	$\mathrm{KL}_{0.1}$	kNN	ℓ -Trust	ℓ -RMSE	KL_{100}	Spear	MSE
GeomAE	0.169 ± 0.023	0.356 ± 0.007	0.938 ± 0.003	6.2 ± 1.2	$2.2e-07 \pm 3e-08$	0.4 ± 0.02	0.0357 ± 0.0003
Vanilla	$\boldsymbol{0.133 \pm 0.007}$	0.322 ± 0.01	0.93 ± 0.004	11 ± 3	$1.8e-07 \pm 2e-08$	0.44 ± 0.05	0.0356 ± 0.0007
${ m TopoReg}$		0.311 ± 0.005	0.925 ± 0.002	8.91 ± 0.05	$9.3\mathrm{e} ext{-}08\pm6\mathrm{e} ext{-}09$	0.64 ± 0.01	$0.03701 \pm 8e-05$
ParametricUMAP	IAP 0.1719 ± 0.0051	0.4162 ± 0.0012	0.9524 ± 0.0004	8.4 ± 0.4	$3.35e-07 \pm 2.1e-08$	0.36 ± 0.007	0.03213 ± 7 e- 05
$\overline{\text{UMAP}}$	0.19 ± 0.002	0.4013 ± 0.0003	$\textbf{0.94638} \pm \textbf{0.00051}$	$\underline{4.79\pm0.03}$	$4.1e-07 \pm 1e-08$	0.3377 ± 0.0042	NaN
$rac{ ext{TSNE}}{ ext{PCA}}$	0.168 ± 0.031 $0.16276402 \pm 2.2e-07$	0.404 ± 0.003	0.9443 ± 0.0005 $0.7456815 \pm 5e-07$	39.8 ± 0.1 $6.5830853 \pm 8e-07$	$2.9e-07 \pm 4e-08$ 1.636274e-07 \pm 2e-13	0.3 ± 0.03 $0.5246475 \pm 7e-07$	$_{ m NaN}$ 0.055636764 \pm 8e-09
			Fas	hionMNIST			
	$\mathrm{KL}_{0.1}$	kNN	ℓ -Trust	ℓ -RMSE	$ m KL_{100}$	Spear	MSE
GeomAE	0.0407 ± 0.0052	0.37 ± 0.03	0.971 ± 0.003	7 ± 1	$9.6\mathrm{e} ext{-}08 \pm 1.1\mathrm{e} ext{-}08$	0.75 ± 0.03	0.02562 ± 0.00013
Vanilla	0.069 ± 0.031	0.34 ± 0.02		14 ± 2	$1.6e-07 \pm 1e-07$	0.66 ± 0.12	0.0253 ± 0.0003
TopoReg	$\boldsymbol{0.049 \pm 0.01}$	0.366 ± 0.003	73	9.569 ± 0.081	$1.1e-07 \pm 2e-08$	$\boldsymbol{0.82\pm0.02}$	0.0261 ± 0.0002
ParametricUMAP	AP 0.091 ± 0.004	0.438 ± 0.002	0.9749 ± 0.0003	13.2 ± 0.6	$5.5e-07 \pm 3e-08$	0.58 ± 0.02	0.0234 ± 0.0001
UMAP	0.0947 ± 0.0021	0.422 ± 0.002	0.971 ± 0.001	4.416 ± 0.022	$3.01e-07 \pm 1e-08$	0.603 ± 0.002	NaN
$ ext{TSNE} \\ ext{PCA}$	0.072 ± 0.004 $0.052010267 \pm 8e-09$	$0.441 \pm 0.002 \\ \hline 0.2076921 \pm 4e-07$	0.96872 ± 0.0006 3 $0.91678396 \pm 5e-08$	39 ± 0.2 4.5253376 \pm 4e-07	$2.5e-07 \pm 1.2e-08$ 7.084261e-08 \pm 2e-14	0.56 ± 0.03 $0.88169565 \pm 1e-08$	$_{ m NaN} \\ 0.046092747 \pm 2e-09$
				PBMC			
	$\mathrm{KL}_{0.1}$	kNN	ℓ -Trust	ℓ-RMSE	KL_{100}	Spear	MSE
GeomAE	0.0297 ± 0.005	0.2771 ± 0.0042	0.924 ± 0.001	9.05 ± 0.6	$8e-08 \pm 2e-08$	0.732 ± 0.032	0.656 ± 0.006
Vanilla	0.05 ± 0.012	0.261 ± 0.003	0.9166 ± 0.0022	17 ± 11	$1.5e-07 \pm 6e-08$	0.7 ± 0.2	0.642 ± 0.007
TopoReg	0.0156 ± 0.0012	0.271 ± 0.003	0.922 ± 0.002	10.3 ± 0.3	$5.7\text{e-}08 \pm 9\text{e-}09$	0.873 ± 0.005	0.645 ± 0.012
Parametric UMAP	0.024 ± 0.003	0.286 ± 0.002	0.9256 ± 0.0012	$\textbf{5.8} \pm \textbf{0.3}$	$2.4e-07 \pm 1.3e-07$	0.776 ± 0.008	0.6018 ± 0.0042
UMAP	0.02832 ± 0.0007	0.25491 ± 0.00061	0.9106 ± 0.0007	6.33 ± 0.09	$2.9e-07 \pm 6e-08$	0.8044 ± 0.0023	NaN
TSNE	0.0418 ± 0.0052		0.9155 ± 0.0013	27.71 ± 0.08	$1.44e-07 \pm 1e-08$		
PCA	$\overline{0.0100239686 \pm 9\text{e-}10}$	$\underline{0}$ 0.133168 \pm 2e-06	$0.833481989 \pm 1e-08$	$6.57269076 \pm 8e-07$	$1.61267521e-07 \pm 4.1e-14$	$0.909258691 \pm 1.1\text{e-}08$	-08 1.10164175 ± 1.2e-07
	$\mathrm{KL}_{0.1}$	kNN	ℓ -Trust	$\ell ext{-RMSE}$	KL_{100}	Spear	MSE
Ğe	GeomAE 0.047 ± 0.009	0.009 0.464 ± 0.01	$0.956 \pm$	$0.002 17.6 \pm 1.2$	$1.4\text{e-}07 \pm 3.1\text{e-}08$	e-08 0.683 ± 0.091	0.73 ± 0.02
Va	Vanilla 0.09 ± 0.03	0.42 ± 0.02		0.007 36 ± 9	$2.8e-07 \pm 1e-07$		0.71 ± 0.02
CElegans To			0.9561	13			0.724 ± 0.004
	tricUMAP			8 1			$\overline{0.671\pm0.006}$
ID E					.05		NaN
LSIT ADA	÷1	80-99	16-07	0.93 ± 0.004 29.8 ± 0.2 0.23 ± 0.2 $0.8143107 + 3e-07 + 14 1533186 + 1e-06$	$1.81e-0.7 \pm 2.3e-0.8$ 1.41e-0.6 = 2.501011e-0.7 + 2e-1.3	0.494 ± 0.02 0.72 ± 0.02	NaN -07 2 06 + 0
	$\mathrm{KL}_{0.1}$	kNN	ℓ -Trust	$\ell ext{-RMSE}$	KL_{100}	Spear	MSE
GeomAE	0.11 ± 0.013	0.3945 ± 0.0072	0.943 ± 0.002	17 ± 2	$2.3\text{e-}07 \pm 1\text{e-}07$	0.71 ± 0.04	0.338 ± 0.004
Vanilla	0.14 ± 0.01	0.361 ± 0.008	0.939 ± 0.003	24 ± 8	$2.7e-07 \pm 6e-08$	0.64 ± 0.12	0.3332 ± 0.0022
TopoReg	0.124 ± 0.003	0.353 ± 0.003	0.924 ± 0.003	19.32 ± 0.06	$2.81e-07 \pm 3.1e-08$	0.734 ± 0.021	0.3431 ± 0.0004
ParametricUMAP		$\textbf{0.4068} \pm \textbf{0.0006}$	0.94653 ± 0.00053	10 ± 0.13	$3e-07 \pm 2e-07$	0.72 ± 0.04	$\textbf{0.3266}\pm\textbf{0.0005}$
$\widetilde{ ext{UMAP}}$	0.099 ± 0.006	0.387 ± 0.002	0.93717 ± 0.00033	12.48 ± 0.23	$3e-07 \pm 3e-08$	0.74 ± 0.03	$_{ m NaN}$
TSNE	$\frac{0.0977 \pm 0.0051}{0.11343118 \pm 10.08}$	0.3967 ± 0.0041	0.938 ± 0.002 0.86533776 ± 110.07	27.09 ± 0.11	$\frac{2.2\text{e-}07 \pm 1.2\text{e-}08}{2.0449645.07 \pm 30.13}$	0.516 ± 0.05	NaN 0 50147804 ± 3 0.08
1777	>> > + > > + > + > + > + > + > + > + >	0.5 0.5 H 10001117:0	· > > : - - >	·)	000141000