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Divine & Conquer

Problem A

- $O(x)$, where x is exponential number
- $O(\log(x))$

Problem B

- Splitting the data exactly in the middle keeps the work quick, giving you the best speed of $O(n \log n)$ because the process only repeats $O(\log n)$ times. If you only split off one item at a time, the process takes too long ($O(n)$ repeats), making the overall speed much slower.
- No, it isn't sufficient enough to assume that the answer for the sequence is $\max(ma, mb)$.
- Yes, maxSum of crossing subsequence may give the larger sum than the one in step 3.
- The crossing subsequence must:
 - Start somewhere in the left half (index between i and mid)
 - End somewhere in the right half (index between $mid+1$ and k)
 - Must include both numbers[mid] and numbers[$mid+1$] (the elements immediately adjacent to the split point)
- In other words, it crosses the midpoint. The beginning index $\leq mid$ and the ending index $\geq mid+1$.
- The sum of the maximum subsequence of the original subsequence (a_i, \dots, a_k) would be the maximum of three values:
 - The maximum sum found entirely in the left half (m_L).
 - The maximum sum found entirely in the right half (m_R).
 - The maximum crossing sum (m_c).
- $O(n)$
- $T(n) = O(n \log n)$
- The divide-and-conquer algorithm is slower than Kadane's algorithm for solving the maximum subarray sum problem.
 - The **Divide-and-Conquer** approach has a time complexity of $O(n \log n)$ because it recursively splits the array and performs $O(n)$ work at each of the $\log n$ levels to find crossing sums.
 - The **Kadane's Algorithm** is faster, with a time complexity of $O(n)$ (linear time), as it only requires a single pass over the array, tracking the current and absolute maximum sums without recursion or re-visiting elements.