

2021141460159-邓钰川-作业2-1

3.6

3.6 [5] <§3.2> Assume 185 and 122 are unsigned 8-bit decimal integers. Calculate $185 - 122$. Is there overflow, underflow, or neither?

考虑8位无符号二进制最大的十进制数是256，有符号是128

$185 - 122 = 63 = 0b00111111 \Rightarrow \text{right}$

$185 - 122 = 63 = 0b00111111 \Rightarrow \text{对}$

所以不会overflow也不会underflow

Neither

185 : 10111001

122 : 01111010

185 - 122 : 00111111

Answer : 63

Neither

3.7

3.7 [5] <§3.2> Assume 185 and 122 are signed 8-bit decimal integers stored in sign-magnitude format. Calculate $185 + 122$. Is there overflow, underflow, or neither?

overflow (65)

$185 + 122 = 0b100110011 \Rightarrow \text{requires 9-bit, overflow will occur.}$

$185 + 122 = 0b100110011 \Rightarrow \text{需要 9 位, 会发生溢出。}$

$128 - 185 + 122 = 65$

185 : 10111001

So 185 will be considered as -57

122 : 01111010

So it is actually $122 - 57$

57 : 00111001

$122 - 57$: 01000001

Answer : 65

Neither

3.8

3.8 [5] <§3.2> Assume 185 and 122 are signed 8-bit decimal integers stored in sign-magnitude format. Calculate $185 - 122$. Is there overflow, underflow, or neither?

Overflow

$128 - 185 - 122 = -179$

185 : 10111001

So 185 will be considered as -57

So it is actually $-57 - 122 = -57 + (-122)$

57 : 00111001

-57 : 10111001

122 : 01111010

-122 : 11111010

$-57 + (-122)$: 10110011

Answer : -51

Overflow

3.9

3.9 [10] <§3.2> Assume 151 and 214 are signed 8-bit decimal integers stored in two's complement format. Calculate $151 + 214$ using saturating arithmetic. The result should be written in decimal. Show your work.

$-105 - 42 = -128$

151 : 10010111

two's complement : 11101001

214 : 11010110

two's complement : 10101010

$151 + 214$ (*saturating arithmetic*) : 11111111

Answer : -1

3.10

3.10 [10] <§3.2> Assume 151 and 214 are signed 8-bit decimal integers stored in two's complement format. Calculate $151 - 214$ using saturating arithmetic. The result should be written in decimal. Show your work.

$$-105 + 42 = -63$$

$$151 : 10010111$$

$$\text{two's complement} : 11101001$$

$$-214 : 01010110$$

$$\text{two's complement} : 01010110$$

$$151 - 214 (\text{saturating arithmetic}) : 00111111$$

$$\text{Answer} : 63$$

3.11

3.11 [10] <§3.2> Assume 151 and 214 are unsigned 8-bit integers. Calculate $151 + 214$ using saturating arithmetic. The result should be written in decimal. Show your work.

$$151 + 214 = 255$$

$$151 : 10010111$$

$$214 : 11010110$$

$$151 + 214 (\text{saturating arithmetic}) : 11111111$$

$$\text{Answer} : 255$$

3.13

3.13 [20] <§3.3> Using a table similar to that shown in [Figure 3.6](#), calculate the product of the hexadecimal unsigned 8-bit integers 62 and 12 using the hardware described in [Figure 3.5](#). You should show the contents of each register on each step.

$$62 \times 12 = 744 = 1011101000$$

62=00111 110

12=00001 100

|迭代次数|步骤|乘数|被乘数|乘积|

|-----|-----|-----|-----|-----|

| 0|初始值 |00001100 |00111110 |00000000|

| 1|1a: 无操作 |00001100 |00111110 |00000000|

| 1|2: 左移被乘数 |00001100 |01111100 |00000000|

| 1|3: 右移乘数 |00000110 |01111100 |00000000|

| 2|1a: 无操作 |00000110 |00111110 |00000000|

| 2|2: 左移被乘数 |00000110 |11111000 |00000000|

| 2|3: 右移乘数 |00000011 |11111000 |00000000|

| 3|1a: 乘积=乘积+被乘数 |00000011 |11111000 |11111000|

| 3|2: 左移被乘数 |00000011 |11110000 |11111000|

| 3|3: 右移乘数 |00000001 |11110000 |11111000|

| 4|1a: 乘积=乘积+被乘数 |00000001 |11110000 |11101000|

| 4|2: 左移被乘数 |00000001 |11110000 |11101000|

| 4|3: 右移乘数 |00000000 |11110000 |11101000|

对的上后八位

0x62(*Multiplicand*) : 0110 0010

0x12(*Multiplier*) : 0001 0010

0x62 = 92(*Decimal*)

0x12 = 18(*Decimal*)

0x62 * 0x12 = 98 * 18(*Decimal*) = 1764(*Decimal*) = 0x06E4 = 0000 0110 1110 0100

| Iteration | Step | Multiplier | Multiplicand | Product |
|-----------|--|------------|--------------|---------------------|
| 0 | Initial values | 0001 0010 | 0110 0010 | 0000 0000 0000 0000 |
| 1 | 1: 0 → No operation | 0001 0010 | 0110 0010 | 0000 0000 0000 0000 |
| | 2: Shift right Multiplier | 0000 1001 | 0110 0010 | 0000 0000 0000 0000 |
| | 3: Shift right Product | 0000 1001 | 0110 0010 | 0000 0000 0000 0000 |
| 2 | 1a: 1 → Add Multiplicand to the left of Product and place the result | 0000 1001 | 0110 0010 | 0110 0010 0000 0000 |
| | 2: Shift right Multiplier | 0000 0100 | 0110 0010 | 0110 0010 0000 0000 |
| | 3: Shift right Product | 0000 0100 | 0110 0010 | 0011 0001 0000 0000 |
| 3 | 1: 0 → No operation | 0000 0100 | 0110 0010 | 0011 0001 0000 0000 |
| | 2: Shift right Multiplier | 0000 0010 | 0110 0010 | 0011 0001 0000 0000 |
| | 3: Shift right Product | 0000 0010 | 0110 0010 | 0001 1000 1000 0000 |
| 4 | 1: 0 → No operation | 0000 0010 | 0110 0010 | 0001 1000 1000 0000 |
| | 2: Shift right Multiplier | 0000 0001 | 0110 0010 | 0001 1000 1000 0000 |
| | 3: Shift right Product | 0000 0001 | 0110 0010 | 0000 1100 0100 0000 |
| 5 | 1a: 1 → Add Multiplicand to the left of Product and place the result | 0000 0001 | 0110 0010 | 0110 1110 0100 0000 |
| | 2: Shift right Multiplier | 0000 0000 | 0110 0010 | 0110 1110 0100 0000 |
| | 3: Shift right Product | 0000 0000 | 0110 0010 | 0011 0111 0010 0000 |
| 6 | 1: 0 → No operation | 0000 0000 | 0110 0010 | 0011 0111 0010 0000 |
| | 2: Shift right Multiplier | 0000 0000 | 0110 0010 | 0011 0111 0010 0000 |
| | 3: Shift right Product | 0000 0000 | 0110 0010 | 0001 1011 1001 0000 |
| 7 | 1: 0 → No operation | 0000 0000 | 0110 0010 | 0001 1011 1001 0000 |
| | 2: Shift right Multiplier | 0000 0000 | 0110 0010 | 0001 1011 1001 0000 |
| | 3: Shift right Product | 0000 0000 | 0110 0010 | 0000 1101 1100 1000 |
| 8 | 1: 0 → No operation | 0000 0000 | 0110 0010 | 0000 1101 1100 1000 |
| | 2: Shift right Multiplier | 0000 0000 | 0110 0010 | 0000 1101 1100 1000 |
| | 3: Shift right Product | 0000 0000 | 0110 0010 | 0000 0110 1110 0100 |

3.14

硬件：一个循环来做加法,一个循环来做移位,一个循环判断完成。（3个）

软件：它需要一个周期确定加数,1个周期做加法,1个周期来做每一个移位,一个周期判断

完成。5个

所以硬件是 $3 * 8 * 4 = 96\text{unit}$

软件是 $5 * 8 * 4 = 160\text{unit}$