## COMP6714 Assignment 1

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## Question 1

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Algorithm 1: Q1(p_1, p_2, p_{\$})
 1 answer \leftarrow \emptyset;
 2 while p_1 \neq \mathbf{nil} \land p_2 \neq \mathbf{nil} \mathbf{do}
          if doc(p_1) = doc(p_2) then
               l \leftarrow [\ ];
 4
               pp_1 \leftarrow positions(p_1); pp_2 \leftarrow positions(p_2);
 \mathbf{5}
               while pp_1 \neq \text{nil do}
 6
                    end \leftarrow \text{skipTo}(p_{\$}, \text{docID}(pp_1), pos(pp_1))
 7
                    while pp_2 \neq \text{nil do}
 8
                         if pos(pp_2) < end then
 9
                               if pos(pp_2) > pos(pp_1) then
10
                                   add(l,pos(pp_2));
11
                         else
12
                          break;
13
                         pp_2 \leftarrow \text{next}(pp_2);
14
                    while l \neq [] \land l[1] < pos(pp_1) do
15
                      delete(l[1]);
16
                    for each ps \in l do
17
                      answer \leftarrow answer \cup [\operatorname{docID}(p_1), \operatorname{pos}(pp_1), ps];
18
                  pp_1 \leftarrow \text{next}(pp_1);
19
              p_1 \leftarrow \operatorname{next}(p_1); p_2 \leftarrow \operatorname{next}(p_2);
20
          else
21
               if docID(p_1) < docID(p_2) then
22
                    p_1 \leftarrow \operatorname{next}(p_1);
\mathbf{23}
               else
\mathbf{24}
                 p_2 \leftarrow \text{next}(p_2);
25
26 return answer
```

## Question 2

(1)

At first, the smallest( $\mathbf{Z_0}$ ) is in memory. If  $\mathbf{Z_0}$  gets to the upper bound of the memory, since the memory is full, it will be written into disk as  $\mathbf{I_0}$ . We can treat this  $\mathbf{I_0}$  as **Generation 0**. However, if  $\mathbf{I_0}$  already exists,  $\mathbf{Z_0}$  and  $\mathbf{I_0}$  will be merged into a new subindex  $\mathbf{Z_1}$ . At this time, if there is no  $\mathbf{I_1}$ ,  $\mathbf{Z_1}$  will be written to disk as  $\mathbf{I_1}$ (**Generation 1**). While if  $\mathbf{I_1}$  is in disk,  $\mathbf{Z_1}$  will merge with  $\mathbf{I_1}$  to form  $\mathbf{Z_2}$  and so on.

From the algorithm of **logarithmic merge**, we can also know that this strategy maintain a series of indexes and each twice as large as the previous one.

Let  $\mathbf{n}$  represent the number of sub-indexes.

- The  $1^{st}$  layer can record **M** pages;
- The  $2^{nd}$  layer can record **2M** pages;

- . . . . . .

- The  $n^{th}$  layer can record  $2^{n-1} \cdot M$  pages;

Thus, 
$$M \cdot t = M \cdot (1 + 2 + 2^2 + 2^3 + \dots + 2^{n-1})$$

We can figure out  $t = 2^n - 1$  and  $n = log_2(t + 1)$ .

Therefore,  $logarithmic\ merge\ will\ result\ in\ at\ most\ \lceil log_2t\rceil$  sub-indexes.

(2)

First of all, writing all pages into disk will cost  $\mathbf{M} \cdot \mathbf{t}$ .

Then, we should consider **merging cost**.

According to (1), the number of sub-indexes  $\mathbf{n} = \lceil \mathbf{log_2t} \rceil$ , so sub-indexes can be record as  $\mathbf{I_0}, \mathbf{I_1}, \mathbf{I_2}, \dots, \mathbf{I_{n-1}}$ .

Since each index is twice as large as the previous one, we can conclude that

$$2^1 \cdot I_0 = 2^0 \cdot I_1$$

$$2^2 \cdot I_0 = 2^1 \cdot I_1 = 2^0 \cdot I_2$$

$$2^3 \cdot I_0 = 2^2 \cdot I_1 = 2^1 \cdot I_2 = 2^0 \cdot I_3$$

. . . . . .

$$2^{n-1} \cdot I_0 = 2^{n-2} \cdot I_1 = 2^{n-3} \cdot I_2 = \dots = 2^1 \cdot I_{n-2} = 2^0 \cdot I_{n-1}$$

Every time when one  $I_{n-1}$  Generating, two  $I_{n-2}$  need to be read. Before reading two  $I_{n-2}$ , they have to be written into the disk.

Therefore, except every  $I_0$  is read once and every  $I_{n-1}$  is written once, the parameters generated in this process are read once and written once respectively.

The calculation process is as follows:

$$\begin{split} merge\_cost &= (2^{n-1} \cdot 2^0 + 2 * (2^{n-2} \cdot 2^1 + 2^{n-3} \cdot 2^2 M + \ldots + 2^1 \cdot 2^{n-2}) + 2^0 \cdot 2^{n-1}) \cdot M \\ &= M \cdot (2^n + 2^n \cdot (n-2)) \\ &= M \cdot 2^n \cdot (n-1) \\ &= M \cdot t \cdot (log_2 t - 1) \\ total\_cost &= write\_cost + merge\_cost \\ &= M \cdot t + M \cdot t \cdot (log_2 t - 1) \\ &= O(M \cdot t \cdot log_2 t) \end{split}$$

Therefore, the total I/O cost of the logarithmic merge is  $O(t \cdot M \cdot log_2 t)$ .

# Question 3

 $\ \, {\rm Decode:} \ \, 01000101 \ \, 11110001 \ \, 01110000 \ \, 00110000 \ \, 11110110 \ \, 11011 \\$ 

0: 1

Let  $10\ 0\ 0$  represents number  $\mathbf{k_1}$ 

$$\therefore k_{1dd} = \lfloor log_2(k_{1d} + 1) \rfloor = 1$$

$$k_{1dr} = (k_{1d} + 1) - 2^{k_{1dd}} = 0$$

$$\therefore k_{1d} = 1$$

$$\therefore k_{1r} = k_1 - 2^{k_{1d}} = 0$$

$$\therefore k_1 = 2$$

Thus, 10 0 0 represents 2.

Let 10 1 11 represents number  $\mathbf{k_2}$ 

$$k_{2dd} = |log_2(k_{2d} + 1)| = 1$$

$$k_{2dr} = (k_{2d} + 1) - 2^{k_{2dd}} = 1$$

$$k_{2d} = 2$$

$$\therefore k_{2r} = k_2 - 2^{k_d} = 3$$

$$\therefore k_2 = 7$$

Thus, 10 1 11 represents 7.

Similarly, we can calculate:

110 00 101: **13** 

110 00 000: 8

110 00 011: **11** 

110 11 011011: **91** 

Therefore, the result of decoding is 1, 2, 7, 13, 8, 11, 91.

Since these numbers The document IDs are 1, 3, 10, 23, 31, 42, 133.

## Question 4

**(1)** 

Line 21 causes the bug in the algorithm in Figure 2.

The main problem is the **pickTerm**() method. According to the original paper, we can know that **pickTerm**() selects the term with the maximal idf. So if the idf of a term is maximum among all terms and is the **pTerm** in one cycle, this algorithm will end up in an infinite loop.

**(2)** 

The table below is from lecture 5b. Infinite loop would appear in the process of this algorithm.

	A	В	$\mathbf{C}$
UB	4	5	8
	$\langle 1, 3 \rangle$	$\langle 1, 4 \rangle$	$\langle 1, 4 \rangle$
	$\langle 2, 4 \rangle$	$\langle 2, 1 \rangle$	$\langle 2, 2 \rangle$
List	$\langle 7, 1 \rangle$	$\langle 7, 2 \rangle$	$\langle 5, 1 \rangle$
LISU		$\langle 8, 5 \rangle$	$\langle 7,7 \rangle$
		$\langle 9, 2 \rangle$	$\langle 10, 1 \rangle$
		$\langle 11, 5 \rangle$	$\langle 11, 8 \rangle$

## In the 1<sup>st</sup> cycle

$$\theta = 0$$
, curDoc = 0

Sorted Term	Α	В	С
Doc	1	1	1
Cumulative Upper Bound	4	9	17

- pTerm = A
- pivot = posting[0].DID = 1
- pivot > curDoc (**Line14**)
  - posting[0].DID = pivot (Line15)
     curDoc = 1, θ = 11
     return (curDoc, posting)

#### In the 2<sup>nd</sup> cycle

$$\theta = 11$$
, curDoc = 1

Sorted Term	A	В	С
Doc	1	1	1
Cumulative Upper Bound	4	9	17

- pTerm = C
- pivot = posting[2].DID = 1
- pivot = curDoc (**Line10**)

aterm = pickTerm(terms[0..pTerm]) (the idf of A is biggest, choose A)

$$posting[A].DID = 2$$

#### In the 3<sup>rd</sup> cycle

$$\theta = 11$$
, curDoc = 1

Sorted Term	В	С	A
Doc	1	1	2
Cumulative Upper Bound	5	13	17

- pTerm = C
- pivot = posting[1].DID = 1
- pivot =  $\operatorname{curDoc} (\mathbf{Line10})$

$$aterm = pickTerm(terms[0..pTerm]) \; (\textbf{assume choose C}) \\ posting[C].DID = 2$$

#### In the 4<sup>th</sup> cycle

$$\theta = 11$$
, curDoc = 1

Sorted Term	В	A	С
Doc	1	2	2
Cumulative Upper Bound	5	9	17

- $\bullet$  pTerm = C
- pivot = posting[2].DID = 2
- pivot > curDoc (**Line14**)
  - curDoc \( \neq \text{posting[0].DID (Line19)} \)
    aterm = pickTerm(terms[0..pTerm]) (the idf of A is biggest, choose A)
    posting[A].DID = 7

## In the 5<sup>th</sup> cycle

$$\theta = 11$$
, curDoc = 1

Sorted Term	В	С	A
Doc	1	2	7
Cumulative Upper Bound	5	13	17

- $\bullet$  pTerm = C
- pivot = posting[C].DID = 2
- pivot > curDoc (**Line14**)
  - posting[0].DID \( \neq \) pivot (**Line19**) aterm = pickTerm(terms[0..pTerm]) (the idf of A is biggest, choose A) posting[A].DID = 7

In this case, **pickTerm**() will always choose A because of the maximum idf.  $\theta$ , curDoc and other parameters would not change as well.

Therefore, this algorithm will end up in an infinite loop.