

Chemmat 121

Alexander Bailey

E-mail: alexkingstonbailey@gmail.com

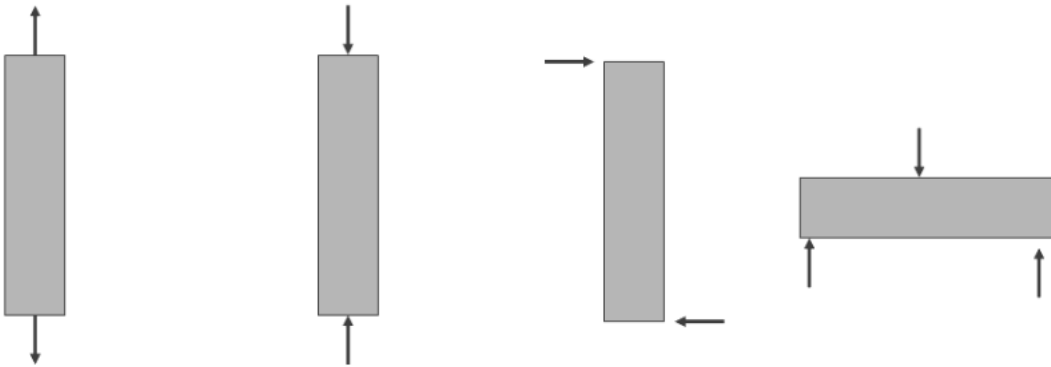
Contents

1	Deformation and structure of solids	1
1.1	Strength	1
1.2	Stress	1
1.3	Strain	2
1.4	Stress-Strain Curve	2
1.5	Poisson's Ratio	3
1.6	Young's Modulus	3
1.7	Steel	3
1.8	0.2% Proof Stress	3
1.9	Safety Factor	3
1.10	Engineering Stress vs Real Stress	3
1.11	Ductility	4
2	Microstructure and mechanical properties	4
2.1	Crystal Structure	4
2.1.1	Body Centered Cubic	4
2.1.2	Face Centered Cubic	5
2.1.3	Hexagonal Close Packed	5
2.2	Density	5
2.3	Polymorphism	5
3	Phase diagrams and Alloying	6
4	Strengthening mechanisms	6
5	Engineering ceramics and glasses	6
6	Polymers	6
7	Failure of materials	6
8	Corrosion of metals	6
9	Engineering composites	6

1 Deformation and structure of solids

1.1 Strength

How much force can a material withstand before it fails? That's a materials strength. A material can fail in several ways but the two most common are fracturing and permanent deformation.



Some types of force that a material/object can undergo
From left: Tension, Compression, Shear and a Combination.

1.2 Stress

Engineers typically talk about stress instead of forces because stress is just a force proportional to its area. Stress is represented by the greek letter sigma (σ) and is given by the force (F) divided by the cross-sectional area (A).

$$\sigma = \frac{F}{A}$$

Cross-sectional area is the area that is perpendicular to the applied force

Example

Given: $m = 25 \text{ kg}$, $d = 10 \text{ mm}$

$$A = \pi r^2$$

$$A = \pi \times \frac{(0.01)^2}{2}$$

$$F = 25 \times 9.81$$

$$\sigma = \frac{F}{A}$$

$$\sigma = 3,120,000 \text{ Pa}$$

$$\sigma = 3.12 \text{ MPa}$$



1.3 Strain

Strain is how long something gets compared to its original size. Stress and strain are related very closely and the stress against strain graph is a very important thing to materials engineering. Strain is given by the change in length over the original length.

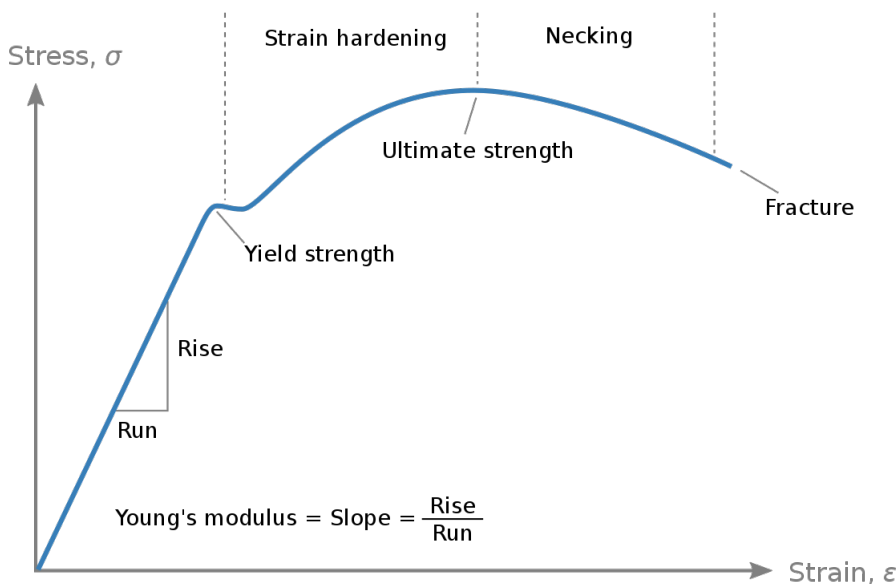
$$\epsilon = \frac{\Delta L}{L_o}$$

Strain is unitless but is commonly expressed as a percentage (%).

Example

$$\begin{aligned}\epsilon &= \frac{\Delta L}{L_o} \\ &= \frac{100.32 \text{ mm} - 100 \text{ mm}}{100 \text{ mm}} \\ &= \frac{0.32 \text{ mm}}{100 \text{ mm}} \\ &= 0.0032 \\ &= 0.32\%\end{aligned}$$

1.4 Stress-Strain Curve



The area under the curve is $F \times d$ and gives the 'toughness' which is approximately the energy required.

Necking is a localised reduction in thickness, which reduces diameter, which reduces area, increasing stress. This causes it to fail.

1.5 Poisson's Ratio

Poisson's ratio is the relationship between deformation for a given material. It is a measure of the Poisson effect, that describes the expansion or contraction of a material in directions perpendicular to the direction of loading. It has no units and is represented by the greek character 'nu' (ν). For most materials $\nu \approx 0.3$.

$$\nu = \frac{-\epsilon_x}{\epsilon_z}$$

1.6 Young's Modulus

The Young's Modulus of a material is a measure of the 'stiffness'. It is the gradient of the elastic part of the stress-strain curve for a given material. It has units of Pascals (Pa) and is represented by the capital letter E.

$$E = \frac{\Delta\sigma}{\Delta\epsilon}$$

1.7 Steel

Steel has what is called a 'discontinuous yield'. This means at the yield strength there is a bit of 'noise' and it moves a little randomly before becoming nonlinear.

1.8 0.2% Proof Stress

The 0.2% Proof Stress of a material is a geometrical construct that is used when the yield stress of a material cannot be properly determined. It is a very slight overestimate (generally) that can be calculated by drawing a line parallel to the actual curve at a strain of 0.002 and finding the intersection with the original curve. This stress value is the approximation.

1.9 Safety Factor

The safety factor is a scalar value that demonstrates how much more stress a material can hold relative to the requirement. I.e. if, for example, $F \approx 1000\text{ N}$ the engineers might pretend $F = 2000\text{ N}$. This would give a safety factor of 2. When the conditions of the material are more uncertain, you would want a higher safety factor.

1.10 Engineering Stress vs Real Stress

In engineering, we draw a stress-strain graph as going 'down' after the ultimate tensile strength. In reality, because of the effect of necking, it goes up after this. As engineers, we use the model because it is easier to handle theoretically.

1.11 Ductility

Ductility is a measure of how much something can deform elastically (with 100% recovery / without permanent deformation). The stress-strain graph of a ductile material will have a longer elastic section while a more brittle material (less ductile) will have a shorter one. It is generally described by one of two equations:

Percentage Elongation

$$= \frac{\Delta L}{L_o} \times 100\%$$

Percentage Reduction in Area

$$= \frac{\Delta A}{A_o} \times 100\%$$

2 Microstructure and mechanical properties

2.1 Crystal Structure

If a material is crystalline, the atoms of a material have **LONG RANGE ORDER**. This means the material is made up of a crystal lattice made of repeating units called 'unit cells'.

There are 14 possible crystal arrangements but this course will only look at three. We describe arrangements by looking at the unit cell. The unit cell is a tessellating shape that has all the information to describe the entire lattice.

The unit cell has 4 important properties:

- Number of atoms
- Co-ordination Number (The number of neighbours for the unit cell)
- Unit Cell Dimension (The length of each side of the cell written 'a')
- Atomic Packing Factor (Amount of space taken up by the atoms)

$$a = \text{Atomic Packing Factor} = \frac{\text{volume of atoms}}{\text{volume of unit cell}}$$

2.1.1 Body Centered Cubic

Body Centered Cubic (BCC) has one atom at each corner of a cube and one right in the middle.



- Number of Atoms = $2 = 1 + 8 \times \frac{1}{8}$
- Co-ordination Number = 8
- Unit cell dimension = $\frac{4R}{\sqrt{3}}$
- APF = 0.68 = 68%

2.1.2 Face Centered Cubic

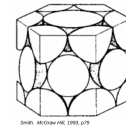
Face Centered Cubic (FCC) has one atom at each corner of a cube and one in the middle of each face of the cube.



- Number of Atoms = 4
- Co-ordination Number = 12
- unit cell dimension = $\frac{4R}{\sqrt{2}}$
- APF = 0.74 = 74%

2.1.3 Hexagonal Close Packed

Hexagonal Close Packed (HCP) is a prism shape with hexagonal arrangements of atoms layered up.



- Number of Atoms = 6
- Co-ordination Number = 12
- APF = 0.74 = 74%

2.2 Density

Density is the degree of compactness of a substance. The amount of mass you get for a given volume. The density of a material is its mass divided by its volume.

$$\rho = \frac{n \cdot A}{V_c \cdot N_a}$$

Where n is the number of atoms per unit cell, A is the atomic mass of the material, V_c is the volume of the unit cell (a^3) and N_a is Avogadro's Number.

Example

Iron

$$\begin{aligned} a &= 0.286 \text{ nm}, n = 2 \\ \rho &= \frac{2 \times 55.85}{(2.86 \times 10^{-8})^3 \times 6.023 \times 10^{23}} \\ \rho &= 7.92 \text{ g.cm}^{-3} \end{aligned}$$

The real density of iron is 7.87 g.cm^{-3} so this is a good estimate.

2.3 Polymorphism

Materials that can exist in more than one crystal form (can have lattices made up of different unit cells) are called polymorphic. For example, Iron at room temperature has a BCC structure but at 912°C it has an FCC structure.

- 3 Phase diagrams and Alloying**
- 4 Strengthening mechanisms**
- 5 Engineering ceramics and glasses**
- 6 Polymers**
- 7 Failure of materials**
- 8 Corrosion of metals**
- 9 Engineering composites**