

# EMT1201: Engineering Mathematics II

| Hours per Semester |    |    |    | Weighted Total Mark | Weighted Exam Mark | Weighted Continuous Assessment Mark | Credit Units |
|--------------------|----|----|----|---------------------|--------------------|-------------------------------------|--------------|
| LH                 | PH | TH | CH | WTM                 | WEM                | WCM                                 | CU           |
| 45                 | 00 | 30 | 60 | 100                 | 60                 | 40                                  | 4            |

## Description

The course builds on Engineering Mathematics I and covers differential equations, infinite series, and real vector and numerical analysis. It also prepares the students for engineering mathematics III.

## Objective

- To introduce students to the concept of Single Predictor-Response mathematical modeling in areas such as electrical circuit problems and vibratory and oscillatory mechanical systems
- To expose students to analytical solutions of classical ordinary differential equations in mathematical physics.
- To expose students to the fundamentals of Real Analysis.
- To introduce students the foundations of Scientific Computing and Numerical Analysis.

## Learning Outcomes

On completion of this course the student will:

- Be able to formulate Ordinary Differential models associated with Electric Circuits
- Obtain analytical and numerical solutions of Ordinary Differential Equations;
- Have acquired the analytical ability critical to engineering problem solving

## Content

### Complex Number (variable) algebra:

Definition, properties (algebraic operations) & applications; Cartesian & polar representations; Absolute values; Products, powers and quotients; Extraction of roots; De-Moivre's theorem; exponential & hyperbolic functions of the complex variable.

### Vector Algebra:

Scalars, vectors and their applications; Properties of vectors –addition, multiplication by scalars, dot & cross products; Vector products in terms of components; Application to analytic geometry –equation of lines, planes, spheres, etc; Physical applications –work done, normal flux, moments, force, angular velocity of rigid body; Coordinate systems and Transformation: Cartesian coordinates, Cylindrical Coordinates, Spherical coordinates. Vector Calculus: Differential length, Area and Volume. Vector Calculus: Line, surface and Volume integrals. Vector Calculus: Gradient, Divergence, Curl and Laplacian.

### Linear transformations & matrix:

Definitions, equality, sum, product of matrices; types of matrices; the identity matrix, inverse of a matrix, transpose of matrix; Symmetric and skew symmetric matrices; Determinants – definition and properties, minors and cofactors, evaluation of determinants by cofactors; Solution of systems of linear algebraic equations; Consistent and inconsistent equations; Systems of homogeneous equations; Cramer's rule; Gauss –Jordan method.

### Vector analysis:

Scalar and vector fields, vector functions, derivatives of vector functions; divergence and curl of vector functions; application of vector function concepts – line and surface integral, triple integrals and Stokes theorems; Physical interpretation of divergence and curl of a vector field; Green's theorem, Line integrals independent of path; exact differential forms.

### Real analysis:

Differentiability, the mean value theorem, Generalization of Taylor's series; Integrability, the definite and indefinite integrals, the fundamental theorem of calculus, differentiation and repeated integrals

### Numerical analysis:

Numerical solutions of polynomial algebraic functions; interpolation formulae; numerical differentiation and integration; trapezoidal and Simpson's rules of integration; numerical solutions of ordinary differential equations; further consideration of integral equations by numerical methods

## Reference books

- Martin M. Lipschutz, Theory and Problems of Differential Geometry, McGraw-Hill, 1969
- C. Ray Wylie and Louis C. Barrett, Advanced Engineering Mathematics, 6th ed., McGraw Hill, New York, 1995.
- Erwin Kreyszig, Advanced Engineering Mathematics, 8th ed., John Wiley and Sons.
- Murray R Spiegel, Theory and Problems of Vector Analysis, SI (Metric) ed., McGraw Hill
- Murray R. Spiegel, 1981. Applied Differential Equations. 3rd Edition. Prentice-Hall, Inc., Englewood Cliffs, N.J. 07632