

# ERASURE CODES IN SOFTWARE

With applications for Online Gaming

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# OVERVIEW

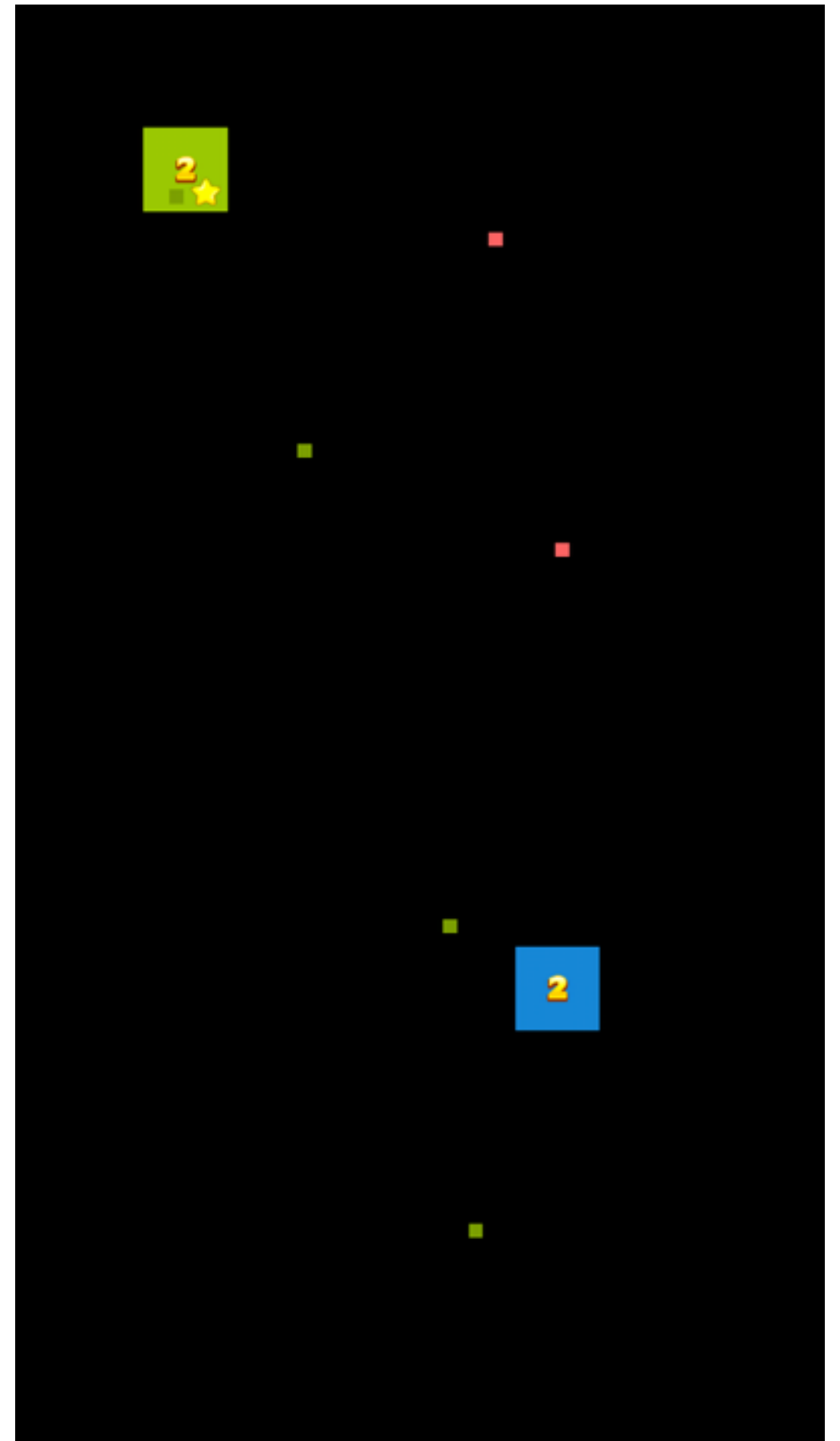
- Erasure codes in software are fast with low-overhead
- Advantages of using erasure codes in online games:
  - > 50% faster delivery over UDP than over TCP
  - > 50% less bandwidth used than naive redundancy
  - > 50% better recovery rate than parity redundancy
- Improves the experience for multiplayer mobile apps

# “SQUARES” ANDROID GAME

<http://dkop.us/squares.apk>

(built with the Game Closure DevKit)

See: “Realtime Multiplayer Game”  
Think: “Low-Latency”



# GAME PACKET TYPES

- **Unordered, Unreliable** (UDP)
  - Example: Time synchronization
  - Loss recovery? Not desired.
- **Ordered, Unreliable** (UDP)
  - Example: Avatar Position updates
  - Loss recovery? Just send another update!

- **Unordered, 99% Reliable** (UDP)
  - Examples: Bomb fired, Voice chat
  - *Erasure codes are useful in this case!*
- **Ordered, Reliable** (TCP)
  - Examples: Chat messages, File downloads
  - A hybrid scheme over rUDP could be used to reduce latency here. But not terribly exciting.

# ERASURE CODE 4 | 1

**Use Redundant packets to fill in for missing packets.**

- Which Original packets are protected by each Redundant packet?
- How much bandwidth for Redundant packets?
- Pick one of three dominant types of software erasure codes:
  - Parity: XOR a set of packets together, recover from single loss
  - Reed-Solomon: 100% recovery rate given enough data
  - Low Density Parity Check: Random (but >97%) recovery

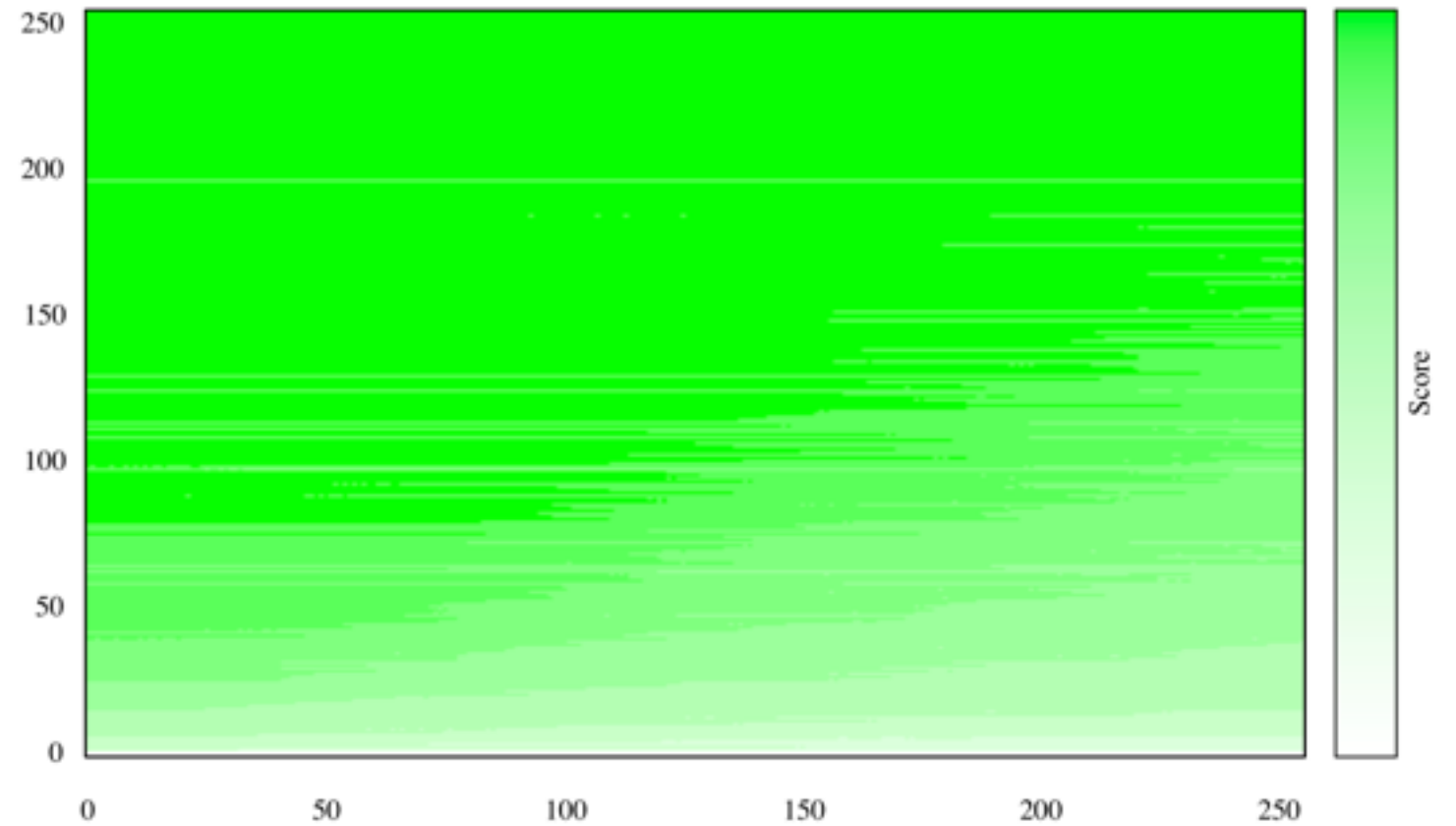
# MY OPEN-SOURCE SOFTWARE

- “Cauchy” RS codes in C++: Longhair (new!)
  - Encodes **>400 MB/s (<40 usec)** for  $K < 30$  packets.
  - <http://github.com/catid/longhair>
- “Raptor” LDPC codes in C++: Wirehair (2 years old)
  - Encodes >200 MB/s for protecting  $K > 30$  packets.
  - <http://github.com/catid/wirehair>

# Performance Showdown

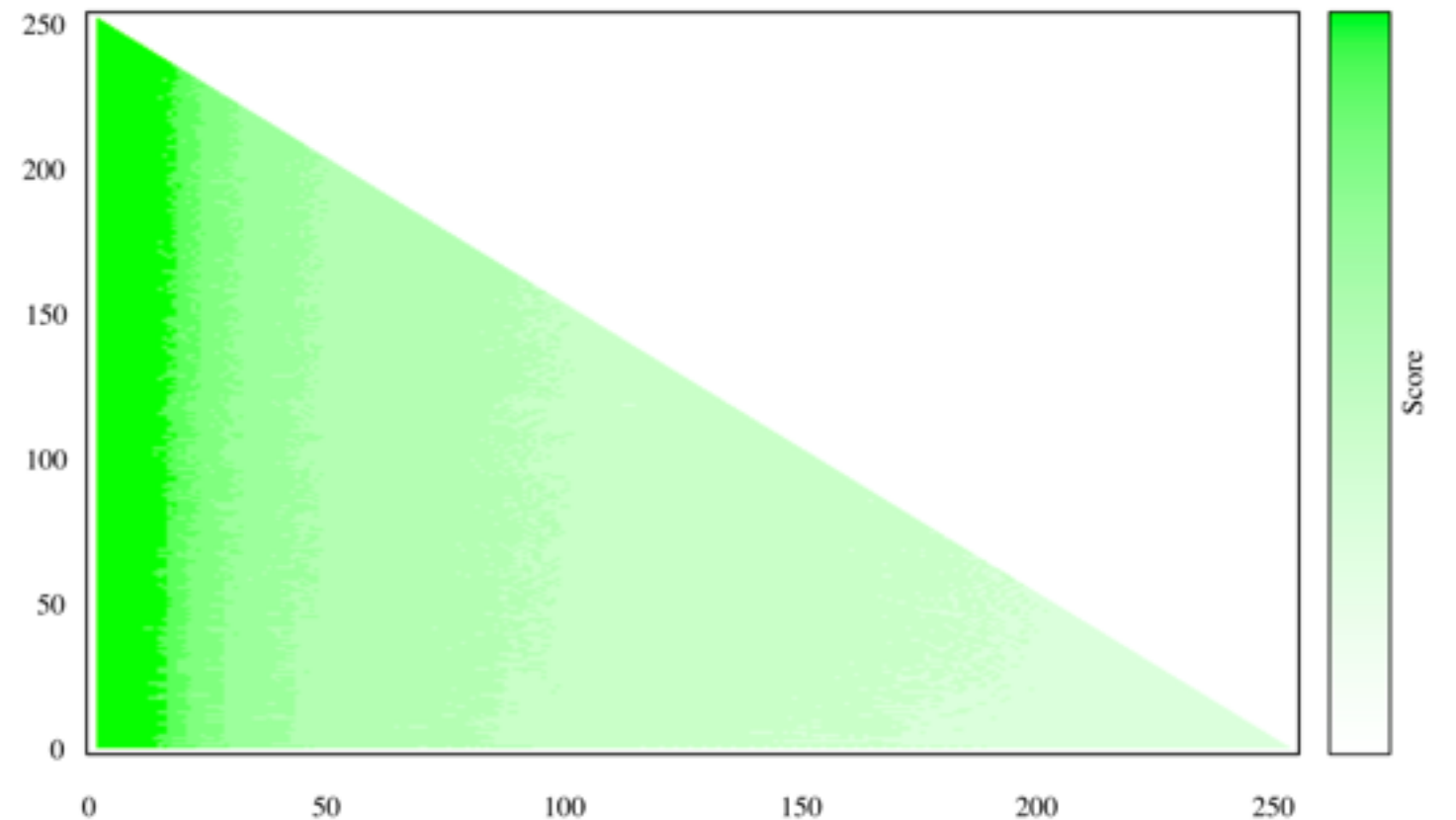
**Wirehair (files):**

Heat Map indicating performance of Wirehair codec



**Longhair**  
**(streams):**

Heat Map indicating performance of CRS codec



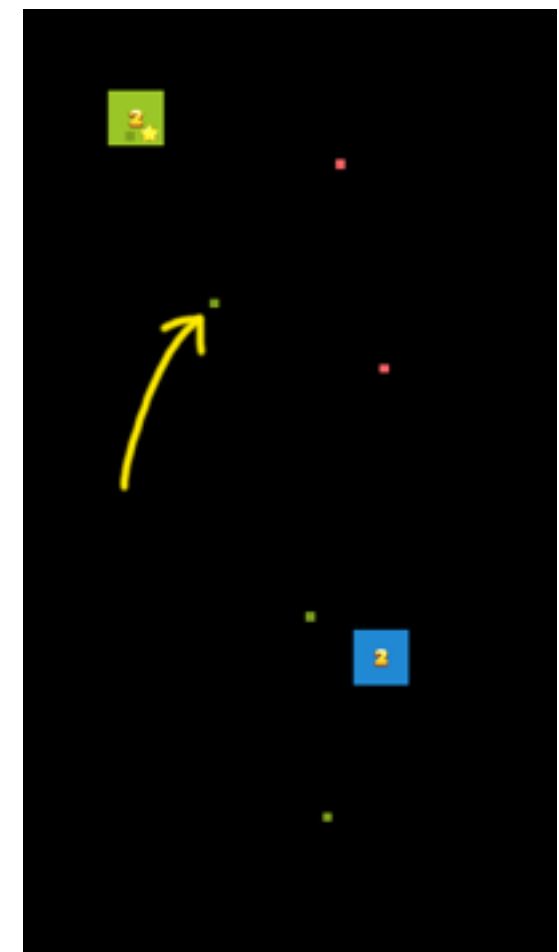


# BACK TO SQUARE ONE

- Squares.APK sends data in three modes:
  - 0 : Unreliable, Unordered : Time synch
  - 1 : Unreliable, Ordered : Position data, JSON
  - **2 : 99% Reliable, Unordered : Bomb fired!**

# > BOMB PACKETS <

- Low latency is essential to quickly display the bomb for everyone.
- Lost bomb packets cause severely-visible desynchronization between players.
- But 1 in 1000 is okay: Desired  $<0.1\%$  loss.
- Solution: Add redundancy, *but how?*
  - Send each bomb packet twice?  
—> Twice the bandwidth. =(
  - Low bandwidth solution: **Erasure codes.**



# SHORTHAIR CODEC

- My “**Shorthair**” codec uses erasure codes for streaming:
  1. Measures packet loss and estimates amount of redundancy required to reach a target loss rate (e.g. 0.1%).
  2. Interleaves sending redundant data for previous RTT/2 of data while delivering latest RTT/2 of data.
- Worst-case RTT delay after loss. Average case RTT/2 delay.
- Low overhead: 5 bytes per packet. Uses Longhair.
- <https://github.com/catid/shorthair>

# LOSS STATISTICS FROM SEQUENCE NUMBER HOLES

- UDP packets may arrive out of order. Average packet loss rate changes.
- Sequence number ranges are tracked in bins. Track only 3 bins:

|<---delay-->|<---delay-->|<---delay-->|

Bin 0 :	^START	^STOP	^SEND
Bin 1 :		^START	^STOP
Bin 2 :			^START

- Whenever statistics are requested, a new bin is started, the last bin is frozen, and the last-last bin is delivered.
  - **Result:** RTT and packet loss statistics are delivered periodically.

# CALCULATE REDUNDANCY

- Statistically modeled just like repeated coin flips. Let  $p = P(\text{loss}) = 0.03$
- This is a Binomial random variable  $X$ . Let  $r = \# \text{redundant}$ ,  $k = \# \text{original}$

$$P(\text{Total erasure code failure}) = P(X > r), \quad X \sim \text{Binomial}(k+r, p)$$
$$\mu = E[X] = (k+r)p, \quad \sigma^2 = \text{SD}[X] = \sqrt{((k+r)p(1-p))}$$

- $X$  is approximated by  $Y \sim \text{Normal}(\mu, \sigma^2)$ 
  - Works when  $(k+r)p \geq 10$ ,  $(k+r)(1-p) \geq 10$ . Otherwise use exact calc.
- So:  $P(X > r) \approx P(Y \geq r + 0.5)$ , which is much easier to code in C:

```
u = (k+r)*p; s = sqrt(u * (1-p));  
Pr = 0.5 * erfc(INVSQRT2 * (r - u - 0.5) / s);
```

# SHORTHAIR PROTOCOL

- $\langle \text{SeqNo [2 bytes]} \rangle$
- $\langle \text{Out-of-Band [1 bit]} \parallel \text{CodeGroup [7 bits]} \rangle$
- OOB=1 packets stop here, but Original data also has:
  - $\langle \text{ID [1 byte]} \rangle \langle (k - 1) [1 \text{ byte}] \rangle$
  - Redundant packets ( $\text{ID} \geq k$ ) also have:
    - $\langle (m - 1) [1 \text{ byte}] \rangle \langle \text{Original Length [2 bytes]} \rangle \{ \text{data} \}$

# SHORTHAIR SCHEDULE

**Redundant packets interleaved with originals:**

	56	57	58	59	60	61
R0	X	X	X	send here		
R1	X	X	X			send here
R2				X	X	X
R3				X	X	X

# BRIEF GLIMPSE AT THE FUTURE

**Redundant packets interleaved with originals:**

	56	57	58	59	60	61
R0	X	X	X	send here		
R1		X	X	X	send here	
R2			X	X	X	send here
R3				X	X	X



# REVIEW

- Erasure codes in software are fast with low-overhead
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“The future is already here.  
— It’s just not evenly distributed.”

-William Gibson, 2003