Significance Testing About Proportions

Using the Rejection Region
Using the p - value



Population Proportion

 A population proportion is a parameter that describes a percentage value associated with a population.

Example:

• Five years ago, 3.9% of children in a certain region lived with someone other than a parent. A sociologist wishes to test whether the current proportion is different. Perform the relevant test at the 5% level of significance using the following data: in a random sample of 2,759 children, 119 lived with someone other than a parent.

Step 1: Assumptions

- Check assumptions
 - ullet Population proportion p is defined
 - n is large enough ($n \ge 30$)

Step 1: Assumptions

 In a random sample of 2,759 children, 119 lived with someone other than a parent.

Population Proportion:

$$\hat{p} = \frac{119}{2759}$$

• Sample size, n=2759

Step 2: State the Hypotheses

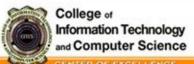
- State the Hypotheses
 - ullet let p_0 be the hypothesized value

Null Hypothesis

$$H_0: p = p_0 \text{ (or } p \ge p_0 \text{ or } p \le p_0)$$

Alternative Hypothesis

$$H_a: p \neq p_0 \text{ (or } p < p_0 \text{ or } p > p_0)$$



Step 2: State the Hypotheses

• let p_0 be the hypothesized value $p_0 = 3.9\% = 0.039$

 H_0 : p = 0.039

 $H_q: p \neq 0.039$



Step 3: Compute the Test Statistic

Compute for the Test Statistic

$$z = \frac{\hat{p} - p_0}{se_0}$$

where

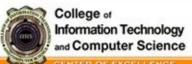
$$se_0 = \sqrt{\frac{p_0(1-p_0)}{n}}$$

Step 3: Compute the Test Statistic

$$se_0 = \sqrt{\frac{p_0(1 - p_0)}{n}}$$

$$se_0 = \sqrt{\frac{0.039 (1 - 0.039)}{2759}} = 0.0037$$

$$z = \frac{\hat{p} - p_0}{se_0} = \frac{\frac{119}{2759} - 0.039}{0.003685684} = 1.12$$

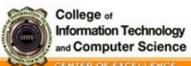


Step 4: Interpret the Test Statistic

Using the Rejection Region

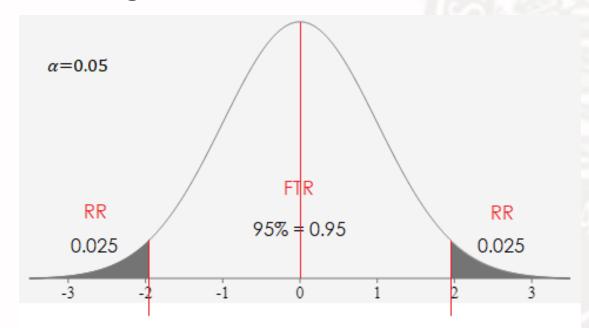
• Determine if one-tailed or two-tailed test based on H_a

 Determine the FTR (Fail To Reject) region and the RR (Rejection Region) based on the confidence level or the significance level



Step 4: Interpret the Test Statistic (Using Rejection Region)

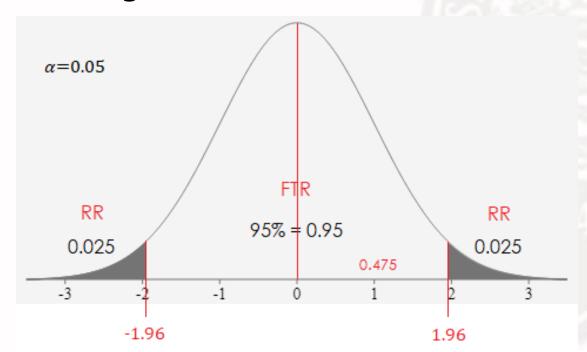
- H_a : $p \neq 0.039$ (two-tailed test)
- 5% level of significance, $\alpha = 0.05$





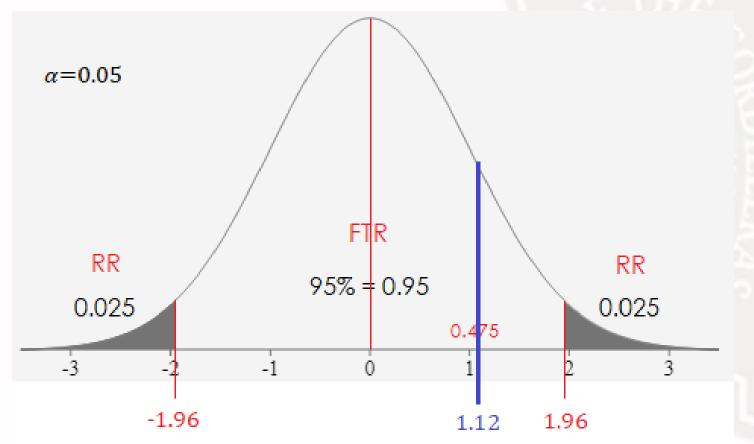
Step 4: Interpret the Test Statistic (Using Rejection Region)

- H_a : $p \neq 0.039$ (two-tailed test)
- 5% level of significance, $\alpha = 0.05$





Step 4: Interpret the Test Statistic (Using Rejection Region)





Step 5: Make a Conclusion

 Since the test statistic lies in the FTR, then we fail to reject the null hypothesis.

• Therefore, there is no significant difference between the current and the past proportion.

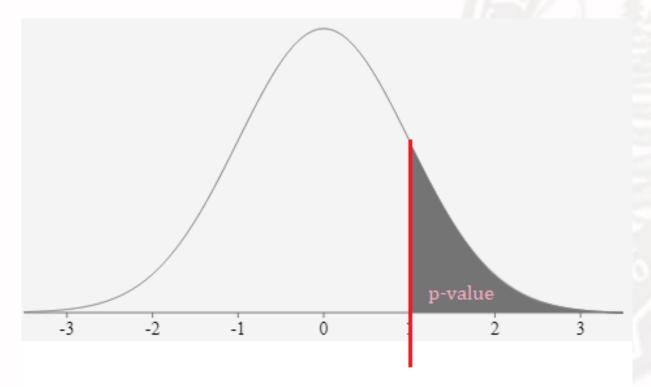
Step 4: Interpret the Test Statistic (Using p-values)

• Compute for the p – value. The p – value is the probability that the test statistic takes the observed value or a value more extreme if we presume H_0 is true.

• The computation of the $\it p-value$ from the test statistic depends on $\it H_a$

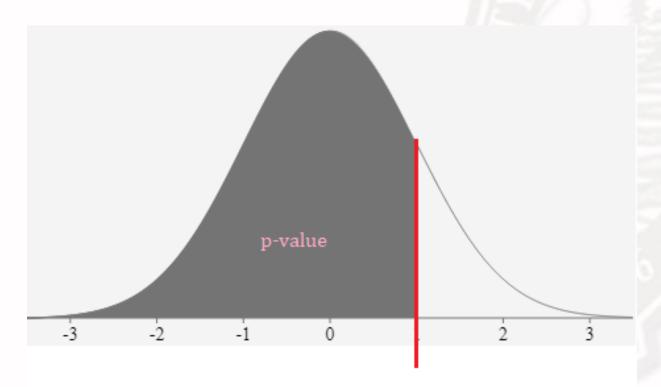
Step 4: Interpret the Test Statistic (Using p-values)

• H_a : $p > p_0$ (right-tailed test)



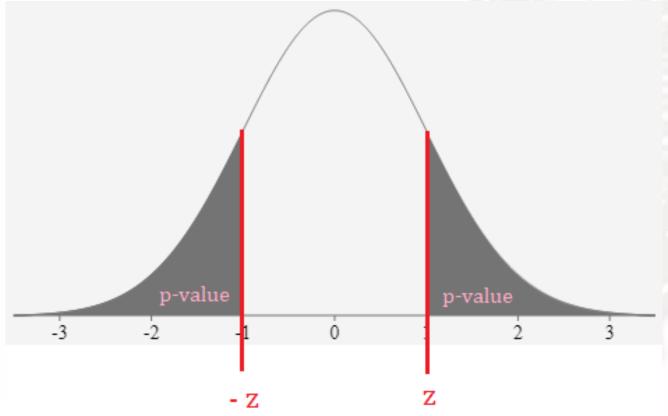
Step 4: Interpret the Test Statistic (Using p-values)

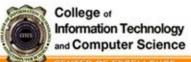
• H_a : $p < p_0$ (left-tailed test)



Step 4: Interpret the Test Statistic (Using p-values)

• H_a : $p \neq p_0$ (two-tailed test)





Step 4: Interpret the Test Statistic (Using p-values)

- H_a : $p \neq 0.039$ (two-tailed test)
- z = 1.12
- p value = 2(0.5 0.3686)= 2(0.1314)= 0.2628

Step 5: Make a Conclusion

• If p – value < significance level, then reject H_0

• If p – value \geq significance level, then do not reject H_0

Step 5: Make a Conclusion

- 5% level of significance, $\alpha = 0.05$
- p value = 0.2628
- p-value > α , so, do not reject the null hypothesis.
- Therefore, there is no difference between the current and the past proportion.

You Try

- Professional astrologers prepared horoscopes for 83 adults. Each adult was shown three horoscopes, one of which was the one an astrologer prepared for him or her and the other two were randomly chosen from ones prepared for other subjects in the study. Each adult had to guess which of the three was his or hers. Of the 83 subjects, 28 guessed correctly. Would you conclude that people are more likely to select their horoscope?
- Set up the hypotheses to test that the probability of a correct prediction is 1/3 against the astrologers' claim that it is greater than 1/3.

college Consider a 95% confidence level

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