

1. Raindrops are falling at an average rate of 20 drops per square inch per minute. What would be a reasonable distribution to use for the number of raindrops hitting a particular region measuring 5 inches<sup>2</sup> in  $t$  minutes? Why? Using your chosen distribution, compute the probability that the region has no rain drops in a given 3 second time interval. A reasonable choice of distribution is P

- Considering time = 1 minute  
20 drops fall in 1 inch square.  
Therefore  $20 \times 5 = 100$  drops fall in 5-inch square.
- For time = 3 seconds
  - o  $x$  drops =  $100 \times (3/60) = 5$  drops per 3 seconds.

**Here we will use Poisson's Distribution for computing the Probability. Since the Poisson's distribution works well when there is some interval given.**

P = Poisson's Distributed

X = Is the event of rainfall happening

$$\begin{aligned} P(X=0) &= (e^{-\mu} * \mu^x) / x! \\ &= (e^{-5} * 1) / 1 \\ &= 0.0068 \end{aligned}$$

2. Let X be a random day of the week, coded so that Monday is 1, Tuesday is 2, etc. (so X takes values 1, 2..., 7, with equal probabilities). Let Y be the next day after X (again represented as an integer between 1 and 7). Do X and Y have the same distribution? What is P(X)

X	Y	P(X)	P(Y)
1	2	1/7	1/7
2	3	1/7	1/7
3	4	1/7	1/7
4	5	1/7	1/7
5	6	1/7	1/7
6	7	1/7	1/7
7	1	1/7	1/7

- X and Y have same probability distribution since all values have equal probability.
- $P(X) = 1/7$