

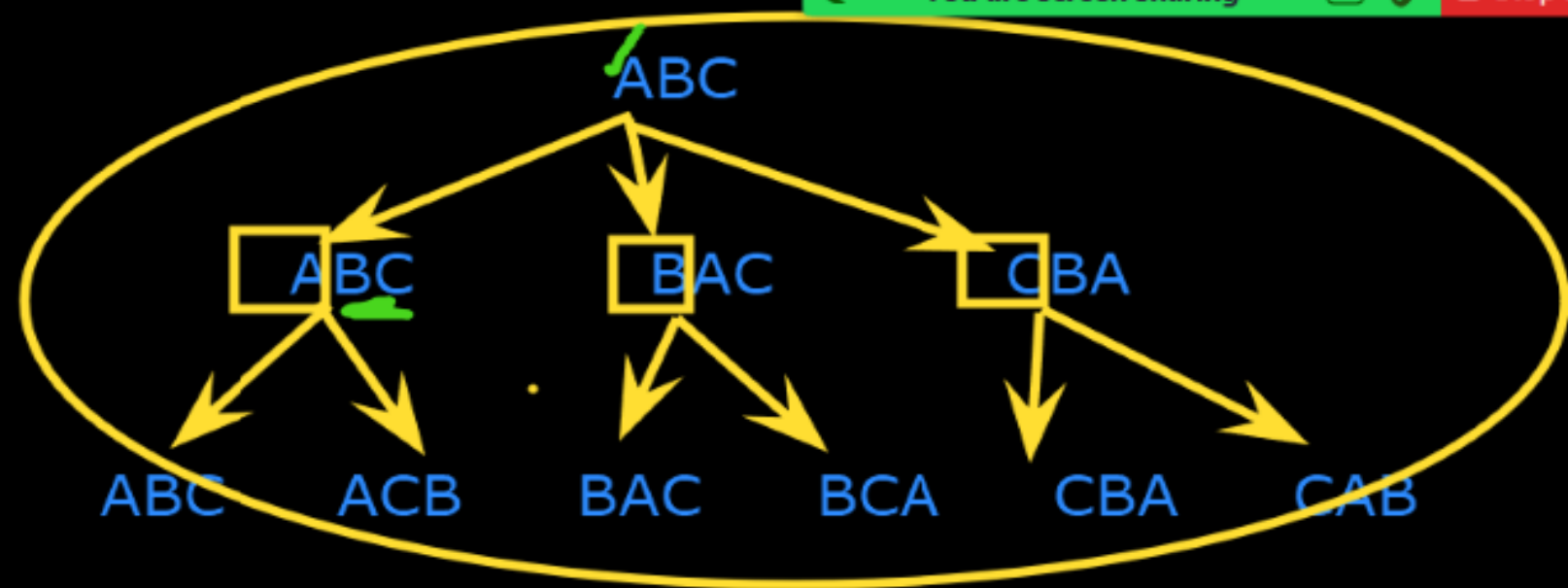


# DATA STRUCTURES AND ALGORITHMS

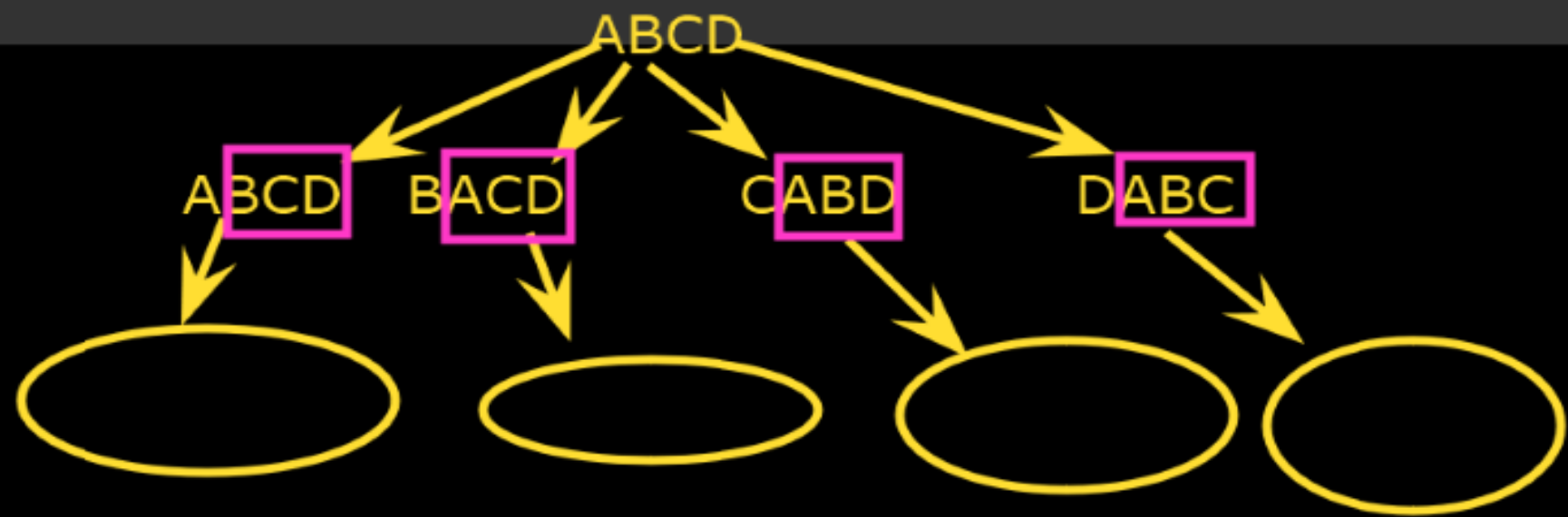
## Sep22 : Day 2

Kiran Waghmare  
CDAC Mumbai

AB  
BA  
-----ABC  
A(BC)  
ACB  
BAC  
BCA  
CAB  
CBA



-----  
ABCD  
A(B(C(D)))  
B(A(C(D)))  
C(A(B(D)))  
D(A(B(C)))



## Homework:

1. write a recursive program for reverse a string. (2/3 types)

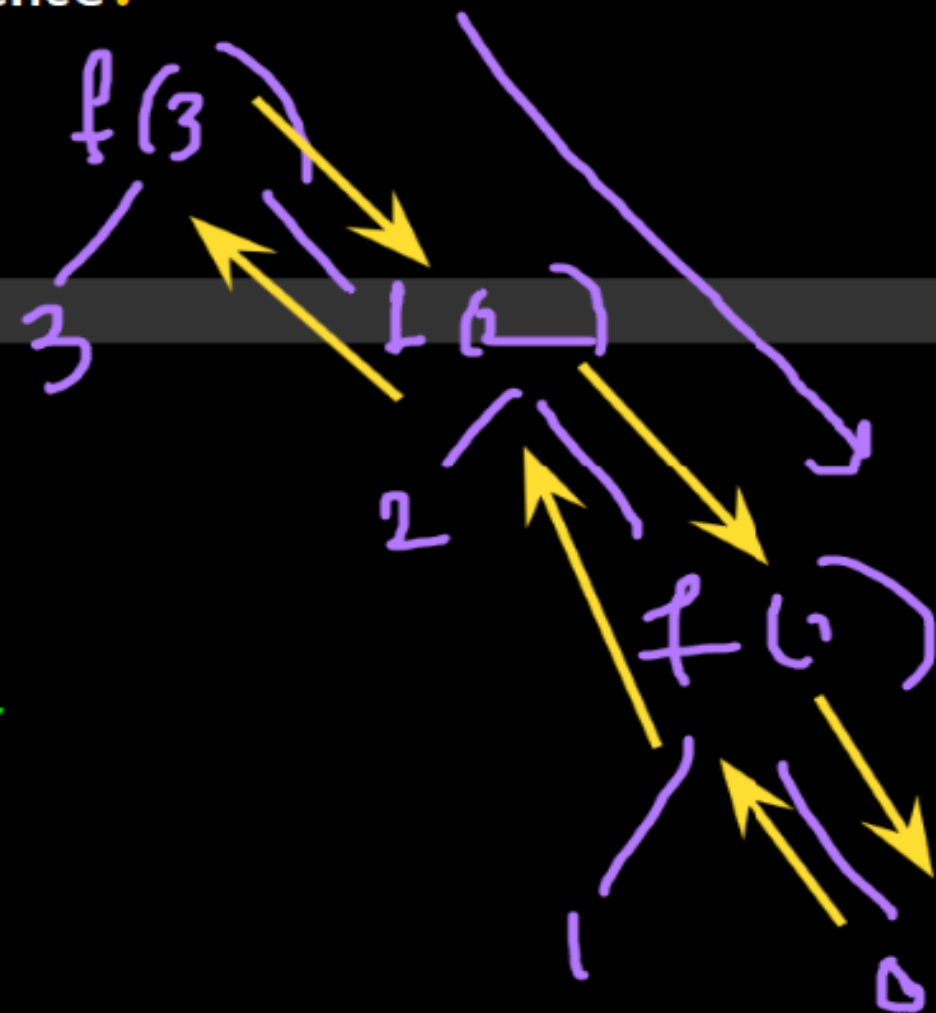
2. write a recursive program to reverse a sentence.

## Types of recursive:

### 1. Tail recursion:

```
void fun(int n)
{
    if(n>0)
        SOP(n);
    else
        fun(n-1); //recursive function call
}
```

### 2. Head recursion



## Homework:

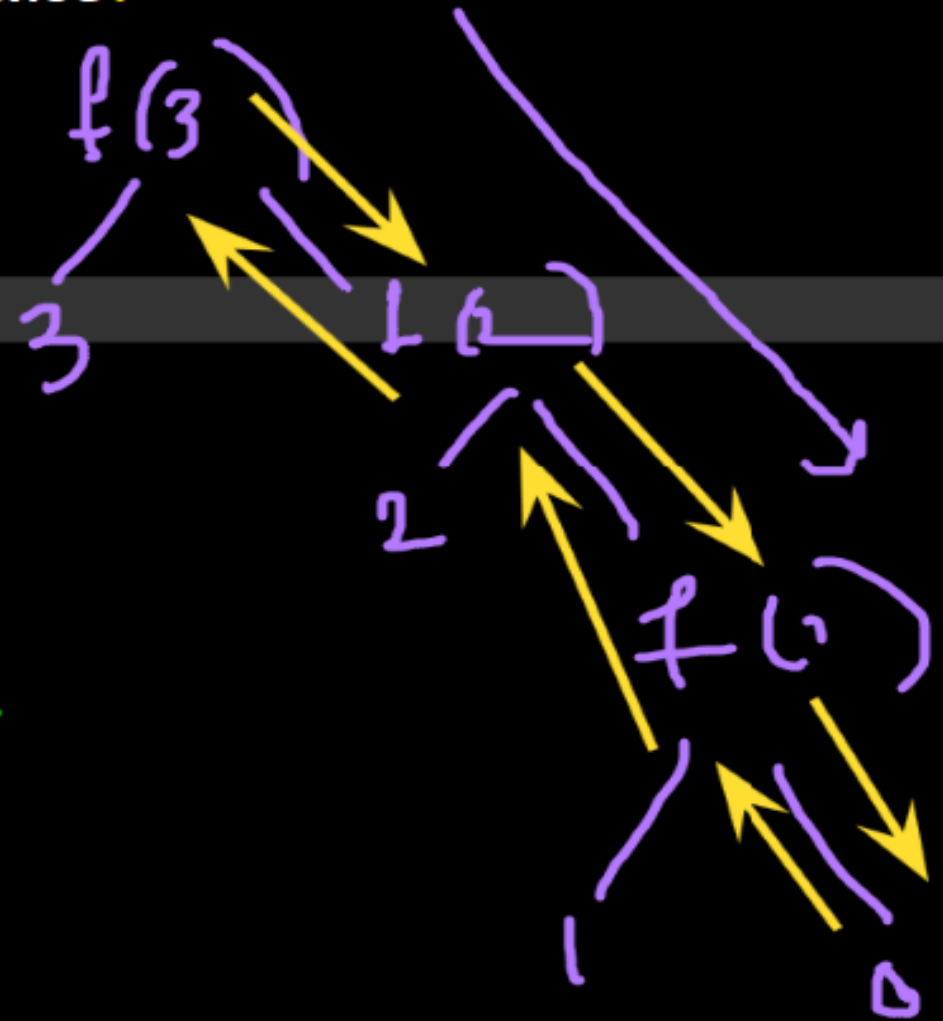
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2. write a recursive program to reverse a sentence.

## Types of recursive:

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# Head vs. Tail recursion

Note: base case is ALWAYS 1st



head(3) is: 2 3

void head(int n) <sup>3</sup>

```
{
    if(n == 1)
        return;
    else
        head(n-1); // ←
    printf("head - n=%i\n",n);
}
```

tail(3) is: 3 2 1

void tail(int n) <sup>3</sup>

```
{
    if(n == 0)
        return;
    else
        printf("tail - n=%i\n",n);
        tail(n-1); // ←
}
```

Handwritten notes for tail recursion: A red arrow points from the top right towards the tail function. To the right of the printf statement, the sequence "3 2 1" is written with a red underline. Below the tail(n-1) call, the sequence "2 1 0" is written vertically in red.

Recursive program to find the Sum of the series  $1 - 1/2 + 1/3 - 1/4 \dots 1/N$

Given a positive integer  $N$ , the task is to find the sum of the series  $1 - (1/2) + (1/3) - (1/4) + \dots (1/N)$  using recursion.

Examples:

Input:  $N = 3$

Output: 0.8333333333333333

Explanation:

$$1 - (1/2) + (1/3) = 0.8333333333333333$$

Input:  $N = 4$

Output: 0.5833333333333333

Explanation:

$$1 - (1/2) + (1/3) - (1/4) = 0.5833333333333333$$

## Recursive Program to print multiplication table of a number

Given a number N, the task is to print its multiplication table using recursion.

Examples

Input: N = 5

Output:

$$5 * 1 = 5$$

$$5 * 2 = 10$$

$$5 * 3 = 15$$

$$5 * 4 = 20$$

$$5 * 5 = 25$$

$$5 * 6 = 30$$

$$5 * 7 = 35$$

$$5 * 8 = 40$$

$$5 * 9 = 45$$

$$5 * 10 = 50$$

Input: N = 8

Output:

$$8 * 1 = 8$$

$$8 * 2 = 16$$

$$8 * 3 = 24$$

$$8 * 4 = 32$$

$$8 * 5 = 40$$

$$8 * 6 = 48$$

$$8 * 7 = 56$$

$$8 * 8 = 64$$

$$8 * 9 = 72$$

$$8 * 10 = 80$$



## Recursive program to print formula for GCD of n integers

Given a function `gcd(a, b)` to find GCD (Greatest Common Divisor) of two number. It is also known that GCD of three elements can be found by `gcd(a, gcd(b, c))`, similarly for four element it can find the GCD by `gcd(a, gcd(b, gcd(c, d)))`. Given a positive integer n. The task is to print the formula to find the GCD of n integer using given `gcd()` function.

Examples:

Input : n = 3

Output : `gcd(int, gcd(int, int))`

Input : n = 5

Output : `gcd(int, gcd(int, gcd(int, gcd(int, int))))`

GCD (4,6)=2

4=2\*2

6=2\*3

```
if(n==1)
return "int"
```

GCD(105,91)=

GCD(a,b)

if(a>b)

GCD(a%b,b)

else

GCD(a,b%a)

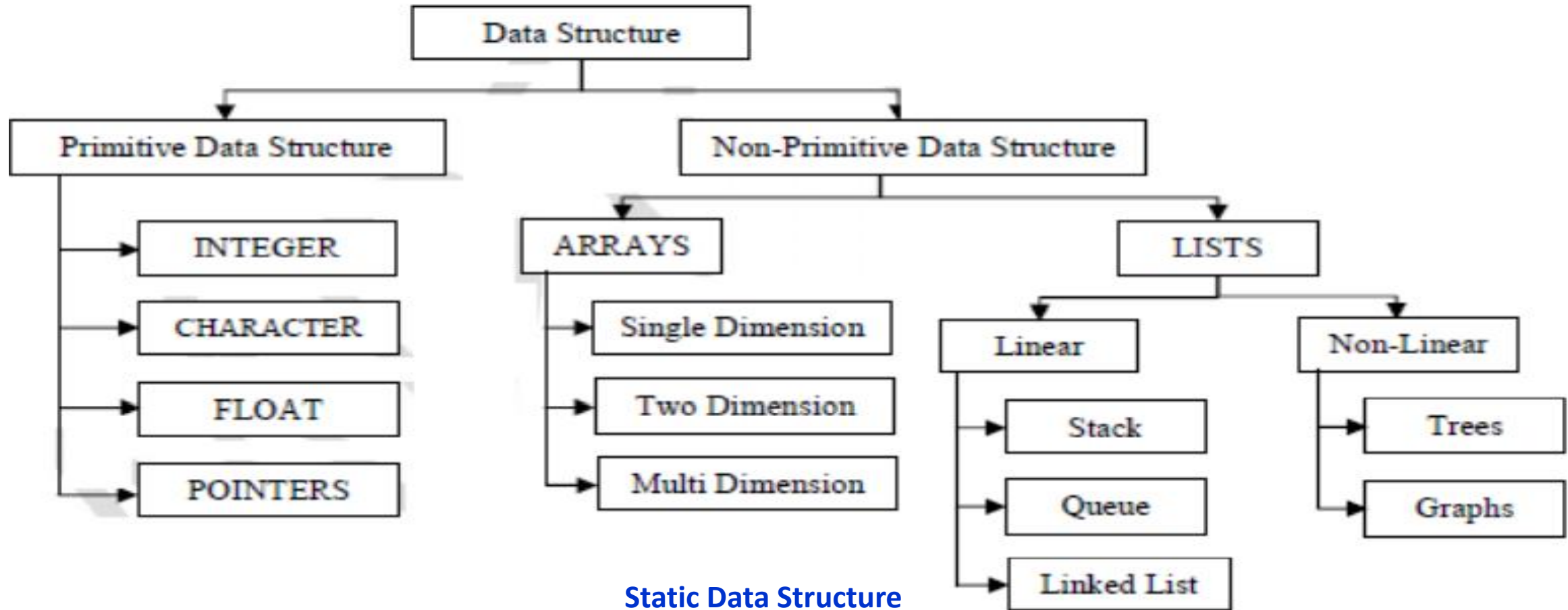


# **Algorithms & Data Structure**

## **Arrays**

**Kiran Waghmare**

# Classification of Data Structure



Static Data Structure

Dynamic data structure

```
SOP("hhjkjkd");  
SOP("hhjkjkd");
```

```
}
```

Linear & Non-linear:

Terminologies:

Linear: data are arranged in sequence.

Non-linear: data elements are not arranged in sequence.

Homogeneous: similar type of elements.

-primitive data type:

-int, float, byte, double, long

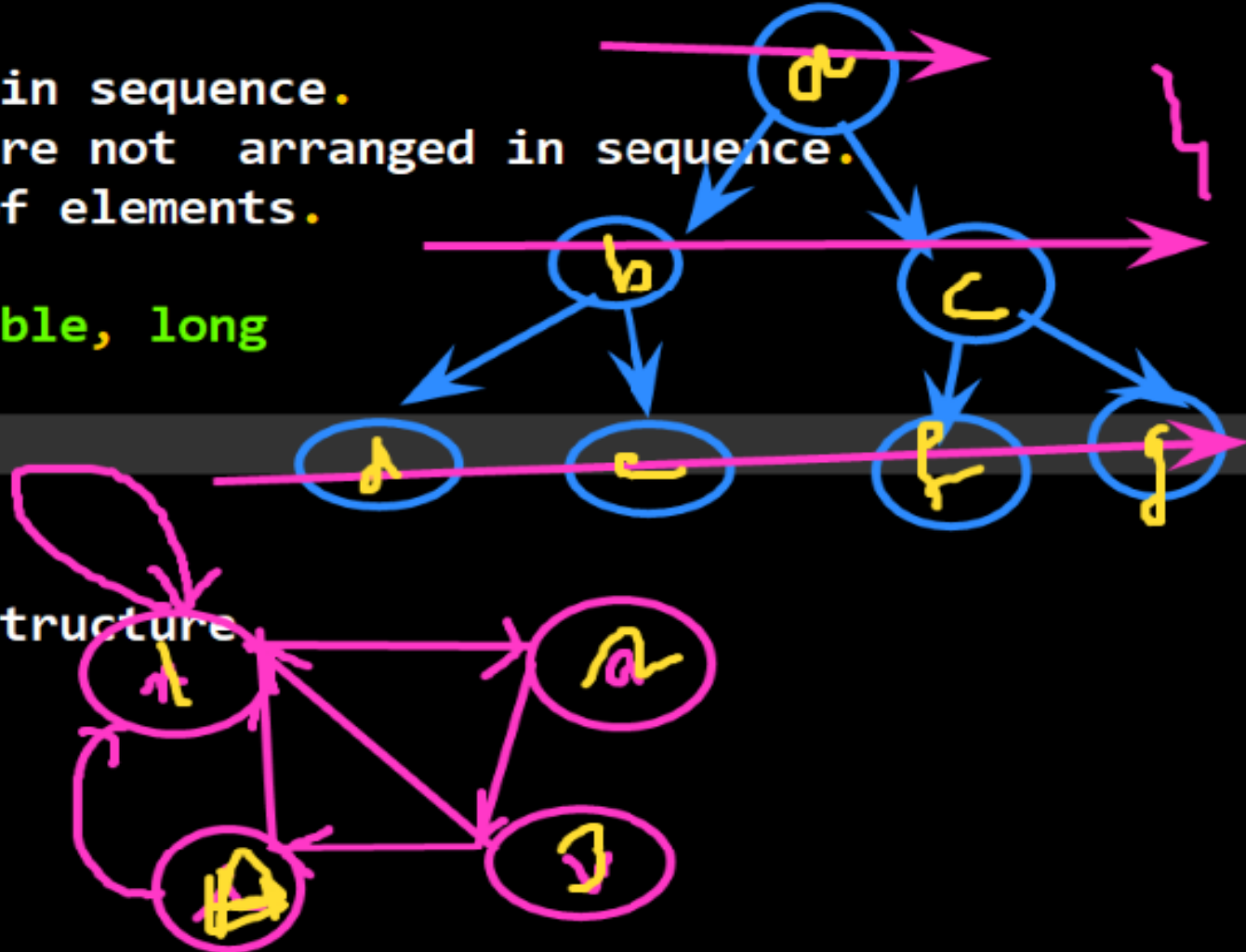
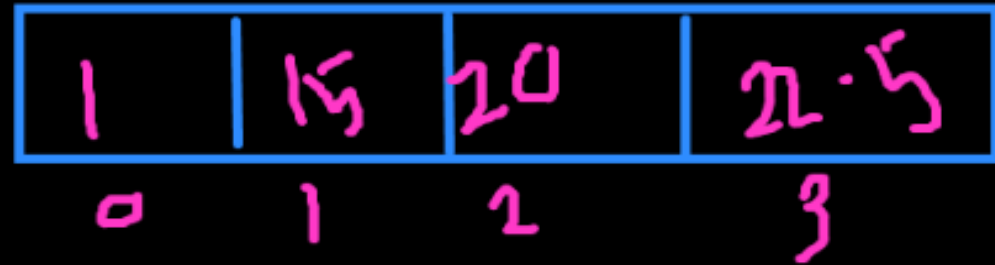
Non-homogeneous: Vector,

Static:

Dynamic:

Note: Data type and Data structure

Array:



## Array:

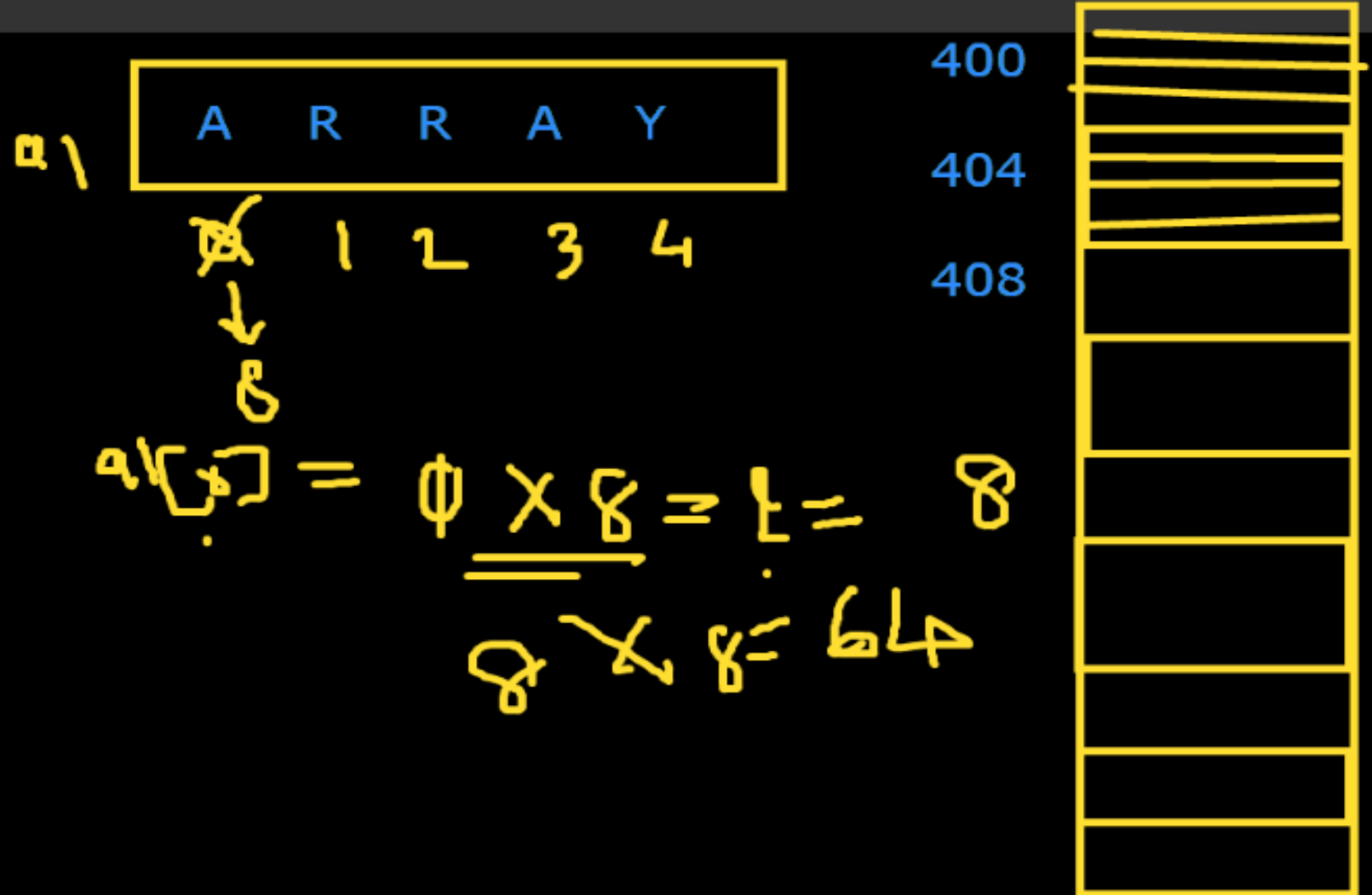
Array is a finite, ordered, and homogenous collection of elements.

Type of indexing:

0: zero-based indexing

1: one-based indexing

n: n-based indexing



## Array:

Array is an finite, ordered, and homogenous collection of elements.

Type of indexing:

0: zero-based indexing

1: one-based indexing

n: n-based indexing

```
int a1[5]={};
```

```
int a1[]={1,2,3,4}; //HW
```



$$O(1) + O(1) + O(1) + O(1) + O(1)$$

Operations:

Insert

Delete

Search

Display

$$O(\log n)$$

$$O(n^3)$$

$$O(n)$$

Linear

$$O(5)$$

constant

$$O(n^2)$$

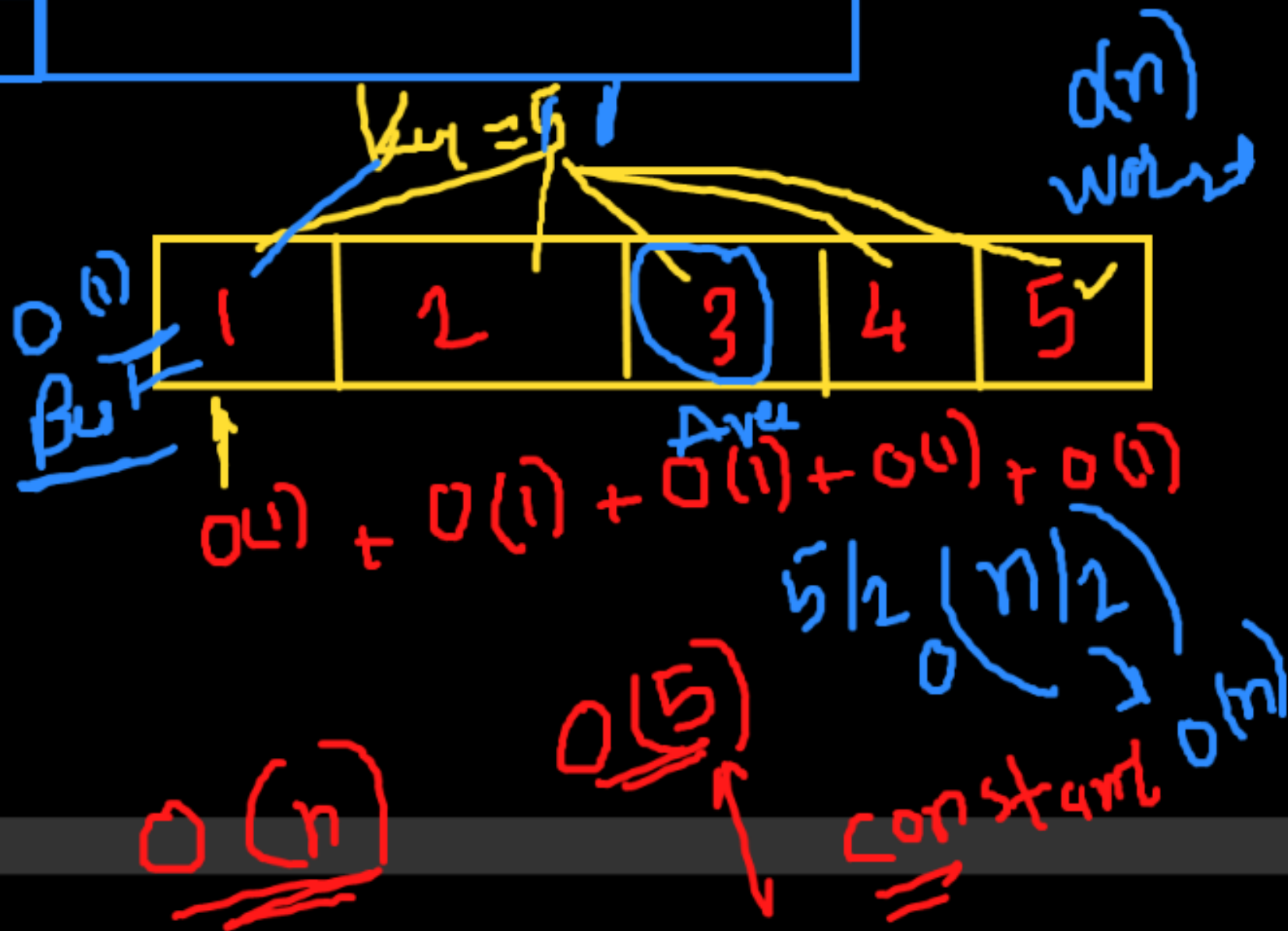

- single element:  $O(1)$
- n elements:  $O(n)$

- single element:  $O(1)$
- n elements:  $O(n)$

- n elements:  $O(n)$
- Best case:  $O(1)$
- Average case:  $O(n)$
- Worst case:  $O(n)$

-0(1)

## Display



# Concept of array





## Size of Array:

$$\begin{aligned}\text{Size}(A) &= U - L + 1 \\ &= 4 - 0 + 1 \\ &= 5\end{aligned}$$

$$\begin{aligned}U &= 365 \\ L &= 211\end{aligned}$$

## Address of Array:

### 1-D:

$$\begin{aligned}A[i] &= M + (i - L) * w \\ M &= 100, i = 2, \text{int} \\ A[2] &= 100 + (2 - 0) * 2 \\ &= 104\end{aligned}$$

### 2-D:

ARRAY

0 1 2 3 4

Logical View

Lower bound

1000

$$A[i] = M + (i - L) * w$$

MMU

Mapping function

Upper bound

2500

Physical view

M

A 3x4 grid of cells labeled  $a_{11}$  through  $a_{34}$ . The cell  $a_{34}$  is highlighted in light blue. Blue arrows indicate movement between adjacent cells (horizontally, vertically, and diagonally). Yellow arrows indicate movement between cells that are two steps apart (horizontally, vertically, and diagonally). A large yellow arrow at the bottom points to the right, and a large blue arrow on the right points upwards.

## Row Major

Column Major

Address of Array:

Kiran Wagh...

1-D:

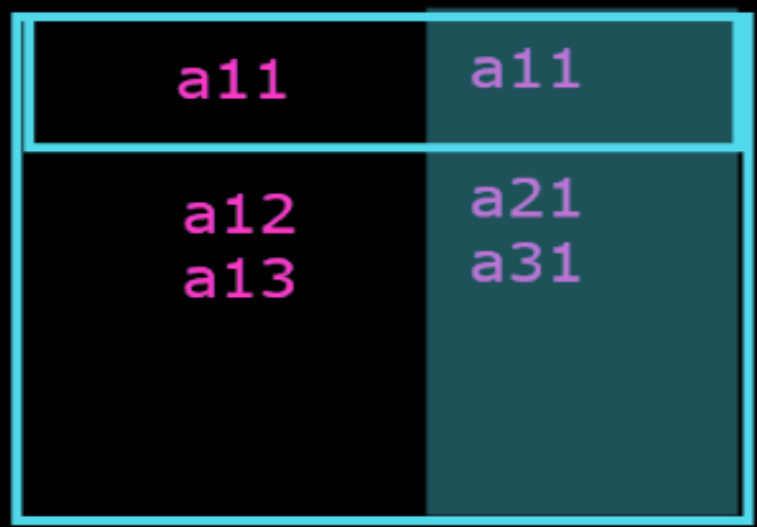
$A[i] = M + (i - L) * w$   
 $M = 100, i = 2, \text{int}$   
 $A[2] = 100 + (2 - 0) * 2$   
 $= 104$



2-D:

Row major Order:

$\text{Address}[a_{ij}] = M + (i - 1) * n + j - 1$   
 $M = 100$   
 $a_{13} = 100 + (1 - 1) * 4 + 3 - 1$   
 $= 102$



Column major Order:

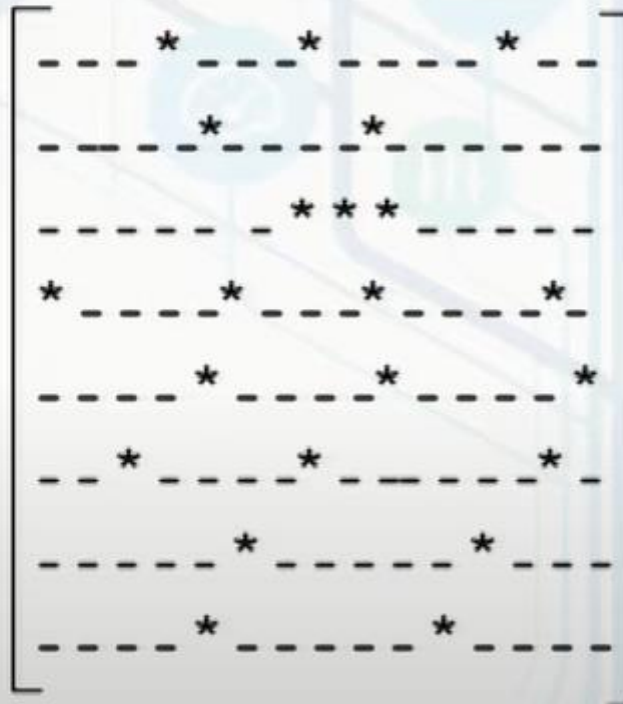
$\text{Address}[a_{ij}] = M + (j - 1) * m + i - 1$   
 $a_{13} = 100 + (3 - 1) * 3 + 1 - 1$

a13

# Sparse matrix

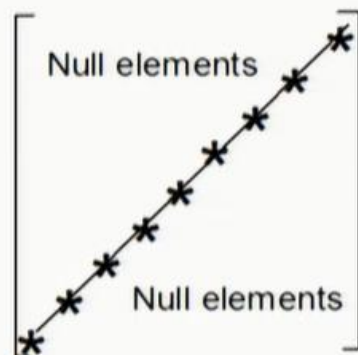
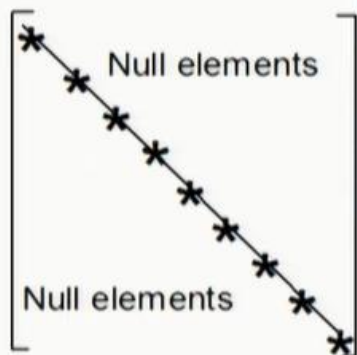
Watch I

A *sparse* matrix is a two-dimensional array having the value of majority elements as null

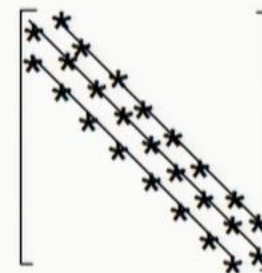
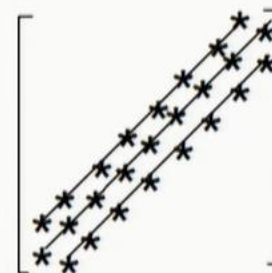


	*		*		*
		*		*	
			*	*	*
*		*		*	*
	*		*		*
	*		*		*
		*		*	
	*		*		

## Diagonal sparse matrices



## Tri-diagonal sparse matrices



# Program

HighArray
public HighArray()//Constructor
public boolean find (int key) public void insert(int value) public boolean delete(int long) public void display()

HighArrayApp
main() create object
insert()// all elements
display() find() delete()