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# Workshop on Decomposition Methods

Vladimir Canudas-Romo, Joo Won Park and Wen Su

# Decomposing Fertility Measures



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Volume 75, 2021 - Issue 2

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Research Article

# Educational composition and parity contribution to completed cohort fertility change in low-fertility settings

Ester Lazzari , Ryohei Mogi & Vladimir Canudas-Romo

Pages 153-167 | Received 17 Jun 2020, Accepted 12 Jan 2021, Published online: 29 Mar 2021

Download citation <https://doi.org/10.1080/00324728.2021.1895291>



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## Abstract

Extensive literature has documented the contribution of rising women's education to decreases in completed cohort fertility (CCF). A key question related to the education-fertility relationship is to what extent the decrease in fertility is the result of changes in educational composition vs changes in fertility behaviours within educational categories. This study quantified the effect of educational expansion on fertility levels

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## Completed Cohort Fertility

$$CCF(t) = \frac{B(t)}{W(t)}$$

$$CCF(t) = \sum_{e=L}^H F^e(t) E^e(t)$$

## Education composition

$$E^e(t) = \frac{W^e(t)}{W(t)}$$

## Education-specific fertility

$$F^e(t) = \frac{B^e(t)}{W^e(t)}$$



## CCF decomposition

$$C\dot{C}F =$$

$$\sum_{e=L}^H [\dot{E}^e(t)F^e(t) + E^e(t)\dot{F}^e(t)]$$

# CFE database

## COHORT FERTILITY AND EDUCATION



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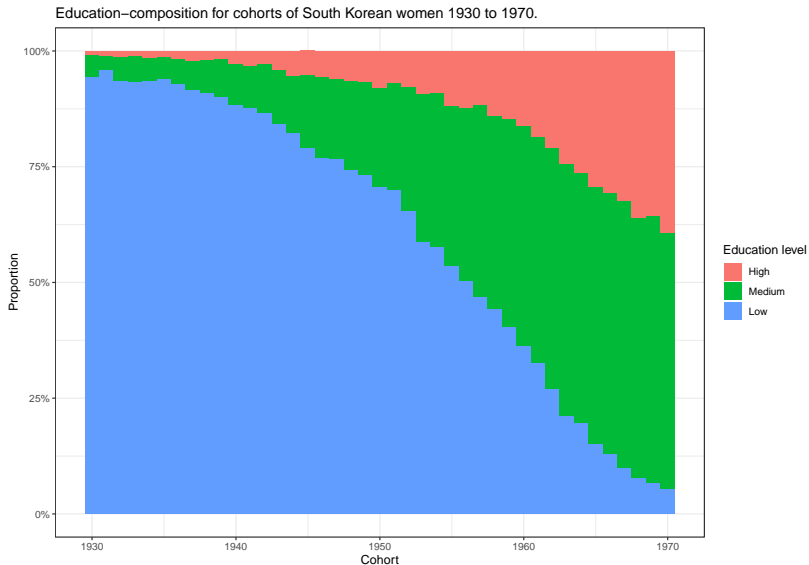
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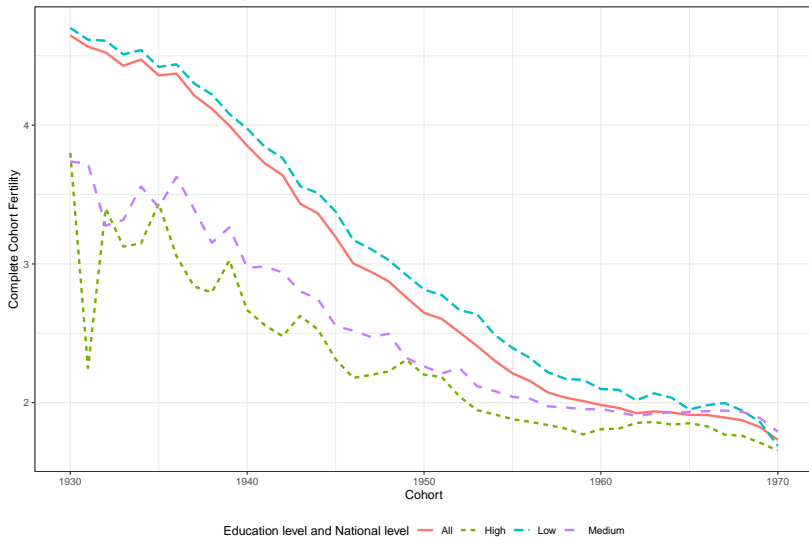
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# Education composition



# Fertility change

Korean Complete Cohort Fertility, 1930–1970

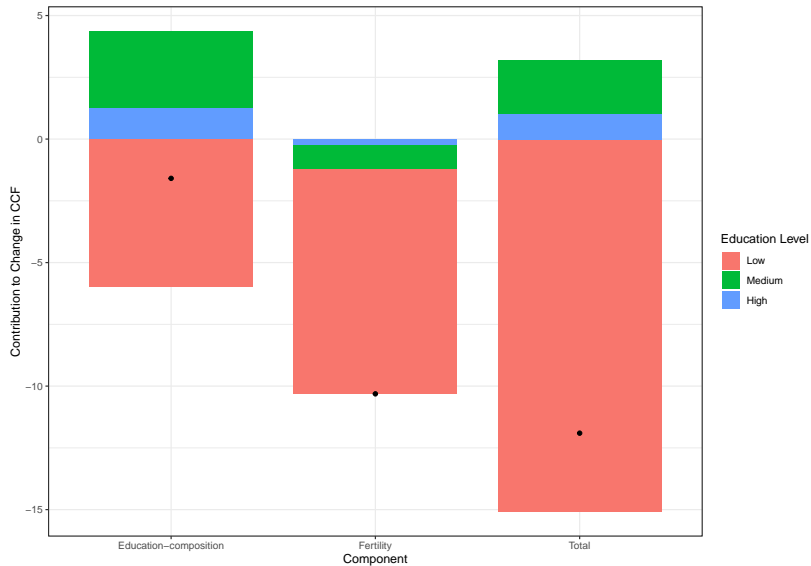


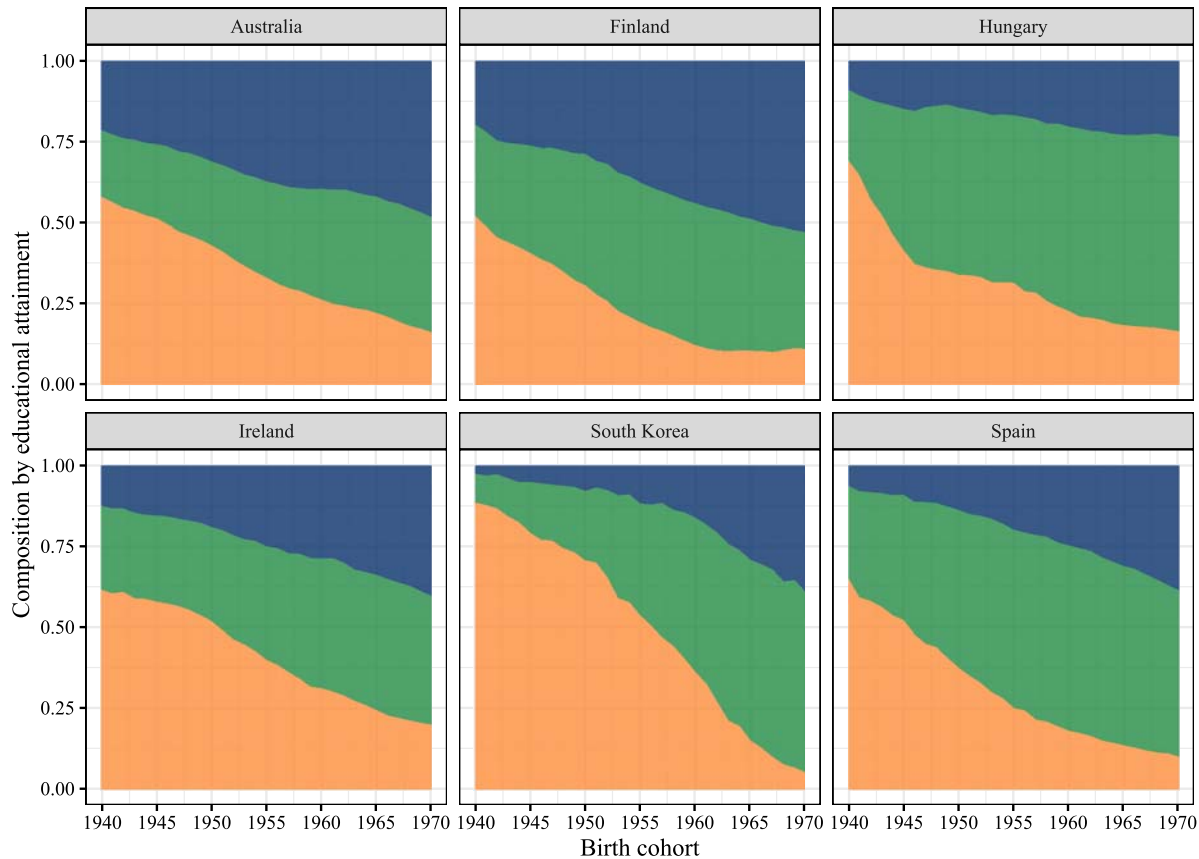
# CCF decomposition

Table 1: CCF decomposition

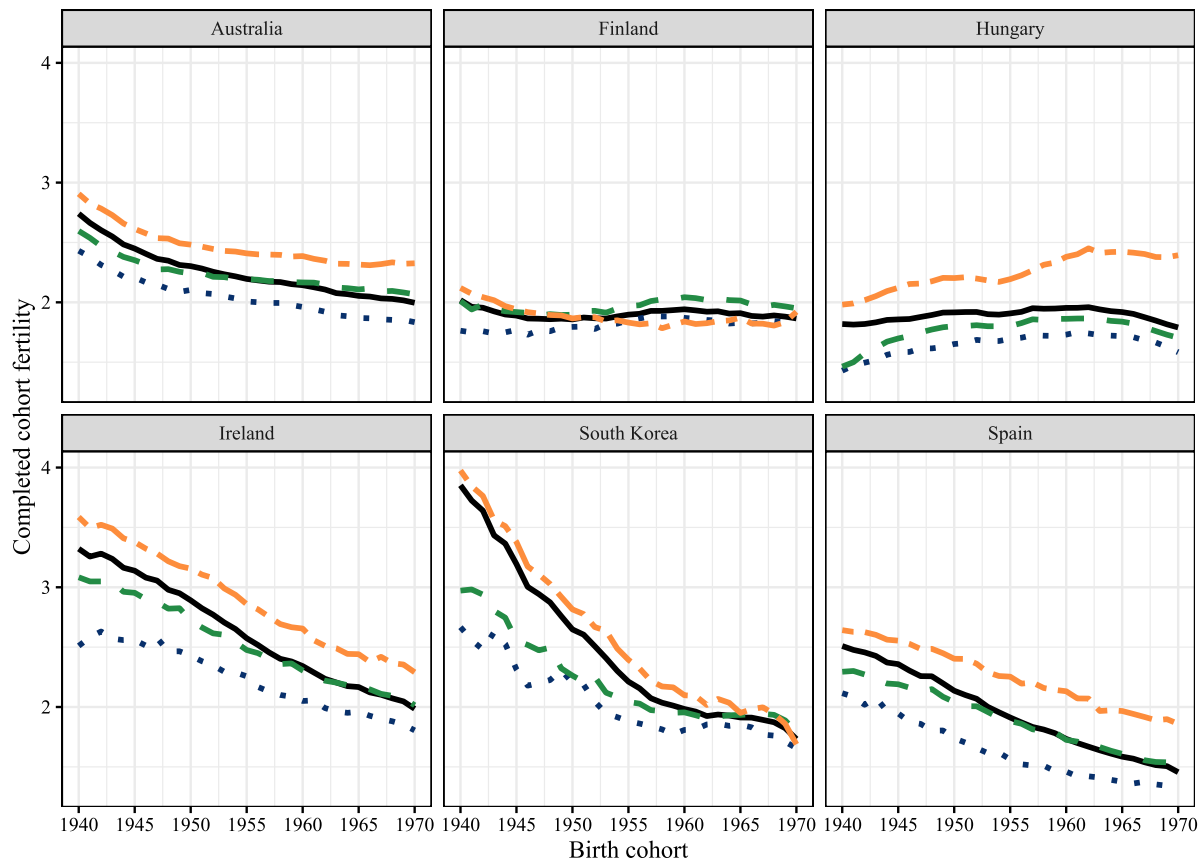
	Korea
CCF in 1940	3.850
CCF in 1950	2.650
Total annualized change	-0.119
Fertility component	-0.103
Education-composition component	-0.016

# CCF decomposition



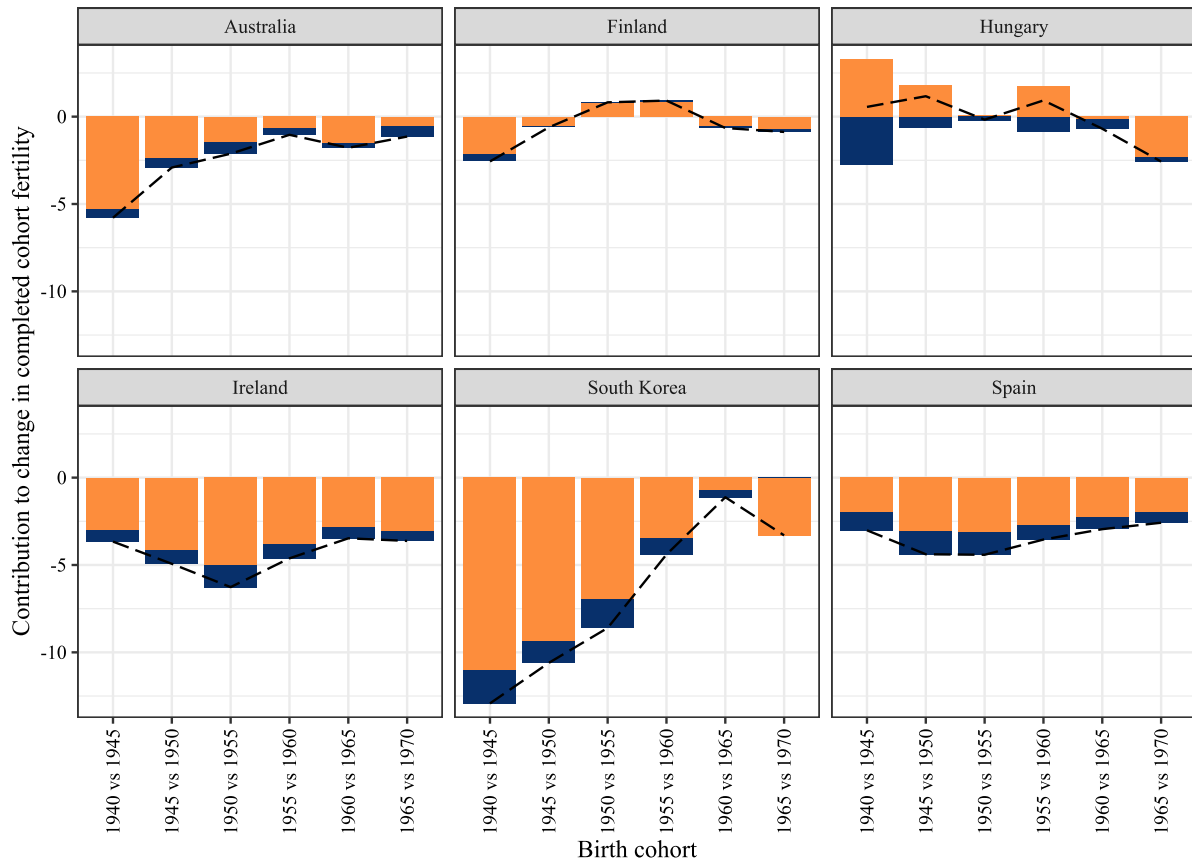


High Medium Low



— All    - - - High    - - - Medium    - - - Low





■ Educational composition (E) ■ Education-specific fertility (F)



RESEARCH ARTICLE | FEBRUARY 01 2021

## Cross-Sectional Average Length of Life Childless

Ryohei Mogi; Jessica Nisén; Vladimir Canudas-Romo

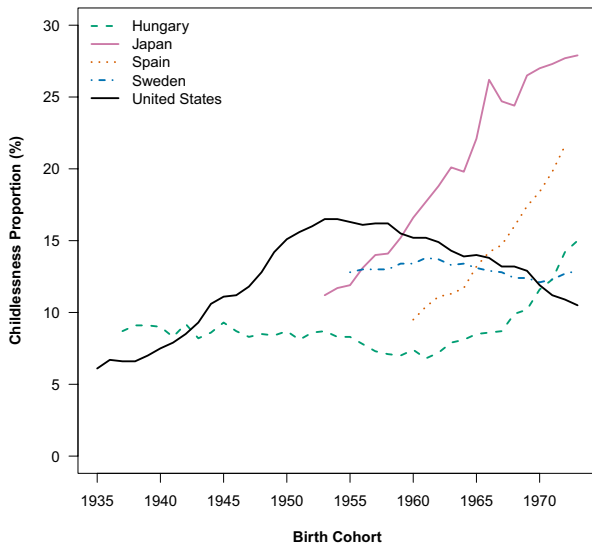
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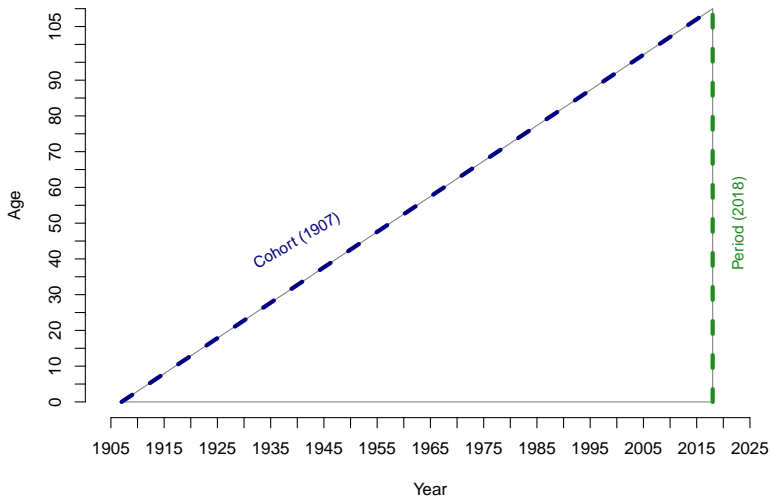
### Abstract

Increases in the average age at first birth and in the proportion of women remaining childless have extended the total number of years that women spend childless during their reproductive lifetime in several countries. To quantify the number of years that reproductive-age women live without children, we introduce the cross-sectional average length of life childless (CALC). This measure includes all the age-specific first-birth information available for the cohorts present at time  $t$ ; it is a period measure based on

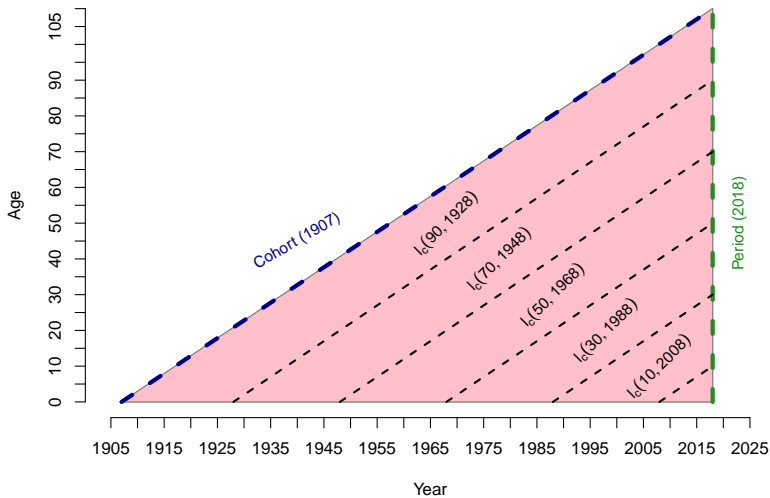


**Fig. 2** Childlessness rate at age 44 or older among women born in 1935–1973 in selected countries. *Source:* Authors' calculations using the Human Fertility Database.

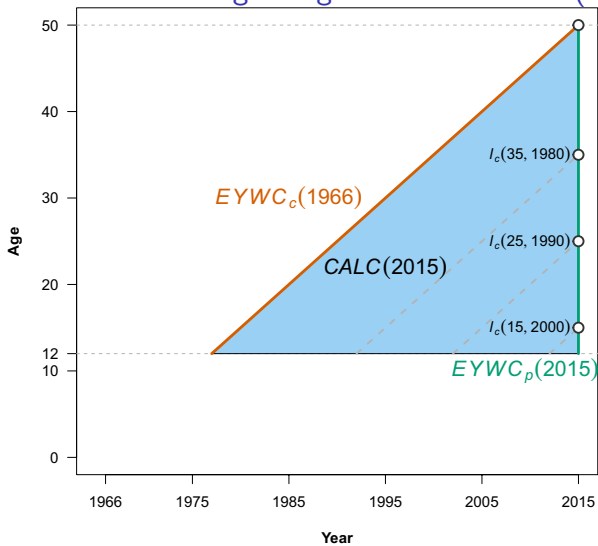
# Cross-sectional Average Length of Life (CAL)



# Cross-sectional Average Length of Life (CAL)



# Cross-sectional Average Length of Life Childless (*CALC*)



## Cross-sectional Average Length of Life Childless (*CALC*)

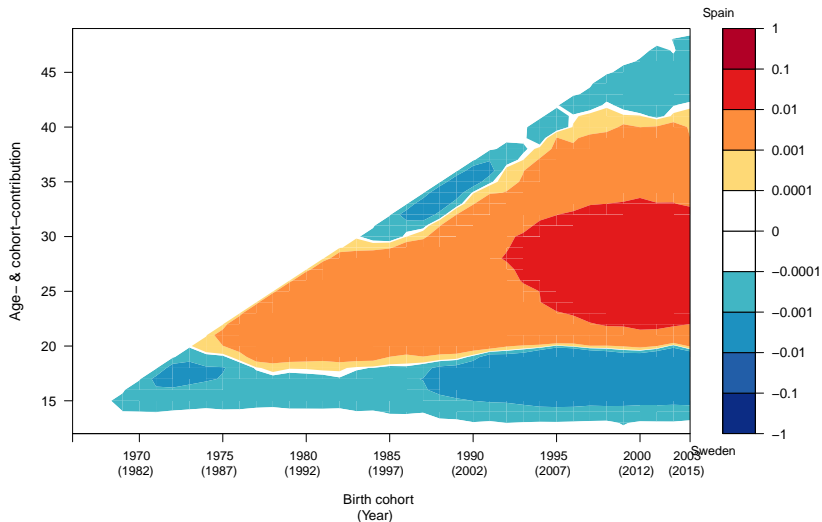
$$CALC(t) = \int_{12}^{50} \ell_c(x, t-x) dx$$

$$C\dot{A}LC(t, \xi) =$$

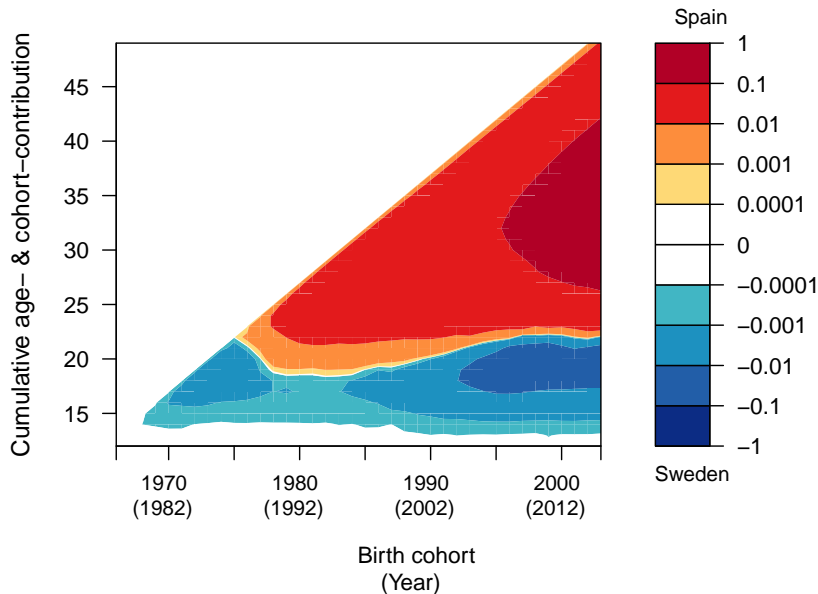
$$\int_{12}^{55} \ell_c(x, t-x, \xi) \sum_{a=12}^{x-1} \frac{\dot{p}_a(t-x, \xi)}{p_a(t-x, \xi)} dx$$

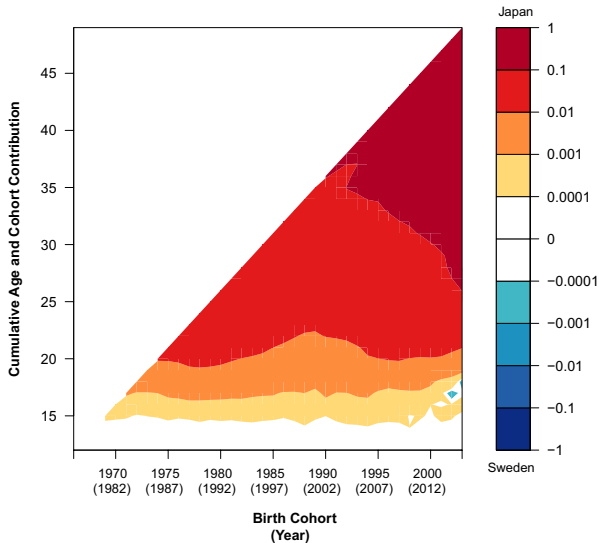


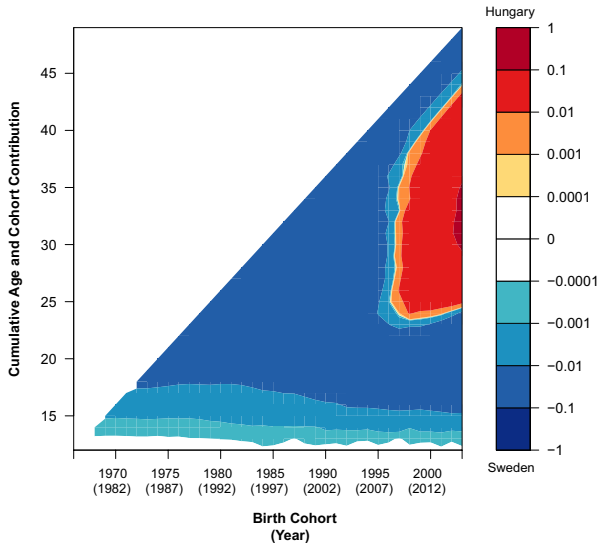
# CALC decomposition

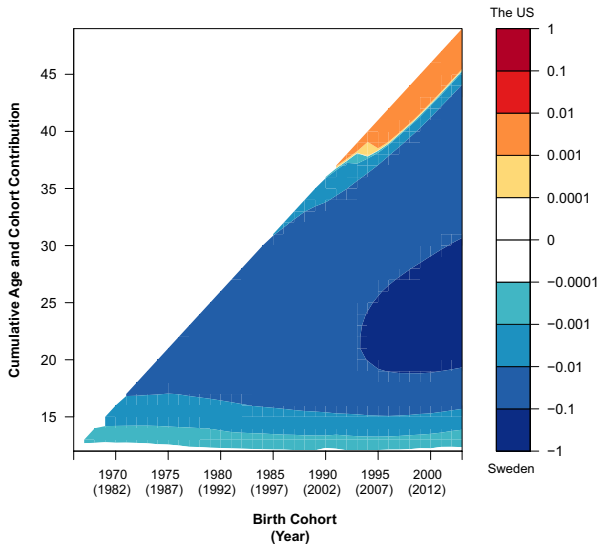


# CALC decomposition











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
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Research Article

# The contribution of survival to changes in the net reproduction rate

Tianyu Shen , Ester Lazzari  & Vladimir Canudas-Romo 

Pages 163-178 | Received 15 Jan 2022, Accepted 14 Nov 2022, Published online: 28 Mar 2023

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## Abstract

The net reproduction rate (NRR) is an alternative fertility measure to the more common total fertility rate (TFR) and accounts for the mortality context of the population studied. This study is the first to compare NRR trends in high- and low-income countries and to decompose NRR changes over time into fertility and survival components. The results show that changes in the NRR have been driven mostly by changes in fertility. Yet improvements in survival have also played an important role in explaining changes in the NRR over the last century and represent a substantial component of change in some low-income countries today. Furthermore, the decomposition of the survival component by

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## Net-Reproduction Rate

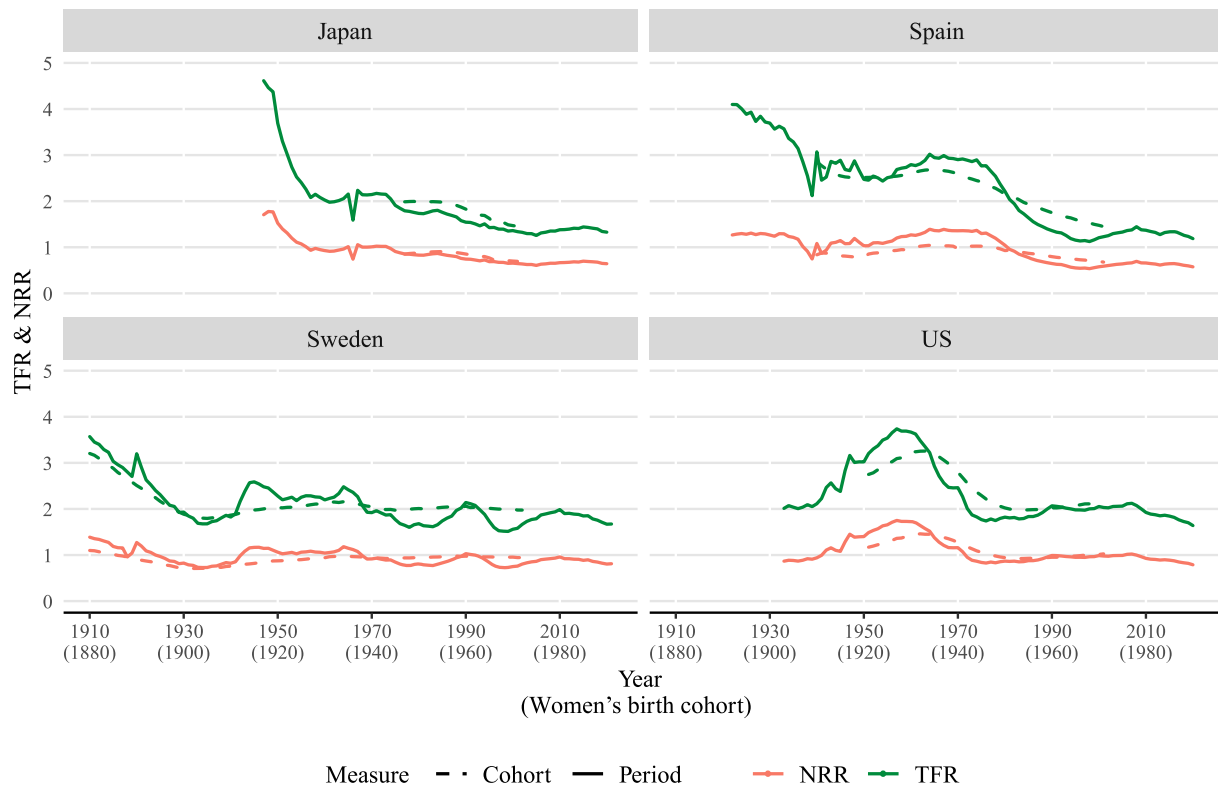
$$NRR(t) =$$

$$\int_{\alpha}^{\beta} \ell(a, t) m(a, t) da$$

## Net-Reproduction Rate

$$m(a, t) = s(a, t)f(a, t)$$





**Figure 1(a)** TFR and NRR for periods 1910–2021<sup>1</sup> and cohorts 1880–1972<sup>2</sup>, selected high-income countries

<sup>1</sup>Or earliest and latest year available, as described in Table 1.

<sup>2</sup>Or earliest and latest birth cohort available, as described in Table A1.

*Note:* Cohort rates are lagged by 30 years.

*Source:* Authors' calculations based on Human Mortality Database (2022) and Human Fertility Database (2022).

$$N\dot{R}R =$$

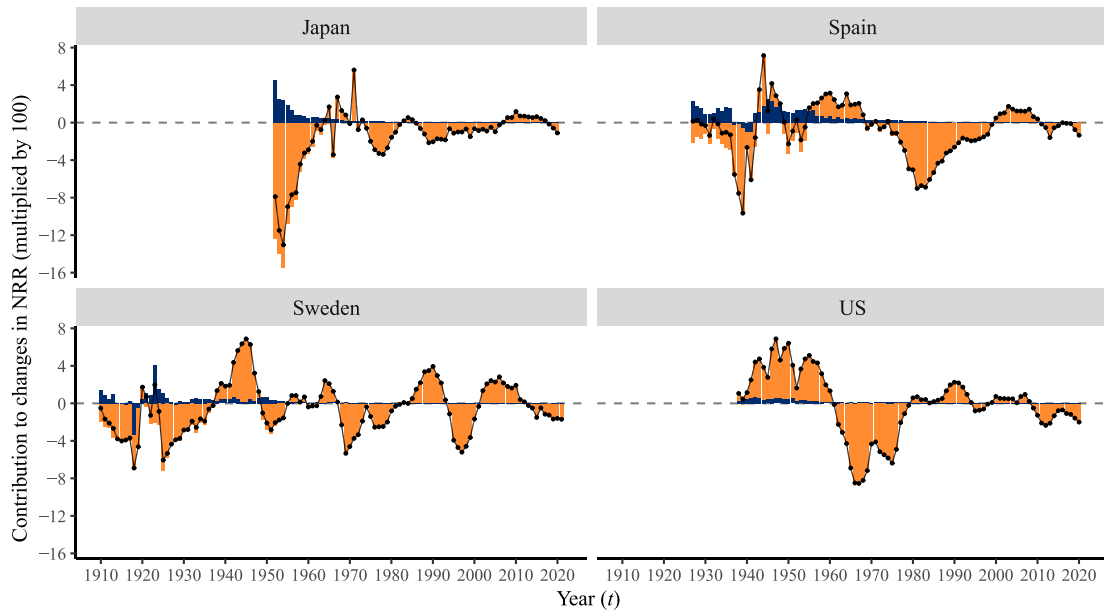
$$\int_{\alpha}^{\beta} \dot{m}(a)\ell(a) + m(a)\dot{\ell}(a) \, da$$

$$\dot{m}(a) =$$

$$\left[ \dot{s}(a) f(a) + s(a) \dot{f}(a) \right]$$

$$\int_{\alpha}^{\beta} m(a,t)\dot{\ell}(a,t) =$$

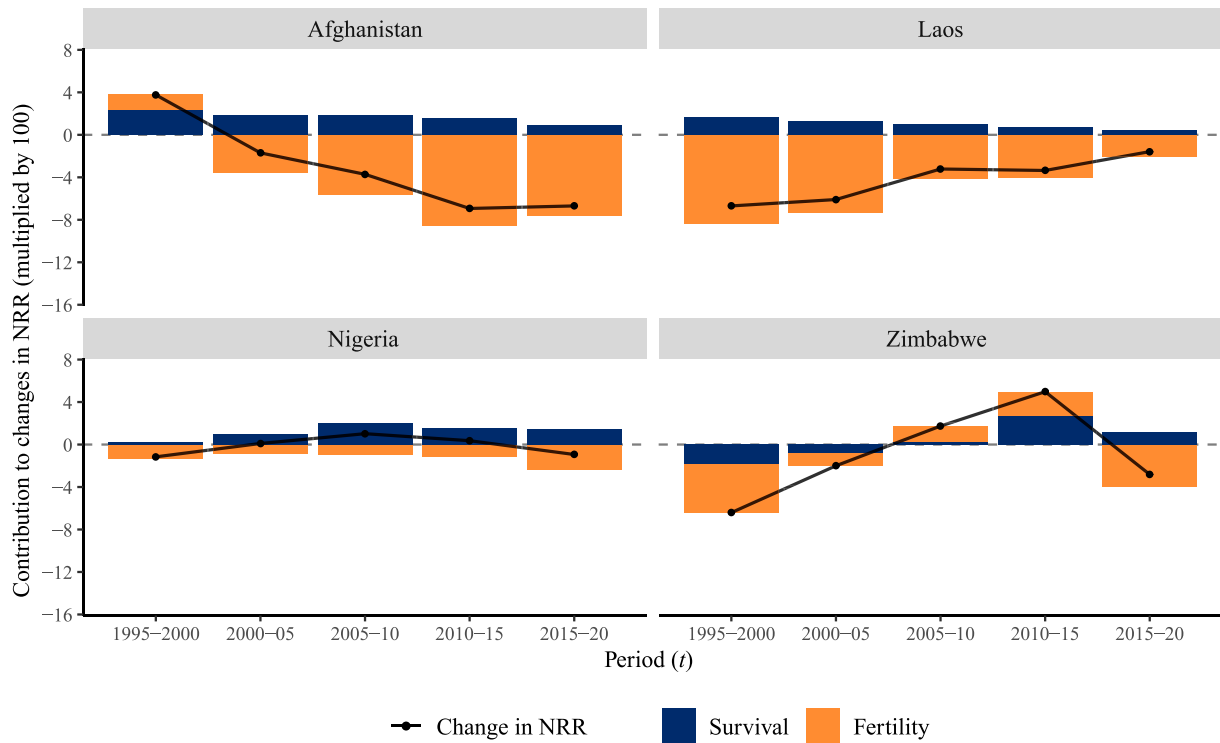
$$\sum_{x=0}^{\beta-1} \frac{\dot{p}_x}{p_x} \int_{x+1}^{\beta} m(a,t)\ell(a,t) \, da$$



—●— Change in NRR

■ Survival

■ Fertility



## Assignment 4

Select one of the measures in the examples of this section and apply to a different population from HMD or HFD.

Submit ONE page: one Figure (or Table) and a brief paragraph describing the results that you find.