FNLP Distributional Semantics

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Q: What's the meaning of life?

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- This is hard to answer
- But we did mention it before

Lexcial Semantics

WordNet is a large lexical database of English. Nouns, verbs, adjectives and adverbs are grouped into sets of cognitive synonyms (synsets), each expressing a distinct concept.

Example (bank)

- S: (n) bank (sloping land (especially the slope beside a body of water)) "they pulled the canoe up on the bank"; ...
- S: (n) depository financial institution, ... (a financial institution that accepts deposits and channels the money into lending activities)
 "that bank holds the mortgage on my home"
- o ...

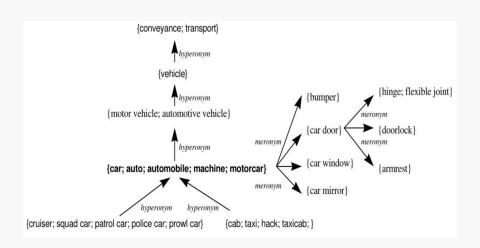
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- o ...
- Lemma or citation form
- Sense

WordNet



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 - not always identical in any contexts

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 - hot / cold
 - rise / fall
- Connotation (sentiment): affective meanings:
 - copy, replica / fake, knockoff

WordSim353 - Similarity

•	idontical	takanc
•	identical	LUKEHS
_		

- synonym
- antonyms
- first is hyponym of second
- first is hyperonym of second
- sibling terms
- first is part of the second one
- second is part of the first one
- topically related, but none of the above

[Agirre et al., 2009]

word1	word2	similarity
tiger	cat	7.35
tiger	tiger	10.00
plane	car	5.77
train	car	6.31
television	radio	6.77
media	radio	7.42
bread	butter	6.19
cucumber	potato	5.92
doctor	nurse	7.00
professor	doctor	6.62
student	professor	6.81
smart	stupid	5.81
wood	forest	7.73
money	cash	9.15

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WordSim353 - Relatedness

word2	relatedness
keyboard	7.62
Israel	8.46
galaxy	8.11
landscape	7.53
country	5.63
summer	3.94
dawn	7.53
citizen	7.31
people	5.75
ecology	8.81
football	8.62
oil	8.59
bank	8.50
software	8.50
	keyboard Israel galaxy landscape country summer dawn citizen people ecology football oil bank

word1	word2	similarity
vanish	disappear	9.8
behave	obey	7.3
belief	impression	5.95
muscle	bone	3.65
modest	flexible	0.98
hole	agreement	0.3

[Hill et al., 2015]

Have Fun



Human

词语相似度和词语相关性有区别吗

Assistant

词语相似度和词语相关性是有区别的。

词语相似度是指两个或多个词语在一定程度上具有相似的含义、结构、发音等特征,可以使用相似度计算方法 进行比较。例如,"苹果"和"梨子"都属于水果,它们的相似度较高。

词语相关性是指两个或多个词语在一定程度上具有相互关联、可以使用相关性计算方法进行比较。例如、"苹 果"和"水果"之间存在相关性、因为它们都属于水果这一类别。

因此、词语相似度和词语相关性是两个不同的概念、它们可以同时存在、也可以分别存在。

Semantic Field

Words that cover a particular semantic domain or bear structured relations with each other.

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Words that cover a particular semantic domain or bear structured relations with each other.

- hospitals
 - surgeon, scalpel, nurse, medication, hospital
- restaurants
 - waiter, menu, plate, food, menu, chef
- houses
 - door, roof, kitchen, family, bed

Word Meaning

- Words have many senses, thus polysemous
- There are complex relationships among senses, thus words

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How to Represent Words?

Naive representation

- The vast majority of rule-based and statistical NLP work regards words as atomic symbols:
 - PKU, study, studies, studied, learn, learning, China, china, ...
- Imagine a vector space, this is a vector with one 1 and a lot of 0s: [0,0,0,0,0,0,0,0,0,0,0,0] in $R^{|vocabulary|}$.

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- It is huge space: |vocabulary| can be very large: 50K (PTB), 13M (Google 1T)
- Less clear how to deal with compositionality
- Still haven't discussed how to do inference

A Motivating Example: POS tagging

Example

 The/det yinkish/adj dripner/noun blorked/verb quastofically/adv into/prep the/det nindin/noun with/prep the/det pidibs/noun.

As a structured prediction problem

- Structured prediction techniques
 - Structured perceptron
 - Conditional random fields
- It is easy to utilize rich features
 - Word form features
 - Morphological features

Features

- Word uni-grams:
- Word bi-grams:
- Prefix strings:
- Suffix strings:

- Word uni-grams: $w_{i-2}, w_{i-1}, w_i, w_{i+1}, w_{i+2}$
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- Prefix strings: $c_1, c_1c_2, c_1c_2c_3...$
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- Prefix strings: $c_1, c_1c_2, c_1c_2c_3...$
- Suffix strings: $c_n, c_{n-1}c_n, c_{n-2}c_{n-1}c_n...$

Features for $wi = c_1...c_n$ in $...w_{i-2}, w_{i-1}, w_i, w_{i+1}, w_{i+2}$

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When we can train a simple discriminative sequential tagger:

accuracy
93.61%
94.30%
94.42%

Error Analysis

Freq.	LLM	LGLM1	LGLM2	SR-HMM
0	78.72%	79.77%	80.66%	77.49%
1-5	87.75%	87.95%	88.13%	87.57%
6-10	90.04%	91.04%	91.28%	90.69%
11-100	94.49%	94.94%	94.80%	94.60%
101-1000	95.68%	96.08%	96.12%	96.23%
-				

Tagging accuracies relative to word frequency.

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Classification of low-frequency words is hard.

Error Analysis

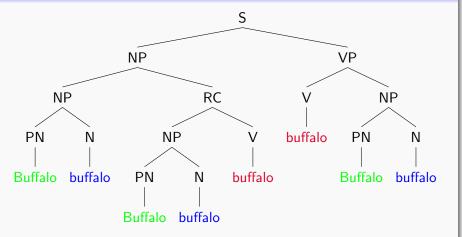
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But we still get something for those 0-frequency words.

Problems

- the noun buffalo, an animal
- the city of Buffalo, New York, United States
- the verb to bully, confuse, deceive, or intimidate

Buffalo buffalo buffalo buffalo buffalo buffalo buffalo.



Problems

Synonyms:

adept, expert, good, practiced, proficient, skillful?

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Missing new words (impossible to keep up to date):

Example (tezgüino)

- A bottle of tezgüino is on the table.
- Everyone likes tezgüino.
- tezgüino makes you drunk.
- We make tezgüino out of corn.

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Example (nindin)

- it was authentic nindin, rather sharp and very strong
- you could taste a famous local product nindin
- we spent hours in the pub drinking nindin

The Intuition

The contexts suggest

- tezgüino may be a kind of alcoholic beverage made from corn mash.
- nindin is a kind of a drink as well, maybe alcoholic.

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- tezgüino may be a kind of alcoholic beverage made from corn mash.
- nindin is a kind of a drink as well, maybe alcoholic.
- Use linguistic context to represent the meaning of words and phrases (partially).
- Meaning space with dimensions corresponding to elements in the context (features).
- Most computational techniques use vectors, or more generally tensors: a.k.a. *semantic space models, vector space models, embeddings*.

Guiding Hypotheses

- John Firth, (1957, A synopsis of linguistic theory)
 - You shall know a word by the company it keeps.
 - the complete meaning of a word is always contextual, and no study of meaning apart from context can be taken seriously.
- **Zellig Harris** (1954, Distributional structure)
 - distributional statements can cover all of the material of a language without requiring support from other types of information.

Distributional semantics: family of techniques for representing word meaning based on (linguistic) contexts of use.

Co-occurrence

First-order co-occurrence (syntagmatic association)

- They are typically nearby each other.
- wrote is a first-order associate of book or poem.

Second-order co-occurrence (paradigmatic association)

- They have similar neighbors.
- wrote is a second-order associate of words like said or remarked.

Clustering Algorithms

Example (Distributional word clustering)

Words that appear in similar context tend to have similar meanings.
 A model based on the word bi-gram context:

$$P(w_i|w_1,...,w_{i-1}) \approx P(C(w_i)|C(w_{i-1}))P(w_i|C(w_i))$$

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Powerful tools:

- http://www.statmt.org/moses/giza/GIZA++.html
- https://github.com/percyliang/brown-cluster

So far

- ullet Naive representation: One-hot vectors in $R^{|vocabulary|}$
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Distributional representation

[0.456, 0.193, 5.391, 1.235, -93.0]

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Distributional representation

Model a word by embedding it in a vector space.

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- Vectors are also called embeddings.

Various Vector Models

Sparse vector representations

- One-hot word representations
- Mutual-information weighted word co-occurrence matrices

Dense vector representations

- Brown clusters, giza++ clusters
- Dimension reduction
- Neural-network-inspired models (skip-grams, CBOW, ...)

Lexical semantics

- fast is similar to rapid
- tall is similar to height

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When question answering

- Q: How tall is Mt. Everest?
- A: The official height of Mount Everest is 29029 feet

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Knowledge based question answering

- Identifying or solving relations or properties in knowledge bases
- mapping natural language expressions with canonical expressions in knowledge bases

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Idea

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- Main approaches: count-based, prediction-based, and task-based.

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Count-based methods

- Define a basis vocabulary C of context words.
- Define a word window size w.
- Count the basis vocabulary words occurring w words to the left or right of each instance of a target word in the corpus.
- Form a vector representation of the target word based on these counts.

An example

Corpus

```
... and the cute kitten purred and then ...
... the cute furry cat purred and miaowed ...
... that the small kitten miaowed and she ...
... the loud furry dog ran and bit ...
```

```
Basis Vocabulary: {..., bit, cute, furry, loud, miaowed, purred, ...}. kitten's context words: {cute, purred, small, miaowed, ...}. cat's context words: {furry, purred, ...}. dog's context words: {furry, ran, ...}.
```

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- More to consider when counting
 - stop word list? the, that, and, ...
 - lemmatization? miaow, miaowed, dog, dogs, ...

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- More to consider when counting
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 - lemmatization? miaow, miaowed, dog, dogs, ...
- Size of windows depends on your goals
 - Shorter windows → more syntactic representation
 - Longer windows → more semantic representation

Raw counts?

Raw word frequency is not a great measure of association between words:

- the and of are very frequent, e.g., appearing in almost every document
- but maybe/definitely not the most discriminative features

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If raw counts are not good, then weight them!

Pointwise mutual information

• information-theoretic measurement: Do events X and Y co-occur more than if they were independent?

$$PMI(X,Y) = \log \frac{P(x,y)}{P(x)P(y)}$$

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Positive PMI

- It is not clear people are good at unrelatedness.
- We just replace negative PMI values by 0

Motivation behind PMI

Suppose the word *apricot* appear 20 times in our training data (which includes 1000 word tokens in total)

- If we see *apricot* appearing $0.02 * L_d$ times in a document d (which is L_d words-long), you will not feel surprised.
- If we see *apricot* appearing $0.2 * L_d$ times in a document d (which is L_d words-long), you will feel surprised!

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- Under the training data, 20/1000 = 0.02 will be the chance we see *apricot* in a document. (in a unigram assumption)
- One way to measure the surprise: compute the ratio of observed frequency of *apricot* in a document, e.g., 0.2, against the chance under the independence/unigram assumption, e.g., 0.02

Positive Pointwise Mutual Information

- event X: see word a (e.g., apricot) co-occurring with context word w, where w appears l_w times in total
- ullet event Y: see word a (e.g., apricot) appearing in the training data with N words in total

$$PMI(X,Y) = \left[\log \frac{\mathsf{count}_w(a)/N}{l_w/N \times \sum_c \mathsf{count}_c(a)/N}\right]_+ = \left[\log \frac{\mathsf{count}_w(a)*N}{\sum_c \mathsf{count}_c(a)*l_w}\right]_+$$

where $[score]_{+} = \max(score, 0)$.

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where $[score]_{+} = \max(score, 0)$.

- ullet if apricot appears with almost the same frequency for every context word w, then its PMI scores for evey w will be nearly ZERO
- if apricot appears only with one context word w^* , then its PMI scores for this w^* will be a large positive value.
- PPMI may tell us: where a unigram model is the most wrong :-)

An Example

Matrix: target words \times context words

	computer	data	pinch	result	sugar	
apricot	0	0	1	0	1	
pineapple	0	0	1	0	1	
digital	2	1	0	1	0	
information	1	6	0	4	0	

raw counts

 $Matrix: \ target \ words \ \times \ context \ words$

	computer	data	pinch	result	sugar	
apricot	0.00	0.00	0.05	0.00	0.05	
pineapple	0.00	0.00	0.05	0.00	0.05	
digital	0.11	0.05	0.00	0.05	0.00	
information	0.05	0.32	0.00	0.21	0.00	

• computing p(.)

 $Matrix: \ target \ words \ \times \ context \ words$

	computer	data	pinch	result	sugar	p(word)
apricot	0.00	0.00	0.05	0.00	0.05	0.11
pineapple	0.00	0.00	0.05	0.00	0.05	0.11
digital	0.11	0.05	0.00	0.05	0.00	0.21
information	0.05	0.32	0.00	0.21	0.00	0.58

• computing p(x)

Matrix: target words \times context words

	computer	data	pinch	result	sugar	p(word)
apricot	0.00	0.00	0.05	0.00	0.05	0.11
pineapple	0.00	0.00	0.05	0.00	0.05	0.11
digital	0.11	0.05	0.00	0.05	0.00	0.21
information	0.05	0.32	0.00	0.21	0.00	0.58
p(context)	0.16	0.37	0.11	0.26	0.11	

• computing p(y)

Matrix: target words \times context words

	computer	data	pinch	result	sugar	p(word)
apricot			2.25		2.25	0.11
pineapple			2.25		2.25	0.11
digital	1.66	0.00		0.00		0.21
information	0.00	0.57		0.47		0.58
p(context)	0.16	0.37	0.11	0.26	0.11	

- ullet computing PPMI
- $\log_2 \frac{1*19}{2*2}$

- PMI is biased toward infrequent events
- Very rare words have very high PMI values
- Solution: Laplace (add-one) smoothing

	computer	data	pinch	result	sugar	
apricot	2	2	3	2	3	
pineapple	2	2	3	2	3	
digital	2	3	2	3	2	
information	3	8	2	6	2	

- PMI is biased toward infrequent events
- Very rare words have very high PMI values
- Solution: Laplace (add-one) smoothing

	computer	data	pinch	result	sugar	
apricot	0.03	0.03	0.05	0.03	0.05	
pineapple	0.03	0.03	0.05	0.03	0.05	
digital	0.11	0.05	0.03	0.05	0.03	
information	0.05	0.14	0.03	0.10	0.03	

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	computer	data	pinch	result	sugar	P(word)
apricot	0.03	0.03	0.05	0.03	0.05	0.20
pineapple	0.03	0.03	0.05	0.03	0.05	0.20
digital	0.11	0.05	0.03	0.05	0.03	0.24
information	0.05	0.14	0.03	0.10	0.03	0.36

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	computer	data	pinch	result	sugar	P(word)
apricot	0.03	0.03	0.05	0.03	0.05	0.20
pineapple	0.03	0.03	0.05	0.03	0.05	0.20
digital	0.11	0.05	0.03	0.05	0.03	0.24
information	0.05	0.14	0.03	0.10	0.03	0.36
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	computer	data	pinch	result	sugar	p(word)
apricot			0.56		0.56	0.20
pineapple			0.56		0.56	0.20
digital	0.62	0.00		0.00		0.24
information	0.00	0.58		0.37		0.36
p(context)	0.19	0.25	0.17	0.22	0.17	

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- Cosine of angle is easy to compute.
 - cos = 1 means angle is 0, i.e. very similar
 - cos = 0 means angle is 90, i.e. very dissimilar

$$cos(\mathbf{u}, \mathbf{v}) = \frac{\mathbf{u}^{\top} \mathbf{v}}{||\mathbf{u}|| \cdot ||\mathbf{v}||}$$

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Many other methods to compute similarity

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Using Syntax to Define a Word's Context

Zellig Harris (1968)

- The meaning of entities, and the meaning of grammatical relations among them, is related to the restriction of combinations of these entities relative to other entities.
- Two words are similar if they have similar syntactic contexts
- duty and responsibility have similar syntactic distribution:
 - Modified by adjectives: additional, administrative, assumed, collective, congressional, constitutional, ...
 - Objects of verbs: assert, assign, assume, attend to, avoid, become, breach, ...

```
I have a brown dog
(have subj l), (I subj-of have), (dog obj-of have), (dog adj-mod brown),
(brown adj-mod-of dog), (dog det a), (a det-of dog)
```

The description of cell

```
count(cell, subj-of, absorb)=1 count(cell, subj-of, adapt)=1 count(cell, subj-of, behave)=1 ... count(cell, pobj-of, in)=159 count(cell, pobj-of, inside)=16 count(cell, pobj-of, into)=30
```

Context based on Dependency Parsing

- hope (N):
 optimism 0.141, chance 0.137, expectation 0.136, prospect 0.126,
 dream 0.119, desire 0.118, fear 0.116, effort 0.111, confidence 0.109,
 promise 0.108
- hope (V):
 would like 0.158, wish 0.140, plan 0.139, say 0.137, believe 0.135,
 think 0.133, agree 0.130, wonder 0.130, try 0.127, decide 0.125
- brief (N): legal brief 0.139, affidavit 0.103, filing 0.098, petition 0.086, document 0.083, argu- ment 0.083, letter 0.079, rebuttal 0.078, memo 0.077
- brief (A): lengthy 0.256, hour-long 0.191, short 0.173, extended 0.163, frequent 0.162, recent 0.158, short-lived 0.155, prolonged 0.149, week-long 0.149

[Dekang Lin, 1998]

Problems

Similarity = Synonymy?

- Antonyms are basically as distributionally similar as synonyms:
- Distributional similarity is not referential similarity.
- Distinguishing synonyms from antonyms is notoriously hard problem.

brief (A):

lengthy 0.256, hour-long 0.191, short 0.173, extended 0.163, frequent 0.162, recent 0.158, short-lived 0.155, prolonged 0.149, week-long 0.149, occasional 0.146

Document?

	d1	d2	d3	d4	d5	d6	d7	d8	d9	d10
against	0	0	0	1	0	0	3	2	3	0
age	0	0	0	1	0	3	1	0	4	0
agent	0	0	0	0	0	0	0	0	0	0
ages	0	0	0	0	0	2	0	0	0	0
ago	0	0	0	2	0	0	0	0	3	0
agree	0	1	0	0	0	0	0	0	0	0
ahead	0	0	0	1	0	0	0	0	0	0
ain't	0	0	0	0	0	0	0	0	0	0
air	0	0	0	0	0	0	0	0	0	0
aka	0	0	0	1	0	0	0	0	0	0

Each cell: count of word w in a document d:

- Each document is a count vector: a column above
- Each word is a count vector: a row above

Document?

d10
ulu
0
0
0
0
0
0
0
0
0
0

- Two documents are similar if their vectors are similar
- Two words are similar if their vectors are similar

Document?

	d1	d2	d3	d4	d5	d6	d7	d8	d9	d10
against	0	0	0	1	0	0	3	2	3	0
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ago	0	0	0	2	0	0	0	0	3	0
agree	0	1	0	0	0	0	0	0	0	0
ahead	0	0	0	1	0	0	0	0	0	0
ain't	0	0	0	0	0	0	0	0	0	0
air	0	0	0	0	0	0	0	0	0	0
aka	0	0	0	1	0	0	0	0	0	0

- Two documents are similar if their vectors are similar
- Two words are similar if their vectors are similar
- The matrix seems not so friendly though

Dimension Reduction

Too sparse?

Dimension Reduction

Too sparse?

We got a plan!

Approximate a high-dimensional matrix using fewer dimensions

- first rotating the axes into a new space
- in which the highest order dimension captures the most variance in the original dataset
- and the next dimension captures the next most variance, etc.
- we may only keep a small number of dimensions, e.g., 50, 100, or 300 ...
- Many such (related) methods: principle components analysis (PCA),
 Factor Analysis, LSA, etc.

Dimensionality Reduction

Why dense vectors?

- Short vectors may be easier to use as features in machine learning
- Dense vectors may generalize better than storing explicit counts

Dense embeddings sometimes work better than sparse PPMI matrices at tasks like word similarity

- Denoising: low-order dimensions may represent unimportant information
- Truncation may help the models generalize better to unseen data.

For a **sparse** word-document co-occurrence matrix A, Latent Semantic Analysis (or Latent Semantic Indexing, LSA, LSI) seeks to find an approximation for A:

$$A \approx \hat{A} = M \times \mathsf{diag}(s) \times C^{\mathsf{T}}$$

 \bullet \hat{A} is the approximated matrix, M the <code>embeddings</code> of words, C contains representations of documents

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 - ullet M stores left singular vectors of A
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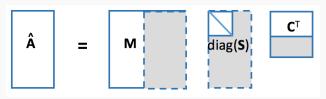
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 - ullet M stores left singular vectors of A
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 - ullet s stores singular values of A, non-negative and usually organized in decreasing order
 - ullet if some values in ${\sf diag}(s)$ are zeros, then A is ${\it low-rank}$
 - ullet we could approximate A by truncating s to keep only k non-negative values

SVD

$$\mathbf{A} = \mathbf{M}$$
 diag(S)

truncated SVD



- create a mapping of words and documents into the same low-dimensional space
- ullet could deal with sparseness or even noise in A
- words that occur in similar contexts have similar meanings.
- could deal with synonyms somehow
- still a bag-of-words assumption
- but, need to cope with new words, new documents

There is a probabilistic version, Probabilistic Latent Semantic Analysis (PLSA, Hofmann, 1999)

For every document d with l_d words in a large corpus:

$$\begin{split} p(\mathbf{x}_d, \mathbf{z}|d) &= \prod_{i=1}^{l_d} p_{topic}(z_i|d) \cdot p_{word}(x_{d,i}|z_i) \\ p(\mathbf{x}_d|d) &= \sum_{\mathbf{z} \in \{1, 2, \dots K\}^{l_d}} p(\mathbf{x}_d, \mathbf{z}|d) \end{split}$$

- we could think each document d is generated by a mixture of K topics
- p_{topic} is a distribution over K topics for each document
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Four Kinds of Vector Models

Sparse vector representations

Mutual-information weighted word co-occurrence matrices

Dense vector representations

- Brown clusters, giza++ clusters
- Neural-network-inspired models (skip-grams, CBOW, ...)

Four Kinds of Vector Models

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- Mutual-information weighted word co-occurrence matrices
- ullet Dimension reduction o dense vectors

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Basic Idea

- To produce dense vector representations based on the context/use of words.
- Three main approaches: count-based, prediction-based, task-based.

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word2vec

• Predict between every word and its context words!

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word2vec

- Predict between every word and its context words!
- Continuous bag of words (CBOW) p(word|context)
 - This is very similar to what we have talked about in the feedforward neural language model (Begnio et al., 2003)
- Skip-gram: p(context|word)

Neural Language Model

Basic form of continuous bag of words:

$$p(w_n|w_{n-2},w_{n-1},w_{n+1},w_{n+2}) =$$

$$\operatorname{softmax}(b + \sum_{j=n-2, j \neq n}^{n+2} \underline{m_{w_j}} A_j + W \tanh(u + \sum_{j=n-2, j \neq n}^{n+2} \underline{m_{w_j}} T_j))$$

- parameters: b, A, W, T, u, M
- vocabulary size: $V = |\mathcal{V}|$, hidden size: H, word embeddings dim. d
- b(V), A(d, V), W(V, H), T(d, H), u(H), M(V, d)

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Skip-gram Model (Mikolov et al., 2013)

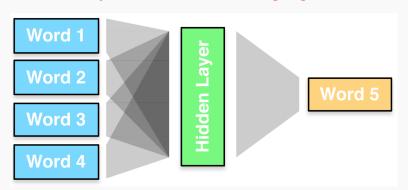
The key is to predict the context words given the target word, $p(\mbox{context}|\mbox{word})$

$$p(\mathsf{context} = c | \mathsf{word} = w) = \frac{1}{Z_w} \exp \mathbf{c}_c^\mathsf{T} \mathbf{w}_w$$

- ullet two different vectors for each word: one w when it is our target word and one c when it is in the context
- using SGD to estimate the vectors
- ullet computing the normalization term Z_w is expensive, so there are many tricks to perform approximations for efficiency
- need to consider how we define the *context*, *k*-words window, sentences, paragraphs, or even document

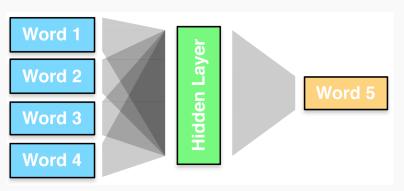
Treat LM in a classification paradigm:

Today, I will talk about language ____



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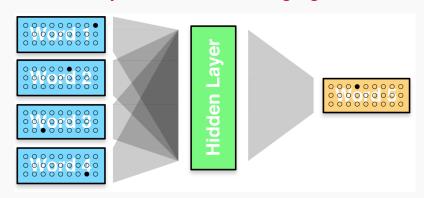


- Using word as itself can be problematic
- Synonyms, Hypernyms, ...

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Treat LM in a classification paradigm:

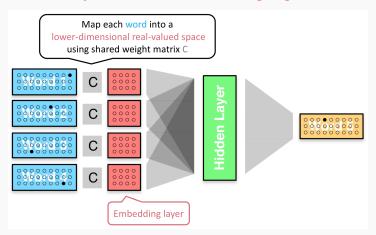
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Vector representations, e.g., one-hot, ...

Treat LM in a classification paradigm:

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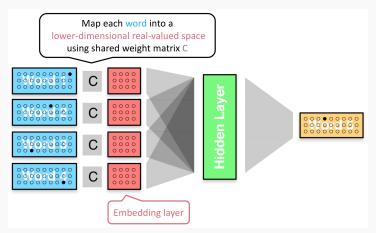
Continuous vector presentations

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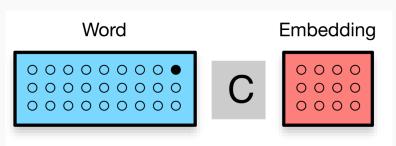


Continuous vector presentations → Lookup table

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Treat LM in a classification paradigm:

Today, I will talk about language ____



- Make lookup table trainable
- NNs naturally produce word embeddings
- Similar words tend to have similar embeddings: car, van, ...

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Evaluating Word Vectors

Intrinsic Evalutions

- first calculate the similarities between pairs of word vectors, and then calculate the correlation with the judgments of similarity given by humans
- have a TOEFL-like synonym test! e.g., select the one that can best replace $rug \rightarrow \{sofa, ottoman, carpet, hallway\}$?
- syntactic analogies, e.g., Peking is to China as Paris is to what?
- human study, e.g., manual inspection

Evaluating Word Vectors

Extrinsic Evalutions

- Use large unannotated corpus to get your word vectors
- Use them in a text classifier or some other NLP systems
 - Plug in word vectors as frozen features, and estimate the other parameters of your model
 - Treat them as parameters of the text classifier; pretraining gives initial values, but they get updated, or *finetuned* during supervised learning.
- Does that system's performance improve?

Count-based vs Prediction-based

Count-based approaches

- Sparse vector representations
- Fast training
- Efficient usage of statistics
- Primarily used to capture word similarity

Prediction-based approaches

- Dense vector representations
- Scales with corpus size
- Inefficient usage of statistics
- Generate improved performance on other tasks
- Can capture complex patterns beyond word similarity

Sparse vectors vs dense vectors

PPMI vectors

- long (length |V| = 20, 000 to 50,000)
- sparse (most elements are zero)

Prediction learned vectors

- short (length 200-1000)
- dense (most elements are non-zero)

Why dense?

- Short vectors may be easier to use as features in machine learning
- Dense vectors may generalize better than storing explicit counts

Word Representations

Words may have multiple distinct meanings.

Example (play)

- The new-look play area is due to be completed.
- These districts favor representatives who play to the party base .
- MJ just completed the three-point play for a 66-63 lead.

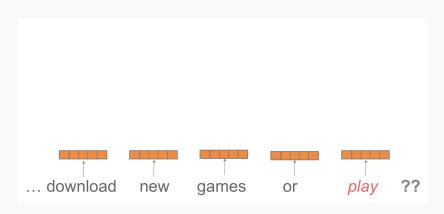
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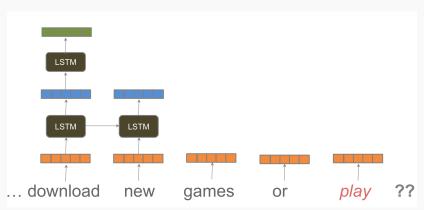
One vector per word is not enough



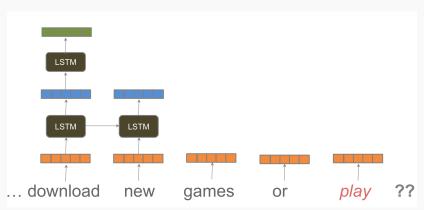
[from Mohit lyyer]

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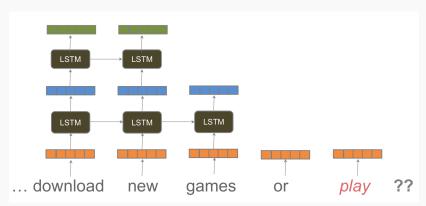
Go Deeper!



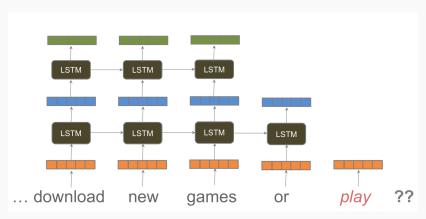
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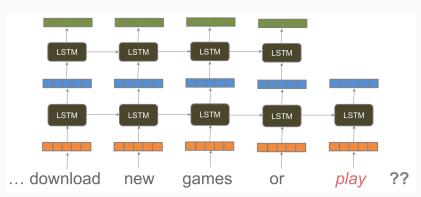
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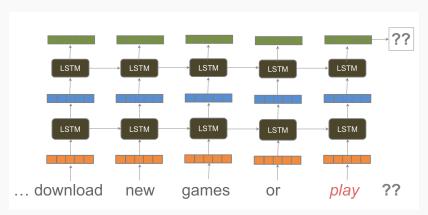
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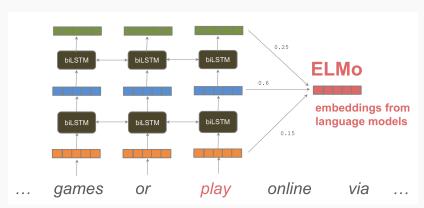
Go Deeper!



Go Deeper!



Go Deeper!



Take-away

- One-hot vectors
- PPMI vectors
- Dimention reduction
- Word2vector, Glove
- Elmo, BERT, ...
- ?

Take-away

- One-hot vectors
- PPMI vectors
- Dimention reduction
- Word2vector, Glove
- Elmo, BERT, ...
- ?
- More data, deeper networks
- Pretrain on alternative tasks to language modeling and masked language modeling
- Purposely select what data and/or tasks should learn over time
- Probing the learned representations to determine the extent to which various linguistic, commonsense, world, or domain knowledge is captured

Readings

- Dekang Lin. 1998. Automatic Retrieval and Clustering of Similar Words.
- Tomas Mikolov, Kai Chen, Greg Corrado and Jeffrey Dean. 2013.
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- Dan Jurasky's LSA tutorial: http://web.stanford.edu/~jurafsky/li15/index.html
- Chapter 6. Speech and Language Processing: https://web.stanford.edu/~jurafsky/slp3/6.pdf
- Eneko Agirre, Enrique Alfonseca, Keith Hall, Jana Kravalova, Marius Pasca, Aitor Soroa, A Study on Similarity and Relatedness Using Distributional and WordNet-based Approaches, In Proceedings of NAACL-HLT 2009.
- Thomas Hofmann. Probabilistic latent semantic indexing. In Proc. of SIGIR, 1999.
- Tomas Mikolov, Ilya Sutskever, Kai Chen, Greg S. Corrado, and Jeff Dean. Distributed representations of words and phrases and their compositionality. In NeurIPS, 2013b

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CHAPTER

6

Vector Semantics and Embeddings

荃者所以在鱼,得鱼而忘荃 Nets are for fish;

Once you get the fish, you can forget the net.

言者所以在意,得意而忘言 Words are for meaning;

Once you get the meaning, you can forget the words 庄子(Zhuangzi), Chapter 26

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