

Quiz 4

$$\begin{matrix} \downarrow \\ 3e^{2x} + 1 \\ 6e^{2x} \end{matrix}$$

① $f(x) = \frac{4\sqrt{x}}{3e^{2x} + 1} = \frac{4x^{1/2} \rightarrow \text{Hi}}{3e^{2x} + 1}$

$$g(x) = \frac{(3e^{2x} + 1)(4x^{1/2})' - (4x^{1/2})(3e^{2x})'}{(3e^{2x} + 1)^2}$$

$$g(x) = \frac{(6e^x)(4x^{1/2})' - (4x^{1/2})(6e^x)}{(6e^x)^2}$$

② $h(x) = 2x^7 f(x)$

$$\downarrow \frac{d}{dx} [2fx^7] \rightarrow 2f \cdot \frac{d}{dx} [x^7] \rightarrow 2f \cdot 8x^6$$

$$\rightarrow \boxed{16fx^6}$$

③ $g(x) = 2(4x^2 - 5x)^3$

$$\downarrow = 2 \cdot \frac{d}{dx} [(4x^2 - 5x)^3]$$

Youtube: $= 2 \cdot 3(4x^2 - 5x)^2 \cdot \frac{d}{dx} [4x^2 - 5x]$

$$6(4x^2 - 5x)^2 (4 \cdot \frac{d}{dx} [x^2] - 5 \cdot \frac{d}{dx} [x])$$

$$= 6(4x^2 - 5x)^2 (4 \cdot 2x - 5 \cdot 1)$$

$$\boxed{= 6x^2 (4x - 5)^2 (8x - 5)}$$

(2)

a) $\frac{d}{dx} [f(x)g(x)]$ at $x=3 \rightarrow (3) : f'(x)g(x) + f(x)g'(x)$

$$f'(3)g(3) + f(3)g'(3) \\ = (10)(4) + (2)(7)$$

b) $\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right]$ at $x=2$

(2) : $\frac{g(x)f'(x) - f(x)g'(x)}{g(x)^2}$

$$= \frac{(4)(-1) - (1)(5)}{(4)^2}$$

(3) $2(4x^2 + 5x)^2 (4x^2 - 5x)^1$
 $6x^2(4x - 5)^2 (8x - 5)$
Inside Inside

Proper way: