

# Previous Lecture

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Basic Concepts:  
Surface atom vs. bulk atom  
Surface energy  
Young-Laplace Equation

# Stability of Nanomaterials

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13<sup>TH</sup> SEPTEMBER 2017

KIRSI YLINIEMI



# In this lecture

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1. Ostwald Ripening

2. DLVO Theory

3. Examples of different sizes and geometries



# After This Lecture You Can

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Explain Electrical Double Layer

Predict the stability by  
DLVO theory or steric  
hinderance

Explain Ostwald  
ripening

Classify nanomaterials to  
0D-3D

# Nanomaterials Are Stable

§ Glazing of pottery for hundreds of years



*Metal salt (Ag, Au, etc.)*

*Vinegar, ocre, clay*

- *mix on the top of glazed pottery*
- *Heat up to 600°C*

Ø *Nanoparticles embedded in the glazing*

§ Michael Faraday's Au nanoparticles (1857)



<http://www.rigb.org/our-history/iconic-objects>

*Au salt + citric acid -> Au nanoparticles*  
*80-100°C for 30 min to 4 hours*

# Problems with Stability?

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§ Particle size(s)

Ø "Dissolution"

Ø Ostwald ripening

§ Forces

Ø "Precipitation"

Ø DLVO theory



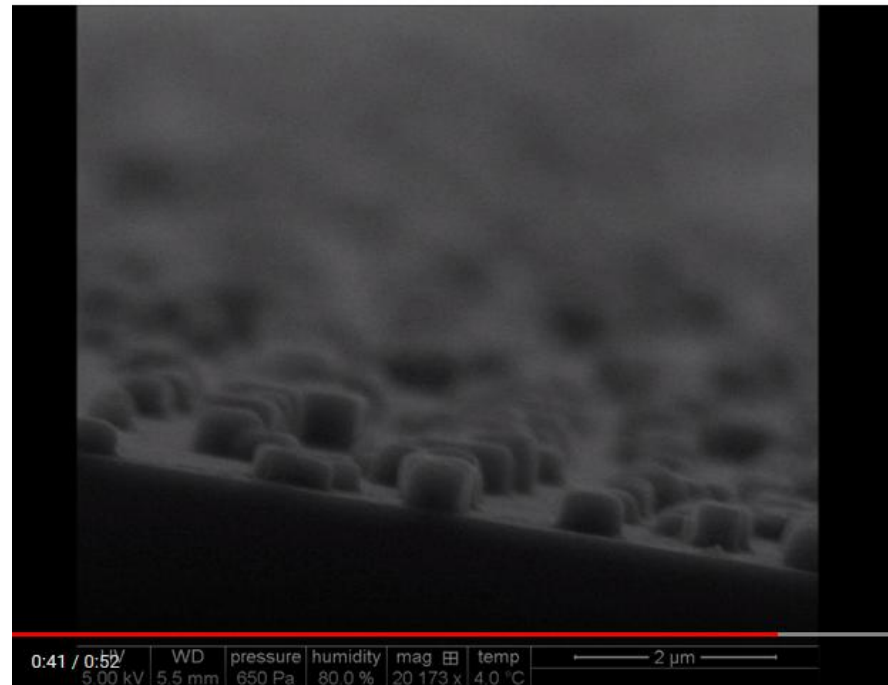
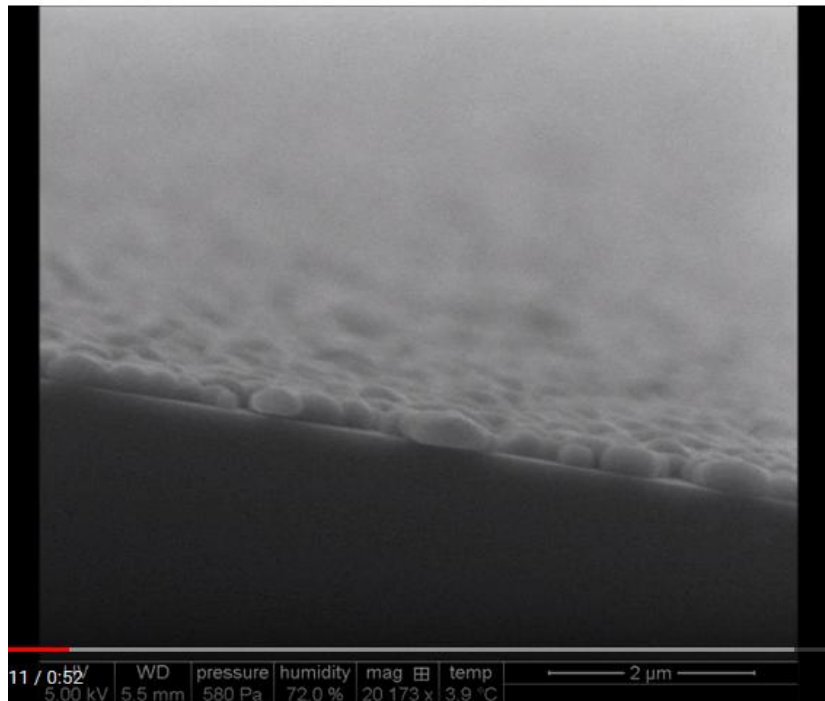


# Ostwald Ripening

PART 1

# Observation

<https://www.youtube.com/watch?v=hDWACXP833Y>

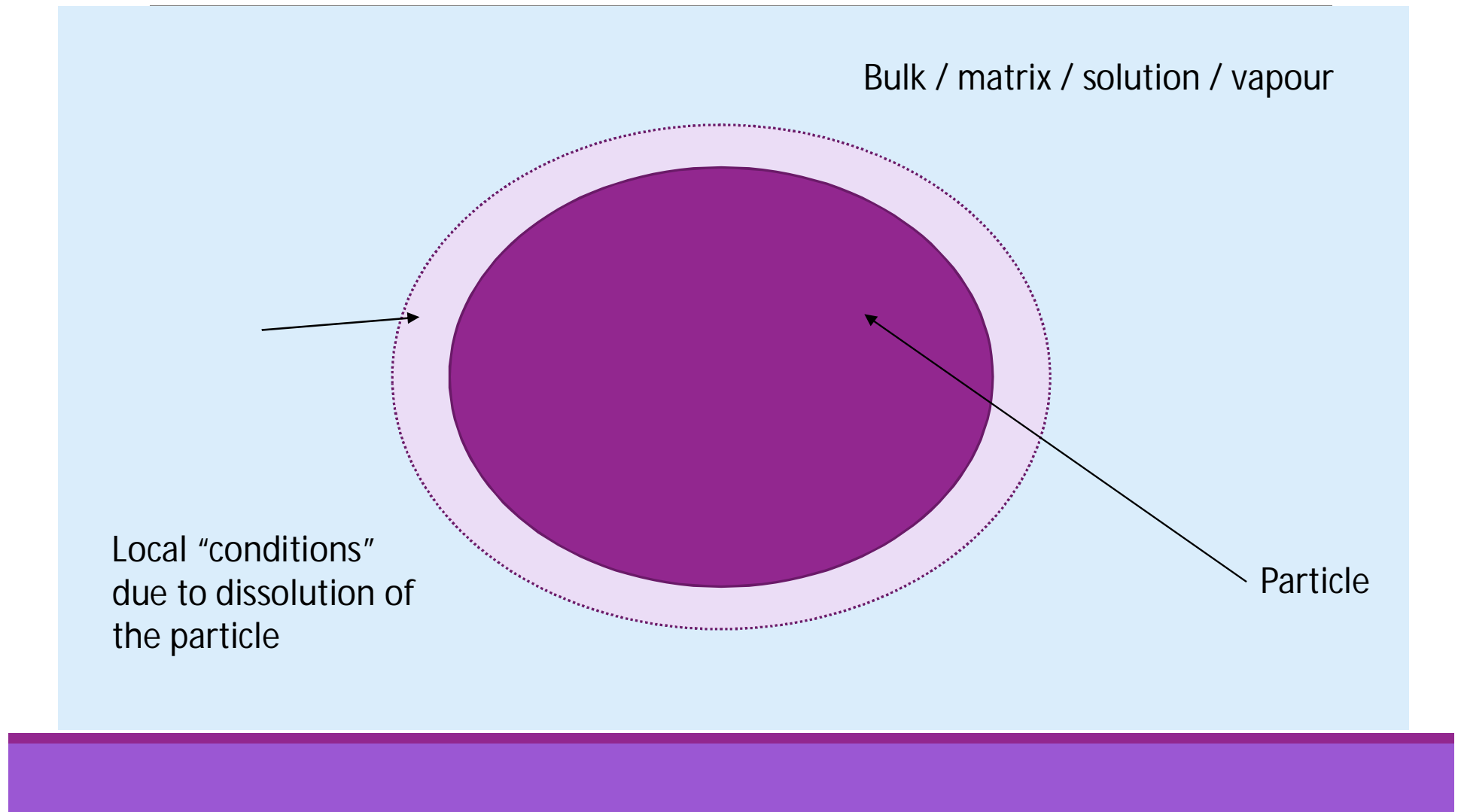






Let's first think only  
one particle

# Dissolving small particles...



# Dissolving small particles...

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Ideal gas law for solid surfaces

*Flat surface:*  $\mu_v - \mu_\infty = -kT \ln P_\infty$

*Curved surface:*  $\mu_v - \mu_c = -kT \ln P_c$

*v*  $\rightarrow$  vapour, *c*  $\rightarrow$  curved surface and  $\infty \rightarrow$  flat surface

*k* Boltzmann's constant

*T* temperature

*P* equilibrium vapour pressure

# Dissolving small particles...

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Ideal gas law for solid surfaces

*Flat surface:*  $\mu_v - \mu_\infty = -kT \ln P_\infty$

*Curved surface:*  $\mu_v - \mu_c = -kT \ln P_c$

Remember Young-Laplace from Lecture 1:  $\Delta\mu = \gamma\Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$

Combining these three equation

(flat – curved =  $\Delta\mu$ )

$$\mu_c - \mu_\infty = kT \ln \left( \frac{P_c}{P_\infty} \right) = \Delta\mu = \gamma\Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

# Dissolving small particles...

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$$\mu_c - \mu_\infty = \Delta\mu = kT \ln \left( \frac{P_c}{P_\infty} \right) = \gamma\Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\ln \left( \frac{P_c}{P_\infty} \right) = \frac{\gamma\Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)}{kT}$$

# Dissolving small particles...

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$$\ln \left( \frac{P_c}{P_\infty} \right) = \frac{\gamma \Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)}{kT}$$

Discuss: What does this equation mean?

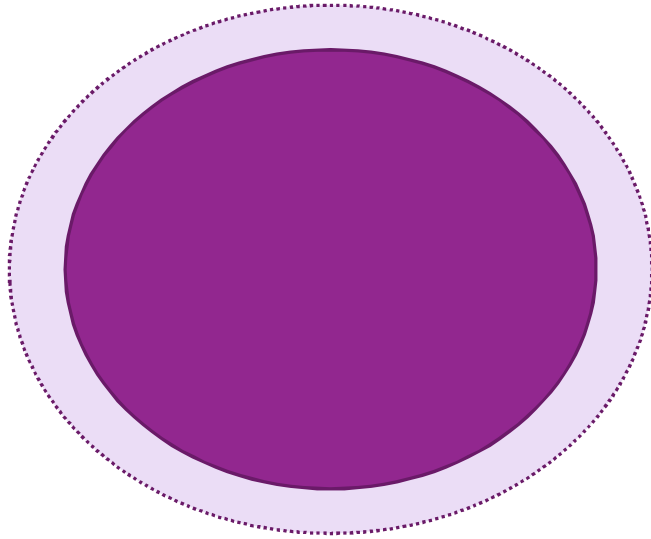
# Dissolving small curved particles...

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Kelvin equation

$$\ln \left( \frac{P_c}{P_\infty} \right) = \frac{\gamma \Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)}{kT}$$

Smaller the particle radius, larger the  $\ln$  term →  
Larger  $\ln$  term means larger  $P_c$ , i.e. higher pressure  
at vapour must be achieved before equilibrium is  
reached



Partial pressure

$$\ln \left( \frac{P_c}{P_\infty} \right) = \frac{\gamma \Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)}{kT}$$

Solubility

$$\ln \left( \frac{S_c}{S_\infty} \right) = \frac{\gamma \Omega \left( \frac{1}{R_1} + \frac{1}{R_2} \right)}{kT}$$

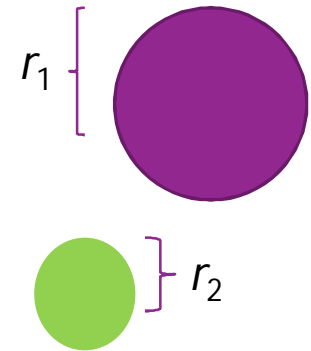
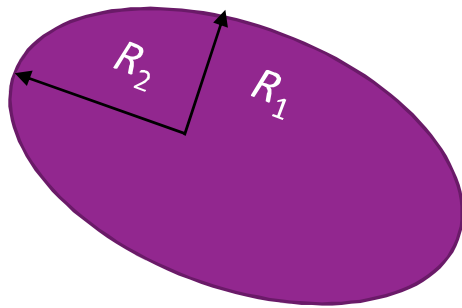




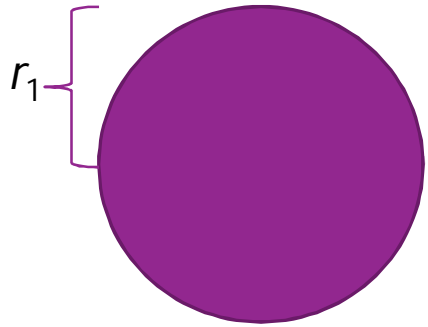
Due to this, small particles tend  
to “dissolve”

But how about if we  
have different size of  
particles?



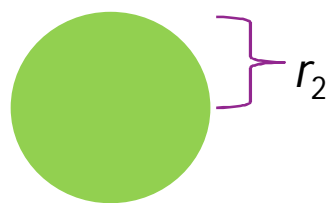


For simplicity, let's think  
only spherical particles

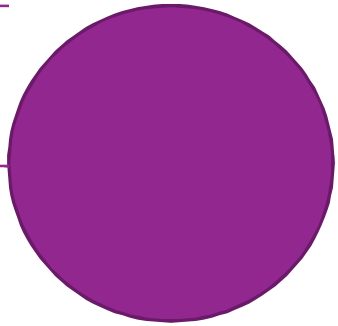


$$\ln\left(\frac{S_{c,large}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_1 kT}$$

$$r_1 > r_2$$




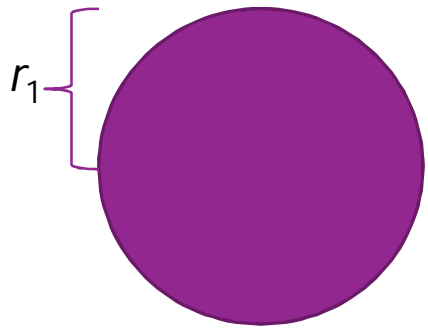
$$\ln\left(\frac{S_{c,small}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_2 kT}$$


$$r_1 \quad \ln\left(\frac{S_{c,large}}{S_\infty}\right) = \frac{2\gamma\Omega}{r_1 kT}$$

$$r_1 > r_2$$

$$\Rightarrow S_{c, small} \gg S_{c, large}$$

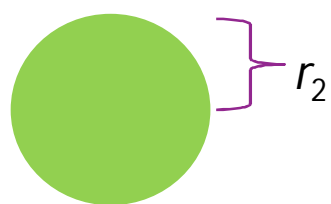

$$r_2 \quad \ln\left(\frac{S_{c,small}}{S_\infty}\right) = \frac{2\gamma\Omega}{r_2 kT}$$



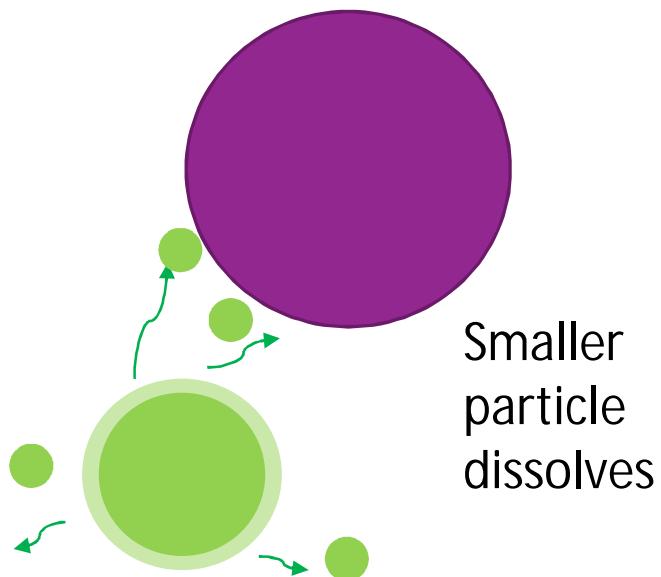
$$\ln\left(\frac{S_{c,large}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_1 kT}$$

$$r_1 > r_2$$

$$\Rightarrow S_{c, small} \gg S_{c, large}$$



$$\ln\left(\frac{S_{c,small}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_2 kT}$$

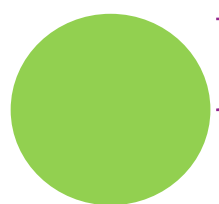




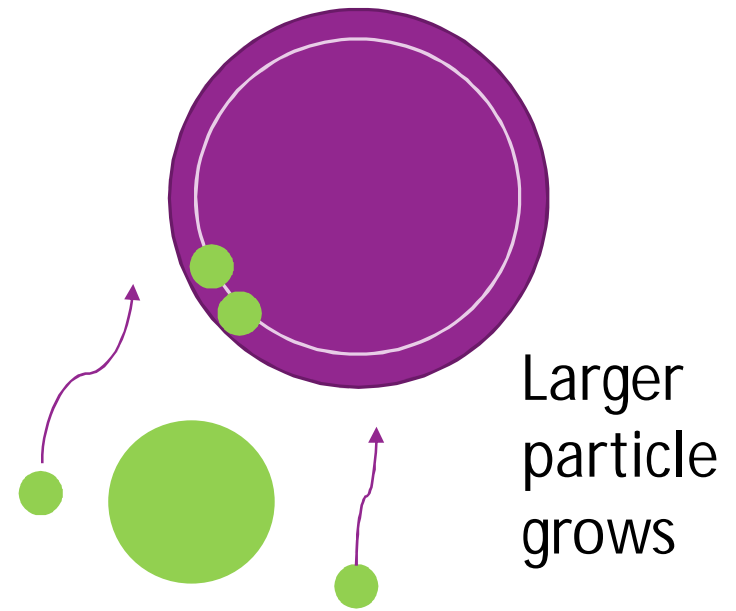
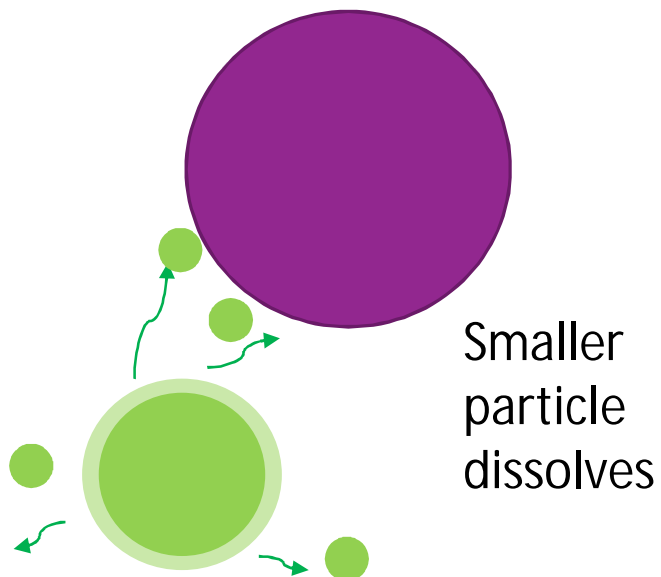
$$\ln\left(\frac{S_{c,large}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_1 kT}$$

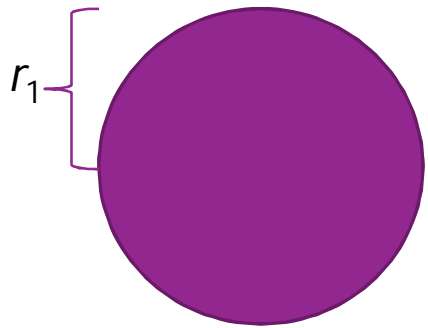
$$r_1 > r_2$$

$$\Rightarrow S_{c, small} \gg S_{c, large}$$



$$\ln\left(\frac{S_{c,small}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_2 kT}$$

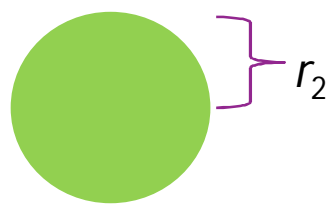




$$\ln\left(\frac{S_{c,large}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_1 kT}$$

$$r_1 > r_2$$

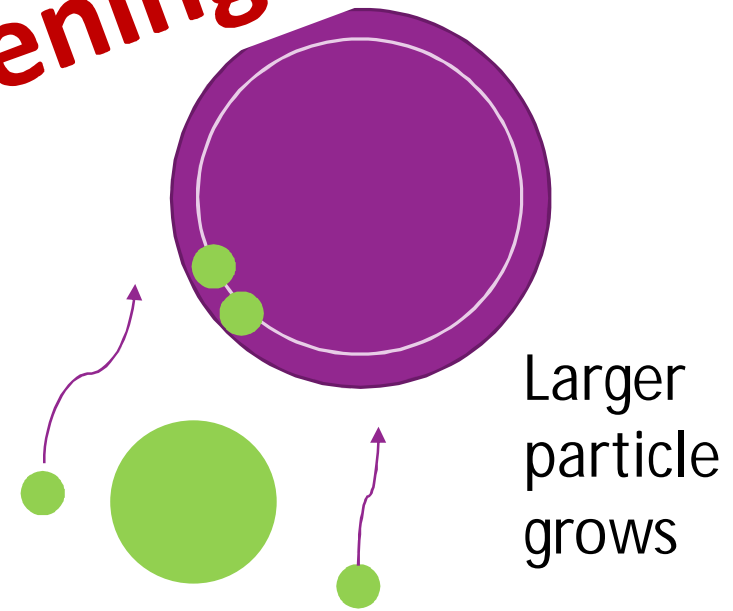
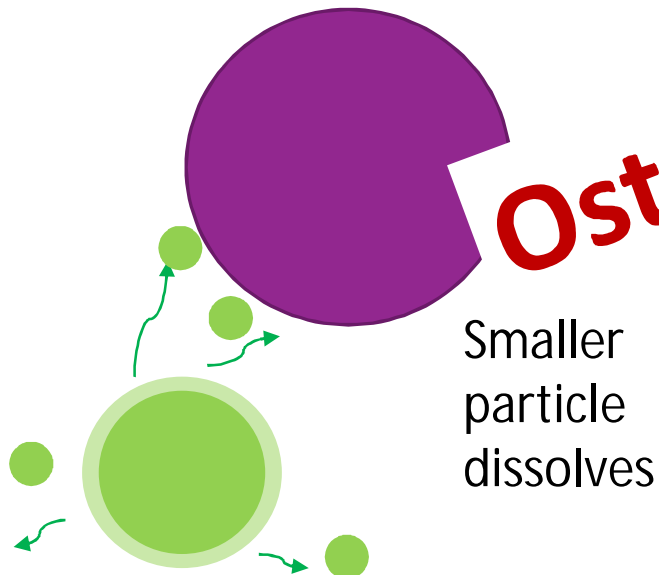
$$\Rightarrow S_{c, small} \gg S_{c, large}$$



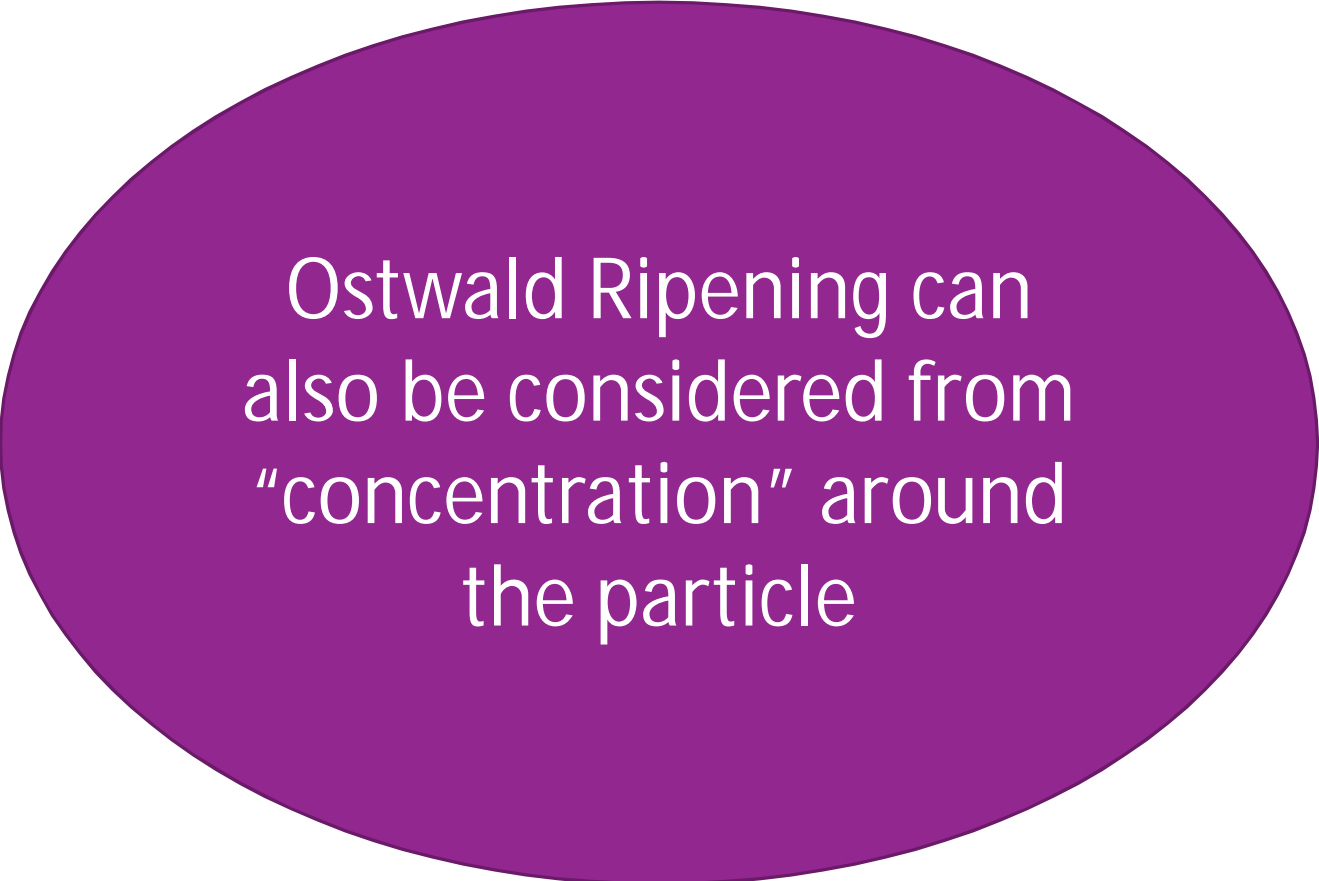
$$\ln\left(\frac{S_{c,small}}{S_{\infty}}\right) = \frac{2\gamma\Omega}{r_2 kT}$$



**Ostwald Ripening**

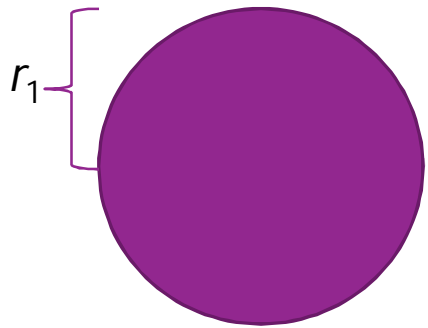







Ostwald Ripening can  
also be considered from  
“concentration” around  
the particle





$$\ln \left( \frac{C_{c,large}}{C_0} \right) = \frac{2\gamma\Omega}{r_1 RT}$$

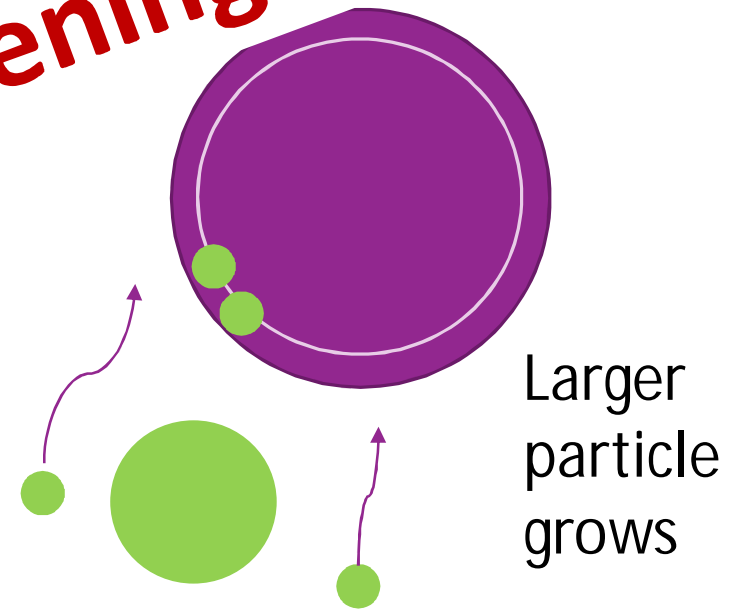
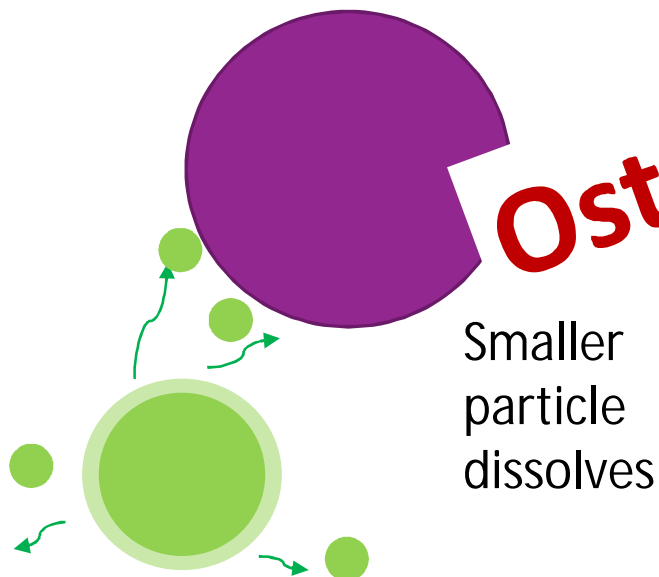
$$\Rightarrow C_{c, small} \gg C_{c, large}$$



$$\ln \left( \frac{C_{c,small}}{C_0} \right) = \frac{2\gamma\Omega}{r_2 RT}$$



**Ostwald Ripening**



# Concept Check #1

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## Ostwald ripening

(a) is due to the higher solubility of smaller particles

(b) is due to lower solubility of smaller particles

(c) is due to lower vapour pressure of smaller particles

# Concept Check #2

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Ostwald ripening can take place

(a) slower at lower temperature

(b) when different sized particles are present in media

(c) only when different sized particles touch each other



## 2<sup>nd</sup> Part: DLVO Theory

# Why some particles precipitate and why some stay in solutions?

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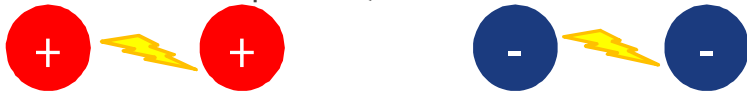
# Electrostatic Stabilization

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## MAIN INTERACTION FORCES

### § Repulsive forces

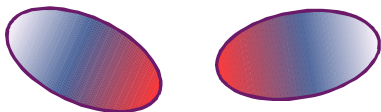
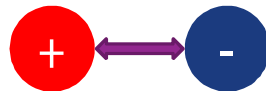
§ Electrostatic (negative-negative, positive-positive)



### § Attractive Forces

§ Electrostatic (negative-positive)

§ Van der Waals



But how this actually works....

∅ Electrical Double Layer

# Electrical Double Layer (EDL)

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Surfaces become charged when in contact with a polar solution

For example:

- Electrode | solution
- Colloidal particle | solution

Theory of electrical double layer (EDL) tries to explain the distribution of ions (=potential distribution) nearby a charged surface

- In a polar solution

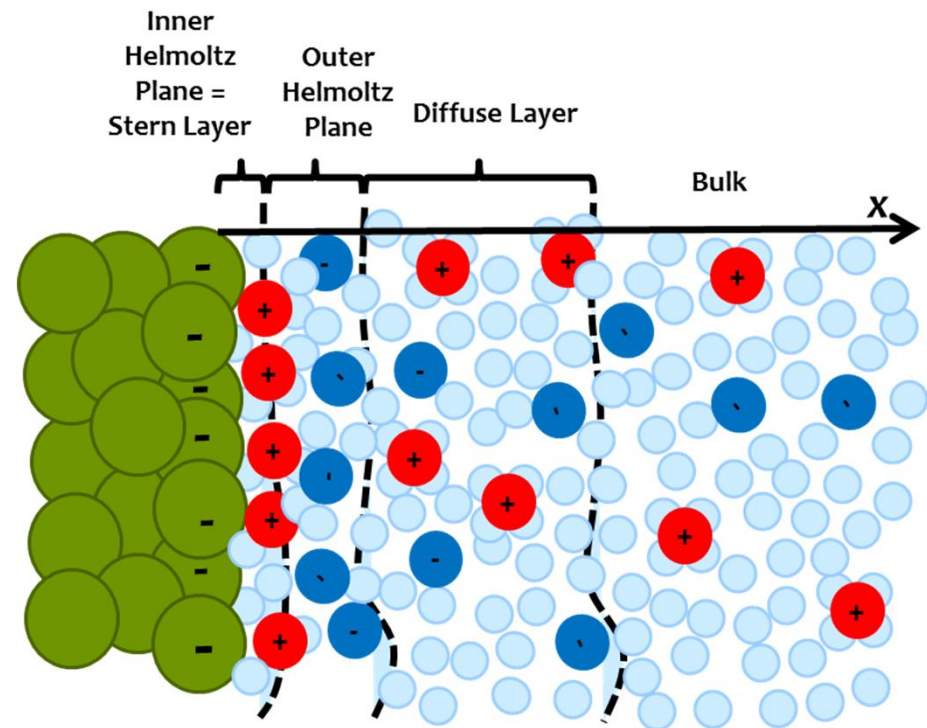




# Electrical Double Layer

Electrical double layer (EDL) can be considered to be divided in three parts

1. Inner Helmholtz layer
  - Specifically adsorbed ions
2. Outer Helmholtz Layer
  - Non-specifically adsorbed ions
3. Diffuse layer
  - Ions moving due to electrostatic field and Brownian motion



The borderline between layers is difficult to determine exactly

# Electrical Double Layer

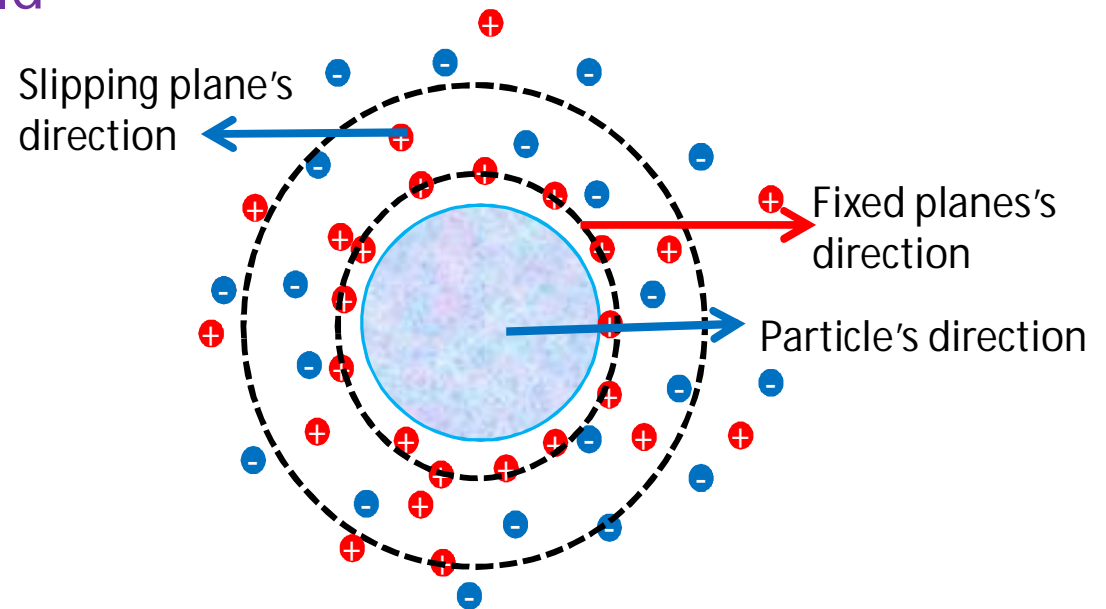
EDL can be also thought of consisting of two layers:

## 1. Fixed Layer (Stern Layer)

- Adsorbed ions move with the particle **in an electric field**

## 2. Mobile Layer

- Diffuse layer to the opposite direction as particle
- Slipping plane



The borderline between layers is difficult to determine exactly

# Potential Field in EDL: Poisson-Boltzman Equation

## Poisson equation

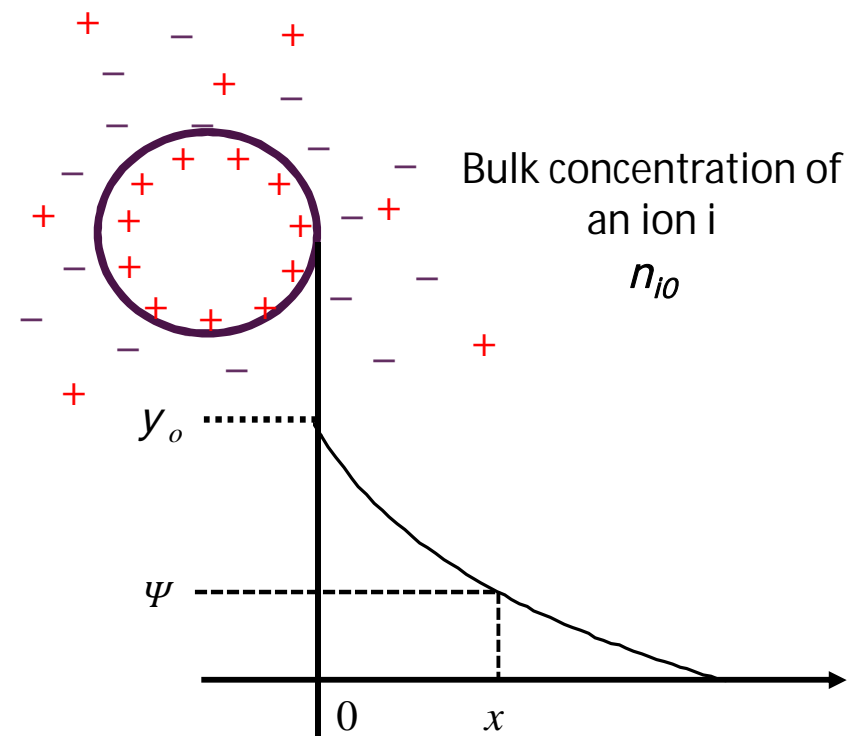
§ non-linear dependence of the potential on the charge density

## Boltzman equation

§ what is the probability to find a particle at certain distance from the surface

## Poisson-Boltzman equation

§ how particles create an electrostatic field around a charged surface



# Solution of Poisson-Boltzman

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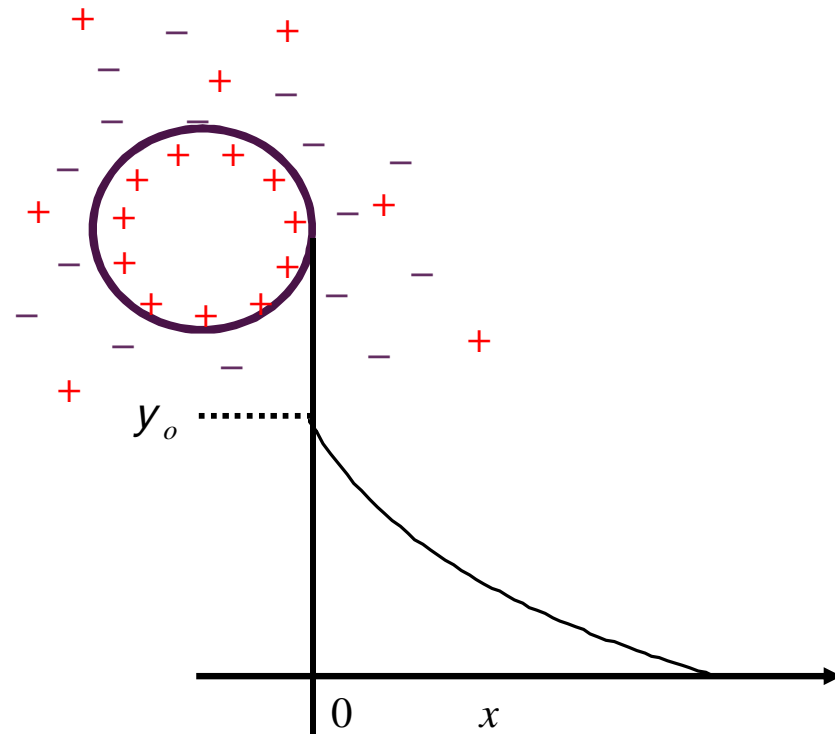
$$\Psi = \Psi_0 \exp(-\kappa x)$$

where

$$\kappa = \left( \frac{e^2 \sum_i z_i^2 n_{i,0}}{\epsilon k T} \right)^{1/2}$$

∅ Potential increases exponentially when approaching the surface

- This equation is not valid extremely close to the surface



# Thickness of EDL $\approx$ Debye length $\kappa^{-1}$

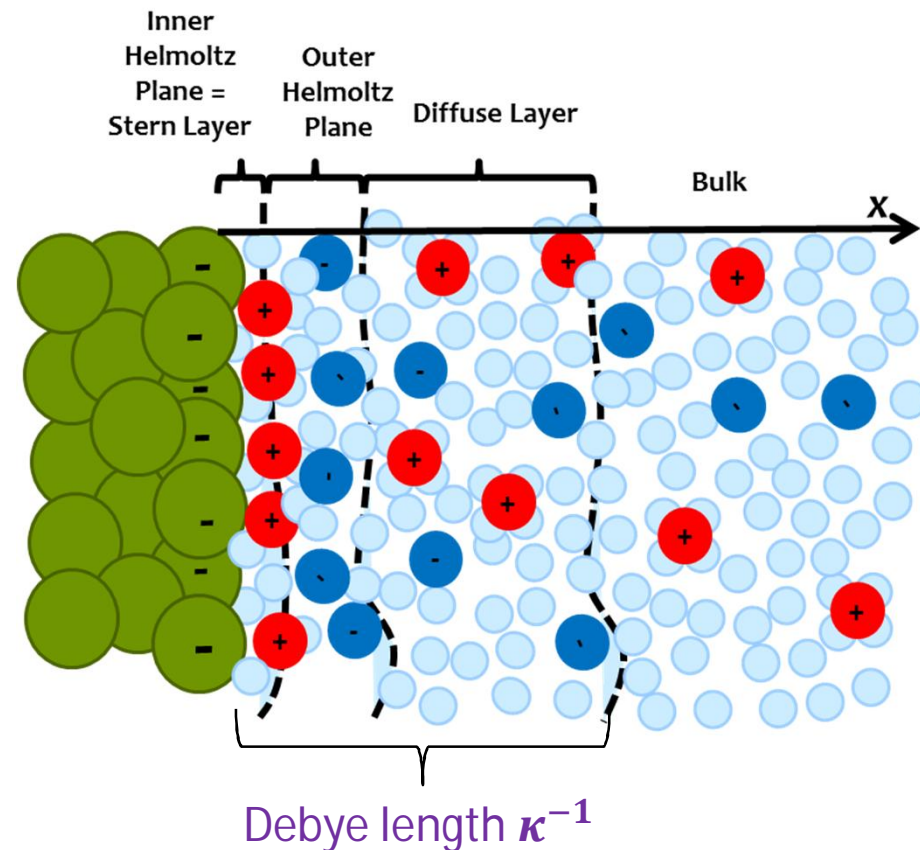
## Debye length $\kappa^{-1}$

- How far away from the surface the ions do "feel" the charged substrate

$$\begin{aligned} & \kappa^{-1} \\ &= \left( \frac{e^2 \sum_i z_i^2 n_{i,0}}{\epsilon kT} \right)^{-1/2} \\ &= \left( \frac{e^2 N_A \sum_i z_i^2 c_{i,0}}{\epsilon kT} \right)^{-1/2} \\ &= \left( \frac{F^2 \sum_i z_i^2 c_{i,0}}{\epsilon RT} \right)^{-1/2} \\ &= \left( \frac{F^2}{\epsilon RT} I \right)^{-1/2} \end{aligned}$$

where  $I$  is ionic strength

$$[\kappa^{-1}] = [\text{m}]$$



# Concept Check #3

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When the ionic strength of solution increases, the thickness of electrical double layer

- 1) Increases?
- 2) Decreases?
- 3) Stays constant?

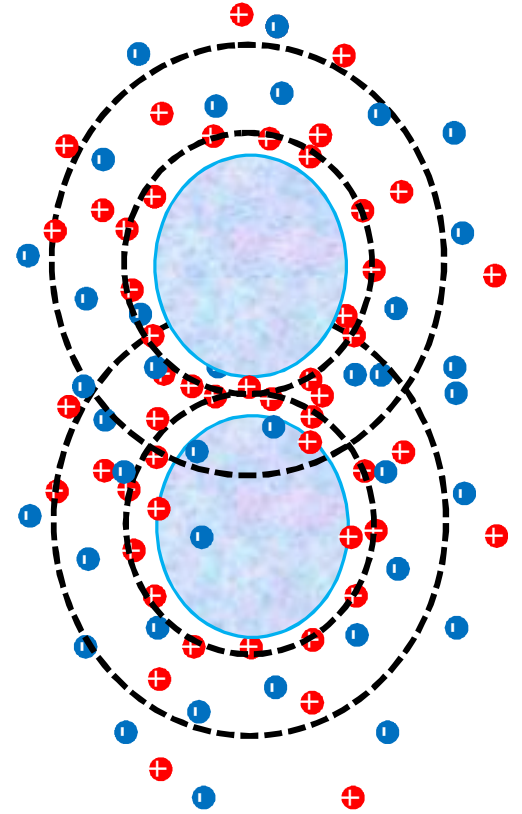
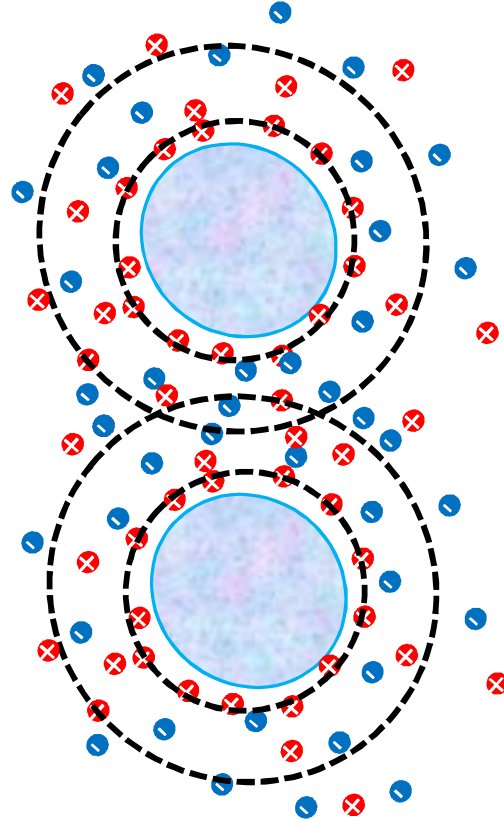
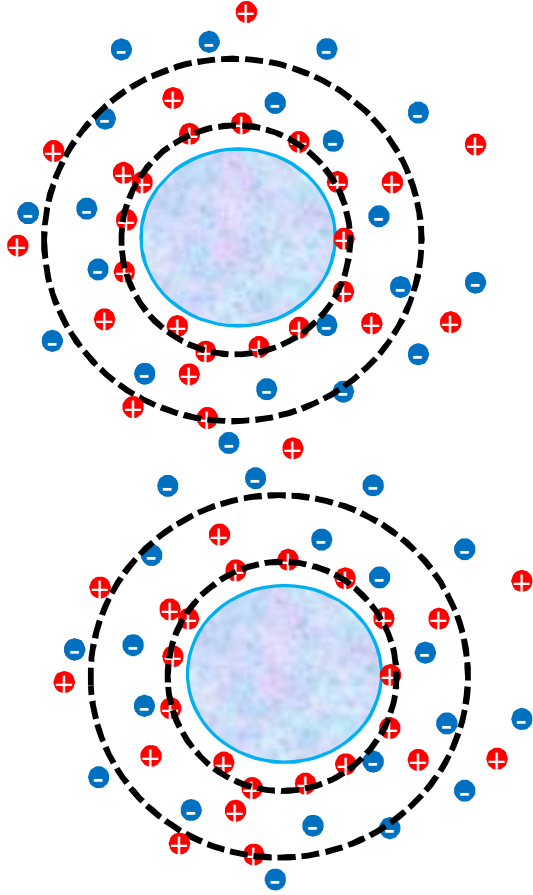


# Example: $\kappa^{-1}$ for (1,1)-electrolyte

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<u>Concentration [mol/dm<sup>3</sup>]</u>	<u>1/k [nm]</u>
0.1	0.96
0.01	3.04
0.001	9.6
0.0001	30.4
Ⓡ 0	Ⓡ 100

Ø When ionic strength increases, thickness of the double layer decreases





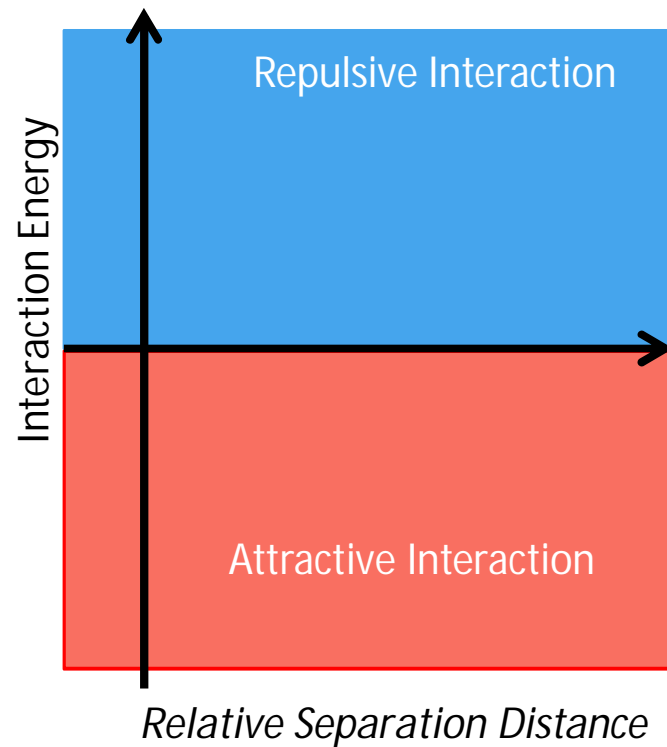
How about other forces?

Let's think forces  
between two particles in  
a solution.

# DLVO\* theory

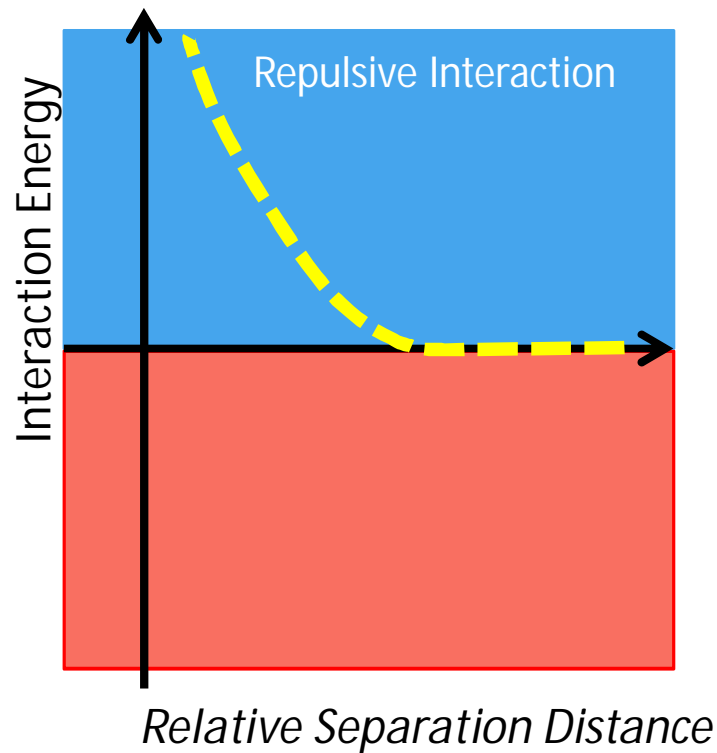
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\* *Derjaguin and Landau,  
Verwey and Overbeek*



# DLVO theory

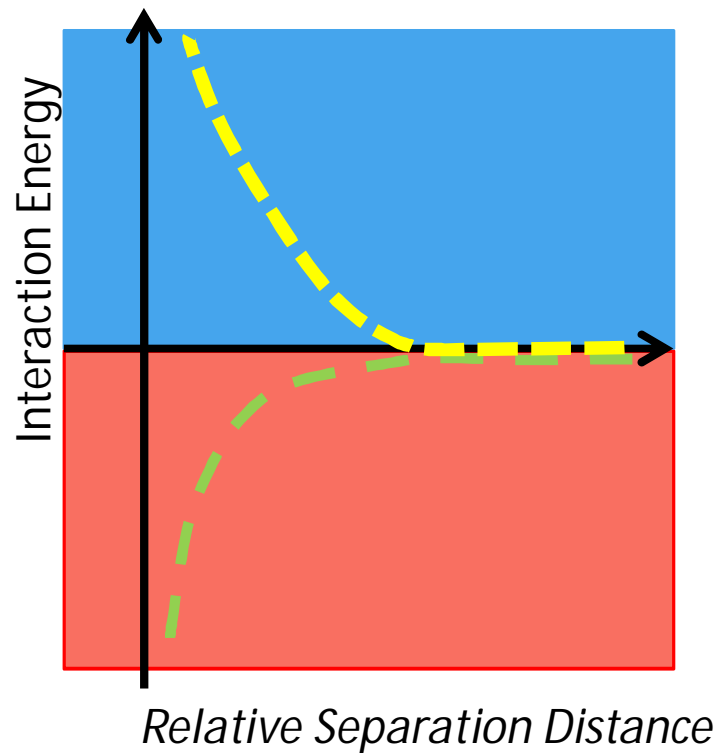
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Net Interaction  
=  
Due to Repulsive forces

# DLVO theory

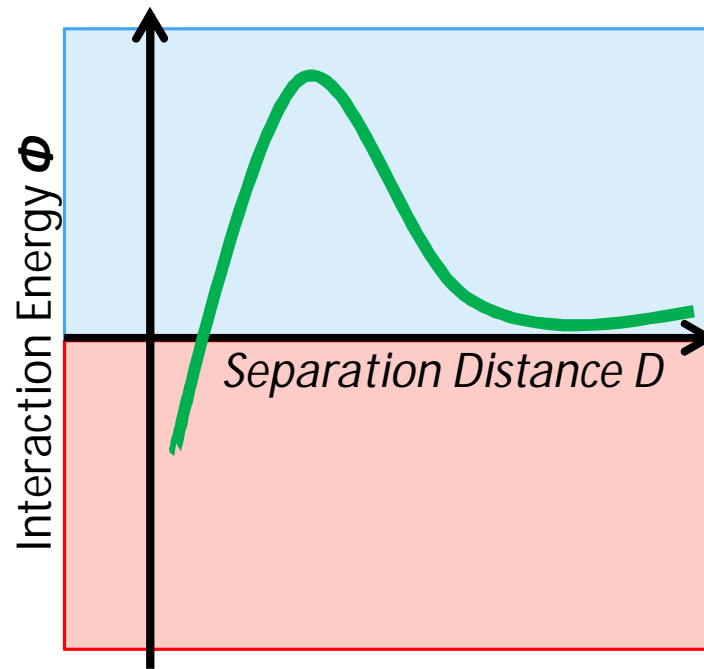
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Net Interaction  
=  
Due to Repulsive forces  
+  
Due to Attractive forces

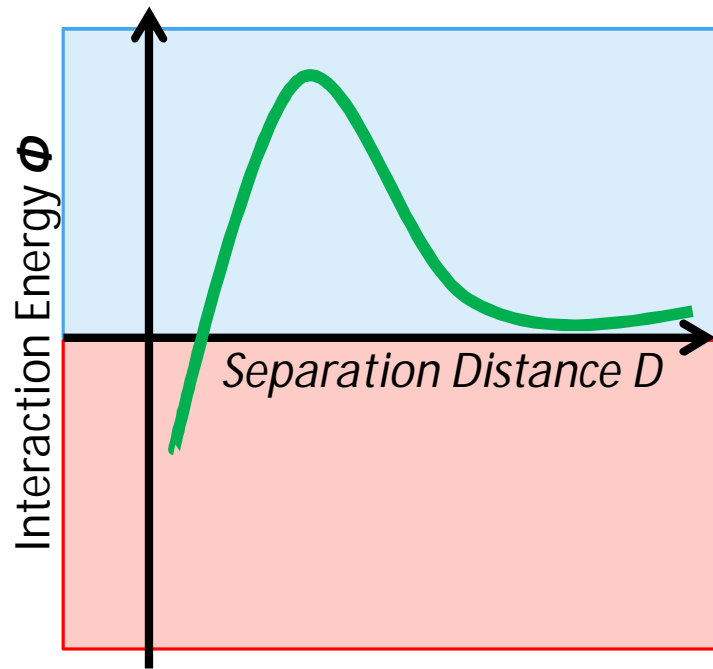
# DLVO Theory

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$$\Phi = \text{Attractive} + \text{repulsive}$$

# DLVO Theory



## Electrostatic energy

$$\Phi_E = 2\pi\epsilon_r\epsilon_0rE^2e^{-\kappa D}$$

Where

$$\kappa = \sqrt{\frac{F^2 \sum_i c_i z_i^2}{\epsilon_r \epsilon_0 RT}}$$

$r$ =radius

$E$  = potential

$\epsilon$  = permittivity;  $r$ =relative,  $_0$ = vacuum

$F$  = Faraday's constant

$c_i$  = concentration of ion  $i$

$z_i$  = charge of ion  $i$

$R$  = gas constant

$T$  = temperature

$A$  = Hamaker constant

$r_1$  = radius of particle 1

$r_2$  = radius of particle 2

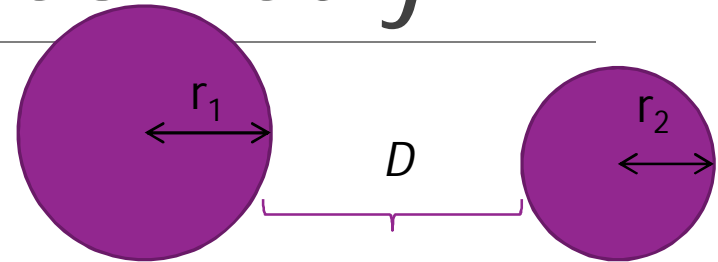
## Van der Waals

$$\Phi = \Phi_E + \Phi_{VdW}$$

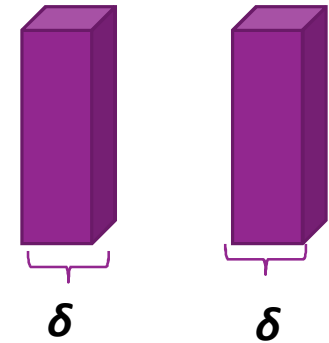
$$\Phi_{VdW} = -\frac{Ar_1r_2}{6D(r_1 + r_2)}$$

# VdW Depends on Geometry

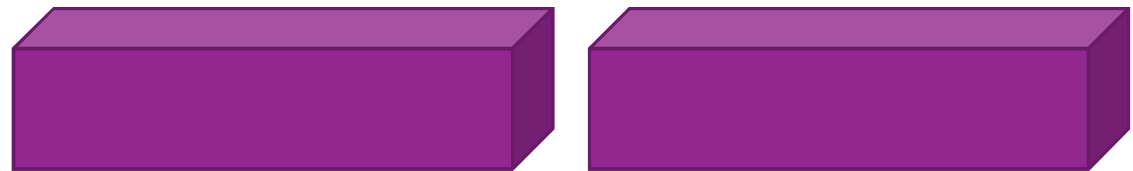
$$\Phi_{VdW} = -\frac{Ar_1r_2}{6D(r_1+r_2)}$$



$$\Phi_{VdW} = -\frac{A}{12\pi} [D^{-2} + (2\delta + D)^{-2} + (\delta + D)^{-2}]$$



$$\Phi_{VdW} = -\frac{A}{12\pi} D^{-2}$$

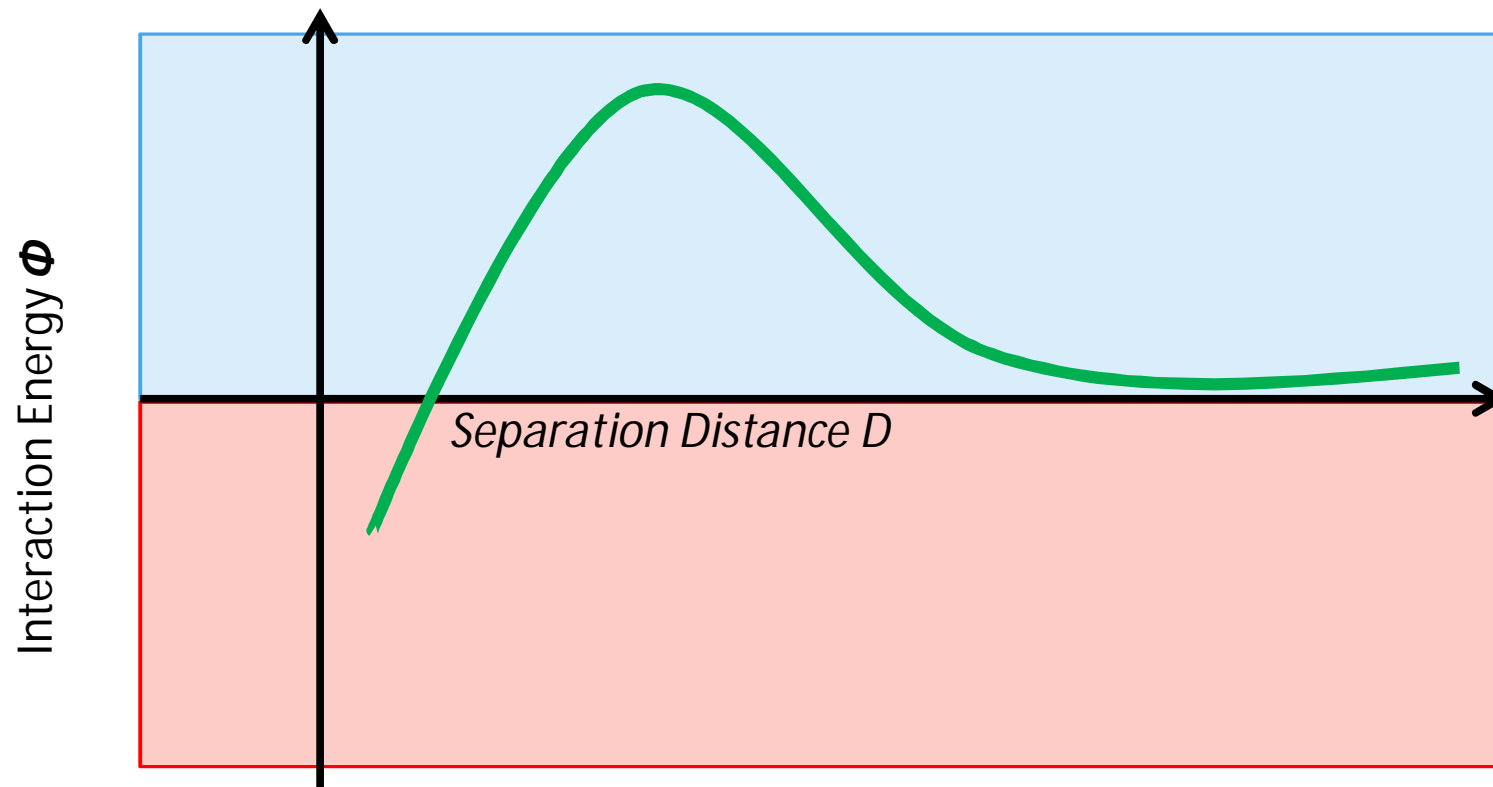


$D$  = separation distance



# DLVO Theory

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$$\Phi = \Phi_E + \Phi_{VdW}$$





# Concept Check #4

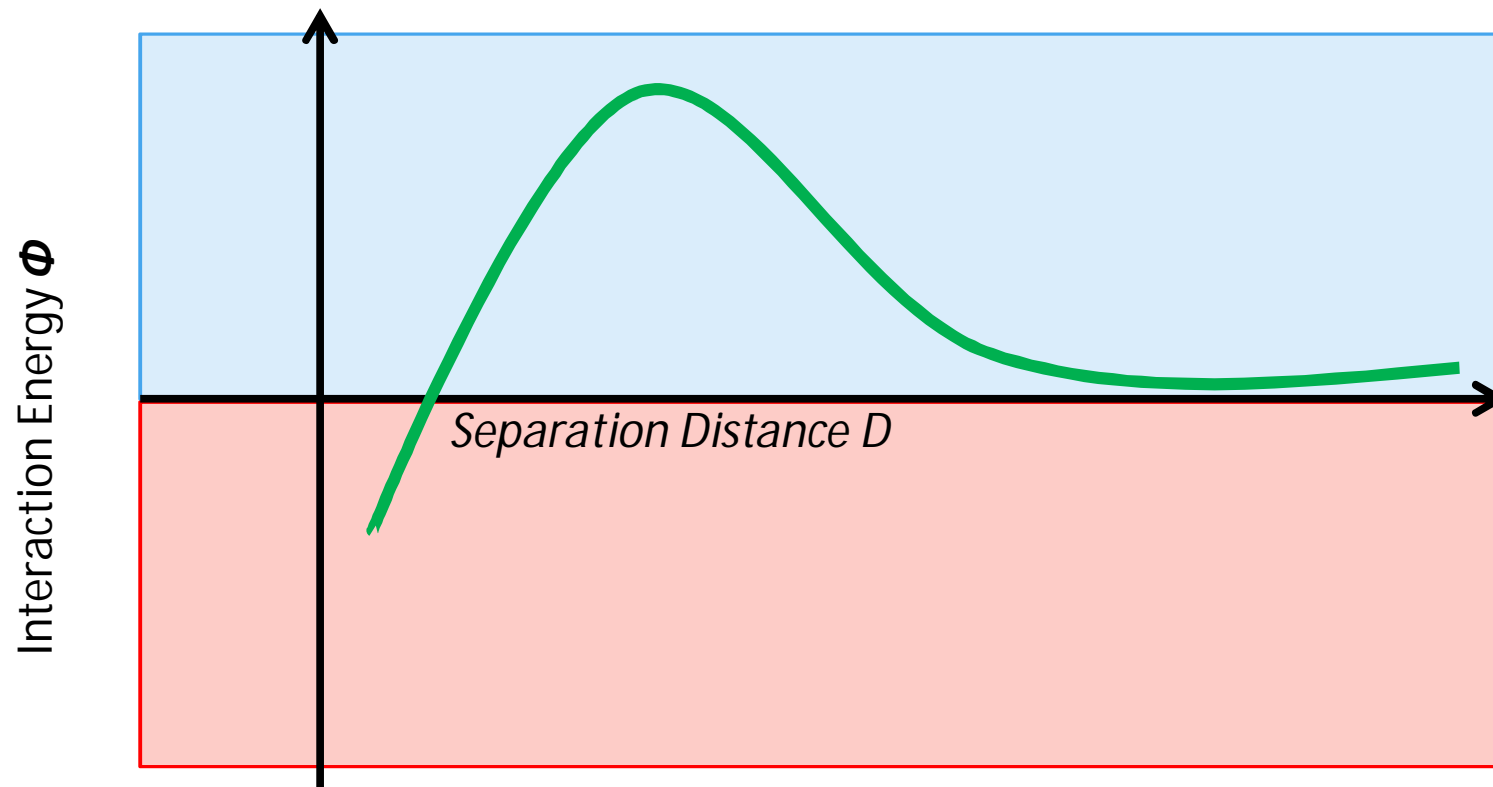
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Based on DLVO theory

- (a) particles aggregate when interaction energy is high
- (b) particles are more likely to aggregate when the salt concentration decreases
- (c) particles are stable in a colloid due to electrostatic repulsion

# DLVO Theory

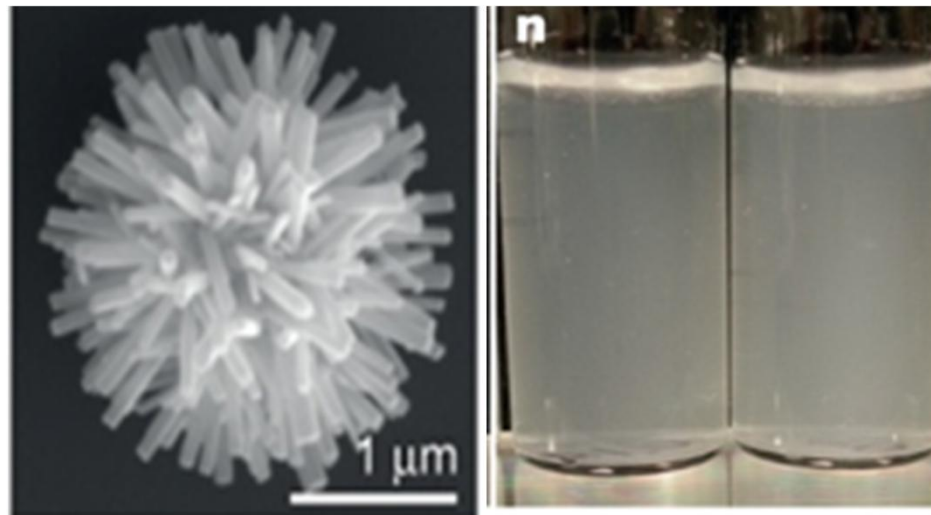
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$$\Phi = \Phi_E + \Phi_{VdW}$$

# Hydrophobic Hedgehog Particles: Stable in Water??

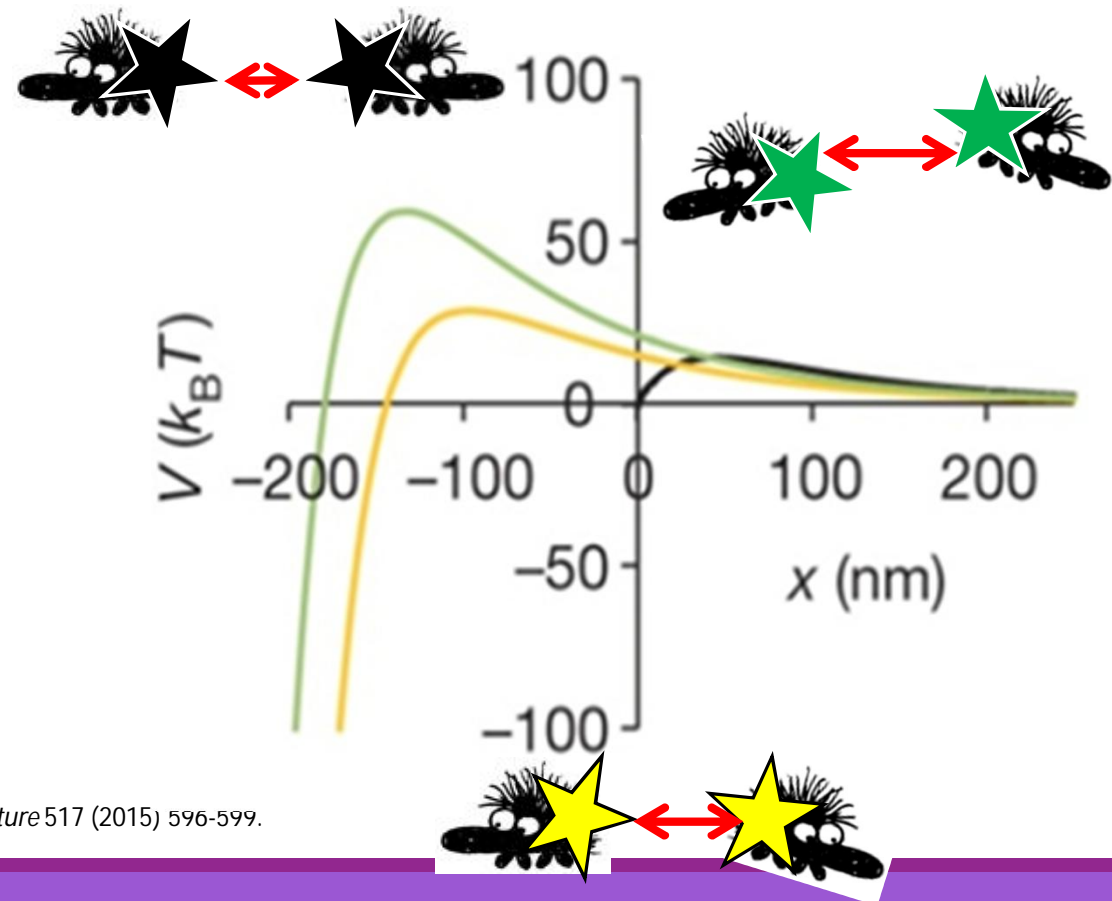
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J. H. Bahng, B. Yeom, Y. Wang, S. O. Tung, J. D. Hoff, N. Kotov, *Nature* 517 (2015) 596-599.

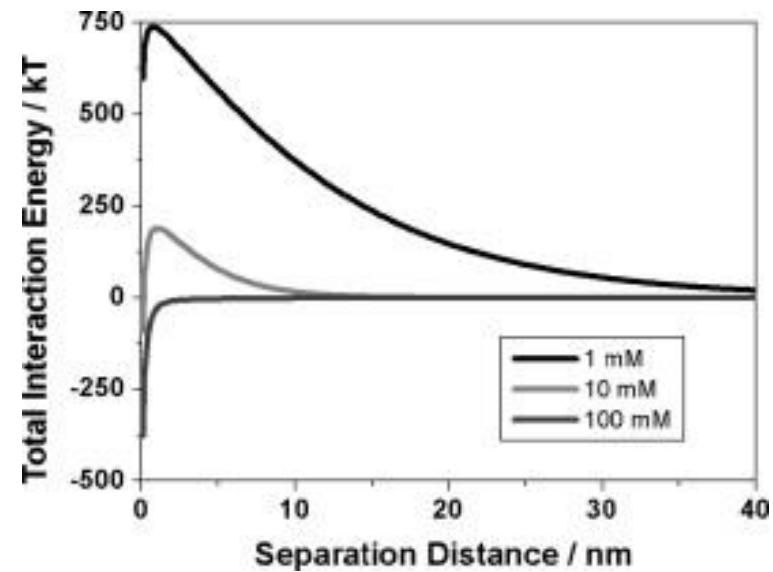
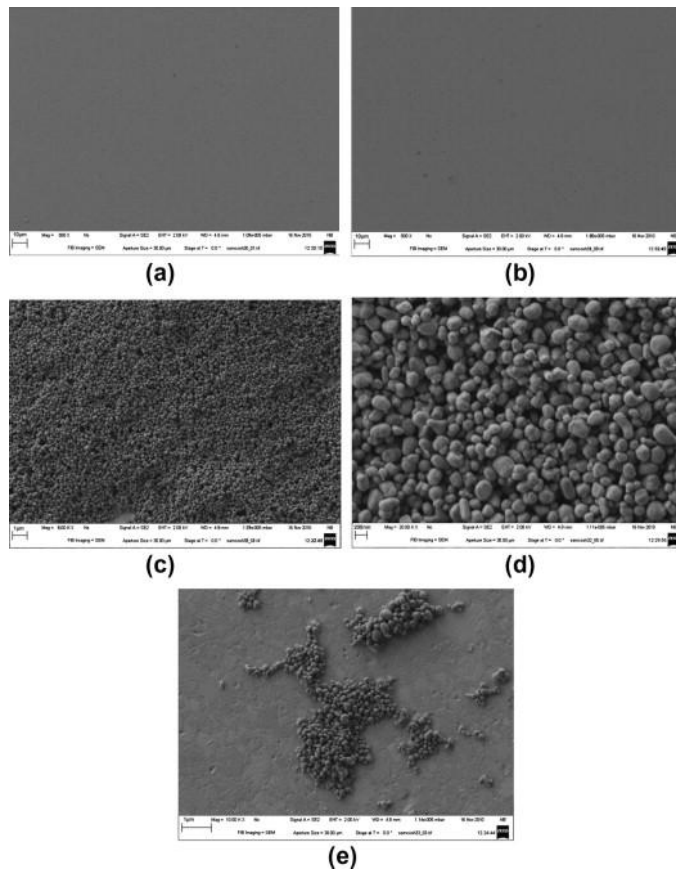
# Hydrophobic Hedgehog Particles: Stable in Water

Smaller contact  
area with spikes



J. H. Bahng, B. Yeom, Y. Wang, S. O. Tung, J. D. Hoff, N. Kotov, *Nature* 517 (2015) 596-599.

# TiO<sub>2</sub> Nanocontainers on Au QCM crystal



A. Pomorska, K. Yliniemi, B. P. Wilson, D. Shchukinc, D. Johannsmannd, G. Grundmeier, *Journal of Colloid and Interface Science* 362 (2011) 180-187 .

# Other Routes to Stability



# Steric Stabilization

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Thermodynamical stabilization

Ø Based on Gibb's energy minimization of polymers in solvents

1. Polymer reduces  $\Delta G$  by expanding in a solvent  
à Good solvent
2. Polymer reduces  $\Delta G$  by coiling up in a solvent  
à Poor solvent

This is also dependent on  $T$

*Flory-Huggins  $\theta$  temperature (or  $\theta T$ )*



# Steric Stabilization

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*Flory-Huggins  $\theta$  temperature (or  $\theta$   $T$ )*

When  $T = \theta$ , no change in Gibb's energy even if polymer conformation changes

$$\Delta G_{\text{mixing}} = \Delta H - T\Delta S$$

$$\Delta G_{\text{mixing}} = RT (n_1 \ln \phi_1 + n_2 \ln \phi_2 + n_1 \phi_2 \psi_{12})$$

$n_1$  = number of solvent moles

$n_2$  = number of solute (polymer) moles

$\phi_1$  = volume fraction of solvent

$\phi_2$  = volume fraction of solvent

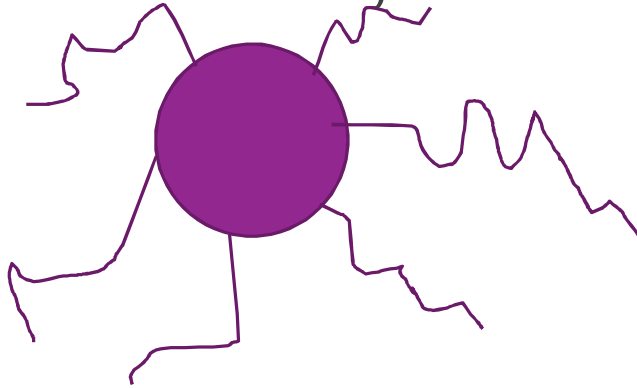
$\psi_{12}$  = free energy parameter (incl. entropy)



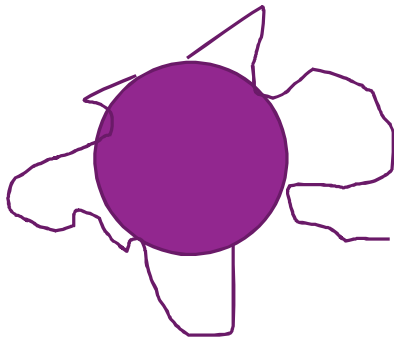
# Steric Stabilization

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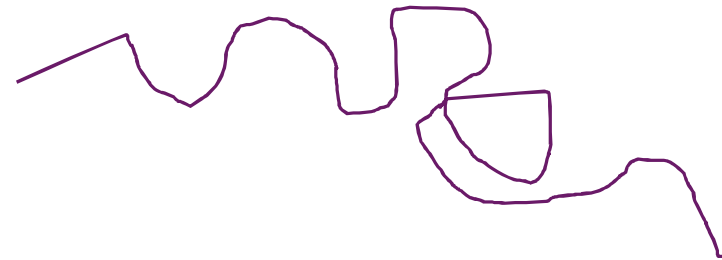
## 1. Anchored Polymers



## 2. Adsorbed Polymers



## 1. Good Solvent

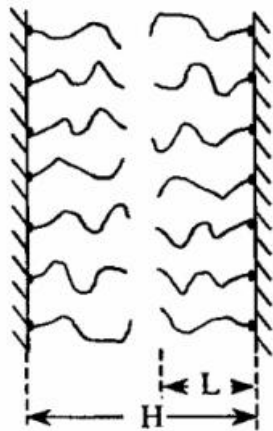


## 2. Poor Solvent

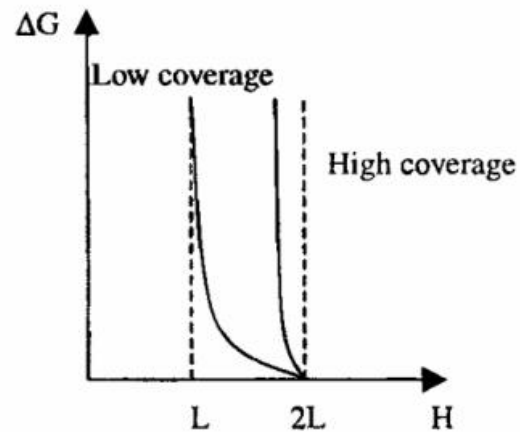


# Solvent Type vs. Coverage

## GOOD SOLVENT



(a)

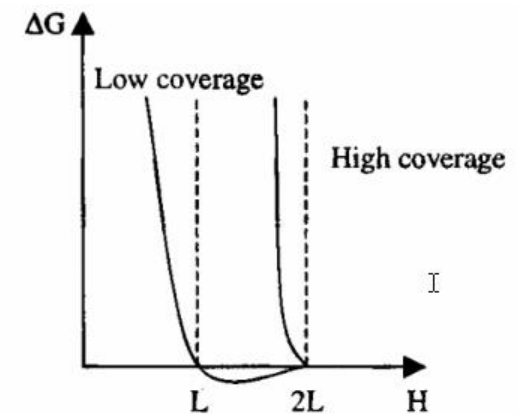


(b)

## POOR SOLVENT



(a)



(b)

# Pair Discussion: How the following parameters affect (colloidal) stability?

---

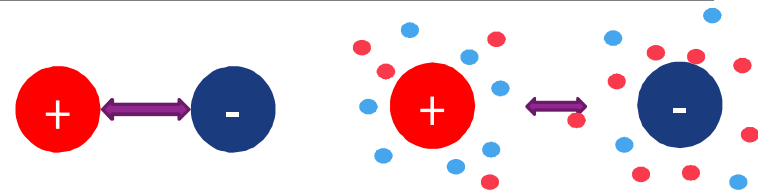
1. Salt concentration in the solution
2. Adding surfactant/polymer on the nanoparticle surface (high coverage)
3. Changing the solvent
4. Changing the geometry



# Pair Discussion: How the following parameters affect (colloidal) stability?

## 1. Salt concentration in the solution

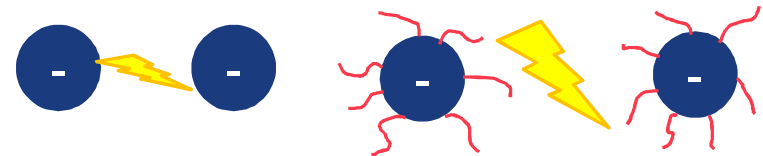
§ Changes the electrostatic interactions



## 2. Adding surfactant/polymer on the nanoparticle surface (high coverage)

§ Changes the electrostatic and Van der Waals interactions

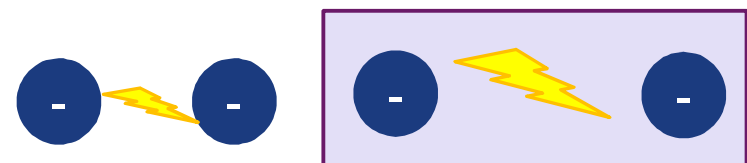
§ Steric hinderance



## 3. Changing the solvent

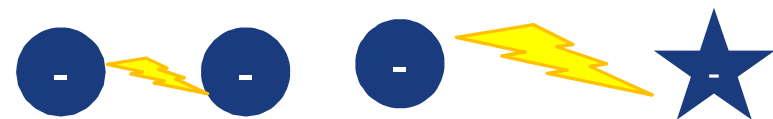
§ Changes the electrostatic and Van der Waals interactions

§ Affects steric hinderance



## 4. Changing the geometry

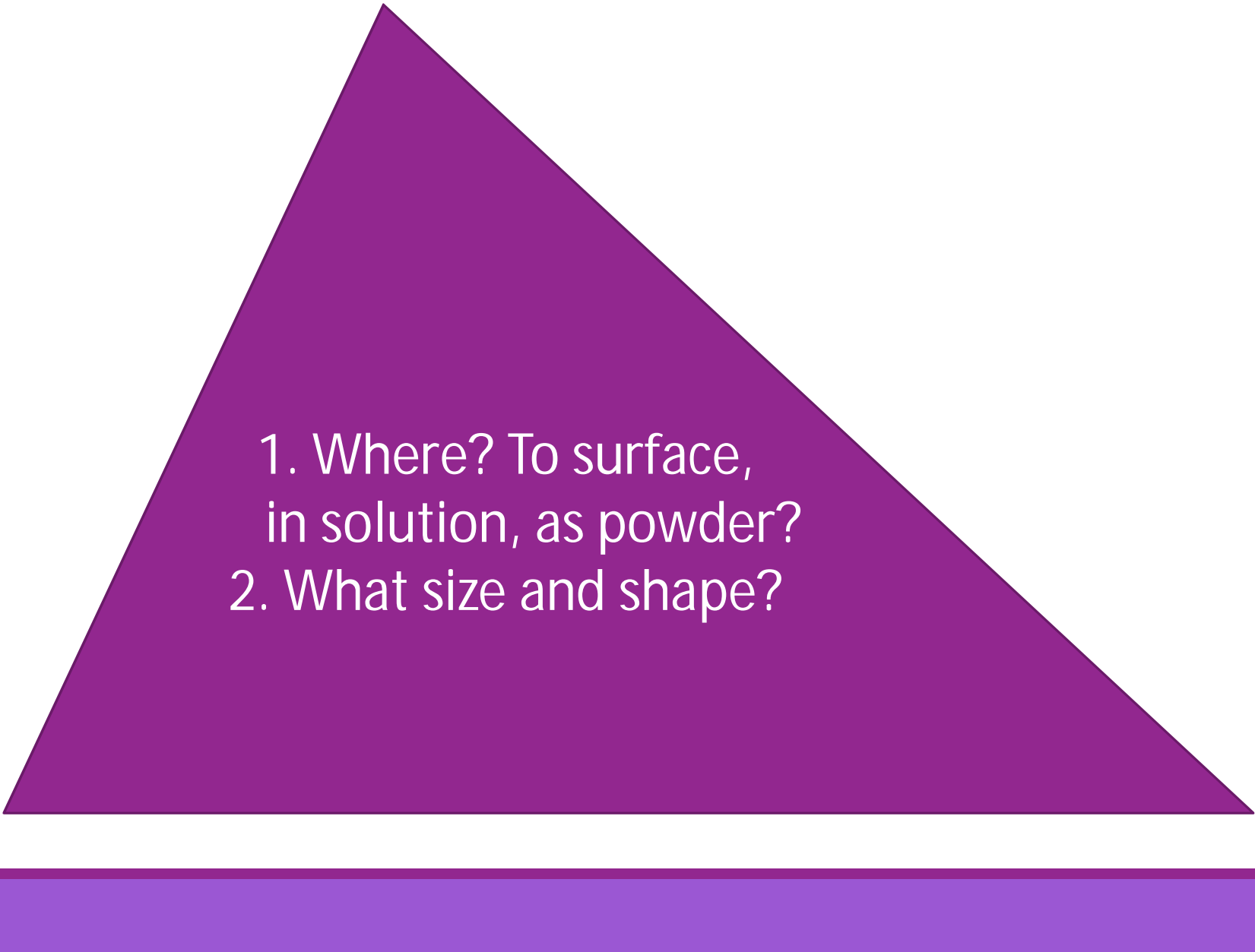
§ Changes Van der Waals interactions





## 3<sup>rd</sup> Part: Synthesis of Nanomaterials (aka Nanochemistry)

# So many questions...

- 
1. Where? To surface,  
in solution, as powder?
  2. What size and shape?

# Examples of self-assemblies – different geometries

0 dimensions: all dimensions on nanoscale (a dot)

- Quantum dots (semiconductor nanoparticles)
- Monolayer protected clusters (metallic nanoparticles with a capping layer)

1 dimension: two dimensions on nanoscale (a line)

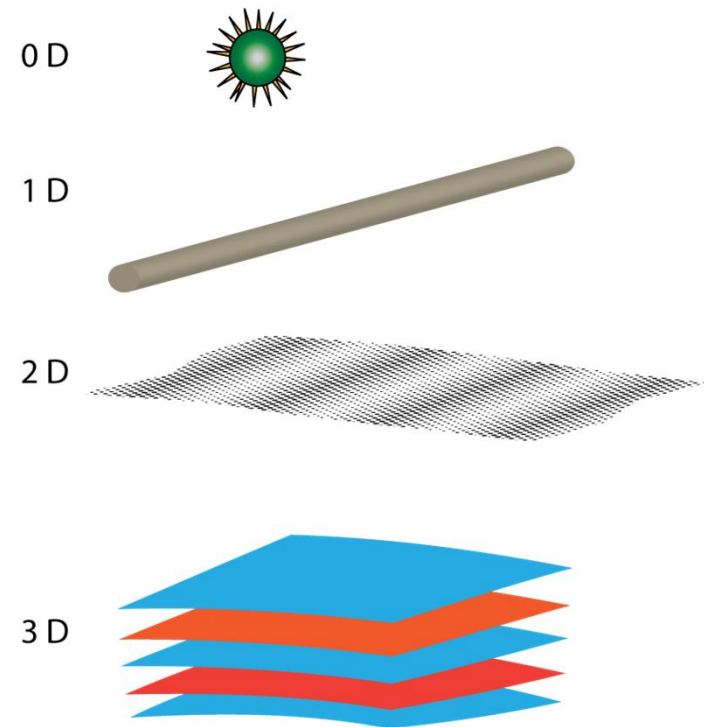
- Metal nanowires
- Carbon nanotubes
- Cellulose nanofibrils

2 dimensions: one dimension on nanoscale (a plane)

- Graphene
- Nanoclay platelets
- Self-assembled monolayers

3 dimensions:

- Layer-by-layer polyelectrolyte structures
- Viral capsides
- Nanocomposites



Nanochemistry is used to achieve these different geometries



# BOTTOM-UP

“Building blocks joined together”

## § Physical

- § Deposition by controlling the atmospheric pressure, ionic strength, temperature, concentrations

## § Chemical

- § Synthesis, i.e. nucleation and growth via chemical reactions
- § In solutions & gases, at surface

# TOP-DOWN

“Shaving of small pieces from a big block”

## § Physical

- § Shaving
- § Grinding
- § Bombarding with ions, electrons (no reaction)

## § Chemical

- § Dissolution
- § Pyrolysis (burning)
- § Bombarding with ions, electrons (causing a reaction)



# BOTTOM-UP

“Building blocks joined together”

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- § Deposition by controlling the atmospheric pressure, ionic strength, temperature, concentrations

## § Chemical

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“Shaving of small pieces from a big block”

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- § Dissolution
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NANOCHEMISTRY



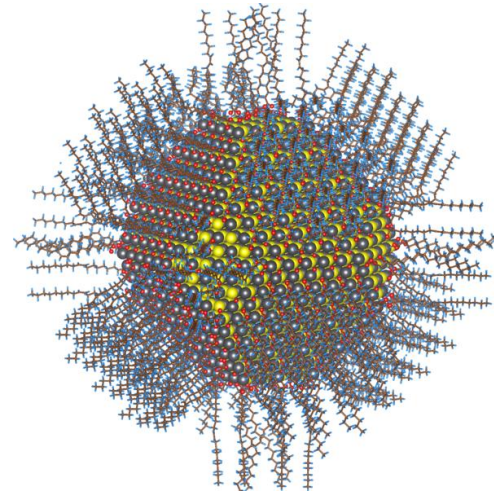
# 0D Nanomaterials

Nanoparticles

Quantum Dots

Inclusions

Example: Lead sulphide nanoparticle protected with oleic acid



Zherebetskyy et al., *Science* 344, (2014) 1380

# Example: Au NPs and Citric Acid

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*Example: Turkevich Method*

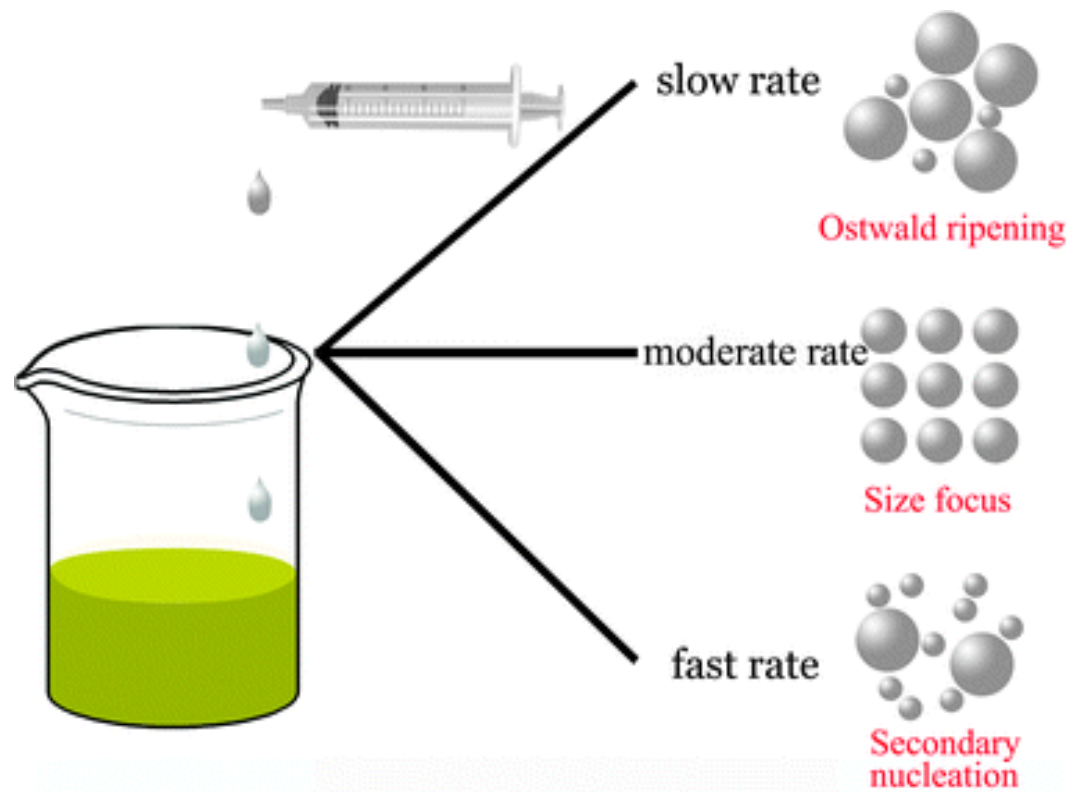


[https://www.tedpella.com/gold\\_html/goldsols.htm](https://www.tedpella.com/gold_html/goldsols.htm)

<https://www.youtube.com/watch?v=SBkGZiTxHKE>

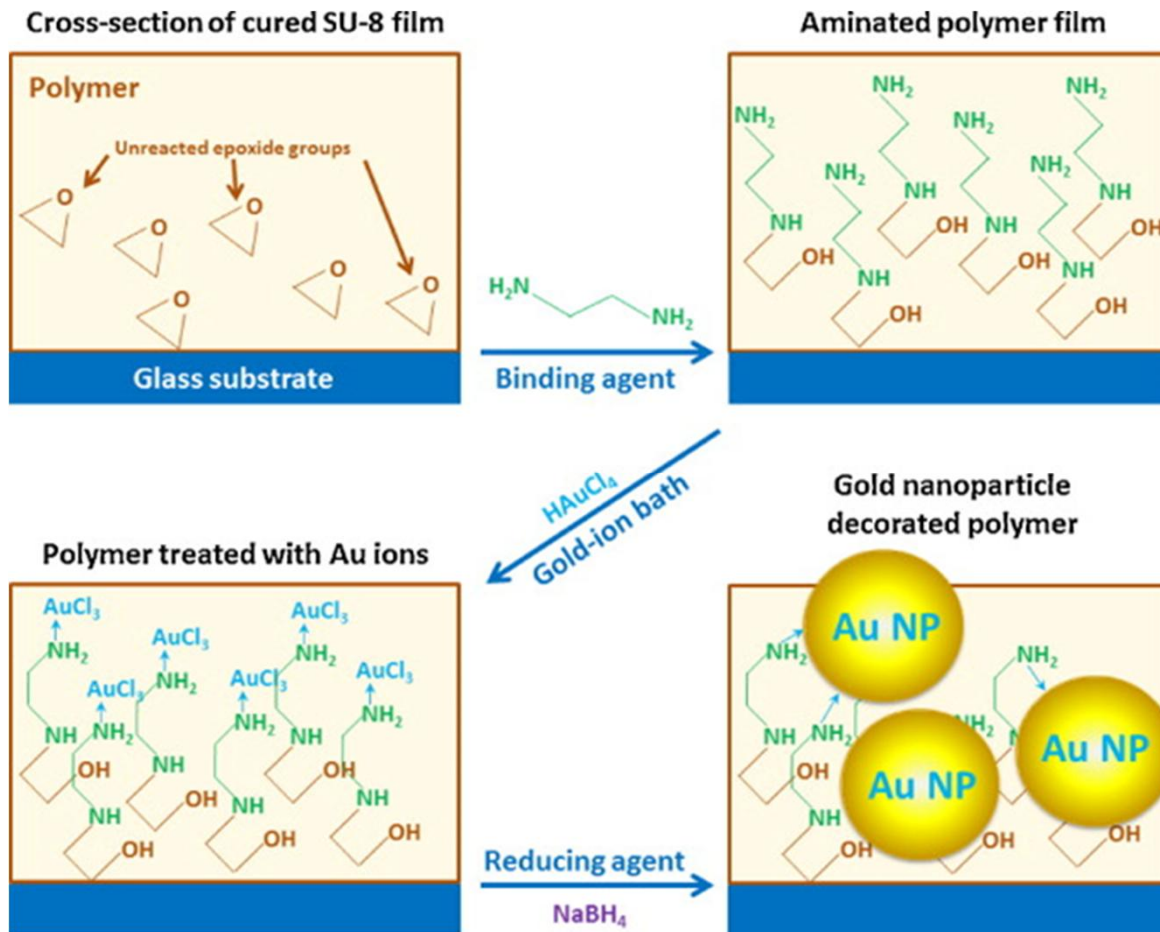
# Example: Seed-and-Feed

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R. Zong, X. Wang, S. Shi, Y. Zhu, PCCP 16 (2014) 4236-4241.

# Example: In-Situ at Surface



# 1D Nanomaterials

Rods

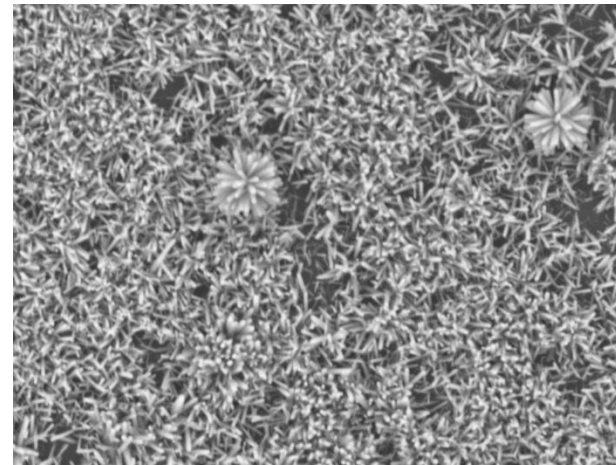
Tubes

Whiskers

Fibres or fibrils

Wires

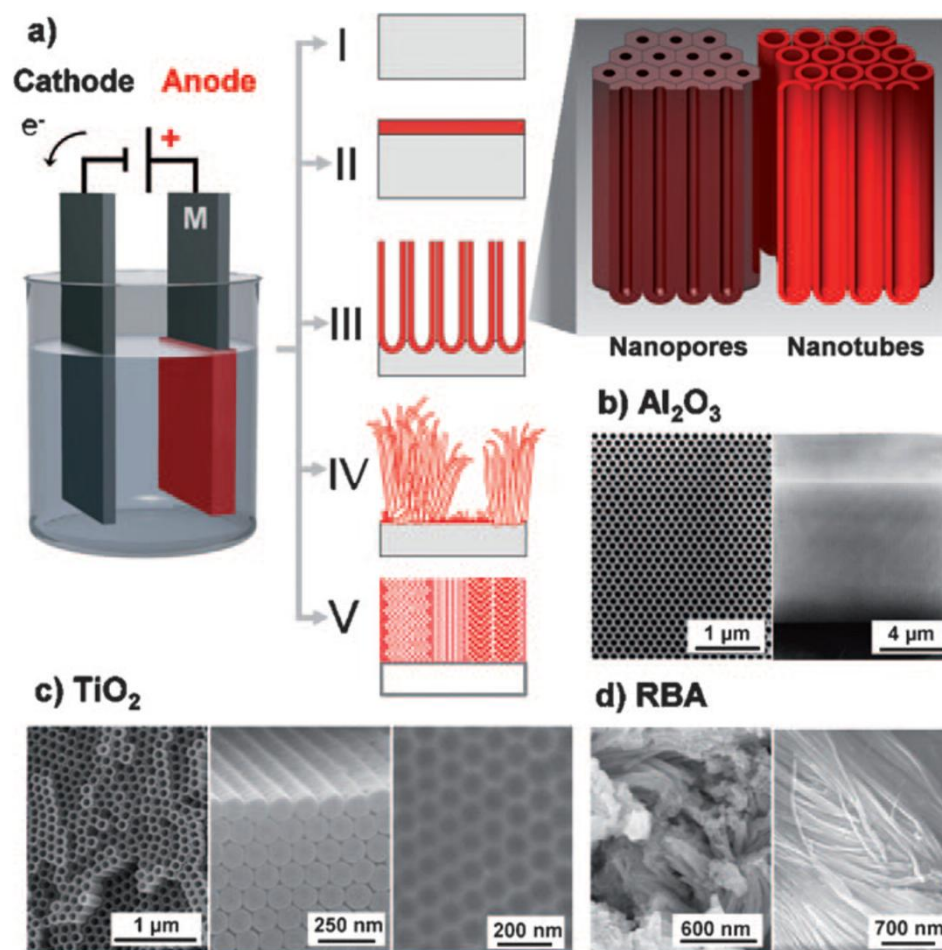
Example: ZnO Nanorods and Hedgehog Particles



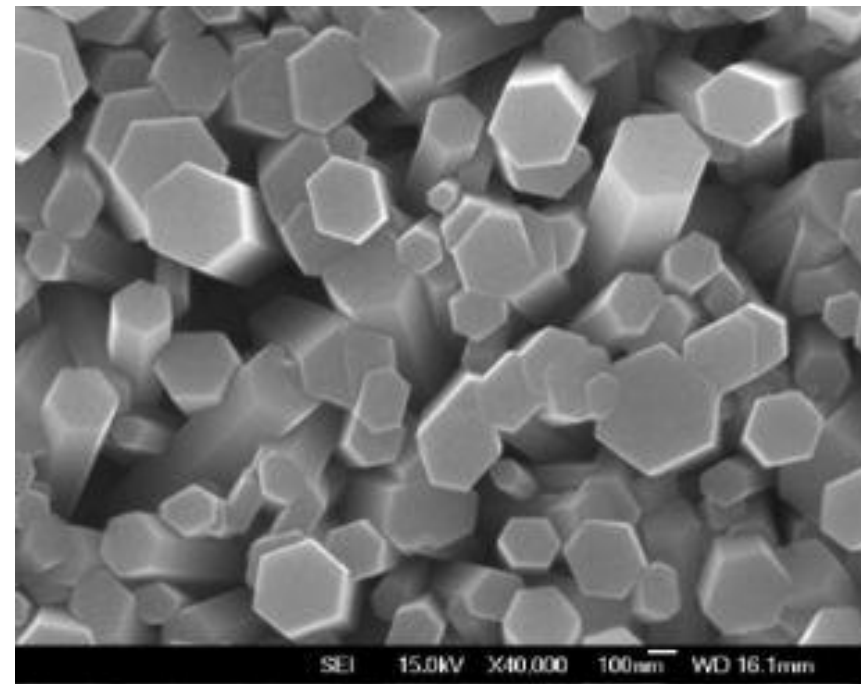
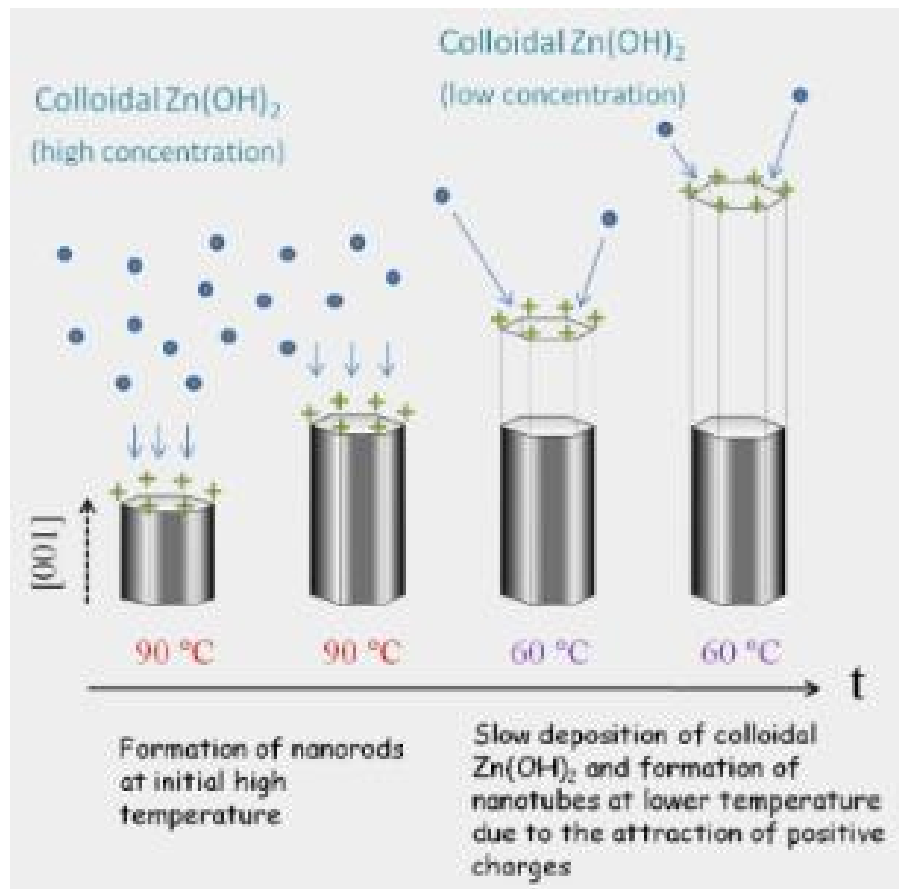
2015/06/12 14:40 D2.7 x4.0k 20 μm

Authors: Manu Tehnunen, Kirsi Yliniemi, Sasha Hoshian, Sami Franssila

# 1D Nanomaterials: Nanotubes



# 1D Nanomaterials: Nanorods

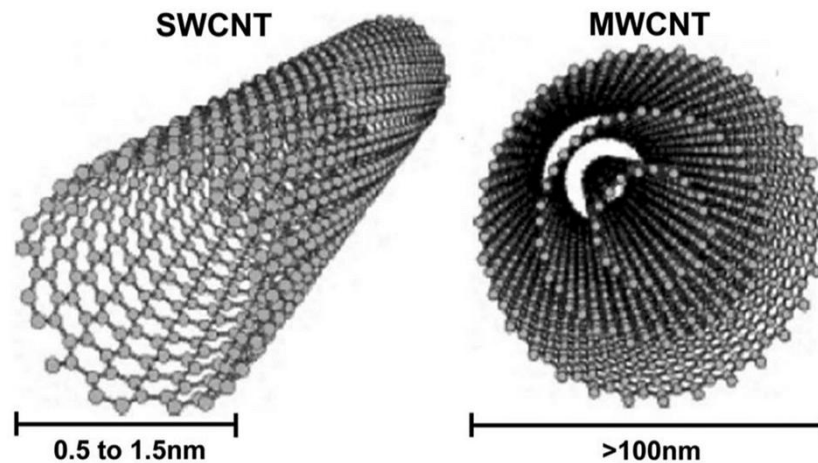


K.-W. Chae, Q. Zhang, J. Seog Kim, Y.-H. Jeong, G. Cao, *Beilstein J. Nanotechnol.* 1 (2010) 128–134.

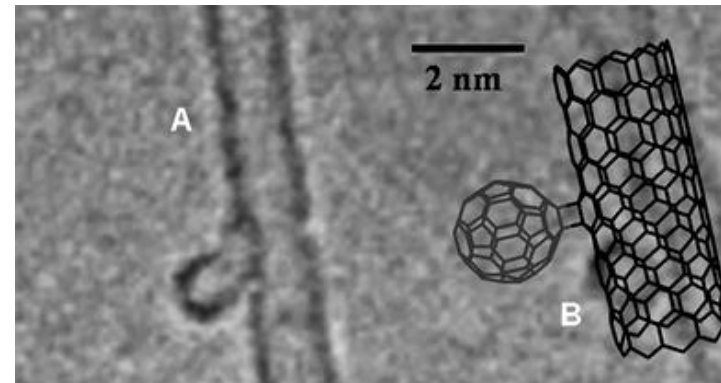


# Carbon Nanotubes (CNT) and Nanobuds (CNB)

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P.A. Martins-Júnior et al. Journal of Dental Research 2013;0022034513490957



A. G. Nasibulin, P. V. Pikhitsa, H. Jiang, D. P. Brown, A. V. Krashennnikov, A. S. Anisimov, P. Queipo, A. Moisala, D. Gonzalez, G. Lientschnig, A. Hassanien, S. D. Shandakov, G. Lolli, D. E. Resasco, M. Choi, D. Tomanek, E. I. Kauppinen, *Nat. Nanotechnol.*, 2 (2007), 156.

More in Lecture 4

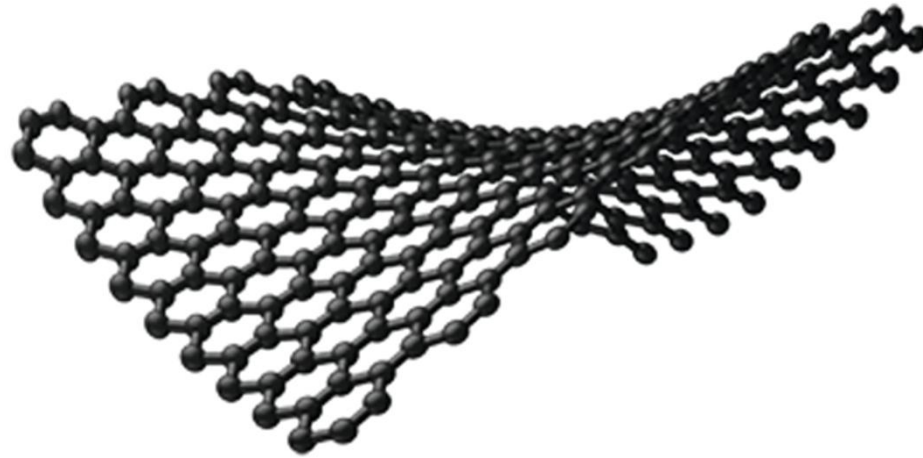
# 2D Nanomaterials

Sheets and foils

Arrays

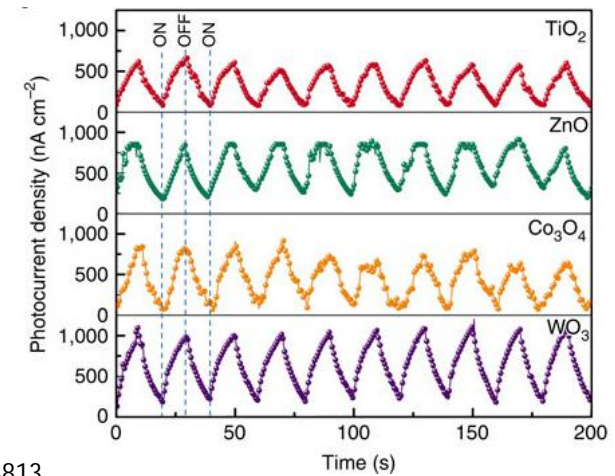
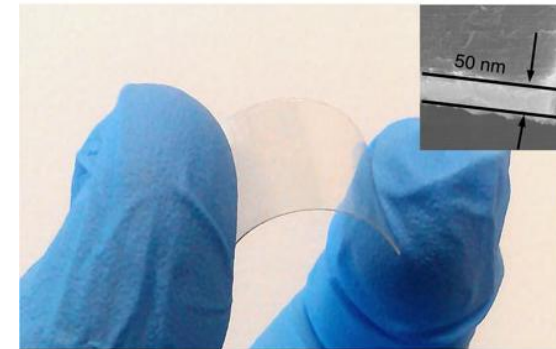
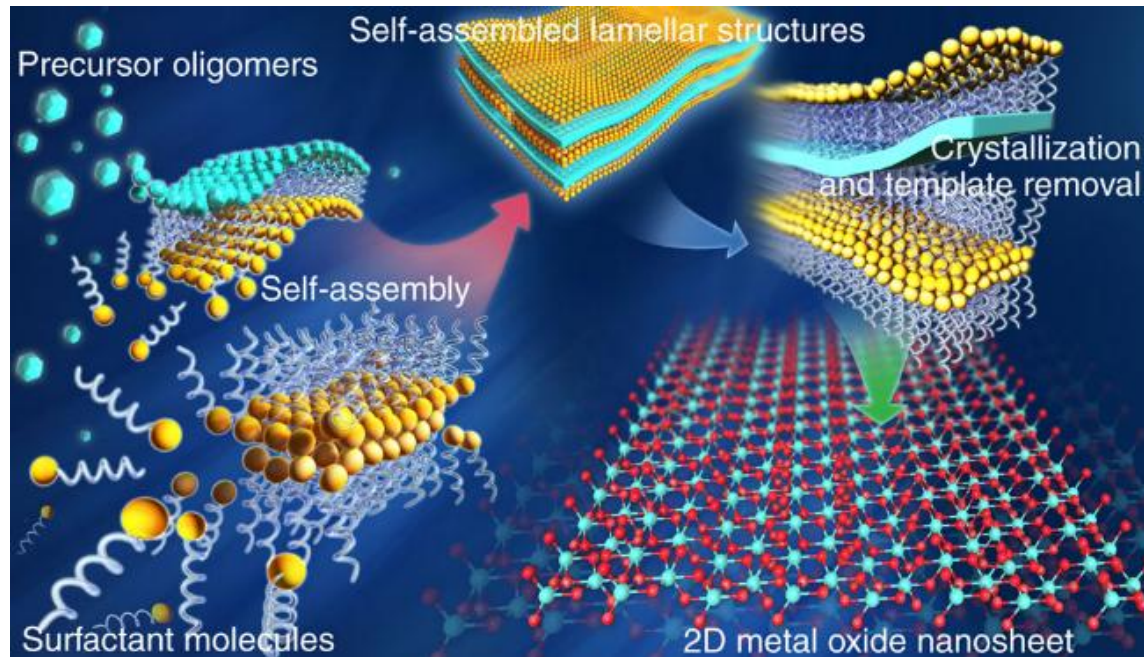
Nanoparticle

Example: Graphene



[http://graphene-flagship.eu/?page\\_id=34#.Vc3BWmO8pio](http://graphene-flagship.eu/?page_id=34#.Vc3BWmO8pio)

# Transition Metal 2D Sheets



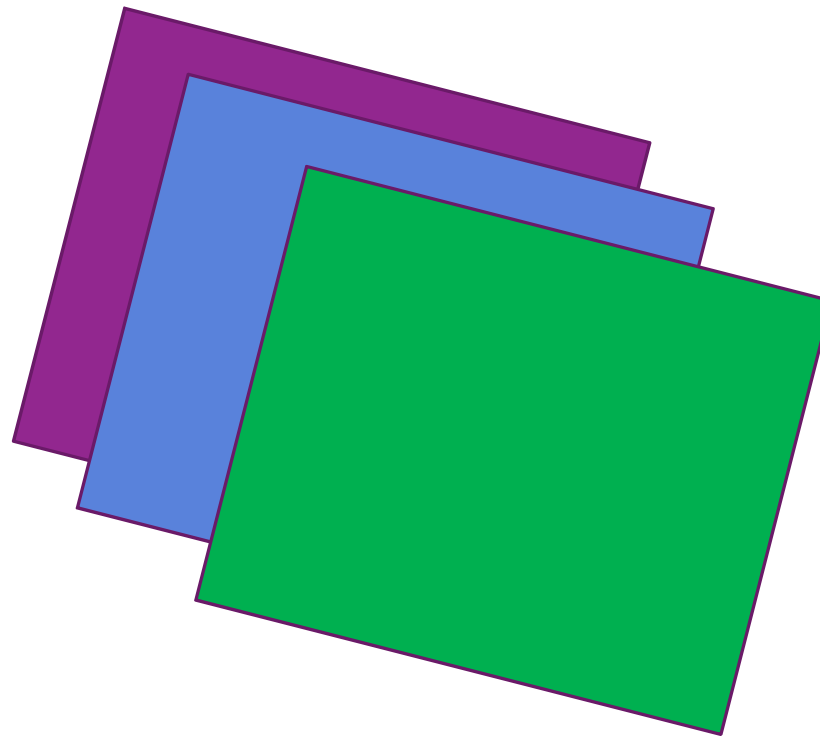
Z. Sun, T. Liao, Y. Dou, S. M. Hwang, M.-S. Park, L. Jiang, J. H. Kim, S. X. Dou, *Nature Comm.* 5 (2014) No. 3813

# 3D Nanomaterials

Composites

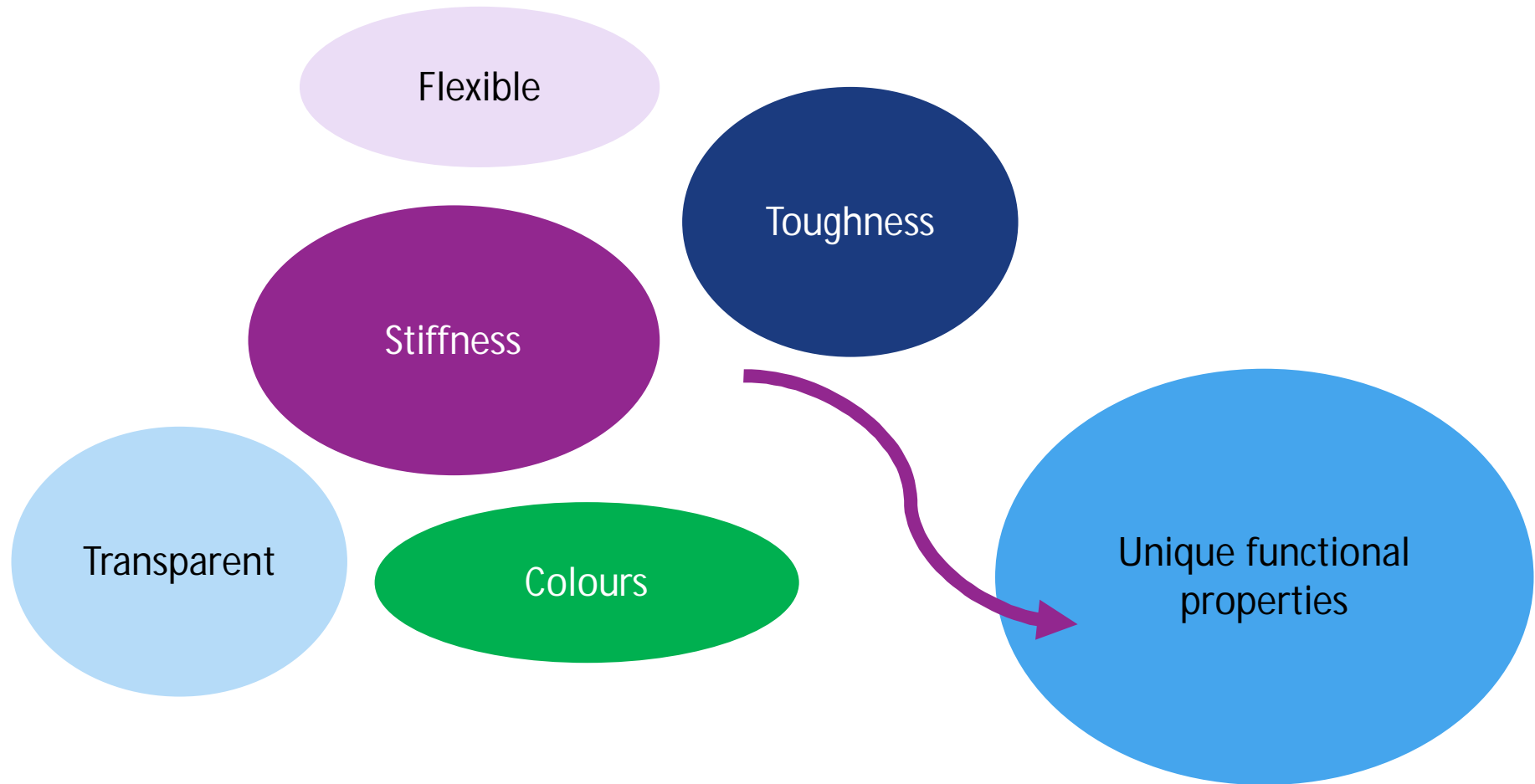
Films      Layer-by-Layer

Self-assembled capsules

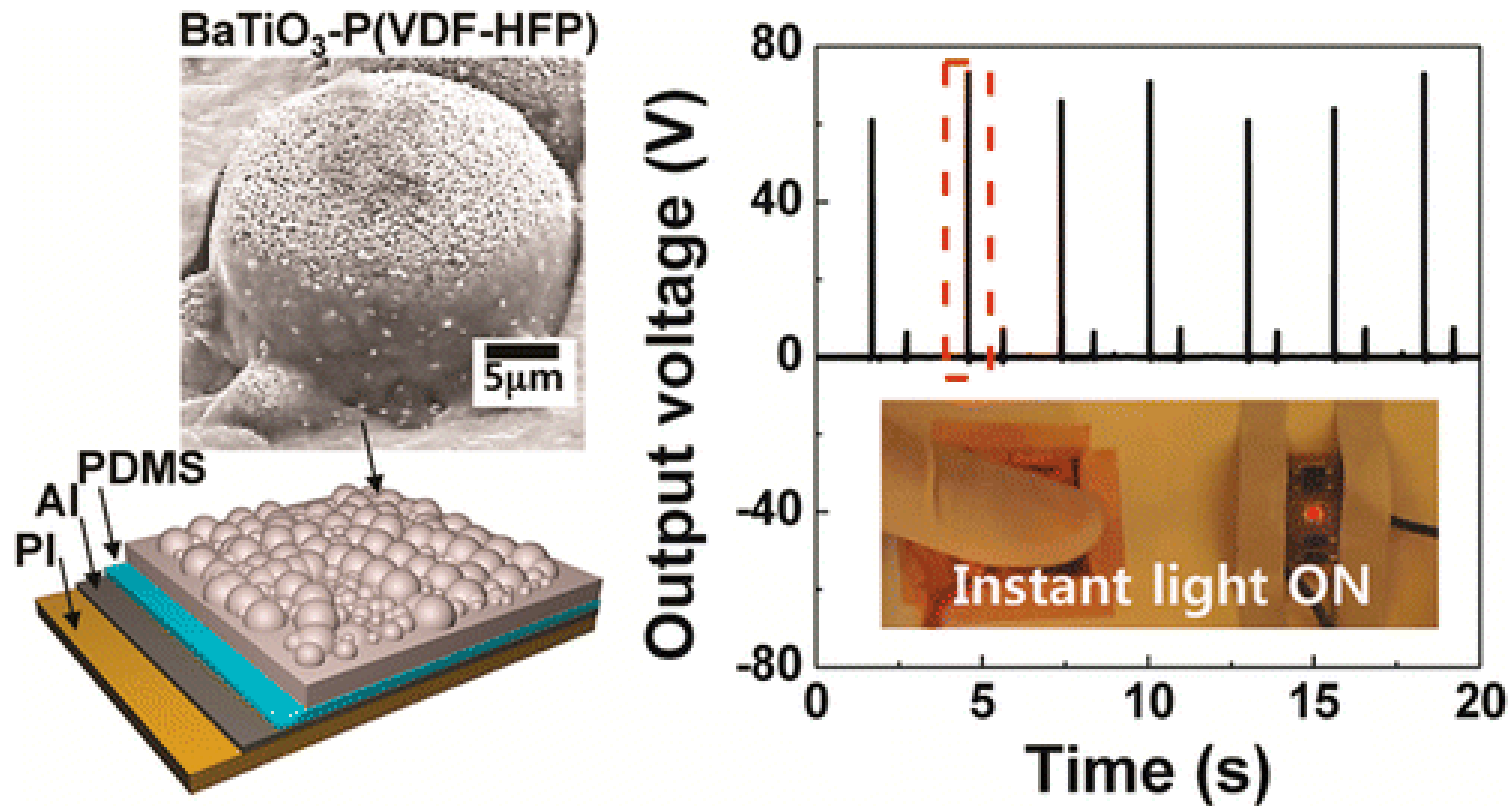


# 3D: Composites

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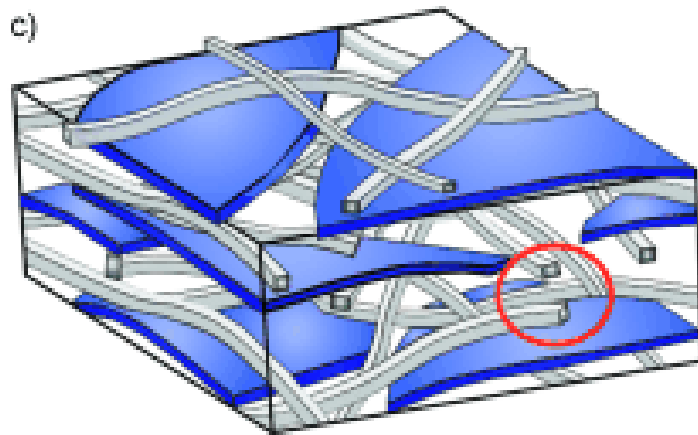


# Composites



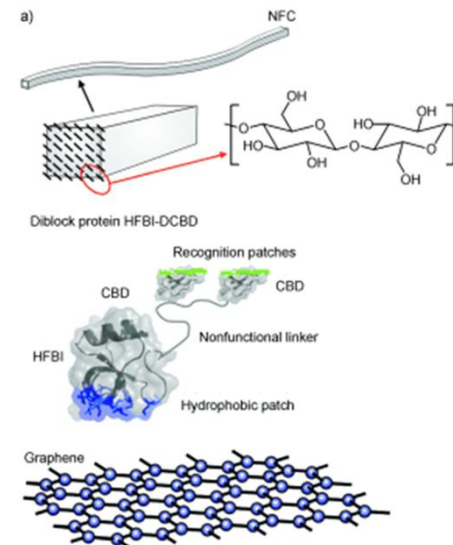
S.-H. Shin *et al.*, *ACS Nano* 8 (2014) 2766–2773.

# Biomimetic Composites



## Self-assembly

- § Combining natural and synthetic materials
- § Manipulating natural materials
  - § Fusion proteins
  - § Nanocellulose



Improving nanocellulose properties  
with graphene – binder = genetically  
engineered protein

*Young's modulus: 20.2 Gpa*

*Strength: 278 MPa*

*Strain-to-failure: 3.1%*

*Work-of-fracture 57.9 kJm<sup>-2</sup>*

# Reading Material

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## *Basic Concepts*

G. Cao, *Nanostructures and Nanomaterials – Synthesis, Properties and Applications*, 1<sup>st</sup> Ed. (2004)  
World Scientific, pp. 32-62. (electronic)

OR

G. Cao, Y. Wang, *Nanostructures and Nanomaterials – Synthesis, Properties and Applications*, 2<sup>nd</sup> Ed.  
(2013) World Scientific, pp. 38-75.

## *For Interested Reader: 0D-3D Materials*

G. Cao, *Nanostructures and Nanomaterials – Synthesis, Properties and Applications*, 1<sup>st</sup> Ed. (2004)  
World Scientific, pp. 32-205. (electronic)

OR

G. Cao, Y. Wang, *Nanostructures and Nanomaterials – Synthesis, Properties and Applications*, 2<sup>nd</sup> Ed.  
World Scientific, pp. 61-266. OR

M.F. Ashby, P.J. Ferreira, D.L. Shodek, *Nanomaterials, Nanotechnologies and Design – An Introduction to Engineers and Architects* (2009) Elsevier pp. 257-289



## MORE ABOUT THIS TOPIC

*CHEM-E4105 Nanochemistry &  
Nanoengineering*

3<sup>rd</sup> Period (January-February 2017)

Prof. Mady Elbahri (Mat. Sci. & Chemistry)



# Next Lecture

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## Self-Assembly

