

Week 4 Answers

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Version 1

The Number of States

Logic Steps I processed:

1. Look at function `comb(i)`. It is called recursively.
2. To get to index i (let's say $i=3$), the code had to make decisions for $i=0$, $i=1$, and $i=2$ first.
3. For each previous item, there were exactly 2 choices: $x[k] = 0$ or $x[k] = 1$.
4. Therefore, the number of unique ways to reach level i is $2 * 2 * 2 * \dots$ (i times).

Answer: 2^i

Different in Values?

Answer: Yes

Reason:

- The function `comb(i)` relies on a hidden global list x .
- Scenario A: You reach item i having picked nothing earlier. The bag is empty. The function calculates a valid profit.
- Scenario B: You reach item i having picked everything earlier. The bag is full. The function returns -1 (Overweight).
- Even though the input i is the same, the Global State (x) is different, so the result changes.

Using Memoization can speed up this?

Answer: No. Memoization requires that a function, given specific inputs, always returns the same output.

Version 3

Question 5

Answer: Yes

The brute-force algorithm repeatedly generates the same state.

Question 6

Answer: Yes

Reason:

- The function $\text{maxVal}(i, C)$ depends only on the arguments i and C .
- There is no global list x acting as a "hidden memory."
- The question "What is the max profit starting from Item 5 with 10kg space?" has only one mathematical answer. It does not matter how one arrived at Item 5; it only matters that one is there.
- Because the answer is consistent, we can write it in the memo table.