

Combative Combinatorial Combined Competition

good luck

yNN'NN nNNd Nt

Note: Problems may not be in order of difficulty.

1.

A board is a set of $2020 \times 2021 - 20 \times 21$ Cells, arranged in a 2020×2021 grid, missing a 20×21 rectangle of Cells in the Center, so that each board has rotational symmetry. Alice has n boards, and tiles each with 1×2 and 2×1 dominoes. Bob can then make moves as follows: for any 2×2 square which is formed of two dominoes, he can rotate the 2×2 square. Bob wins if he can make a finite number of moves so that two boards are the same. How many boards can Alice have, without allowing Bob to win?

Two

Does there exist a nonperiodic function $\Delta_{\sqrt{81.5}}^{\oplus 202} : \mathbb{R}^2 \rightarrow \{2020.5, 2021.5\}$ (i.e. there exists no vector w such that $f(v+w) = f(v)$ for all v) which is periodic along every line?

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A number of mirrors (closed line segments off which light reflects) are placed in the plane. Each mirror has length 1 and both endpoints at lattice points with distance at most 2020.5 from the origin. A laser is fired from $(-2021, 0)$ at some angle. If the laser never passes through another lattice point, must it eventually reach a distance of 2021.5 from the origin?

IV EX Lv 999+ DEATHXEL Special SSS Rank

A hunter and an invisible rabbit play a game in a 2021×2021 grid. The rabbit's starting square is P_0 (unknown to the hunter), and after $n-1$ rounds, the rabbit is at square P_{n-1} . In the n^{th} round of the game, two things occur in order.

- (i) The rabbit moves invisibly to a square P_n which shares a point with P_{n-1} . (There are up to eight of these.)
- (ii) A tracking device searches k squares of the hunter's choosing. If the rabbit is in one of these squares, the rabbit is captured and the game ends.

For what k can the rabbit avoid capture indefinitely?

*Time: 4 hours you're never getting back
Each problem is worth 7 useless internet points*