
Adaptive MCMC algorithm with normal proposal and vanishing adaptation

- 1: Set starting values $X_0, \mu_0, \Sigma_0, \lambda_0, \alpha^*, \delta$ ($\delta > 0$), and draws T .
 - 2: Set $t = 0$ and repeat steps 3–10 while $t \leq T$:
 - 3: Draw a candidate $Y_t \sim MVN(X_t, \lambda_t \Sigma_t)$.
 - 4: Compute $\alpha(Y_t, X_t) = \min \left\{ \frac{\pi(Y_t)}{\pi(X_t)}, 1 \right\}$.
 - 5: Set $X_{t+1} = Y_t$ with prob. $\alpha(Y_t, X_t)$,
 $X_{t+1} = X_t$ otherwise.
 - 6: Compute weighting parameter $\gamma_t = \frac{1}{(1+t)^\delta}$.
 - 7: Update $\lambda_{t+1} = \exp \{ \gamma_t (\alpha(Y_t, X_t) - \alpha^*) \} \lambda_t$.
 - 8: Update $\mu_{t+1} = \mu_t + \gamma_t (X_{t+1} - \mu_t)$.
 - 9: Update $\Sigma_{t+1} = \Sigma_t + \gamma_t \{ (X_{t+1} - \mu_t) (X_{t+1} - \mu_t)' - \Sigma_t \}$.
 - 10: Increment t .
- Output: The sequence $(X_t)_{t=1}^T$.
-