Signals and Systems

Lab1: Introduction to Matlab in Signals and Systems

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Outline

- Course Introduction
- Signals and Systems
- 3 Assignments

Course Introduction

Assignments of computer exercises in parallel with traditional written problems can help to develop a stronger intuition and a deeper understanding of linear systems and signals.

 Reference: Computer Explorations in SIGNALS AND SYSTEMS USING MATLAB

 Tool: MATLAB
 (Download inside the campus: https://pan.zju.edu.cn/share/eacc667811fae1e16f122ed724)

Outline

- Course Introduction
- Signals and Systems
 - Basic MATLAB Functions for Representing Signals
 - Discrete-Time Sinusoidal Signals
 - Properties of Discrete-Time Systems
 - Implementing a First-Order Difference Equation
 - Continuous-Time Complex Exponential Signals
- Assignments

Basic MATLAB Functions for Representing Signals

How to represent, manipulate, and analyze basic signals and systems in MATLAB.

- Signals will be represented by a row or column vector.
- All vectors represented in MATLAB are indexed starting with 1, i.e., y(1) is the first element of the vector y.
- For example, to represent the discrete-time signal

$$x[n] = \begin{cases} 2n, -3 \le n \le 3, \\ 0, \text{ otherwise} \end{cases}$$

$$\gg$$
 n = [-3 : 3];

$$\gg x = 2 * n;$$

To plot this signal: stem(n,x)

Basic MATLAB Functions for Representing Signals

 Examine the signal over a wider range of indices: extend both n and x.

$$\gg n = [-5:5];$$

 $\gg x = [0\ 0\ x\ 0\ 0];$

• Greatly extend the range of the signal: use the function **zeros**.

$$\gg n = [-100 : 100];$$

 $\gg x = [zeros(1,95) x zeros(1,95)];$

Basic MATLAB Functions for Representing Signals

- Define $x_1[n]$ to be the discrete-time unit impulse function and $x_2[n]$ to be a time-advanced version of $x_1[n]$, i.e., $x_1[n] = \delta[n]$ and $x_2[n] = \delta[n+2]$. $\gg nx1 = [0:10]$; $\gg x1 = [1 \ zeros(1,10)]$; $\gg nx2 = [-5:5]$; $\gg x2 = [zeros(1,3) \ 1 \ zeros(1,7)]$;
- Without the index vectors, and simply typed stem(x1) and stem(x2), you would make plots of the signals $\delta[n-1]$ and $\delta[n-4]$ and not of the desired signals.

Representing a continuous-time signal by discrete-time samples

- Two simple methods are to use the colon operator with the optional step argument. Exp: create a vector that covered the interval $-5 \le t \le 5$ in steps of 0.1 seconds t=[-5:0.1:5]; t=linspace(-5,5,l01).
- Sinusoids and complex exponentials are important signals for the study of linear systems. MATLAB provides several functions that are useful for defining such signals, like sin, cos, exp.
 - $\gg \operatorname{plot}(t, \sin(t))$
- In general, use stem to plot short discrete-time sequences, and plot for sampled approximations of continuous-time signals or for very long discrete-time signals where the number of stems grows unwieldy.

To represent the discrete-time signal $x[n] = e^{j(\pi/8)n}$ for $0 \le n \le 32$

- $\gg n = [0:32];$ $\gg x = exp(j*(pi/8)*n);$
- To plot complex signals, you must plot their real and imaginary parts, or magnitude and angle, separately. The MATLAB functions real, imag, abs, and angle compute these functions of a complex vector on an term-by-term basis.
- **angle**: phase of the complex numbers in radians.
- Add (+), subtract (-), multiply (.*), divide (./), scale (2*) and exponentiate (.^)signals.

- For multiplying, dividing and exponentiating on a term-by-term basis: .*
- Matrix multiplication operator: *
- Similar: ./ and .^ when operating on vectors term-by-term, / and ^ are matrix operators.

Commands to label plots appropriately, and print them out

- title
- xlabel, ylabel
- print

Ability to write M-files.

Two types of M-files: functions and command scripts. A
command script is a text file of MATLAB commands whose
filename ends in .m in the current working directory or
elsewhere on your MATLABPATH.

```
• %prob1.m
  n = [0:16];
  xl = cos (pi*n/4);
  y1 = mean(x1);
  stem(n,xl)
  title('x1 = cos(pi*n/4)')
  xlabel('n (samples)')
  ylabel('x1[n]')
```

An M-file implementing a function is a text file with a title ending in .m whose first word is function.

- The rest of the first line of the file specifies the names of the input and output arguments of the function.
- function [y,z] = foo(x)%[y,z] = foo(x) accepts a numerical argument x and returns two %arguments y and z, where y is 2*x and z is (5/9)*(x-32)y = 2*x; z = (5/9)*(x-32);

Discrete-Time Sinusoidal Signals

- Discrete-time complex exponentials play an important role in the analysis of discrete-time signals and systems. A discrete-time complex exponential has the form α^n , where α is a complex scalar.
- The discrete-time sine and cosine signals can be built from complex exponential signals by setting $\alpha = e^{\pm i\omega}$.

$$\begin{split} \cos(\omega n) &= \frac{1}{2} \left(e^{i\omega n} + e^{-i\omega n} \right) \\ \sin(\omega n) &= \frac{1}{2i} \left(e^{i\omega n} - e^{-i\omega n} \right) \end{split}$$

Basic Problems

Problem 1

Consider the signal

$$x_k[n] = \sin(\omega_k n) \,,$$

where $\omega_k = 2\pi k/5$. For $x_k[n]$ given by k = 1, 2, 4, and 6, use stem to plot each signal on the interval $0 \le n \le 9$. All of the signals should be plotted with separate axes in the same figure using subplot. How many unique signals have you plotted? If two signals are identical, explain how different values of ω_k can yield the same signal.

Problem 2

Now consider the following three signals

$$\begin{split} x_1[n] &= \cos\left(\frac{2\pi n}{N}\right) + 2\cos\left(\frac{3\pi n}{N}\right)\,,\\ x_2[n] &= 2\cos\left(\frac{2n}{N}\right) + \cos\left(\frac{3n}{N}\right)\,,\\ x_3[n] &= \cos\left(\frac{2\pi n}{N}\right) + 3\sin\left(\frac{5\pi n}{2N}\right)\,. \end{split}$$

Assume N=6 for each signal. Determine whether or not each signal is periodic. If a signal is periodic, plot the signal for two periods, starting at n=0. If the signal is not periodic, plot the signal for $0 \le n \le 4N$ and explain why it is not periodic. Remember to use stem and to appropriately label your axes.

Intermediate Problems

Problem 3

Plot each of the following signals on the interval $0 \le n \le 31$:

$$egin{aligned} x_1[n] &= \sin\left(rac{\pi n}{4}
ight)\,\cos\left(rac{\pi n}{4}
ight)\;, \ x_2[n] &= \cos^2\left(rac{\pi n}{4}
ight)\;, \ x_3[n] &= \sin\left(rac{\pi n}{4}
ight)\,\cos\left(rac{\pi n}{8}
ight)\;. \end{aligned}$$

What is the fundamental period of each signal? For each of these three signals, how could you have determined the fundamental period without relying upon MATLAB?

Problem 4

Consider the signals you plotted in Problem 2 and 3. Is the addition of two periodic signals necessarily periodic? Is the multiplication of two periodic signals necessarily periodic? Clearly explain your answers.

Properties of Discrete-Time Systems

Linearity, time invariance, stability, causality, and invertibility

Problem 5

Basic Problems

For these problems, you are told which property a given system does not satisfy, and the input sequence or sequences that demonstrate clearly how the system violates the property. For each system, define MATLAB vectors representing the input(s) and output(s). Then, make plots of these signals, and construct a well reasoned argument explaining how these figures demonstrate that the system fails to satisfy the property in question.

- (a). The system $y[n] = \sin((\pi/2)x[n])$ is not linear. Use the signals $x_1[n] = \delta[n]$ and $x_2[n] = 2\delta[n]$ to demonstrate how the system violates linearity.
- (b). The system y[n]=x[n]+x[n+1] is not causal. Use the signal x[n]=u[n] to demonstrate this. Define the MATLAB vectors ${\bf x}$ and ${\bf y}$ to represent the input on the interval $-5 \le n \le 9$, and the output on the interval $-6 \le n \le 9$, respectively.

Implementing a First-Order Difference Equation

$$y[n] = ay[n-1] + x[n], (1.6)$$

Problem 6

(a). Write a function y=diffeqn(a,x,yn1) which computes the output y[n] of the causal system determined by Eq. (1.6). The input vector x contains x[n] for $0 \le n \le N-1$ and yn1 supplies the value of y[-1]. The output vector y contains y[n] for $0 \le n \le N-1$. The first line of your M-file should read

function y = diffeqn(a,x,yn1)

Hint: Note that y[-1] is necessary for computing y[0], which is the first step of the autoregression. Use a for loop in your M-file to compute y[n] for successively larger values of n, starting with n = 0.

(b). Assume that a=1, y[-1]=0, and that we are only interested in the output over the interval $0 \le n \le 30$. Use your function to compute the response due to $x_1[n] = \delta[n]$ and $x_2[n] = u[n]$, the unit impulse and unit step, respectively. Plot each response using stem.

Continuous-Time Complex Exponential Signals

Problem 7

Consider the continuous-time sinusoid

$$x(t) = \sin(2\pi t/T).$$

A symbolic expression can be created to represent x(t) within MATLAB by executing

```
>> x = sym('sin(2*pi*t/T)');
```

The variables of x are the single character strings 't' and 'T'. The function explot can be used to plot a symbolic expression which has only one variable, so you must set the fundamental period of x(t) to a particular value. If you desire T=5, you can use subs as follows

```
>> x5 = subs(x,5,'T');
```

Thus x5 is a symbolic expression for $\sin(2\pi t/5)$. Create the symbolic expression for x5 and use explot to plot two periods of $\sin(2\pi t/5)$, beginning at t=0. If done correctly, your plot should be as shown in Figure 1.2.

Continuous-Time Complex Exponential Signals

Problem 8

In the following problems you will write M-files for extracting the real and imaginary components, or the magnitude and phase, of a symbolic expression for a complex signal.

(d). Store in x a symbolic expression for the signal

$$x(t) = e^{i2\pi t/16} + e^{i2\pi t/8}.$$

Remember to use 'i' rather than 'j' within symbolic expressions to represent $\sqrt{-1}$. The function explot cannot be used directly for plotting x(t), since x(t) is a complex signal. Instead, the real and imaginary components must be extracted and then plotted separately.

(e). Write a function xr=sreal(x) which returns a symbolic expression xr representing the real part of x(t). If your function is working properly, ezplot(xr) will plot the real component of x(t). Similarly, write a function xi=simag(x) which returns a symbolic expression xi representing the imaginary component of x(t). The first line of the M-file sreal.m should be

function
$$xr = sreal(x)$$

You can then use compose('real(x)',x) to create a symbolic expression for the real component of x(t). Use explot and the functions you created to plot the real and imaginary components of x(t) on the interval $0 \le t \le 32$. Use a separate plot for each component. What is the fundamental period of x(t)?

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Assignments

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You should hand in the Matlab code (.m files), graphics, audio files and a brief description of your reasoning as well as comments if any. Please make sure that your Matlab code can be run on Matlab R2007b or higher version. You should pack all of your files into a .rar or .zip file, titled as xxxxxxx(your student ID) xxxx(your name) Lab pre, and then upload to blackboard before 11:59pm of the due day.