## Zero-Dimensional Nanostructures: Nanoparticles

Principles of homogeneous nucleation

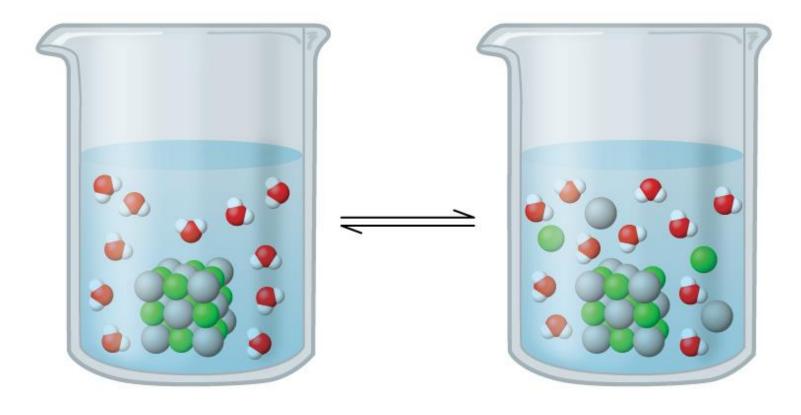
#### Video

Reaction between AgNO3 and NaCl (Silver nitrate + Sodium Chloride)

https://www.youtube.com/watch?v=0AyLFP26r4o

#### Reflection:

- 1) How much Cl<sup>-</sup> is needed to precipitate the Ag+?
- 2) Assume that you take away all the Na+ and the NO<sub>3</sub> ions, and you are just left with the AgCl. What happens afterward?



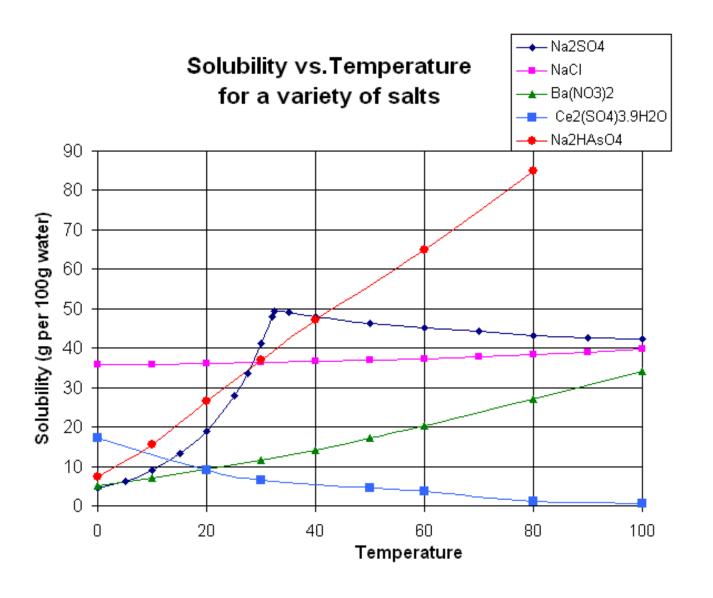
AgCl(s). 
$$\rightleftharpoons$$
. Ag+(aq). +. Cl-(aq)

$$Ksp = [Ag+(aq)][Cl-(aq)]$$

#### **Constantes del Producto** de Solubilidad Apéndice C

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Compuesto	Nombre	Kps	
AgBr	Bromuro de plata	5 × 10 <sup>-13</sup>	
AgCl	cloruro de plata	$1.8 \times 10^{-10}$	
AgI	yoduro de plata	8,3 × 10 <sup>-17</sup>	
AgBrO <sub>3</sub>	bromato de plata	$4 \times 10^{-5}$	
AgIO <sub>3</sub>	yodato de plata	$3.0 \times 10^{-8}$	
Ag <sub>2</sub> S	sulfuro de plata	$2,1 \times 10^{-49}$	
Ag <sub>3</sub> PO <sub>4</sub>	fosfato de plata	$1,3 \times 10^{-20}$	
Ag <sub>2</sub> CO <sub>3</sub>	carbonato de plata	$6.2 \times 10^{-12}$	
Ag <sub>2</sub> Cr <sub>2</sub> O <sub>7</sub>	dicromato de plata	$2,7 \times 10^{-11}$	
Ag <sub>2</sub> SO <sub>4</sub>	sulfato de plata	$1.6 \times 10^{-5}$	
Ag <sub>3</sub> AsO <sub>4</sub>	arseniato de plata	$1.0 \times 10^{-22}$	
AgCN	cianuro de plata	$1,2 \times 10^{-16}$	
Ag <sub>2</sub> CrO <sub>4</sub>	cromato de plata	$1.9 \times 10^{-12}$	
Al(OH) <sub>3</sub>	hidróxido de aluminio	$5 \times 10^{-33}$	
AuC1	cloruro de oro(I)	$2,0 \times 10^{-13}$	
AuCl <sub>3</sub>	cloruro de oro(III)	$3,2 \times 10^{-25}$	
BaCO <sub>3</sub>	carbonato de bario	8,1 × 10 <sup>-9</sup>	
BaC <sub>2</sub> O <sub>4</sub>	oxalato de bario	$1.7 \times 10^{-7}$	
BaCrO <sub>4</sub>	cromato de bario	$1,2 \times 10^{-10}$	
BaF <sub>2</sub>	fluoruro de bario	$2,4 \times 10^{-5}$	
Ba(IO <sub>3</sub> ) <sub>2</sub>	yodato de bario	$6.0 \times 10^{-10}$	
Ba(OH) <sub>2</sub>	hidróxido de bario	$5 \times 10^{-3}$	
BaSO <sub>4</sub>	sulfato de bario	$1.1 \times 10^{-10}$	
Be(OH) <sub>2</sub>	hidróxido de berilio	$2,0 \times 10^{-18}$	
Bi <sub>2</sub> S <sub>3</sub>	sulfuro de bismuto(III)	$3.0 \times 10^{-96}$	
CaCO <sub>3</sub>	carbonato de calcio	4,8 × 10 <sup>-9</sup>	
CaC <sub>2</sub> O <sub>4</sub>	oxalato de calcio	$2,6 \times 10^{-9}$	
CaCrO <sub>4</sub>	cromato de calcio	$7.1 \times 10^{-4}$	

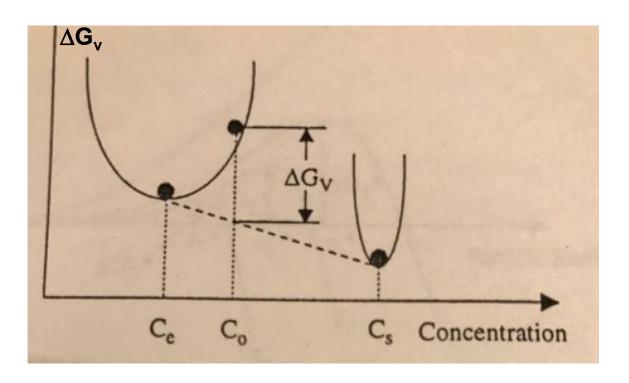


## Thermodynamic Approach

$$DG_V = -\frac{kT}{W}\ln(\frac{C}{Co}) = -\frac{kT}{W}\ln(1+S)$$

Atomic volume

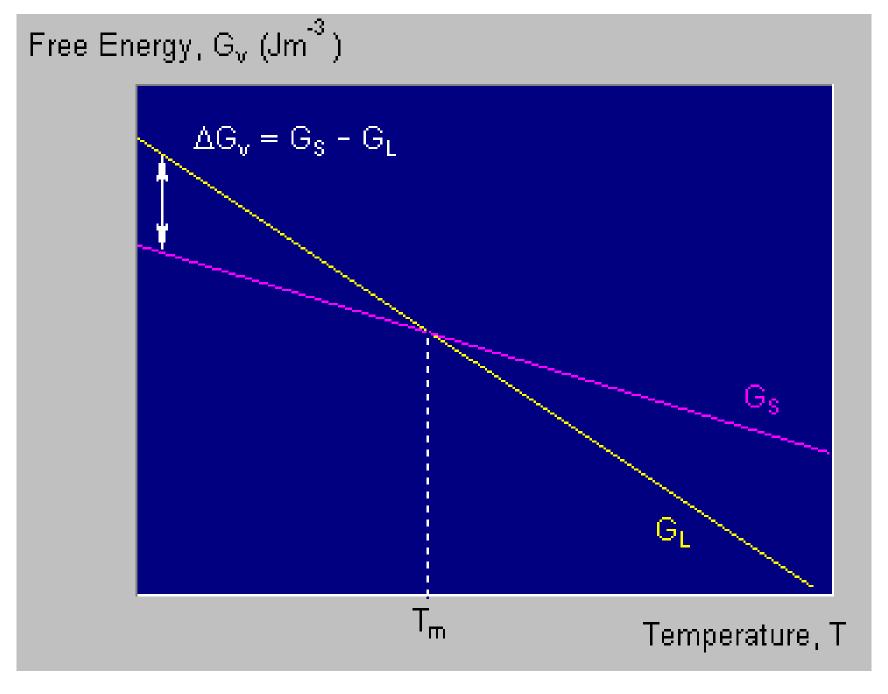
$$S = (C-Co)/Co$$



#### Solidification

 Solidification of metals and alloys usually represents a transformation from a non-crystalline liquid to a crystalline solid.

 If a liquid metal is cooled below its equilibrium melting point, T<sub>m</sub>, the system can lower its free energy (G = H-TS) by forming a solid phase.



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The change in free energy for solidification,  $\Delta G_v = G_S - G_L$ , or

$$\Delta G_{v} = \Delta H_{v} - T \Delta S_{v} \tag{1}$$

where  $\Delta H_v$  and  $\Delta S_v$  are the changes in enthalpy and entropy.

At the equilibrium melting temperature,  $T_m$ , the driving force for transformation,  $\Delta G_v = ?$ 

$$\Delta H_v - T_m \Delta S_v = 0$$
  
 $\Delta S_v = \Delta H_v / T_m$ 

Substituting this expression for  $\Delta S_v$  into Equation (1):

$$\Delta G_{v} = \Delta H_{v} - (T \Delta H_{v} / T_{m})$$

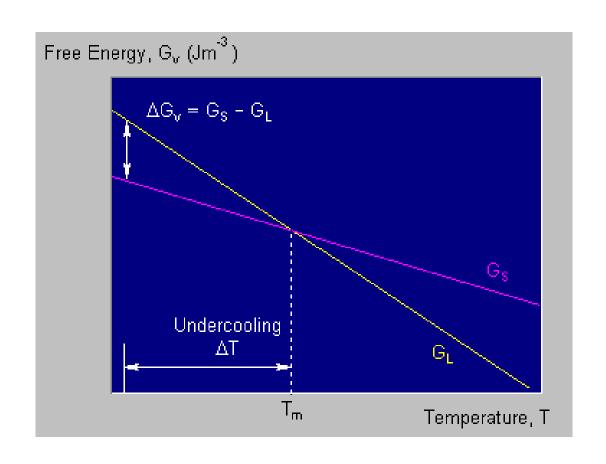
$$= \Delta H_{v} (1 - T / T_{m})$$

$$= \Delta H_{v} (T_{m} - T) / T_{m}$$

But  $T_m - T = \Delta T$ , the undercooling, and so we have:

$$\Delta G_v = \Delta H_v \Delta T / T_m$$

$$\Delta G_{V} = \frac{\Delta H_{V} \Delta T}{T_{m}}$$



This energy change is the **driving force** for solidification.

Although solidification cannot occur without a **thermodynamic** driving force, the rate (**kinetics**) cannot be predicted from this alone.

Yes, this is the thermodynamic explanation, but...

How is the phenomenon at the molecular/atomic level?

#### Principles of phase transformation

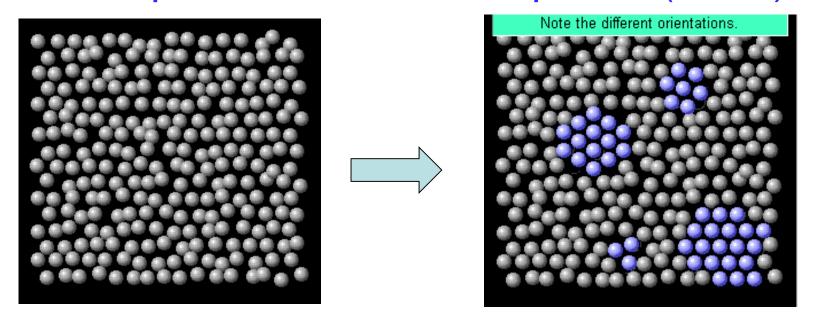
#### Nucleation:

- The physical process by which a new phase is produced in a material. In the case of solidification, this refers to the formation of a tiny, stable solid particles in the liquid.

#### Growth:

 The pysical process by which a new phase increases in size. In the case of solidification, this refers to the formation of a stable solid as the liquid freezes.

# Nucleation is the **initial stage** of formation of one phase from another phase (L o S)

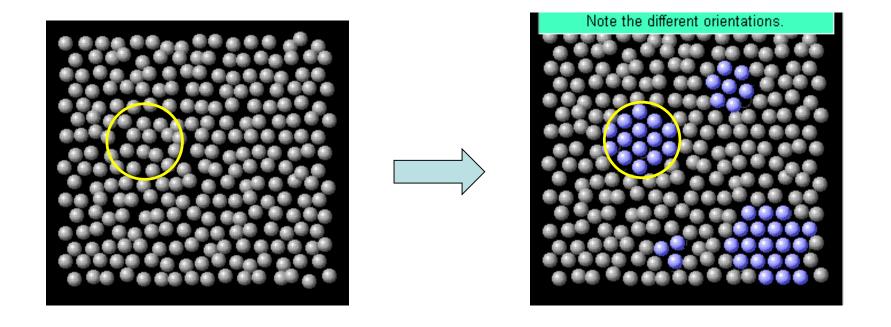


When a liquid metal is cooled towards the melting temperature, some atoms are already beginning to **randomly arrange** themselves into small **crystal**-like clusters.

The formation of such clusters arises from the **random motion** of the atoms within the liquid.

The average cluster **size increases** as the temperature falls **below T<sub>m</sub>**.

#### When the cluster form we have:



Total Free Energy Change



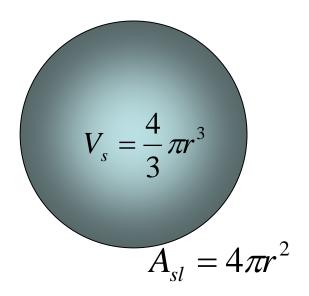
Volume Free Energy Change

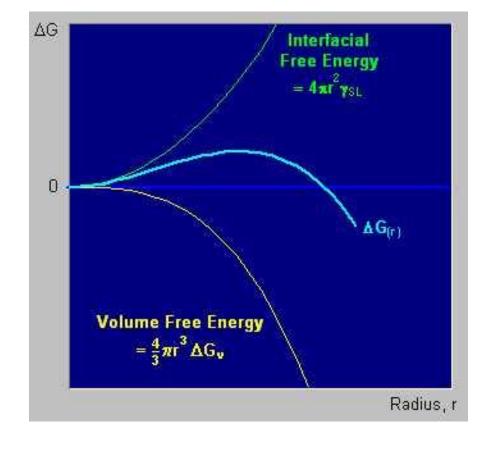
Surface FreeEnergy Change

$$\Delta G = V_s \Delta G_V + A_{sl} \sigma_{sl}$$

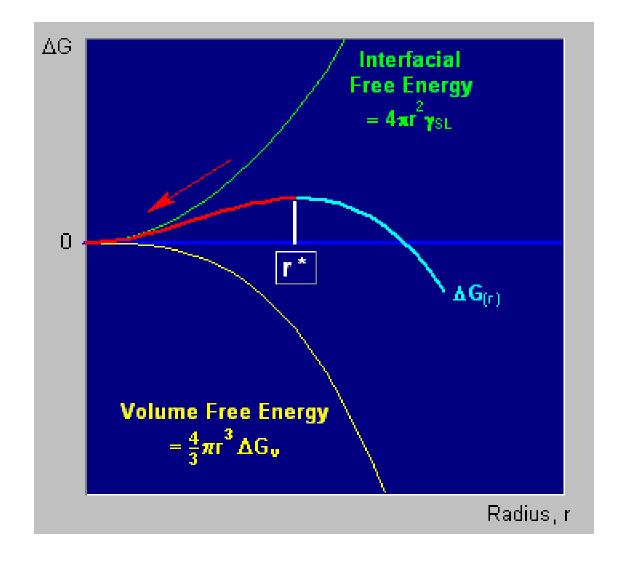
# Assuming the interfacial free energy is isotropic, the cluster will grow spherically.

$$\Delta G = V_s \Delta G_V + A_{sl} \sigma_{sl}$$





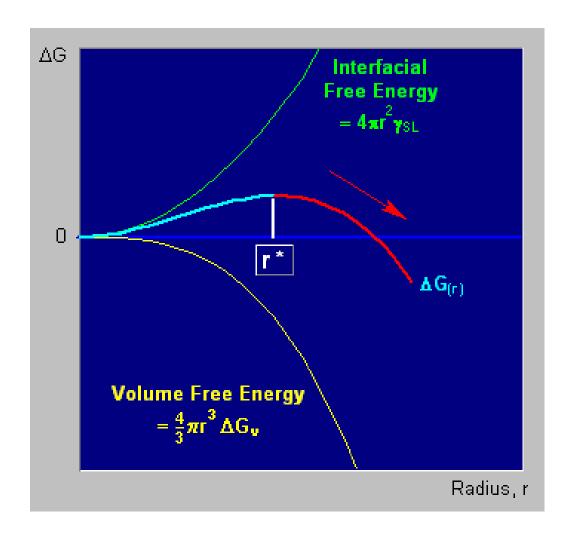
## $R_{embryo} < r^*$



Free energy increase.

The solid remelts,

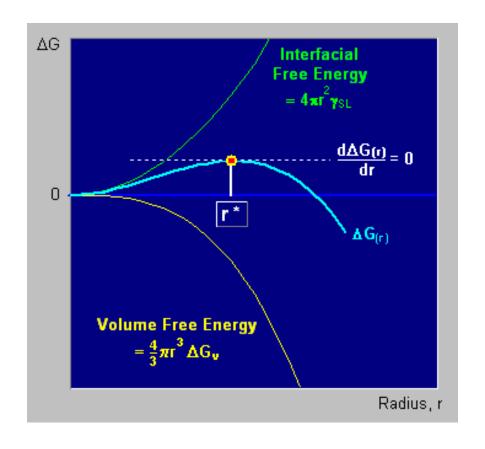
## $R_{embryo} > r^*$



The solid will grow,

free energy decrease.

#### r\* to Homogeneous Nucleation



$$\Delta G_V = \frac{\Delta H_V \Delta T}{T_m}$$

$$\Delta G = V_s \Delta G_V + A_{sl} \sigma_{sl}$$

$$\Delta G = \frac{4}{3} \pi r^3 \Delta G_V + 4 \pi r^2 \sigma_{sl}$$

$$4 \pi r^{*2} \Delta G_V + 8 \pi r^* \sigma_{sl} = 0$$

$$r^* = \frac{-2\sigma_{sl}}{\Delta G_V}$$

$$r^* = \frac{2\sigma_{sl}T_m}{\Delta H_V \Delta T}$$

TABLE 8-1 ■ Values for freezing temperature, latent heat of fusion, surface energy, and maximum undercooling for selected materials

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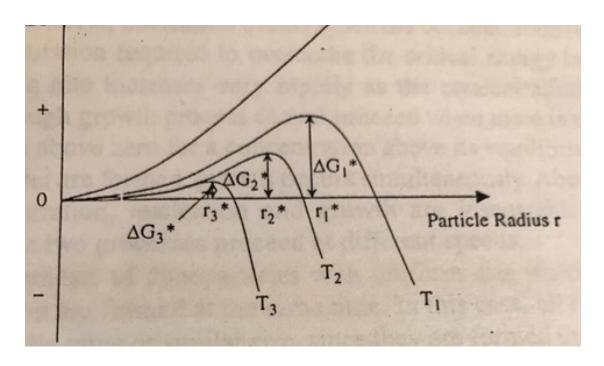
	Freezing Temperature $(T_m)$	Heat of Fusion $(\Delta H_f)$	Solid-Liquid Interfacial Energy $(\sigma_{sl})$	Typical Undercooling for Homogeneous Nucleation $(\Delta T)$
Metal	(°C)	(J/cm³)	(J/cm²)	(°C)
Ga	30	488	$56 \times 10^{-7}$	76
Bi	271	543	$54 \times 10^{-7}$	90
Pb	327	237	$33 \times 10^{-7}$	80
Ag	962	965	$126 \times 10^{-7}$	250
Cu	1085	1628	$177 \times 10^{-7}$	236
Ni	1453	2756	$255 \times 10^{-7}$	480
Fe	1538	1737	$204 \times 10^{-7}$	420
NaCl	801			169
CsCl	645			152
H <sub>2</sub> O	0			40

## Is it possible to reduce the r\*

$$r^* = -2\frac{\gamma}{\Delta G_{\nu}}$$

The free energy is a function of T and supersaturation (C-Co)/Co However...

the supersaturation decreases as T increases the surface tension \_\_\_\_\_ as T increases



## Important considerations

- Identical size
- Identical shape or morphology
- Identical chemical composition and crystal structure
- Individually disperse or monodispersed

### **Debate**

#### Debate...

Based on the information provided so far...

Depict a process to get small particles with the narrowest size distribution possible

## Synthesis Methods

- Thermodynamic approach
  - i. supersaturation
  - ii. nucleation
  - iii.growth

Kinetic approach

#### Desirable features

Uniform size distribution

- Identical shape or morphology
- Identical chemical composition and crystal structure

Individually dispersed

### Critical size (r\*)

How to reduce the value of r\*?

$$r^* = -2\frac{\gamma}{\Delta G_V}$$

$$\Delta G^* = \frac{16\pi\gamma}{\left(3\Delta G_V\right)^2}$$

Energy barrier to overcome, so nulceation can start

SO

$$\Delta G_{V}$$
  $\uparrow$ 

$$\Delta G_V = \frac{kT}{\Omega} \ln \left( \frac{C}{C_0} \right) = \frac{kT}{\Omega} \ln \left( 1 + \sigma \right)$$

$$C \uparrow$$

$$T \uparrow \longrightarrow$$

It affects
surface energy
(specially near
roughening
temperature)

## Other variables affecting r\*

Besides of C and T:

Solvent type (polarity)

Additives (i.e.: viscosity)

Impurities

## Rate of nucleation (R<sub>N</sub>)

$$R_N = f(n, P, \Gamma)$$

n is the number of growth species/volume

P is the probability of fluctuations of the critical free energy  $\Delta G^*$ 

 $\Gamma$  is the frecuency of species jumping from one growing site to another one

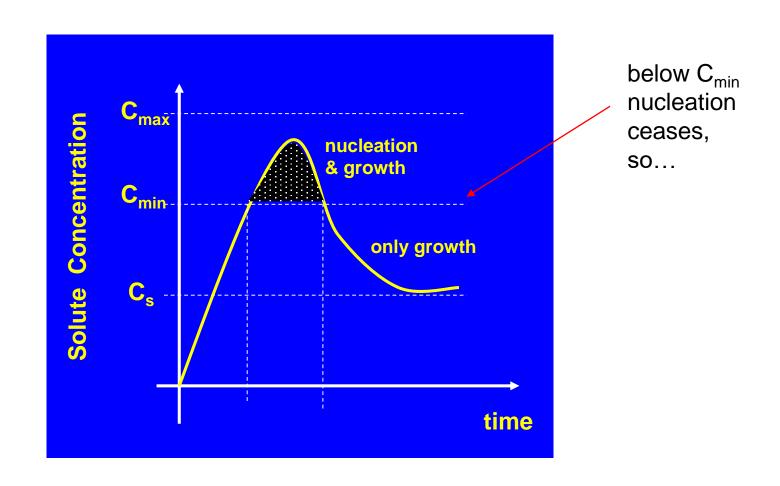
$$P = \exp\left(\frac{-AG^*}{kT}\right)$$

$$\Gamma = \frac{kT}{3\pi\lambda^3\eta}$$

$$\Delta G^* = \frac{16\pi\gamma}{(3\Delta G_V)^2}$$

$$R_N = nP\Gamma = \left[\frac{C_0 kT}{3\pi\lambda^3\eta}\right] \exp\left[\frac{-\Delta G^*}{kT}\right]$$

$$\Delta G_V = \frac{kT}{\Omega} \ln\left(\frac{C}{C_0}\right) = \frac{kT}{\Omega} \ln(1+\sigma)$$



#### Growth of the nulcei

#### Steps:

- generation of the species
- · diffusion from the bulk to the surface

- · adsorption onto the growth surface
- surface growth onto the solid surface

diffusion limited

growth limited

### Diffusion controlled growth

Promotes the formation of uniformly sized particles

$$\frac{dr}{dt} = D(C - Cs) \frac{V_m}{r}$$

D is the diffusion coefficient

$$rdr = D(C - Cs)V_m dt$$

at time t=0,  $r=r_0$ 

$$r^2 = 2D(C - Cs)V_m t + r_o^2$$

$$r^2 = k_D t + r_o^2$$

where:  $k_D=2D(C-C_s)V_m$  is the diffusion constant

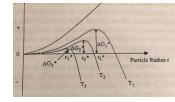
For this type of growth the radius difference among particles is given by:

$$\rightarrow$$
  $r \delta r = r_o \delta r_o$ 

$$\delta r = \frac{r_0 \delta r_0}{r}$$

Therefore such difference decreases with time as well as with higher values of  $r_o$  and higher  $k_D$ 

$$\delta r = \frac{r_0 \delta r_0}{\sqrt{k_D t + r_0^2}}$$



## Surface controlled growth

Does not promote the formation of uniformly sized particles

#### Monolayered

 $\frac{dr}{dt}\alpha$  surface area

$$\frac{dr}{dt} = k_m r^2$$

$$\frac{dr}{r^2} = k_m dt$$

$$\frac{1}{r} = \frac{1}{r_0} - k_m t$$

If the radius of the nulcei increases, then the radius difference among particles increases:

$$\rightarrow \delta r/r^2 = \delta r_o/r_o^2$$

$$\delta r = \frac{r^2 \delta r_0}{r_0^2}$$

substitution of r:

$$\delta r = \frac{\delta r_0}{\left(1 - k_m r_0 t\right)^2}$$

therefore:

as t increases...

## Surface controlled growth

Does not promote the formation of uniformly sized particles

#### Polinuclear growth

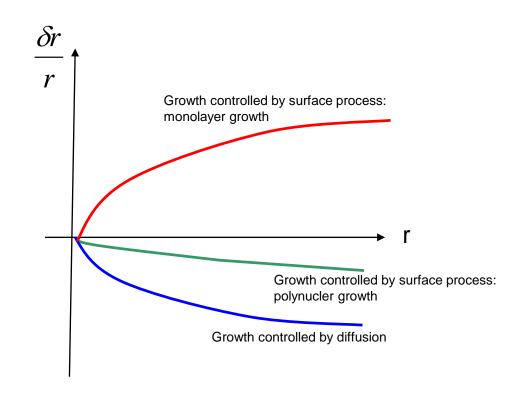
surface process is very fast, growth rate is constant

$$\frac{dr}{dt} = k_p$$

$$r = k_p t + r_0$$

Therofore, the radius difference remains constant:

$$\delta r = \delta r_0$$



#### Advantages of solution processes

#### It is easy to:

- prevent agglomeration
- extract
- do surface modifications and applications
- control the process
- have mass production