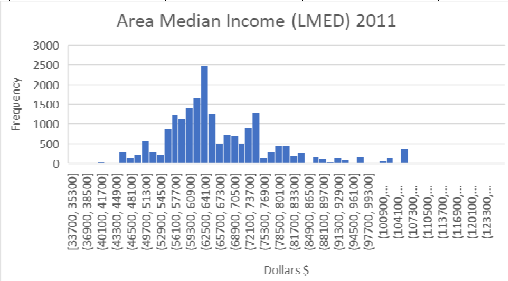


Fair Market Monthly Rent (LN_FMR_2011)



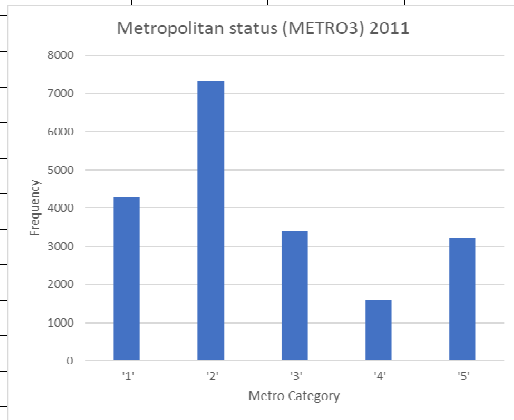
Graphs and Charts

Histograms

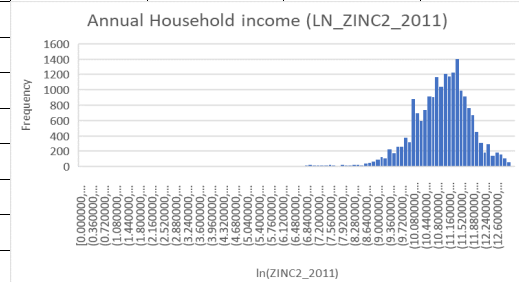
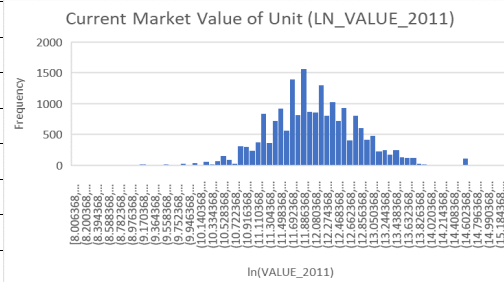
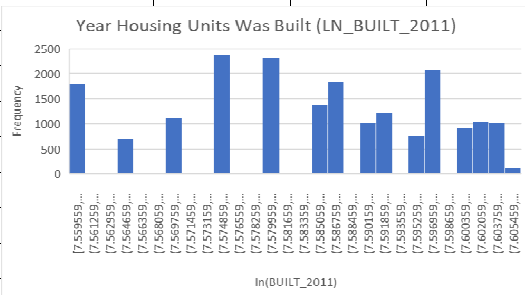


Bar Graphs

Category	Frequency
'1'	4289
'2'	7325
'3'	3375
'4'	1581
'5'	3215

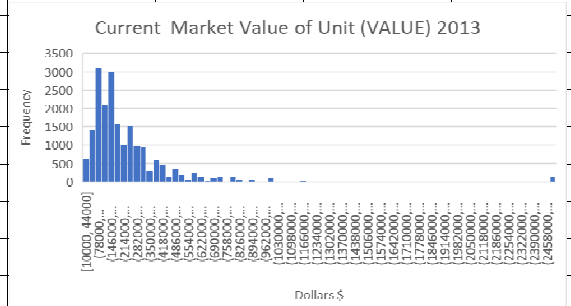
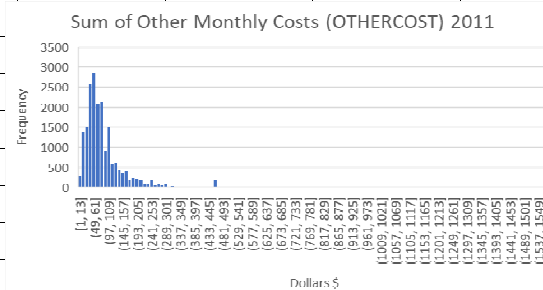
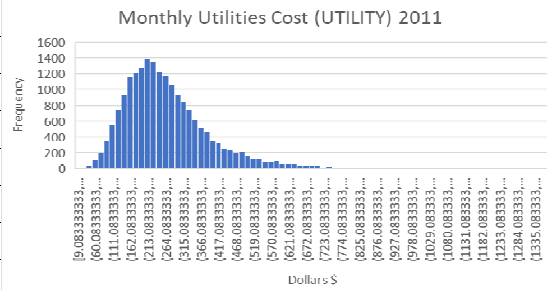
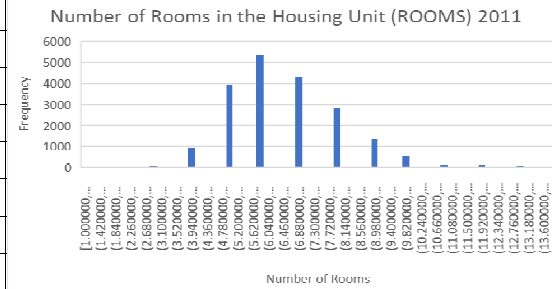
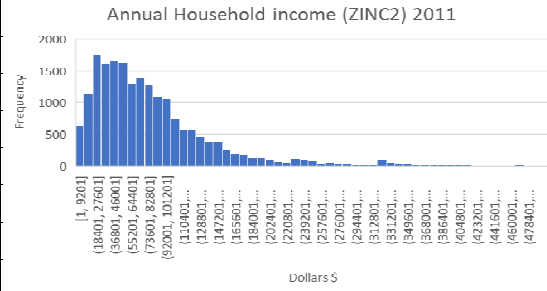
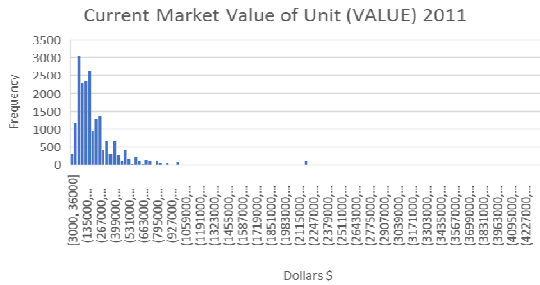


Transformed Variables: all natural log

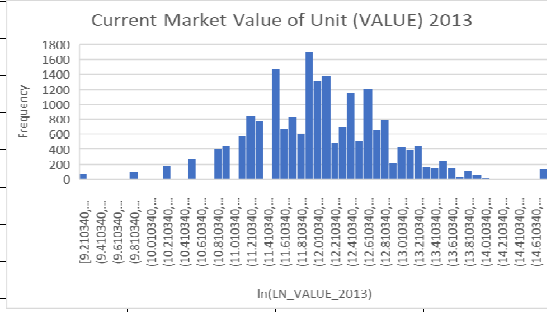
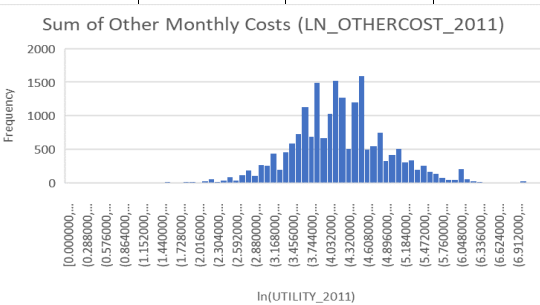


Graphs and Charts

Histograms



Transformed Variables: all natural log



SUMMARY OUTPUT

$$\begin{aligned} \ln(\text{VALUE } 2013) = & \beta_0 + \beta_1 \text{AGE} + \beta_2 \text{BEDRMS} + \beta_3 \ln(\text{LN_PER } 2011) \\ & + \beta_4 \text{REGION_WEST} + \beta_5 \text{REGION_MIDWEST} + \beta_6 \text{REGION_NORTHEAST} \\ & + \beta_7 \ln(\text{LN_LMED } 2011) + \beta_8 \ln(\text{LN_FMR } 2011) + \beta_9 \ln(\text{LN_BUILT } 2011) \\ & + \beta_{10} \ln(\text{LN_VALUE } 2011) + \beta_{11} \ln(\text{LN_ZINC2 } 2011) + \beta_{12} \text{ROOMS } 2011 \\ & + \beta_{13} \text{ZADEQ_ADEQUACY} + \beta_{14} \text{ALL_OTHER_METROS} + \beta_{15} \ln(\text{LN_UTILITY } 2011) \\ & + \beta_{16} \ln(\text{LN_OTHERCOST } 2011) \end{aligned}$$

Regression Statistics

Multiple R	0.773180316	Note: "ALL_OTHER_METROS" is a dummy variable = 1 when METRO3 variable is = '1', otherwise it is =0
R Square	0.597807802	Note: "REGION_MIDWEST", "REGION_NORTHEAST" and "REGION_WEST" are dummy variables for the categorical variable REGION
Adjusted R Square	0.597482272	Note: "ZADEQ_ADEQUACY" is a dummy variable =1 when the categorical variable ZADEQ is ="2" OR "3", otherwise it is =0
Standard Error	0.489471832	Note: This regression also takes a logarithmic transformation of many of the 'X' variables
Observations	19785	Note: This regression also uses the natural logarithm of the 2011 Market Value as one of the 'X' variables

ANOVA

	df	SS	MS	F	Significance F
Regression	16	7039.569112	439.9730695	1836.414387	0
Residual	19768	4736.070301	0.239582674		
Total	19784	11775.63941			

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	-28.46876578	2.208516882	-12.89044517	7.24018E-38	-32.79764438	-24.13988718	-32.79764438	-24.13988718
AGE 2011	0.000868058	0.000257736	3.368013524	0.000758563	0.000362874	0.001373242	0.000362874	0.001373242
BEDRMS 2011	-0.035885372	0.007429493	-4.830123779	1.3747E-06	-0.050447802	-0.021322941	-0.050447802	-0.021322941
LN_PER 2011	-0.001230281	0.007836278	-0.15699808	0.875247965	-0.016590043	0.014129482	-0.016590043	0.014129482
REGION_WEST	0.100258313	0.011159758	8.983914661	2.84251E-19	0.07838425	0.122132376	0.07838425	0.122132376
REGION_MIDWEST	-0.002677998	0.010223408	-0.26194769	0.793364501	-0.022716737	0.017360741	-0.022716737	0.017360741
REGION_NORTHEAST	0.031800174	0.011871696	2.678654602	0.007397974	0.008530652	0.055069696	0.008530652	0.055069696
LN_LMED_2011	0.178080715	0.034186527	5.209090524	1.91672E-07	0.11107225	0.24508918	0.11107225	0.24508918
LN_FMR_2011	0.355400737	0.023762164	14.95658136	2.65904E-50	0.3088249	0.401976575	0.3088249	0.401976575
LN_BUILT_2011	3.708232994	0.287226705	12.91047428	5.59513E-38	3.145244525	4.271221463	3.145244525	4.271221463
LN_VALUE_2011	0.586730767	0.006650353	88.22550142	0	0.573695515	0.599766018	0.573695515	0.599766018
LN_ZINC2_2011	0.046791803	0.004296218	10.89139485	1.51704E-27	0.038370856	0.055212751	0.038370856	0.055212751
ROOMS 2011	0.049687272	0.003431601	14.47932762	2.85776E-47	0.042961046	0.056413498	0.042961046	0.056413498
ZADEQ_ADEQUACY	-0.036620853	0.023662464	-1.547634845	0.121726245	-0.08300127	0.009759563	-0.08300127	0.009759563
ALL_OTHER_METROS	0.042565793	0.008668048	4.910654818	9.14971E-07	0.02557569	0.059555896	0.02557569	0.059555896
LN_UTILITY_2011	3.84903E-05	6.6615E-05	0.577801714	0.563404579	-9.20808E-05	0.000169061	-9.20808E-05	0.000169061
LN_OTHERCOST_2011	0.010707253	0.00561791	1.905913896	0.056675867	-0.000304323	0.021718829	-0.000304323	0.021718829

Pairwise Correlation across all "X" variables in "Data for Estimation"																
	AGE 2011	BEDRMS 2011	LN_PER 2011	REGION_WEST	REGION_MIDWEST	REGION_NORTHEAST	LN_LMED_2011	LN_FMR 2011	LN_BUILT 2011	LN_VALUE 2011	LN_ZINC2 2011	ROOMS 2011	ZADEQ_ADEQUACY	ALL_OTHER_METROS	LN_UTILITY_2011	LN_OTHERCOST 2011
AGE 2011	1															
BEDRMS 2011	-0.113842141	1														
LN_PER 2011	-0.420884458	0.33144339	1													
REGION_WEST	-0.008215396	0.04535066	0.04396629	1												
REGION_MIDWEST	-0.018194589	-0.043188474	-0.020250119	-0.300818637	1											
REGION_NORTHEAST	0.022895832	-0.006608494	0.026182655	-0.226393592	-0.276506819	1										
LN_LMED_2011	-0.027009782	0.103166236	0.075704554	0.147587016	-0.091923158	0.390408332	1									
LN_FMR_2011	-0.053912095	0.46794254	0.217975391	0.425747734	-0.409588455	0.200657125	0.655984605	1								
LN_BUILT_2011	-0.151937581	0.15270929	0.114667856	0.068100776	-0.109826379	-0.191525044	-0.119031562	0.040950555	1							
LN_VALUE_2011	-0.011059779	0.34400851	0.153504992	0.253062638	-0.214230034	0.150377505	0.383143014	0.531501081	0.192223042	1						
LN_ZINC2_2011	-0.3069871	0.253593506	0.365731734	0.058837645	-0.028705184	0.045374549	0.16277149	0.225575388	0.153736244	0.369294806	1					
ROOMS 2011	-0.060209079	0.739940818	0.270393142	0.004351461	-0.014622942	0.036311417	0.140736976	0.342761774	0.129914906	0.41570461	0.31486811	1				
ZADEQ_ADEQUACY	0.020544438	-0.054359895	-0.018120514	-0.030047922	-0.025990007	0.010979435	-0.037823366	-0.045170812	-0.079025468	-0.095459756	-0.079685212	-0.052685844	1			
ALL_OTHER_METROS	0.025685303	0.023932706	0.005127435	-0.100847849	0.017268425	0.069448633	-0.068087086	-0.092601875	0.129021247	0.030824477	0.023349116	0.034026312	-0.009350927	1		
LN_UTILITY_2011	-0.01192511	0.000765193	-0.008334368	-0.00405662	-0.005840874	-0.001466795	-0.003163499	-0.001257905	0.002903875	0.005193316	0.0085949	0.004953757	-0.001227025	0.003361652	1	
LN_OTHERCOST_2011	-0.000372894	0.190489216	0.076954858	0.073909306	-0.15244744	0.010407759	0.147274902	0.297328915	0.212681702	0.502186043	0.237762222	0.250972854	-0.053872861	0.013917845	0.013469525	1