



Data Structure

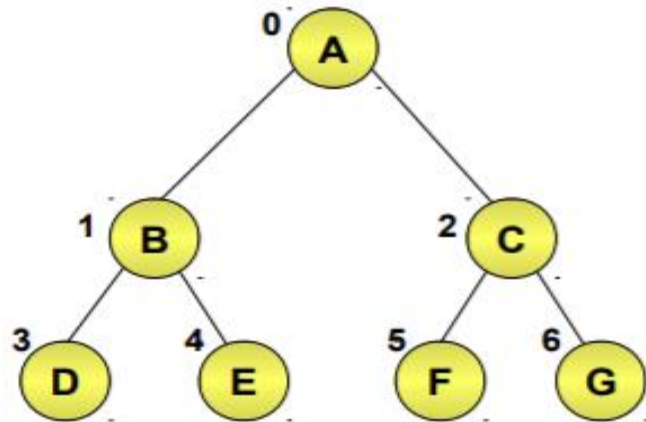
Sep23 : Day 6

Kiran Waghmare
CDAC Mumbai

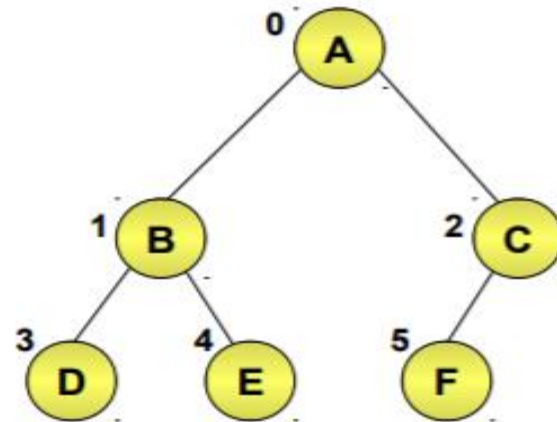
Defining Binary Trees (Contd.)

◆ Complete binary tree:

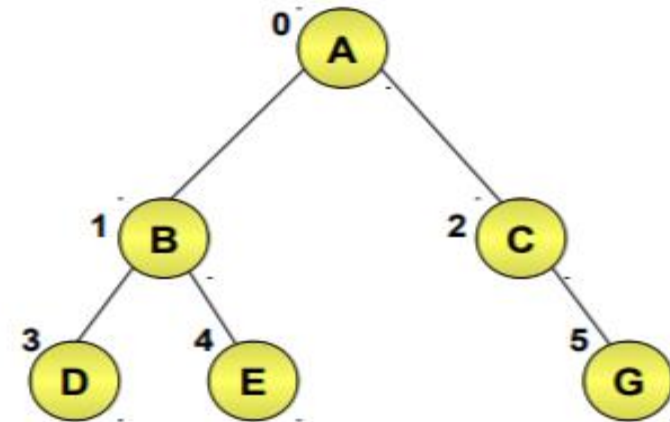
- ◆ A binary tree with n nodes and depth d whose nodes correspond to the nodes numbered from 0 to $n - 1$ in the full binary tree of depth k .



Full Binary Tree



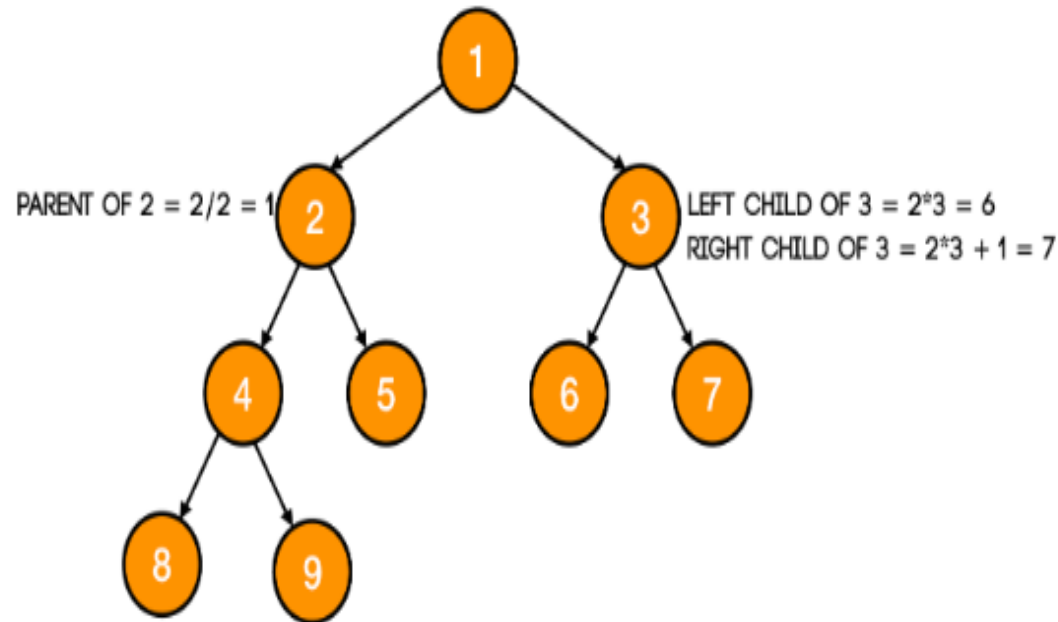
Complete Binary Tree



Incomplete Binary Tree

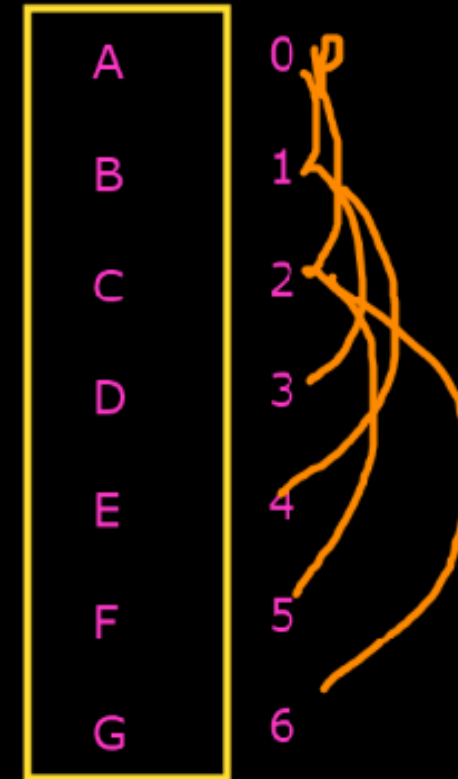
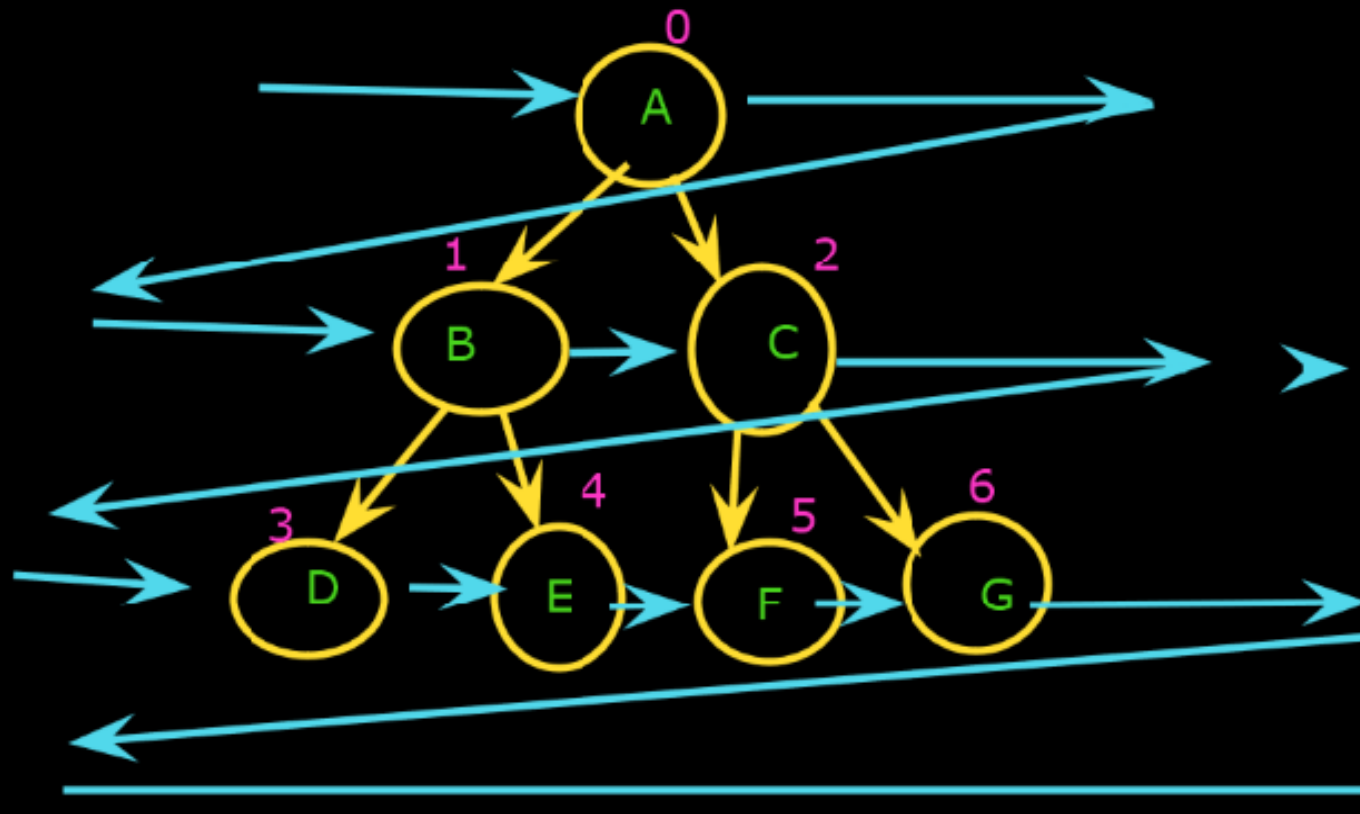
A complete binary tree also holds some important properties. So, let's look at them.

- The **parent of node i** is $\lfloor \frac{i}{2} \rfloor$. For example, the parent of node 4 is 2 and the parent of node 5 is also 2.
- The **left child of node i** is $2i$.
- The **right child of node i** is $2i + 1$



Binary Tree:

A binary tree is a tree in which every node has at most two children.
0,1,2,2



Array Representation of Binary Tree

OPERATIONS ON TREES

Traversing a Binary Tree

1) TRAVERSING

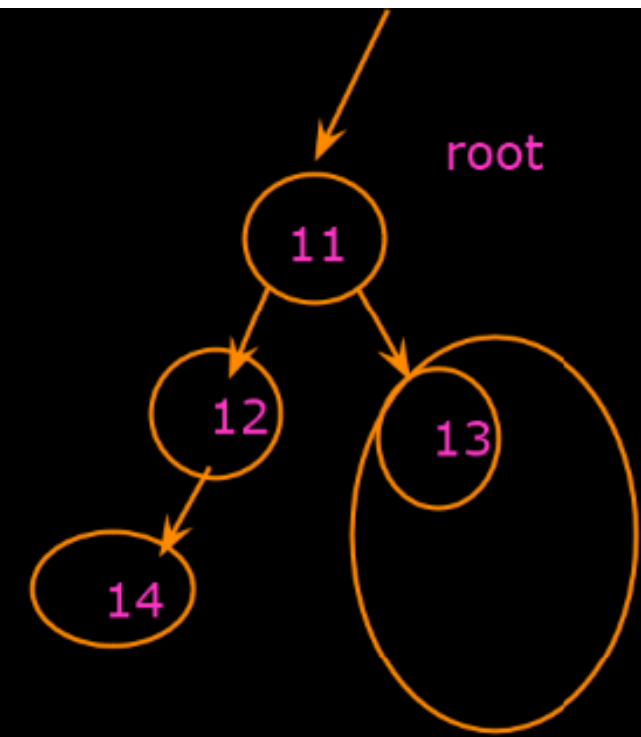
- ◆ You can implement various operations on a binary tree.
- ◆ A common operation on a binary tree is traversal.
- ◆ Traversal refers to the process of visiting all the nodes of a binary tree once.
- ◆ There are three ways for traversing a binary tree:
 - ◆ Inorder traversal
 - ◆ Preorder traversal
 - ◆ Postorder traversal

```
System.out.println(root.data + " ");  
printInorder(root.right);  
  
}
```

```
void printPreorder(Node root)
```

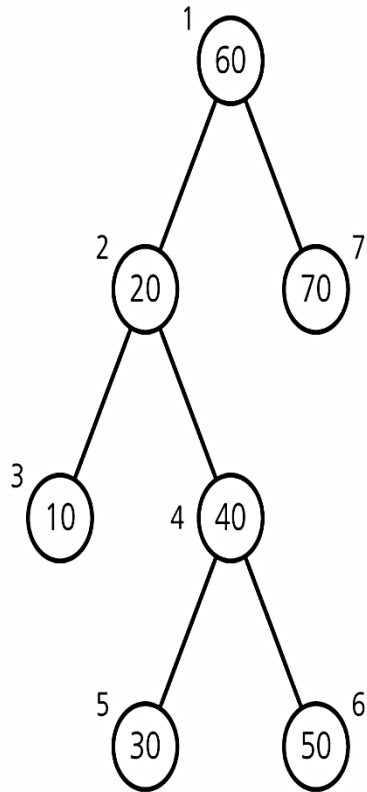
```
{  
    if(root == null)  
        return;
```

```
    System.out.println(root.data + " ");  
    printPreorder(root.left);  
    printPreorder(root.right);  
}
```

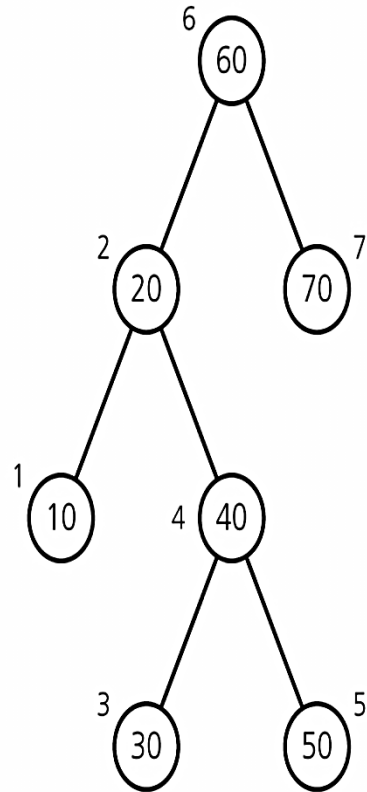


```
void printPostorder(Node root)  
{  
    if(root == null)  
        return;
```

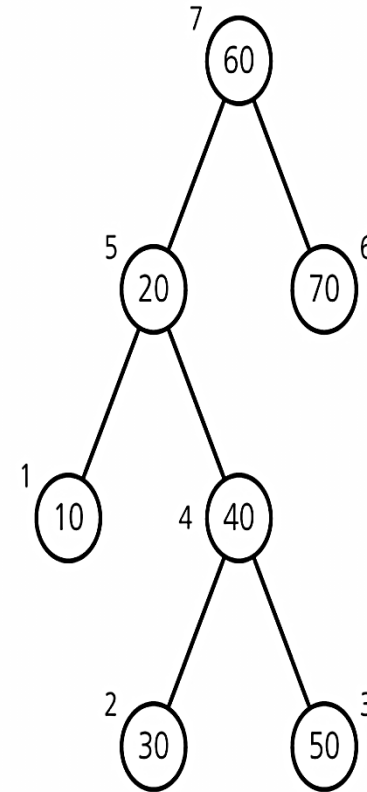

Binary Tree Traversals



(a) Preorder: 60, 20, 10, 40, 30, 50, 70



(b) Inorder: 10, 20, 30, 40, 50, 60, 70



(c) Postorder: 10, 30, 50, 40, 20, 70, 60

(Numbers beside nodes indicate traversal order.)

InOrder(root) visits nodes in the following order:

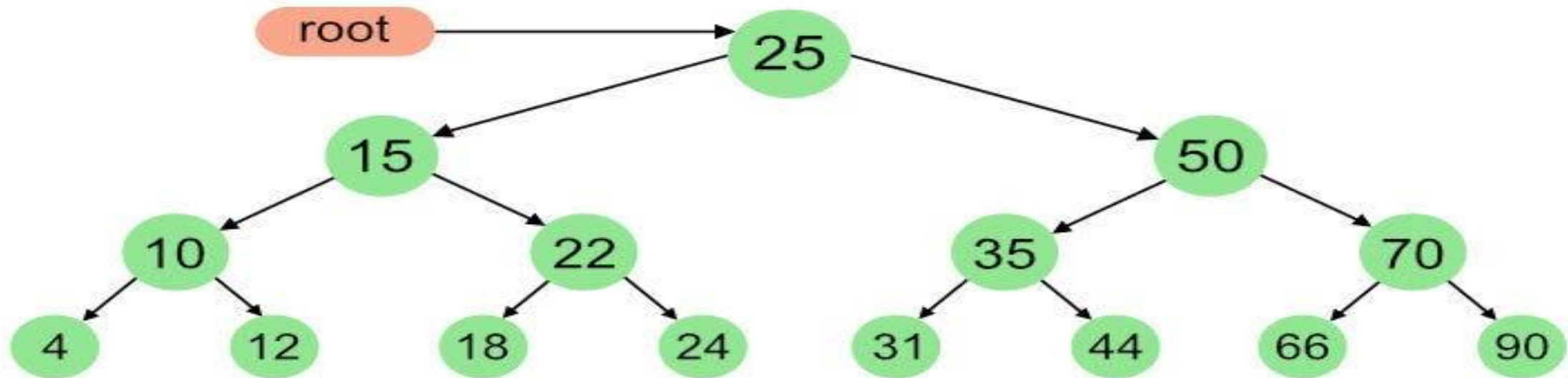
4, 10, 12, 15, 18, 22, 24, 25, 31, 35, 44, 50, 66, 70, 90

A Pre-order traversal visits nodes in the following order:

25, 15, 10, 4, 12, 22, 18, 24, 50, 35, 31, 44, 70, 66, 90

A Post-order traversal visits nodes in the following order:

4, 12, 10, 18, 24, 22, 15, 31, 44, 35, 66, 90, 70, 50, 25




```
class BT1{
```

```
Node root;
```

```
static class Node{
```

```
int data;
```

```
Node left, right;
```

```
Node(int d)
```

```
{
```

```
    data = d;
```

```
    left = right = null;
```

```
}
```

```
}
```

```
BT1()
```

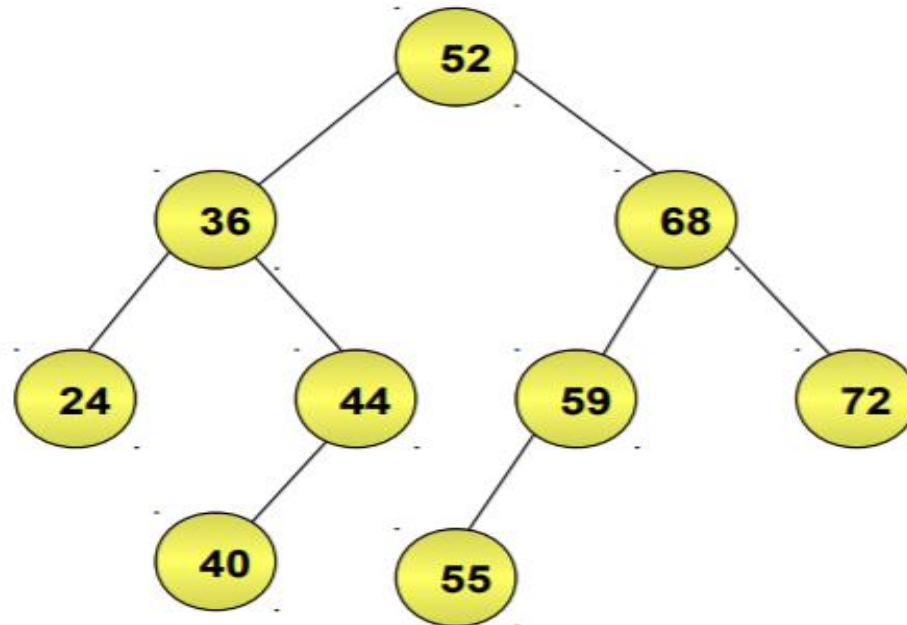
```
{
```

```
    root = null;
```

```
}
```

Binary Search Tree

- ◆ Binary search tree is a binary tree in which every node satisfies the following conditions:
 - ◆ All values in the left subtree of a node are less than the value of the node.
 - ◆ All values in the right subtree of a node are greater than the value of the node.
- ◆ The following is an example of a binary search tree.



Operations on a Binary Search Tree

- The following operations are performed on a binary search tree...
 - Search
 - Insertion
 - Deletion
 - Traversal

Insertion of a key in a BST

Algorithm:- InsertBST (info, left, right, root, key, LOC)

```
{
    key is the value to be inserted.
    1. call SearchBST ( info, left, right, root, key, LOC , PAR )    // Find the parent of the new node
    2. If ( LOC != NULL)
        2.1 Print “ Node already exist”
        2.2 Exit
    3. create a node [ new1 = ( struct node*) malloc ( sizeof( struct node) ) ]
    4. new1 -> info = key
    5. new1 -> left = NULL , new1 -> right = NULL
    6. If ( PAR = NULL ) Then
        6.1 root = new1
        6.2 exit
        elseif ( new1 -> info < PAR -> info)
        6.1 PAR -> left = new1
        6.2 exit
        else
        6.1 PAR -> right = new1
        6.2 exit
}
```

```
System.out.println  
System.out.println  
t1.Postorder();
```

```
//case 1: Deletion  
t1.delete(9);  
System.out.println  
System.out.println  
t1.Inorder();
```

```
//case 2: Deletion  
t1.delete(5);  
System.out.println  
System.out.println  
t1.Inorder();
```

```
//case 3: Deletion  
t1.delete(25);  
System.out.println  
System.out.println("Inorder");  
t1.Inorder();
```

Microsoft Windows [Version 10.0.22621.2134]
(c) Microsoft Corporation. All rights reserved.

```
D:\Test>javac BST.java
```

```
D:\Test>java BST
```

```
Inorder  
10 20 25 30
```

```
Preorder  
10 20 30 25
```

```
Postorder  
25 30 20 10
```

```
D:\Test>javac BST.java
```

```
D:\Test>java BST
```

```
Inorder  
2 5 8 9 10 22 25 42
```

```
Preorder  
10 8 5 2 9 25 22 42
```

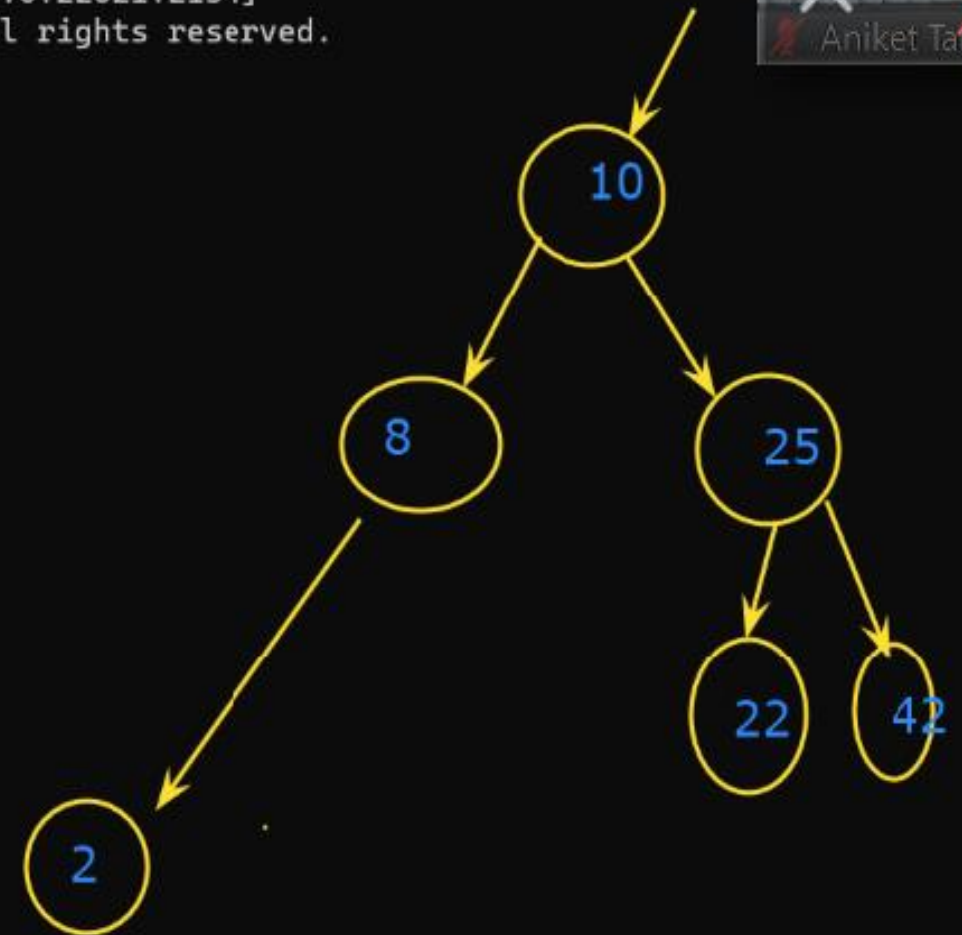
```
Postorder  
2 5 9 8 22 42 25 10
```

```
Inorder  
2 5 8 10 22 25 42
```

```
Inorder  
2 8 10 22 25 42
```

```
Inorder  
2 8 10 22 42
```

```
D:\Test>
```



//case 3

```
root.data = minvalue(root.right);
```

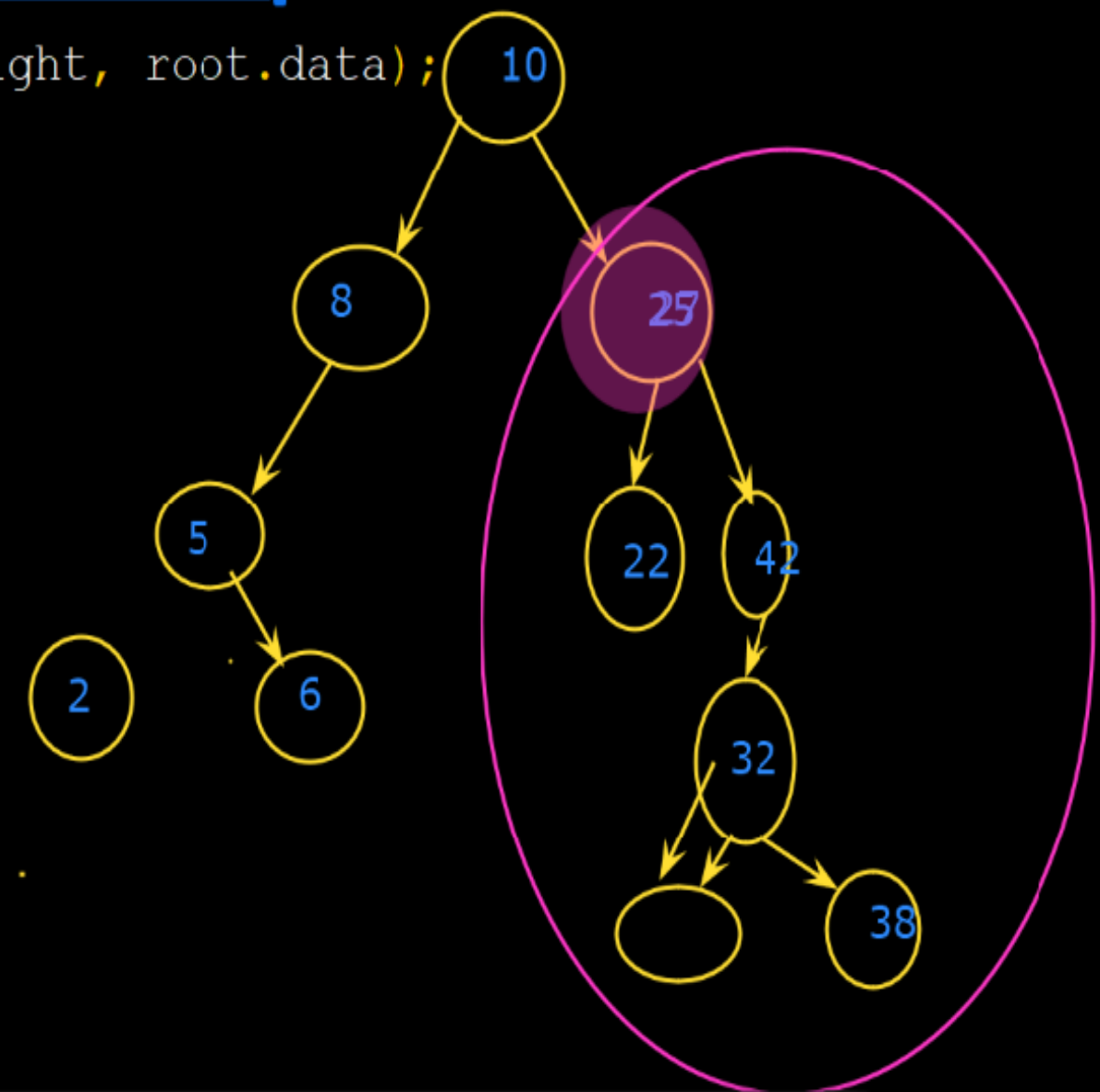
Kiran Waghmare

```
root.right = deletedata(root.right, root.data);
```

```
}  
return root;
```

```
int minvalue(Node root)  
{  
    int x = root.data;  
    while(root.left != null)  
    {  
        x = root.left.data;  
        root = root.left;  
    }  
    return x;  
}
```

```
void delete(int key)
```



Deleting Nodes from a Binary Search Tree

- ◆ Write an algorithm to locate the position of the node to be deleted from a binary search tree.
- ◆ Delete operation in a binary search tree refers to the process of deleting the specified node from the tree.
- ◆ Before implementing a delete operation, you first need to locate the position of the node to be deleted and its parent.
- ◆ To locate the position of the node to be deleted and its parent, you need to implement a search operation.

Deleting Nodes from a Binary Search Tree (Contd.)

- ◆ Once the nodes are located, there can be three cases:
 - ◆ **Case I:** Node to be deleted is the leaf node
 - ◆ **Case II:** Node to be deleted has one child (left or right)
 - ◆ **Case III:** Node to be deleted has two children

Deletion of a key from a BST

Algorithm:- Delete1BST (info, left, right, root, LOC, PAR)

// When leaf node has no child or only one child

{

1. if ((LOC -> left = NULL) and (LOC -> right = NULL))

1.1 Child = NULL

elseif (LOC -> left != NULL)

1.1 Child = LOC -> left

else

1.1 Child = LOC -> right

2. if (PAR != NULL)

2.1 if (LOC = PAR -> left)

2.1.1 PAR -> left = Child

2.1 else

2.1.1 PAR -> right = Child

else

2.1 root = Child

}

Deletion of a key from a BST

Algorithm:- Delete2BST (info, left, right, root, LOC, PAR)

// When leaf node has both child

```
{
  1. ptr1 = LOC
  2. ptr2 = LOC -> right
  3. While ( ptr2 -> left != NULL )
      3.1 ptr1 = ptr2
      3.2 ptr2 = ptr2 -> left
  4. call Delete1BST (info, left, right, root, ptr2, ptr1)
  5. If ( PAR != NULL)
      5.1 If LOC = PAR -> left
          5.1.1 PAR -> left = ptr2
      5.1 else
          5.1.1 PAR -> right = ptr2
      else
          5.1 root = ptr2
  6. ptr2 -> left = LOC -> left
  7. ptr2 -> right = LOC -> right
}
```

Deletion of a key from a BST

Algorithm:- DeleteBST (info, left, right, root, key)

```
{
key is the value to be deleted.
  1. call SearchBST ( info, left, right, root, key, LOC, PAR )
    // To find the location LOC and parent PAR of the
    node to be deleted.
  2. If ( LOC = NULL ) Then
    2.1 Print “ Node does not exist”
    2.2 exit
  3. if ( ( LOC -> left != NULL) and ( LOC -> right != NULL))
    // when the node to be deleted has both child
    3.1 call Delete2BST (info, left, right, root, LOC, PAR)
  else
    3.1 call Delete1BST (info, left, right, root, LOC, PAR)
}
```

```
private boolean search(BSTNode r, int val)
{
    boolean found = false;
    while ((r != null) && !found)
    {
        int rval = r.getData();
        if (val < rval)
            r = r.getLeft();
        else if (val > rval)
            r = r.getRight();
        else
        {
            found = true;
            break;
        }
        found = search(r, val);
    }
    return found;
}
```


Heap

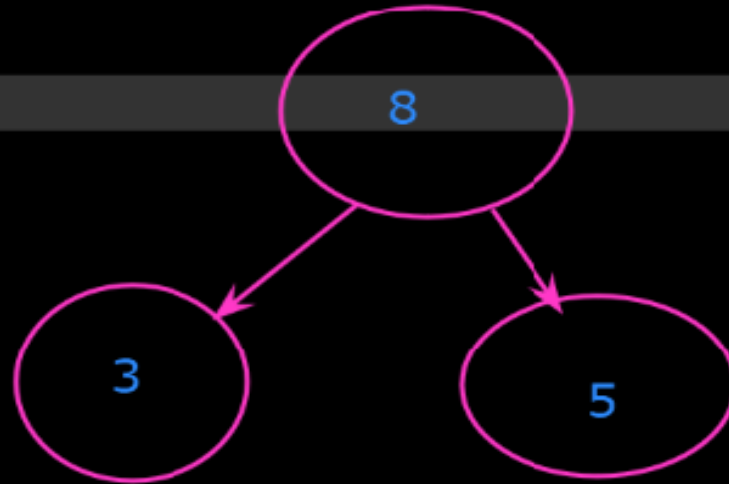
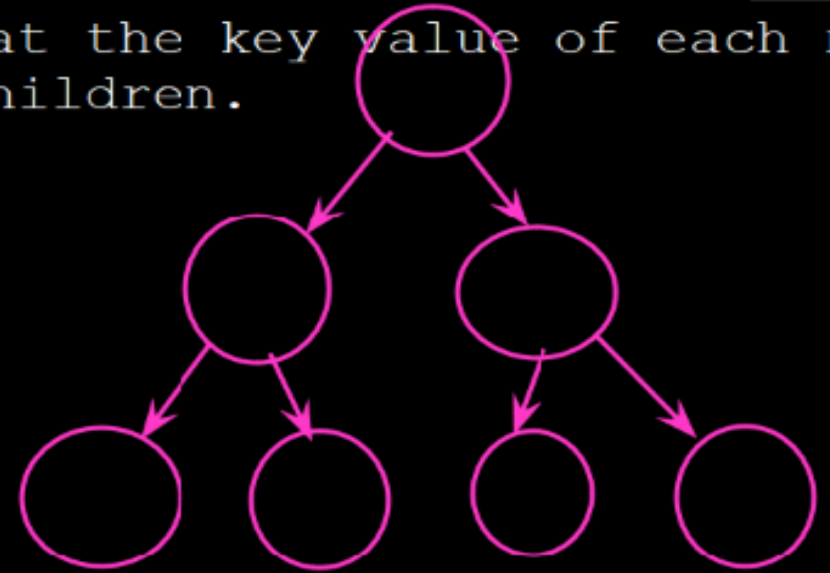


Definition:

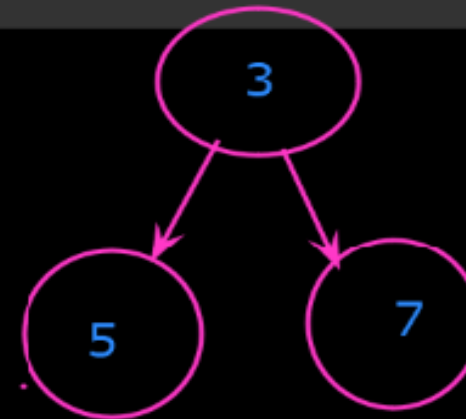
-a special form of complete binary tree that the key value of each node is smaller (larger) than the key value of its children.

Types of heap:

1. Max-Heap: root node has largest value
2. Min-Heap: root node has smallest value



Max Heap



Min Heap

Heap

Heap

- **Definition in Data Structure**

- **Heap:** A special form of **complete binary tree** that key value of each node is no smaller (larger) than the key value of its children (if any).

- **Max-Heap: root node has the largest key.**

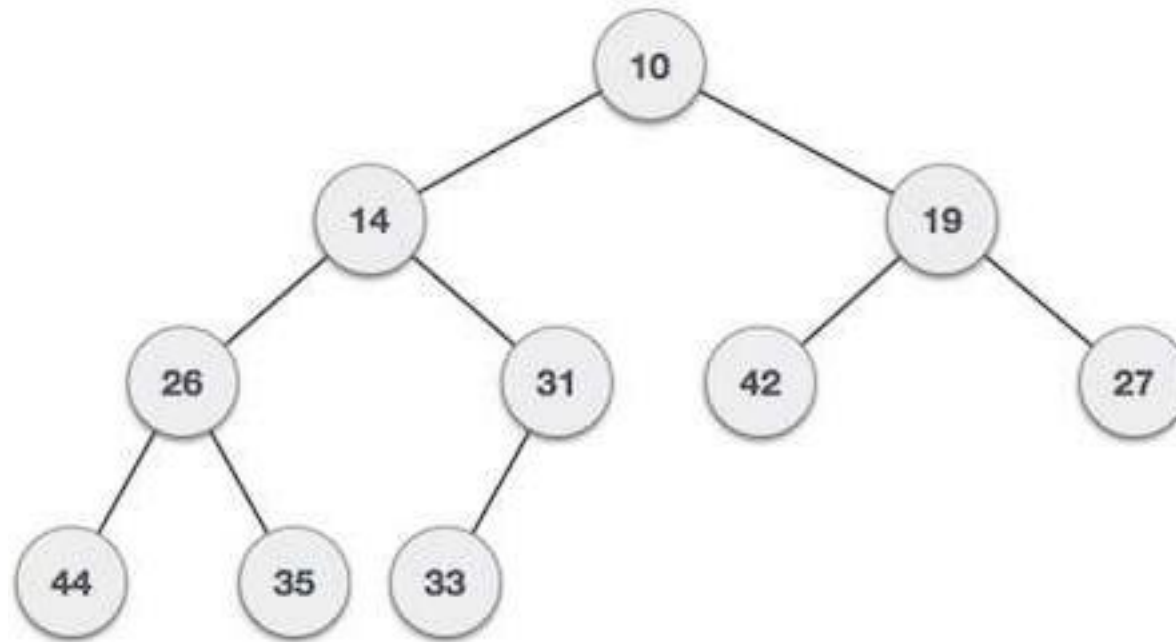
- A **max tree** is a tree in which the key value in each node is **no smaller than** the key values in its children.
- A **max heap** is a **complete binary tree** that is also a max tree.

- **Min-Heap: root node has the smallest key.**

- A **min tree** is a tree in which the key value in each node is **no larger than** the key values in its children.
- A **min heap** is a **complete binary tree** that is also a min tree.

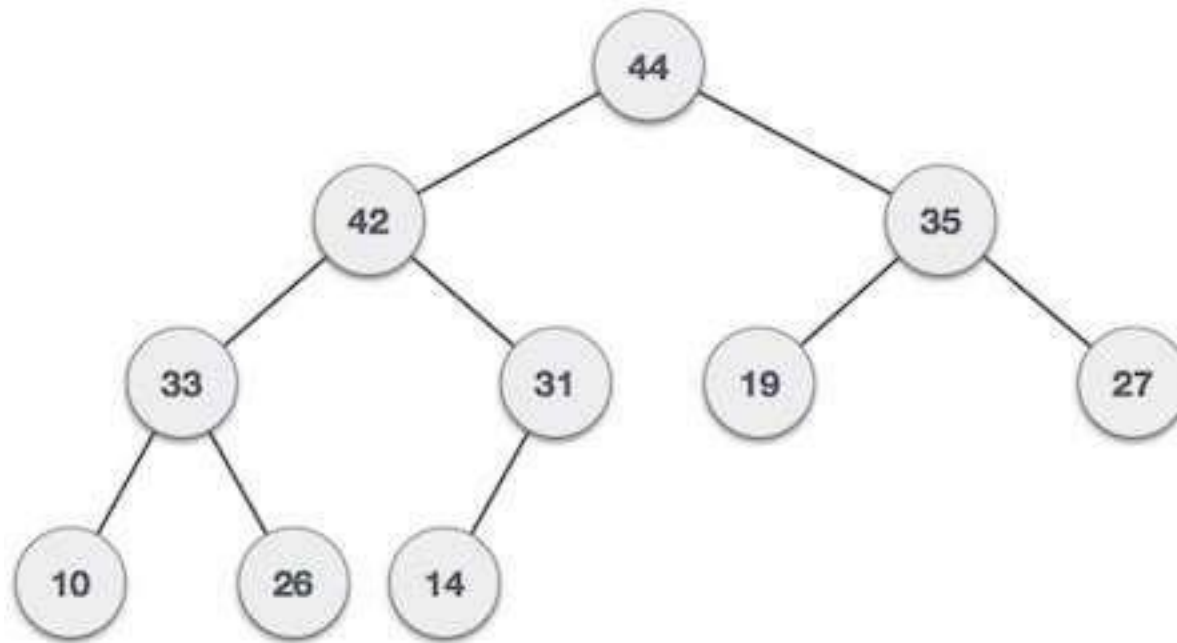
Heap

- Min-Heap
 - Where the value of the root node is less than or equal to either of its children
 - For input 35 33 42 10 14 19 27 44 26 31



Heap

- Max-Heap –
 - where the value of root node is greater than or equal to either of its children.
 - For input 35 33 42 10 14 19 27 44 26 31



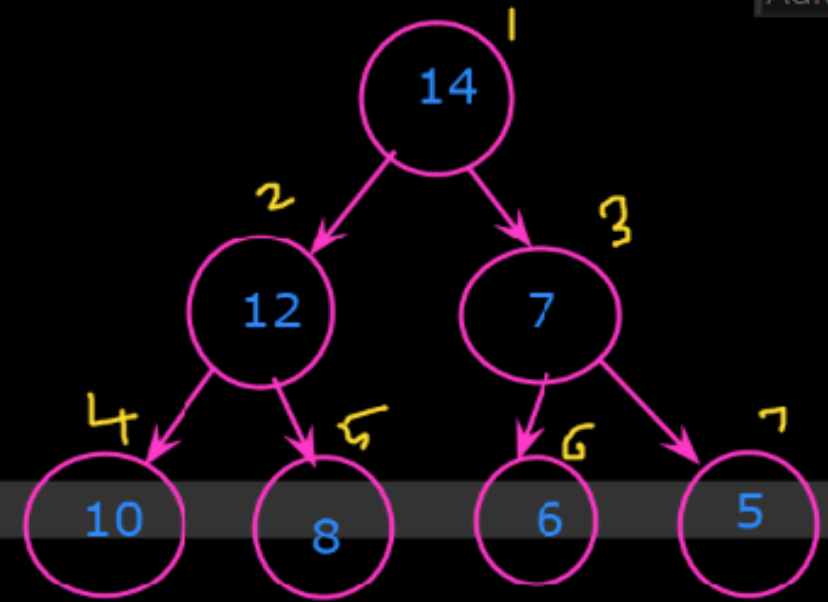
Types of heap:

1. Max-Heap: root node has largest value
2. Min-Heap: root node has smallest value

$$\text{Parent} = i/2$$

$$\text{Lc} = 2i$$

$$\text{RC} = 2i+1$$



Max heap

14 12 7 10 8 6 5

1 2 3 4 5 6 7

Types of heap:

1. Max-Heap: root node has largest value
2. Min-Heap: root node has smallest value

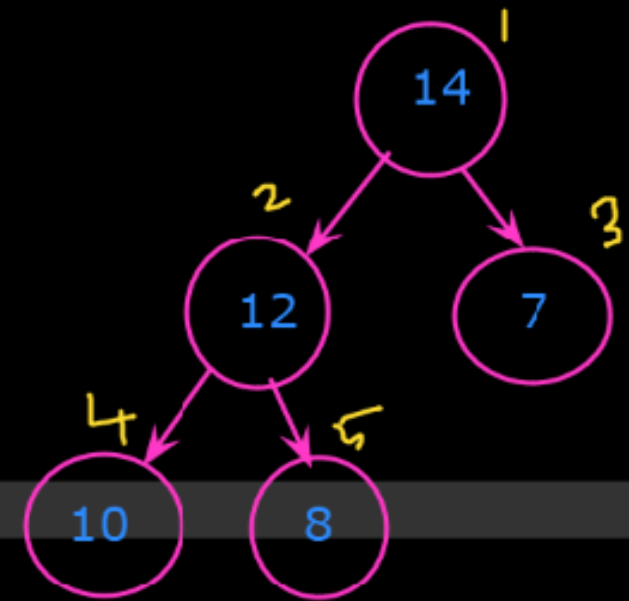
$$\text{Parent} = i/2$$

$$\text{Lc} = 2i$$

$$\text{RC} = 2i+1$$

14 12 7 10 8

1 2 3 4 5 6 7



Max heap

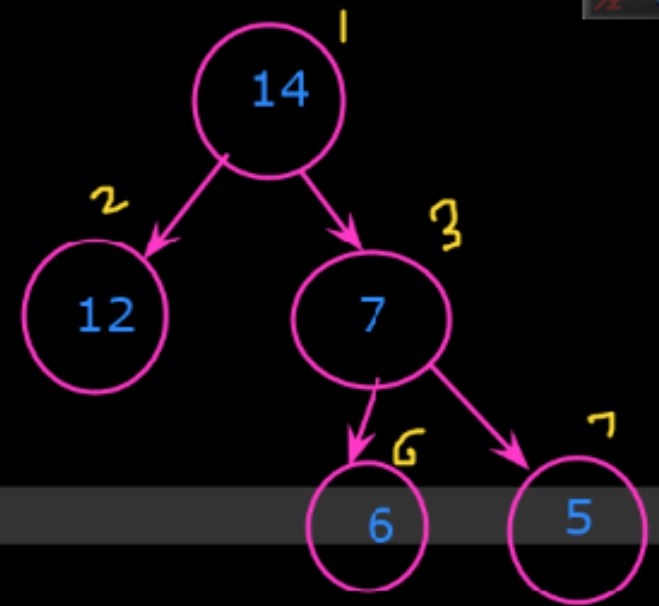
Types of heap:

1. Max-Heap: root node has largest value
2. Min-Heap: root node has smallest value

$$\text{Parent} = i/2$$

$$\text{Lc} = 2i$$

$$\text{RC} = 2i+1$$



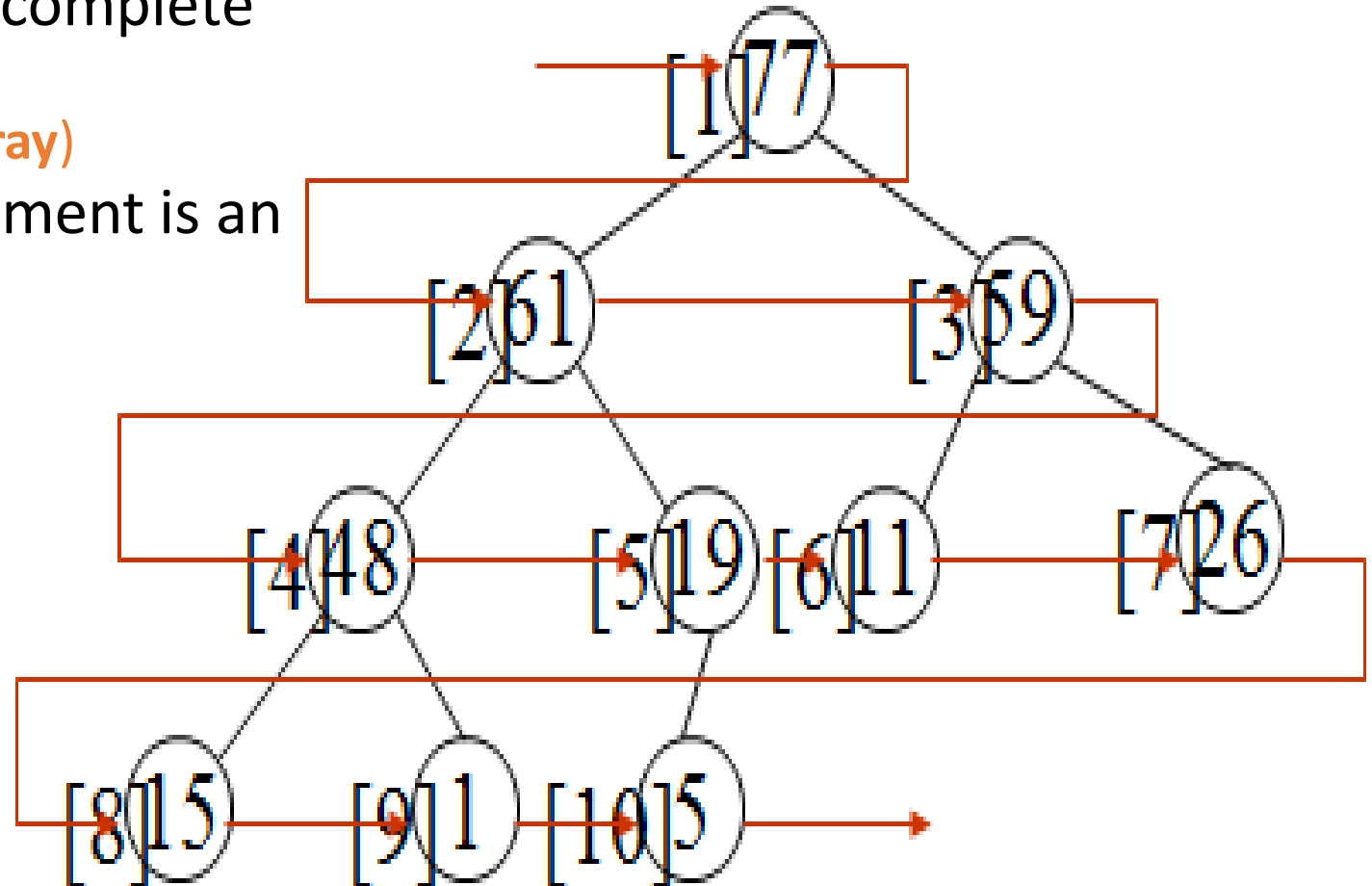
Max heap

14 12 7 - - 6 5

1 2 3 4 5 6 7

- **Note:**

- Heap in data structure is a complete binary tree!
 - (Nice representation in Array)
- Heap in C program environment is an array of memory.



— Stored using array in C

index	1	2	3	4	5	6	7	8	9	10
value	77	61	59	48	19	11	26	15	1	5

Thanks