

4) Normal or Gaussian Distribution.

$\mu = \text{median} = \text{mode}$

$$N(\mu, \sigma^2)$$

$\mu \in \mathbb{R} = \text{mean}$

$\sigma^2 \in \mathbb{R} > 0 = \text{variance}$

$x \in \mathbb{R}$

$$\text{pdf.} = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{x-\mu}{\sigma} \right)^2}$$

Mean = μ

Variance = σ^2 , S.D. = $\sqrt{\sigma^2} = \sigma$

Empirical Rule of Normal Distribution

$$P(\mu - \sigma \leq x \leq \mu + \sigma) \approx 68\%$$

$$P(\mu - 2\sigma \leq x \leq \mu + 2\sigma) \approx 95\%$$

$$P(\mu - 3\sigma \leq x \leq \mu + 3\sigma) \approx 99.7\%$$

e.g. ① Weight of the student in class

② IRIS dataset

2) Uniform Distribution

① Continuous uniform Distribution - (pdf.)

$$U(a, b) \quad -\infty < a < b < \infty$$

$$\text{pdf} = \begin{cases} \frac{1}{b-a} & \text{for } x \in [a, b] \\ 0 & \text{o.w.} \end{cases}$$

$$\text{cdf} = \begin{cases} 0 & \text{for } x < a \\ \frac{x-a}{b-a} & \text{for } x \in [a, b] \\ 1 & \text{for } x > b \end{cases}$$

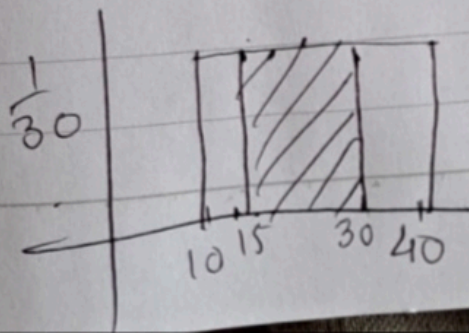
$$\text{mean} = \frac{1}{2}(a+b)$$

$$\text{median} = \frac{1}{2}(a+b)$$

$$\text{variance} = \frac{1}{12}(b-a)^2$$

e.g. The no. of candies sold at a shop is uniformly distributed with a maximum of 40 & min of 10.

i) What is the prob. of daily sales to fall betn 15 & 30.



$$P(15 \leq x \leq 30) = (x_2 - x_1) \times \frac{1}{b-a}$$

$$= \frac{15}{30} = 0.5$$

$$P(x \geq 20) = (40 - 20) \cdot \frac{1}{30}$$

$$= \frac{20}{30} = \frac{2}{3} =$$

1) Discrete Uniform Distribution -

eg) Rolling a dice

$$\{1, 2, 3, 4, 5, 6\}$$

$U(a, b)$ a, b with $b > a$

$$\text{pmf} = \frac{1}{n}$$

$$n = b - a + 1$$

$$\text{mean} = \frac{a+b}{2} = \text{median}$$