

G



D



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### ③ Sets -

\* write orders alphabetically

3.1 Set preliminaries {, }

→ ascending order, increasing order

Set Definition: A set is an unordered collections of objects or members of the set.

A set is void to contain its elements

\* a list \* usually capital letters of the alphabet

\* Roster A = {1, 2, 3, 4} C = {1, 3, 5} E = {a, b, c, d ... z}

Method B = {1, 2, 3} D = {1, 2, 3, 4, ..., 10} F = {1, 2, 3, 4, 5, ...}

\* Rule Method - uses set builder notation

- specify one or more property

G = {x | x is a positive integer less than or equal to 10}

G = {y | y is a counting number less than 11  
starts at 1, used to count}

\* Rules should be specific

E  $\notin$

Canvas /in /not in

Kunkunyari: Insert E or  $\notin$  to complete each statement

1. 3 A E

2. 4 B  $\notin$

3. 4 C  $\notin$

4. 9 D E

5. u E E

Definition: Equal sets  $\equiv \neq \setminus$

Let A and B be sets. A is equal to B, written  $A = B$ , iff  $\forall x (x \in A \leftrightarrow x \in B)$

$$\star p \leftrightarrow q = (p \rightarrow q) \wedge (q \rightarrow p)$$

$$\star x \in A \leftrightarrow x \in B = (x \in A \rightarrow x \in B) \wedge$$

Kunkunyari: Insert  $=$  or  $\neq$  to complete each statement  $(x \in B \rightarrow x \in A)$

1.  $A \neq B$
2.  $D \neq F$
3.  $F \neq G$
4.  $D = G$
5.  $B = \{2, 1, 3\}$
6.  $C = \{1, 1, 3, 3, 3, 3, 5, 5, 5\}$

- \* even if you repeat an element, still considered an element
- \* omit dups in answers.

Definition: Subset  $\subseteq \setminus$

Let A and B be sets. A is a subset of B, written  $A \subseteq B$  iff

All  $\forall (x \in A \rightarrow x \in B)$

Kunkunyari: Insert  $\subseteq$  or  $\not\subseteq$  to complete each statement

1.  $B \subseteq A$
2.  $A \not\subseteq B$
3.  $C \subseteq D$
4.  $D \not\subseteq F$
5.  $H \not\subseteq E$
6.  $G \subseteq D$
7.  $G \not\subseteq \{\}$   $\{\}$  is an empty set
8.  $\{\} \subseteq G$
9.  $H \subseteq H$



Definition: The empty set  $\emptyset$

The empty set or null set, denoted by  $\emptyset$  or  $\{\}$ , is the set with no elements.

$\{x \mid x^2 + 7 = -6\}$  does not satisfy property / set

Definition: Singleton set

A singleton set is a set containing one element

Theorem:

If  $S$  is any set, then (i)  $\emptyset \subseteq S$  and (ii)  $S \subseteq S$

Definition: Proper subset  $\subset$  \subset \not\subset

Let  $A$  and  $B$  be sets.  $A$  is a proper subset of  $B$ , written  $A \subset B$ , iff  
 $\forall x(x \in A \rightarrow x \in B) \wedge \exists x(x \in B \wedge x \notin A)$

Kunkunyari:  $\subset$  or  $\not\subset$  to complete each statement.

1.  $B \subset A$
2.  $C \subset D$
3.  $F \not\subset D$
4.  $G \not\subset G$
5.  $H \not\subset \{3\}$
6.  $\{\} \subset H$

$$U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9, 10\}$$

$$C = \{0, 2, 4, 6, 8, 10\}$$

$$D = \{1, 3, 5, 7, 9\}$$

$$E = \{0, 1, 4, 5, 8, 9\}$$

$$F = \{3, 4, 5, 6, 7\}$$

## Union

Given two sets A and B, the Union of A and B, denoted by  $A \cup B$ , is defined as

$$A \cup B = \{x \mid (x \in A) \vee (x \in B)\}$$

$x$  such that  $x$  is an element of set A or set B

Ex: 1  $A \cup B$

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9, 10\}$$

$$A \cup B = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\} = U$$

2.  $B \cup C$

$$B = \{6, 7, 8, 9, 10\}$$

$$C = \{0, 2, 4, 6, 8, 10\}$$

$$B \cup C = \{0, 2, 4, 6, 7, 8, 9, 10\}$$

### Observations

$$A \cup B = B \cup A \quad \text{by Commutativity}$$

$$A \cap D = D \cap A$$

$$A \cap (A \cup B) = A \quad \text{by Absorption}$$

$$A \cup (A \cap B) = A$$

$$A \cup \emptyset = A \quad \text{by Identity}$$

$$A \cap U = A$$

$$\overline{(B)} = B \rightarrow \text{Complementation}$$

$$\overline{E \cap F} = \overline{E} \cup \overline{F} \rightarrow \text{De Morgan's Laws}$$

## intersection

Given two sets A and B, the intersection of A and B, denoted by  $A \cap B$ , is defined as

$$A \cap B = \{x | (x \in A) \wedge (x \in B)\}$$

x such that x is an element of set A and set B

Ex.

### 1. AND

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$B = \{1, 3, 5, 7, 9\}$$

$$A \cap B = \{1, 3, 5\}$$

### 2. DNA

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$B = \{1, 3, 5, 7, 9\}$$

$$D \cap A = \{1, 3, 5\}$$

### 3. A ∩ B

$$A = \{5, 1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9, 10\}$$

$$A \cap B = \emptyset \text{ or } \{\}$$

\*  $\emptyset$  = disjoint sets

### 3. A ∩ (A ∪ B)

$$A = \{5, 1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9, 10\}$$

$$A \cap (A \cup B) = \{0, 1, 2, 3, 4, 5\} = A$$

### 5. AU(A ∩ B)

$$A = \{5, 1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9, 10\}$$

$$A \cup (A \cap B) = \{0, 1, 2, 3, 4, 5\} = A$$

### 6. A ∩ U

$$U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$A \cap U = \{0, 1, 2, 3, 4, 5\} = A$$

## Difference (Relative Complement)

Given two sets  $A$  and  $B$ , the difference of  $A$  and  $B$ , denoted by  $A - B$ , is defined as

$$A - B = \{x | (x \in A) \wedge (x \notin B)\}$$

$x$  such that  $x$  is an element of  $A$  but not an element of  $B$

The difference of  $A$  and  $B$  is also called the (relative) complement of  $B$  with respect to  $A$ .

1. A-C

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$C = \{0, 2, 4, 6, 8, 10\}$$

$$A - C = \{1, 3, 5\}$$

2. C-A

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$C = \{0, 2, 4, 6, 8, 10\}$$

$$C - A = \{6, 8, 10\}$$

3. D-F

$$D = \{1, 3, 5, 7, 9\}$$

$$F = \{3, 4, 5, 6, 7\}$$

$$D - F = \{1, 9\}$$

4. (DAF)-B

$$B = \{6, 7, 8, 9, 10\}$$

$$D = \{1, 3, 5, 7, 9\}$$

$$F = \{3, 4, 5, 6, 7\}$$

$$DAF = \{3, 5, 7\}$$

$$(DAF) - B = \{3, 5\}$$

5. A-D-E

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$D = \{1, 3, 5, 7, 9\}$$

$$E = \{0, 1, 4, 5, 8, 9\} \quad \text{pada pag opnito pag iingatitive}$$

$$(A - D) \cap E = \{0, 1, 2, 3, 4, 5\} - \{1, 3, 5, 7, 9\} \cap \{0, 1, 4, 5, 8, 9\}$$

$$= \{0, 2, 4\} \cap \{0, 1, 4, 5, 8, 9\}$$

$$= \{0, 4\}$$

## (Absolute) Complement

Let  $U$  be the universal set. The (absolute) complement of a set  $A$ , denoted by  $\bar{A}$ , is defined as

$$\bar{A} = \{x | (x \in U) \wedge (x \notin A)\}$$

Set of all  $x$  such that  $x$  is an element of  $U$  and  $x$  is not in  $A$

Ex:

$$1. \bar{A}$$

$$U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$A = \{0, 1, 2, 3, 4, 5\}$$

$$\bar{A} = \{6, 7, 8, 9, 10\}$$

$$2. \bar{(B)}$$

$$U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$B = \{0, 7, 8, 9, 10\}$$

$$\bar{(B)} = \overline{\{0, 7, 8, 9, 10\}}$$

$$= \{0, 1, 2, 3, 4, 5, 6\}$$

$$\bar{(B)} = \emptyset \{6, 7, 8, 9, 10\} = B$$

$$3. \bar{E} \cup \bar{F}$$

$$U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

$$E = \{0, 1, 4, 5, 8, 9\}$$

$$F = \{3, 4, 5, 6, 7\}$$

$$\bar{E} \cup \bar{F} = \overline{\{0, 1, 4, 5, 8, 9\}} \cup \overline{\{3, 4, 5, 6, 7\}}$$

$$= \{2, 3, 6, 7, 10\} \cup \{0, 1, 2, 8, 9, 10\}$$

$$= \{0, 1, 2, 3, 6, 7, 8, 9, 10\}$$

## Symmetric Difference

Given two sets  $A$  and  $B$ , the symmetric difference of  $A$  and  $B$ , denoted by  $A \Delta B$ , is defined as

$$A \Delta B = (A \cup B) - (A \cap B)$$

or equivalently

$$A \Delta B = (A - B) \cup (B - A)$$



Ex:

1.  $D \Delta F$

$$D = \{1, 3, 5, 7, 9\}$$

$$F = \{3, 4, 5, 6, 7\}$$

$$D \Delta F = (D \cup F) - (D \cap F)$$

$$= (\{1, 3, 5, 7, 9\} \cup \{3, 4, 5, 6, 7\}) - (\{1, 3, 5, 7, 9\} \cap \{3, 4, 5, 6, 7\})$$

$$= \{1, 3, 4, 5, 6, 7, 9\} - \{3, 5, 7\}$$

$$= \{1, 4, 6, 9\}$$

2.  $A \Delta C$

$$A = \{0, 1, 2, 3, 4\}$$

$$C = \{0, 2, 4, 6, 8, 10\}$$

$$A \Delta C = (\{0, 1, 2, 3, 4\} - \{0, 2, 4, 6, 8, 10\}) \cup (\{0, 2, 4, 6, 8, 10\} - \{0, 1, 2, 3, 4\})$$

$$= \{1, 3, 5\} \cup \{6, 8, 10\}$$

$$= \{1, 3, 5, 6, 8, 10\}$$

3.

$$0, 1, 2, 8, 9, 10$$

$$0, 1, 8, 9$$

$$3, 5, 7 \cup 0, 1, 8$$

Illustration

3.  $D \Delta (E \cap F)$

$$\begin{aligned} D \Delta (E \cap F) &= \{1, 3, 5, 7, 9\} \Delta ((0, 1, 4, 5, 8, 9) \cap \{3, 4, 5, 6, 7\}) \\ &= \{1, 3, 5, 7, 9\} \Delta (0, 1, 4, 5, 8, 9) \cap \{0, 1, 2, 8, 9, 10\} \\ &= \{1, 3, 5, 7, 9\} \Delta (0, 1, 8, 9) \\ &= (\{1, 3, 5, 7, 9\} \cup \{0, 1, 8, 9\}) - ((\{1, 3, 5, 7, 9\} \cap \{0, 1, 8, 9\}) \\ &= (0, 1, 3, 5, 7, 8, 9) - \{1, 9\} \\ D \Delta (E \cap F) &= \{0, 3, 5, 7, 8\} \end{aligned}$$

$$A(A \cup \bar{C}) \cap (\bar{E} \cup D)$$

1, 3, 5, 7, 9

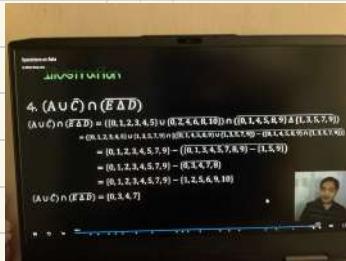
0, 1, 2, 3, 4, 5, 7, 9

1, 2, 3, 9

0, 4, 8 ∪ 3, 7

0, 4, 8, 3, 7

1, 2, 5, 6, 9, 10



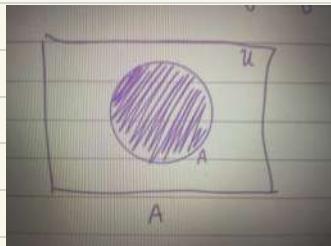
## 3.3 - Venn Diagram

↳ John Venn

(graphical tool) that helps us understand sets

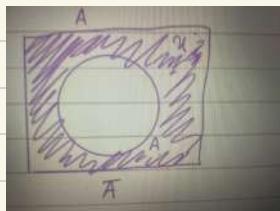
### Illustration

1. A

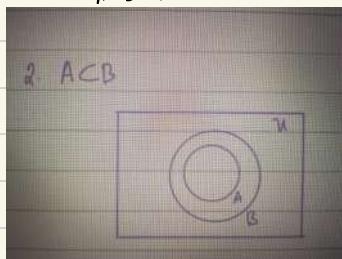


$A \subset B$

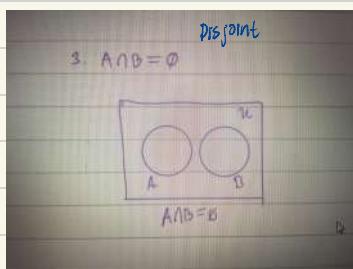
$\bar{A}$



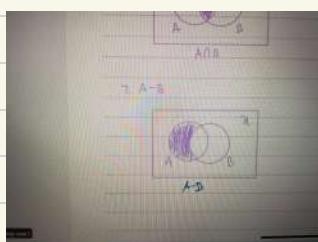
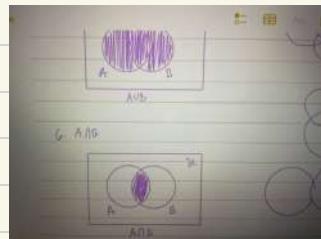
+ intersection



3.  $A \cap B = \emptyset$   
disjoint



4.  $A \cup B$

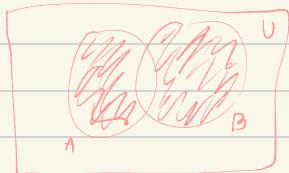


$\cap \Delta$

9.  $A \Delta B$

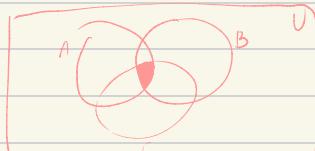
$$A \Delta B = (A - B) \cup (B - A)$$

$$A \Delta B = (A \cup B) - (A \cap B)$$

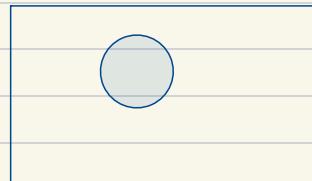


$A \Delta B$

10.  $A \cap (B \cup C)$



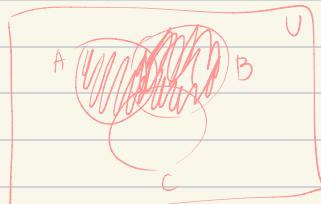
$A \cap (B \cup C)$



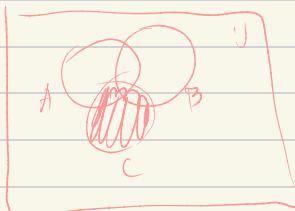
Carbonej, Radac Danyli A.

$\cap C - C$

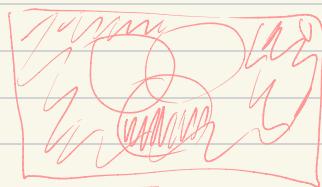
II.  $A \cup B \cap C$



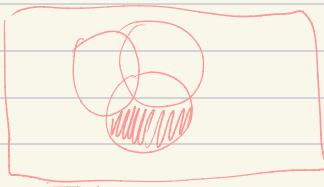
$A \cup B$



$C$



$A \cup B$

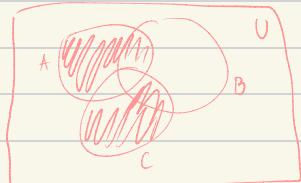


$A \cup B \cap C$

Carbone) / Raggio Darijil A:

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12.  $(A \Delta C) - \overline{B}$

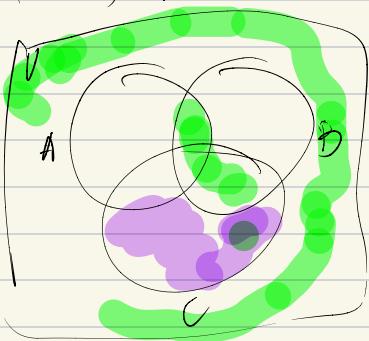


$A \Delta C$

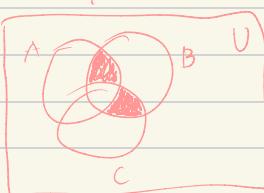


B

$(A \Delta C) - \overline{B}$

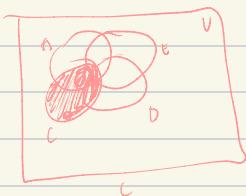


$\overline{B}$

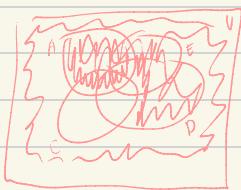


$(A \Delta C) - \overline{B}$

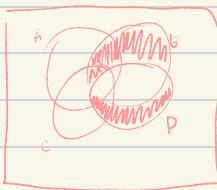
$(A \cup \overline{C}) - (\overline{E} \Delta D)$



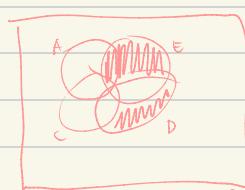
Sorry sorry  
che



$A \cup \overline{C}$

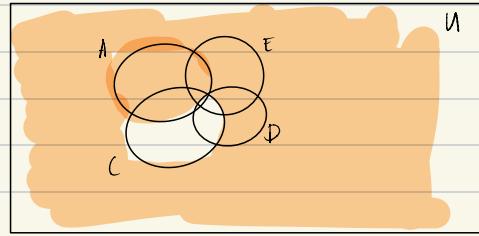
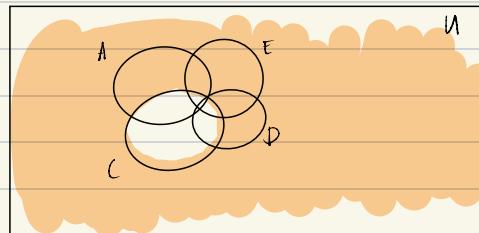
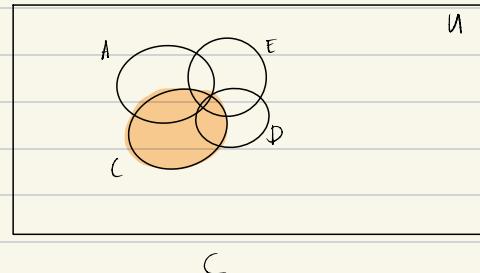
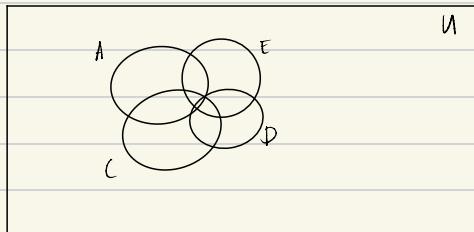
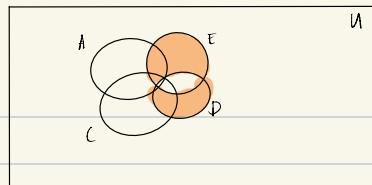


$E \Delta D$



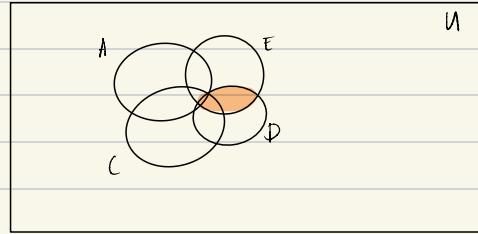
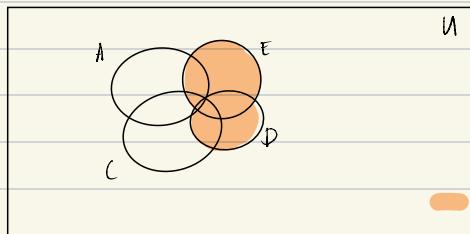
$(A \cup \overline{C}) - (E \Delta D)$

$$(A \cup \bar{C}) - (\bar{E} \Delta D)$$



$\bar{C}$

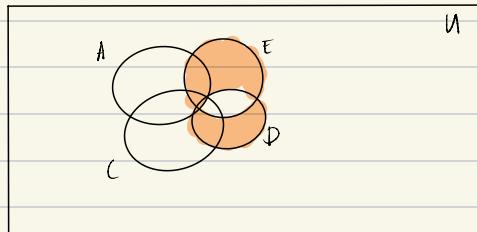
$A \cup \bar{C}$



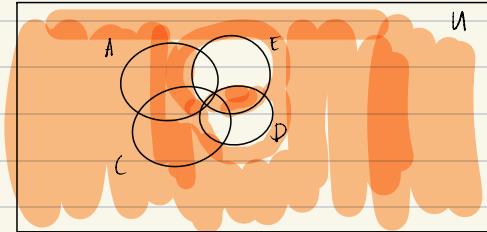
$E \Delta D$  ( $\neq D$ )

$E \Delta D$  ( $\neq D$ )

$$\underline{(A \cup B) - (A \cap B)}$$



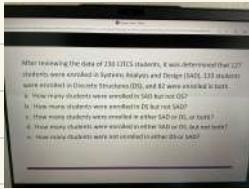
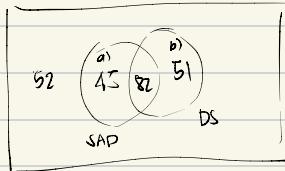
$$(\neq D) - (\neq A)$$



$$(\bar{E} \Delta D)$$

### 3.4 Cardinality of sets

Value for the number of unique items in a set

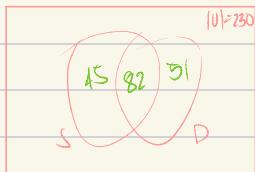


- c) total: 178
- d) total (no both): 96
- e) 52

230 overall

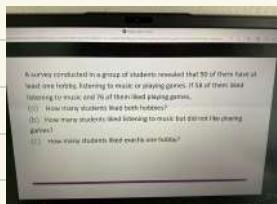
1. Let  $S = \{x | x \text{ is a CITCS student enrolled in SAD}\}$

$D = \{x | x \text{ is a CITCS student enrolled in DS}\}$



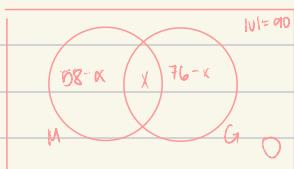
- a. 45 students
- b. 51 students
- c. 178 students
- d. 96 students
- e. 52 students

2.



Let  $M = \{z | z \text{ likes listening to music}\}$

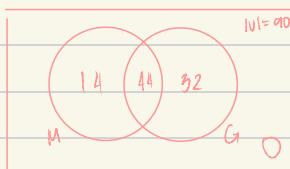
$G = \{z | z \text{ likes playing games}\}$



$$|U| = 90 : (58 - x) + x + (76 - x)$$

$$-x = -44$$

$$x = 44$$



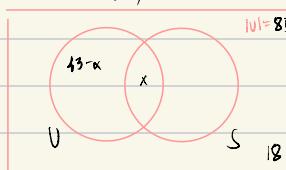
- a. 44 people
- b. 14 students
- c. 46 students

# Carbonech, Badge Daryl A.

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3. Let  $V = \{x | x \text{ students who like The Umbrella Academy}\}$

$S = \{y | y \text{ students who like Stranger Things}\}$

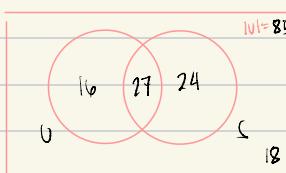
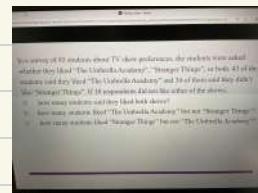


$$34 = (43 - x) + 18$$

$$34 = 61 - x$$

$$x + 25 = 95$$

$$x = 27$$



a. 27 students

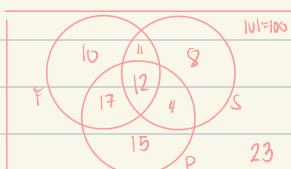
b. 16 students

c. 24 students

4. Let  $F = \{x | x \text{ like "The fault in our stars"}\}$

$S = \{x | x \text{ like "The Spectacular Now"}\}$

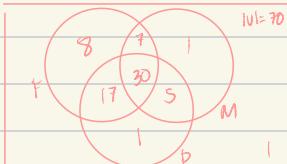
$P = \{x | x \text{ like "The Perks of being a Wallflower"}\}$



b. Let  $F = \{x | x \text{ like "The Father"}\}$

$M = \{x | x \text{ like "Minari"}\}$

$P = \{x | x \text{ like "Promising Young Woman"}\}$



a: 8 students

b: 5 students

c: 24 students

d: 1 student

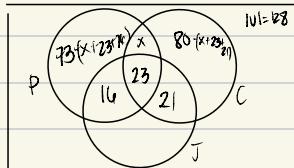
Carbone), Badge Day 11 A.

CCA-1C

5. Let  $P = \{x \mid x \text{ know Python}\}$

$$C = \{x \mid x \text{ know C++}\}$$

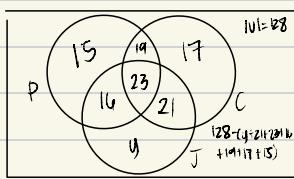
$$J = \{x \mid x \text{ know Java}\}$$



$$|U| = 53$$

$$|J| = 50 - x$$

$$x = 19$$



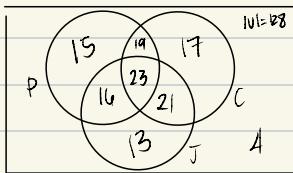
$$|J| = 15 + 19 + 17 + (28 - (y + 21 + 23 + 16))$$

$$= 51 + 128 - y - 11$$

$$53 = 68 - y$$

$$y + 53 = 68$$

$$y = 15$$



a. 4 students

b. 15 students

c. 19 students

carbone, badge Danyll A.

CCA-1C

Let L = {x | x about love}

P = {x | x about prison}

T = {x | x about trucks}

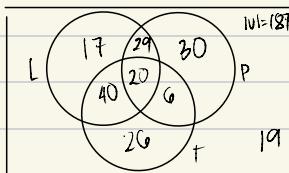
a) 92 songs

b) 85 songs

c) 102 songs

d) 81 songs

e) 187 songs



carbone, badge Danyll A.

CCA-1C

Let N = {x | x subscribes to Netflix}

D = {x | x subscribes to Disney+}

A = {x | x subscribes to Amazon Prime}

$$800 = 119 + 79 + 107 + 111 + 87 + (406 - (x + 111 + 87)) + x + 386 - (x + 107 + 87)$$

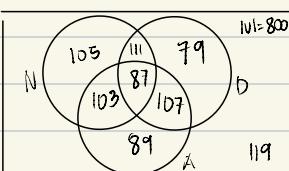
$$800 = 503 + (406 - x - 198) + x + (386 - x - 191)$$

$$800 = 603 + 208 - x + x + 192 - x$$

$$800 = 903 - x$$

$$x + 800 = 903$$

$$x = 103$$



a. 103 households

b. 105 households

c. 89 households

d. 184 households

e. 321 households