

So we are given an expression:

$$\sin(x \cdot \log_{10} x)$$

Let's differentiate it!

$$\cos(x \cdot \log_{10} x) \cdot \left( 1 \cdot \log_{10} x + \frac{(x^{(-1)} \cdot 1 \cdot \ln 10 - \ln x \cdot 0 \cdot 10^{(-1)})}{\ln 10} \cdot x \right) \cdot (-1)$$

Uhhh, let's simplify it a bit... SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{(x^{(-1)} \cdot 1 \cdot \ln 10 - \ln x \cdot 0 \cdot 10^{(-1)})}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{(x^{(-1)} \cdot \ln 10 - \ln x \cdot 0 \cdot 10^{(-1)})}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{(x^{(-1)} \cdot \ln 10 - 0 \cdot 10^{(-1)})}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{(x^{(-1)} \cdot \ln 10 - 0 \cdot 0 \cdot 1)}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{(x^{(-1)} \cdot \ln 10 - 0)}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^{(-1)} \cdot \ln 10}{\ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^{(-1)} \cdot \ln 10}{\ln 10 \cdot \ln 10} \cdot x \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^{(-1)} \cdot \ln 10}{5.3019} \cdot x \right) \cdot (-1)$$

STRUCTURE

$$\cos(x^1 \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^{(1+(-1))} \cdot \ln 10}{5.3019} \cdot 1 \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^{(1+(-1))} \cdot \ln 10}{5.3019} \cdot 1 \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{x^0 \cdot \ln 10}{5.3019} \cdot 1 \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{1 \cdot \ln 10}{5.3019} \cdot 1 \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \cdot 1 \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \right) \cdot (-1)$$

SIMPLE

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \right) \cdot (-1)$$

So finally:

$$\cos(x \cdot \log_{10} x) \cdot \left( \log_{10} x + \frac{\ln 10}{5.3019} \right) \cdot (-1)$$