

1.

$$(a) f(A, B, C, D) = \sum m(1, 2, 7, 12, 15) + d(5, 9, 10, 11, 13)$$

真值表:

| | A | B | C | D | f |
|----|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 |
| 2 | 0 | 0 | 1 | 0 | 1 |
| 3 | 0 | 0 | 1 | 1 | 0 |
| 4 | 0 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 0 | 1 | X |
| 6 | 0 | 1 | 1 | 0 | 0 |
| 7 | 0 | 1 | 1 | 1 | 1 |
| 8 | 1 | 0 | 0 | 0 | 0 |
| 9 | 1 | 0 | 0 | 1 | X |
| 10 | 1 | 0 | 1 | 0 | X |
| 11 | 1 | 0 | 1 | 1 | X |
| 12 | 1 | 1 | 0 | 0 | 1 |
| 13 | 1 | 1 | 0 | 1 | X |
| 14 | 1 | 1 | 1 | 0 | 0 |
| 15 | 1 | 1 | 1 | 1 | 1 |

卡诺图:

| AB \ CD | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | 0 | 1 | 0 |
| 01 | 1 | X | X | X |
| 11 | 0 | 1 | 1 | X |
| 10 | 1 | 0 | 0 | X |

质蕴涵项: $B'CD'$, $C'D$, ABC' , BD 实质蕴涵项: $B'CD'$, $C'D$, ABC' , BD

$$(b) f(A, B, C, D) = \prod M(3, 4, 10, 13, 15) \cdot D(6, 7, 14)$$

真值表:

| | A | B | C | D | f |
|----|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 | 1 |
| 2 | 0 | 0 | 1 | 0 | 1 |
| 3 | 0 | 0 | 1 | 1 | 0 |
| 4 | 0 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 0 | 1 | 1 |
| 6 | 0 | 1 | 1 | 0 | X |
| 7 | 0 | 1 | 1 | 1 | X |
| 8 | 1 | 0 | 0 | 0 | 1 |
| 9 | 1 | 0 | 0 | 1 | 1 |
| 10 | 1 | 0 | 1 | 0 | 0 |
| 11 | 1 | 0 | 1 | 1 | 1 |
| 12 | 1 | 1 | 0 | 0 | 1 |
| 13 | 1 | 1 | 0 | 1 | 0 |
| 14 | 1 | 1 | 1 | 0 | X |
| 15 | 1 | 1 | 1 | 1 | 0 |

卡诺图:

| AB \ CD | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | | 0 | | |
| 01 | | | 0 | |
| 11 | 0 | X | 0 | |
| 10 | | X | X | 0 |

质蕴涵项:

$$A+B'+D', A+C'+D', A'+B'+D', A'+C'+D, B'+C'$$

实质蕴涵项:

$$A+B'+D', A+C'+D', A'+B'+D', A'+C'+D'$$

2. $f(A,B,C,D) = \sum m(0,1,4,7,9,12) + d(8,11,15)$

| 最小项 | ABCD | 最小项 | ABCD | 最小项 | ABCD |
|-----|--------|-------|----------------------|----------|----------------------|
| 0 | 0000 ✓ | 0,1 | 000_ ✓ | 0,1,8,9 | -00_ PI ₁ |
| 1 | 0001 ✓ | 0,4 | 0_00 ✓ | 0,4,8,12 | --00 PI ₂ |
| 4 | 0100 ✓ | 0,8 | -000 ✓ | | |
| 8 | 1000 ✓ | 1,9 | -001 ✓ | | |
| 9 | 1001 ✓ | 8,9 | 100_ ✓ | | |
| 12 | 1100 ✓ | 4,12 | -100 ✓ | | |
| 7 | 0111 ✓ | 8,12 | 1_00 ✓ | | |
| 11 | 1011 ✓ | 9,11 | 10_1 PI ₃ | | |
| 15 | 1111 ✓ | 7,15 | -111 PI ₄ | | |
| | | 11,15 | 1_11 PI ₅ | | |

✓ ✓ ✓ ✓

0 1 4 7 9 12.

*PI₁ X ⊗ X

PI₂ X X X

PI₃ X

*PI₄ ⊗

⇒

PI₃.

4 12

*PI₂ ⊗ ⊗

∴ 选 PI₁. PI₄. PI₂.

$f(ABCD) = B'C' + C'D' + BCD$

3.

| | Next State | | Present Out | |
|---|------------|-----|-------------|-----|
| | X=0 | X=1 | X=0 | X=1 |
| A | A | E | 1 | 0 |
| B | C | F | 0 | 0 |
| C | B | H | 0 | 0 |
| D | E | F | 0 | 0 |
| E | D | A | 0 | 0 |
| F | B | F | 1 | 0 |
| G | D | H | 0 | 0 |
| H | H | G | 1 | 0 |

划分法

P_0 (A B C D E F G H)
 out X=0 1 0 0 0 0 1 0 1 (A F H) (B C D E G)
 X=1 0 0 0 0 0 0 0 0

P_1 (A F H) (B C D E G)
 Next X=0 A B H | C B E D D (A H) (F)
 Next X=1 E F G | F H F A H (A H) (F)

P_2 (A H) (F) (B C D E G)
 Next X=0 A H | B | C B E D D
 Next X=1 E G | F | F H F A H (B D) (C E G)

P_3 (A H) (F) (B D) (C E G)
 Next X=0 A H | B | C E | B D D
 Next X=1 E G | F | F F | H A H

$P_4 = P_3$. (A H) (F) (B D) (C E G) \Rightarrow No. (A H) (B D) (C E G) (F)

\therefore $A' = (A H)$
 $B' = (B D)$
 $C' = (C E G)$
 $D' = (F)$

| | Next | | Out | |
|----|------|-----|-----|-----|
| | X=0 | X=1 | X=0 | X=1 |
| A' | A' | C' | 1 | 0 |
| B' | C' | D' | 0 | 0 |
| C' | B' | A' | 0 | 0 |
| D' | B' | D' | 1 | 0 |

蕴涵表法

| | | | | | | | |
|---|--------------------------------|--------------------------------|--------------------------------|--------------------------------|---------------|---|---|
| B | X | | | | | | |
| C | X | BC EH | | | | | |
| D | X | CE | BE HF | | | | |
| E | X | CD AF | BD AH | DE AF | | | |
| F | AB EF | X | X | X | X | | |
| G | X | CD HF | BD | DE FH | AH | BC EH FG | |
| H | AH EG | X | X | X | X | X | X |
| | A | B | C | D | E | F | G |

| | |
|---|------|
| A | (AH) |
| B | (BD) |
| C | (CG) |
| D | - |
| E | (EG) |
| F | - |
| G | - |

$$\therefore P_k = (AH)(BD)(CEG)(F)$$

$$A' \quad B' \quad C' \quad D'$$

| | Next | | Out | |
|----|------|-----|-----|-----|
| | X=D | X=1 | X=D | X=1 |
| A' | A' | C' | 1 | 0 |
| B' | C' | D' | 0 | 0 |
| C' | B' | A' | 0 | 0 |
| D' | B' | D' | 1 | 0 |

4.

根据规则1: $C' \text{ adj. } D'$, $B' \text{ adj. } D'$

规则2: $A' \text{ adj. } C'$, $C' \text{ adj. } D'$, $B' \text{ adj. } A'$
 $B' \text{ adj. } D'$

$\therefore A'-C', A'-B', C'-D', B'-D'$

应相邻

$\therefore \overbrace{A'-C'-D'-B'}$
 或 $\underbrace{A'-B'-D'-C'}$

\therefore 编码.

| | ① | ② | ③ | ④ | ⑤ | ⑥ | ⑦ | ⑧ |
|------|----|----|----|----|----|----|----|----|
| A' | 00 | 01 | 11 | 10 | 00 | 01 | 11 | 10 |
| B' | 10 | 00 | 01 | 11 | 01 | 11 | 10 | 11 |
| C' | 01 | 11 | 10 | 00 | 10 | 00 | 01 | 00 |
| D' | 11 | 10 | 00 | 01 | 11 | 10 | 00 | 01 |