



$\sigma \rightarrow \text{Mean} \leftarrow \mu - \text{population}$
 $\bar{x} - \text{sample}$

Interpret - pval
 - test stat
 - test stat \rightarrow f-test

$$H_0 = 70$$

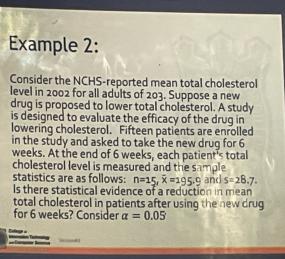
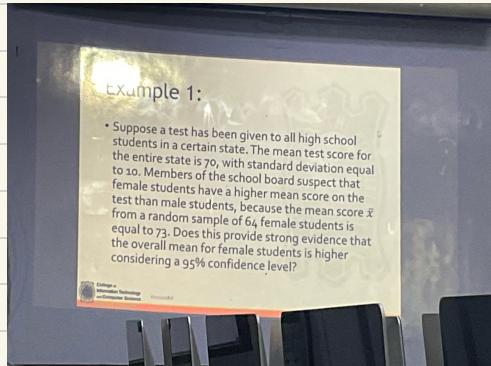
$$\sigma = 10$$

$$n = 64$$

$$\bar{x} = 73$$

$$C = 95\%$$

$$\alpha = 0.05 \text{ or } 5\%$$



$$H_0 = M \geq 203$$

$$\sigma = 28.7$$

$$n = 15 \text{ (n < 30) } \Rightarrow t\text{-test}$$

$$\bar{x} = 195.9$$

$$\alpha = 0.05$$

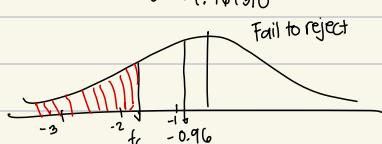
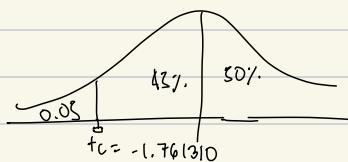
$$H_0 \approx M \geq 203$$

$$H_a = M < 203 \text{ (left-tailed)}$$

$$df = n - 1$$

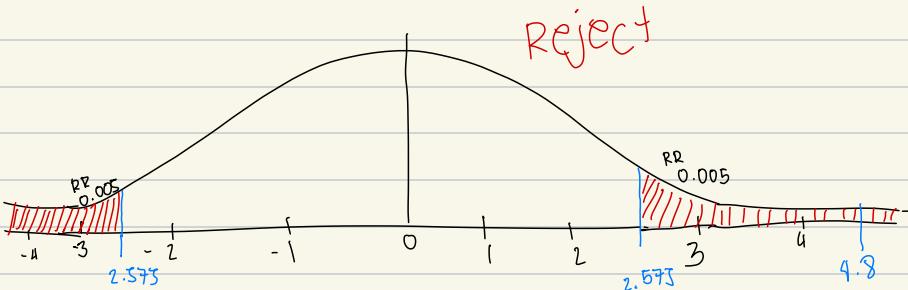
$$= 14$$

$$= 14$$



$$SE_0 = \frac{s}{\sqrt{n}} = \frac{28.7}{\sqrt{15}} = 7.41$$

$$t = \frac{\bar{x} - M_0}{SE_0} = \frac{195.9 - 203}{7.41} = -0.96$$



$$S = 4.99$$

$$M_0 = 7$$

$$n = 15$$

$$\bar{X} = 5.9$$

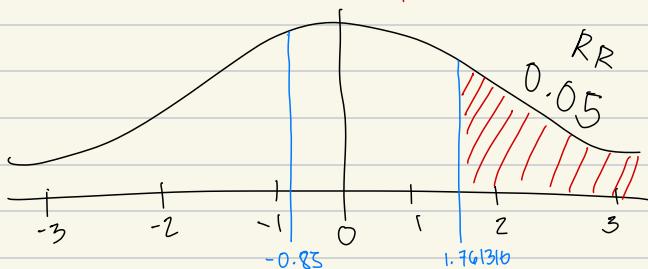
$$H_0: M = 7$$

$$H_a: M > 7$$

$$\alpha = 0.05$$

$$SE_0 = \frac{S}{\sqrt{n}} = \frac{4.99}{\sqrt{15}} = 1.288401873$$

FTR



Two Groups ↘ Proportions (Categorical - Qualitative) ↘ Variable
 Means (Numerical - Quantitative) ↘

Comparing Means

• independent

↳ samples that have no direct association

ex. → Method 1 → students A
 ↳ method 2 → students B

Paired

diet program

↳ connected

pre-diet weight

↓ sample

post-diet weight

Independent

Groups A \bar{x} SD Is there a difference

① Cars 45 5.3 22 between the two means

② Trucks 40 7.1 3.0 consider

$$\alpha = 90\%$$

two tailed

$$\alpha \approx 10\% \rightarrow 10\% = 5\% / 0.05$$

interpret the

P-value

⑤ ∵ Reject H_0 , that states that

$$2(0.5 - 0.4999)$$

$$= 0.0022 - p\text{-val}$$

$$\approx 0.05 - \alpha \rightarrow \text{bigger}$$

Assumption

$$n_1 = 40 \rightarrow z\text{-test}$$

$$n_2 = 40 \rightarrow z\text{-test}$$

Hypothesis

$$H_0: M_1 = M_2 \quad (M_1 - M_2 = 0)$$

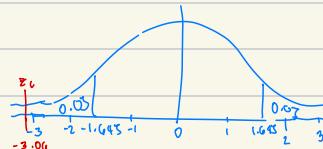
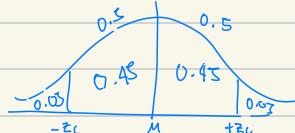
$$H_a: M_1 \neq M_2$$

③ Test statistic

$$SE_0 = \sqrt{\frac{(S_1)^2}{n_1} + \frac{(S_2)^2}{n_2}} \quad Z = \frac{(\bar{x}_1 - \bar{x}_2) - (M_1 - M_2)}{SE_0}$$

$$= \sqrt{\frac{(2.2)^2}{40} + \frac{(3.0)^2}{40}} \quad = \frac{(5.3 - 7.1) - 0}{0.5882}$$

$$= 0.5882 \quad \approx -3.06 \approx 0.1999$$



(celing price)

Group	n	\bar{x}	s	s^2
i) PHP 13 Group 1 (ceiling) 5	10	171	26	676
ii) PHP 10 Group 2 (ceiling) 5	10	198	29	841

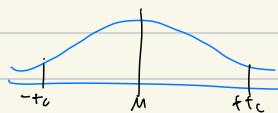
Is there a difference

between the means

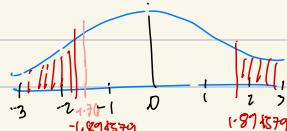
Consider:

$$\alpha = 0.10\% \approx 10\% / 2 = 5\% / 0.05$$

∴



$$df = 7 \quad F_C = 1.894579 \\ \alpha = 0.05$$



∴ FTR the H_0 because ...
∴ Reject the H_0 because ...

$$\textcircled{1} \quad n_1 = 10 \rightarrow t\text{-test}$$

$$n_2 = 5 \rightarrow t\text{-test}$$

$$\textcircled{2} \quad H_0 = M_1 = M_2 \quad (M_1 - M_2 = 0)$$

$$H_a = M_1 \neq M_2 \quad (\text{two-tailed})$$

$$\begin{aligned} \textcircled{3} \quad se_0 &= \sqrt{\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}} \\ &= \sqrt{\frac{(26)^2}{10} + \frac{(29)^2}{5}} \\ &= 15.3558 \end{aligned}$$

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (M_1 - M_2)}{se_0}$$

$$= \frac{(171 - 198) - 0}{15.3558}$$

$$\approx -1.76$$

unbiased

$$\begin{aligned} \textcircled{4} \quad df &= \left[\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2} \right]^2 \\ &\quad \frac{1}{n_1} \left(\frac{(s_1)^2}{n_1} \right)^2 + \frac{1}{n_2} \left(\frac{(s_2)^2}{n_2} \right)^2 \\ &\approx \frac{\left[\frac{(26)^2}{10} + \frac{(29)^2}{5} \right]^2}{10-1 \left(\frac{(26)^2}{10} \right)^2 + 5-1 \left(\frac{(29)^2}{5} \right)^2} \\ &\approx 7.33 \end{aligned}$$

$$\approx 7$$

mcAct4: Comparing Proportions

Quiz Instructions

over the following questions.

A study considered whether greater levels of television watching by teenagers were associated with a greater likelihood of aggressive behavior. The researchers randomly sampled 707 families in two counties in northern New York state and made follow-up observations over 17 years. Table 10.3 shows results about whether a sampled teenager later conducted any aggressive act against another person, according to a self-report by that person or by his or her parent. The bar chart in the margin figure summarizes the results.

Table 10.3 TV Watching by Teenagers and Later Aggressive Acts

TV Watching	Aggressive Act		Total
	No	Yes	
Less than 1 hour per day	5	83	88
At least 1 hour per day	154	465	619

We identify Group 1 as those who watched less than 1 hour of TV per day, on average, as teenagers. Group 2 consists of those who averaged at least 1 hour of TV per day as teenagers. Denote the population proportion committing aggressive acts by p_1 for the lower level of TV watching and by p_2 for the higher level of TV watching. Compute the proportions of the two groups and make a decision about the null hypothesis using a significance level of 0.05.

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$$\textcircled{1} \quad n_1 = 88 \quad \textcircled{2} \quad p_1 = p_2 \quad (p_1 - p_2 = 0)$$

$$n_2 = 619 \quad p_1 \neq p_2$$

$$\textcircled{3} \quad \text{se}_{\hat{p}} = \sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}$$

$$\hat{p} = \frac{x_1 + x_2}{n_1 + n_2} = \frac{154 + 465}{88 + 619} = \frac{619}{707} = 0.87563346$$

$$\sqrt{0.2248...} = 0.47510608$$

$$0.01363636 + 0.00161333$$

$$= \frac{88 + 619}{88 + 619} = 0.012979145$$

$$= \frac{159}{707} = \sqrt{0.00226249} = 0.047563346$$

$$= 0.224893912$$

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\text{se}_{\hat{p}}}$$

$$= 0.056818182 - 0.24578827$$

$$= -0.19197019$$

Paired Samples

- > 1 sample group
- > direct association

\bar{x}_d - difference of n \leftarrow before after

$$H_0 = \mu_1 = \mu_2 (\mu_1 - \mu_2 = 0)$$

Example:

① $n=8$ (not large enough) t-test

② $H_0 = \mu_1 = \mu_2 (\mu_1 - \mu_2 = 0)$

$H_a = \mu_1 \neq \mu_2$ (two-tailed test)

③ $s_{eo} = \frac{sd}{\sqrt{n}}$

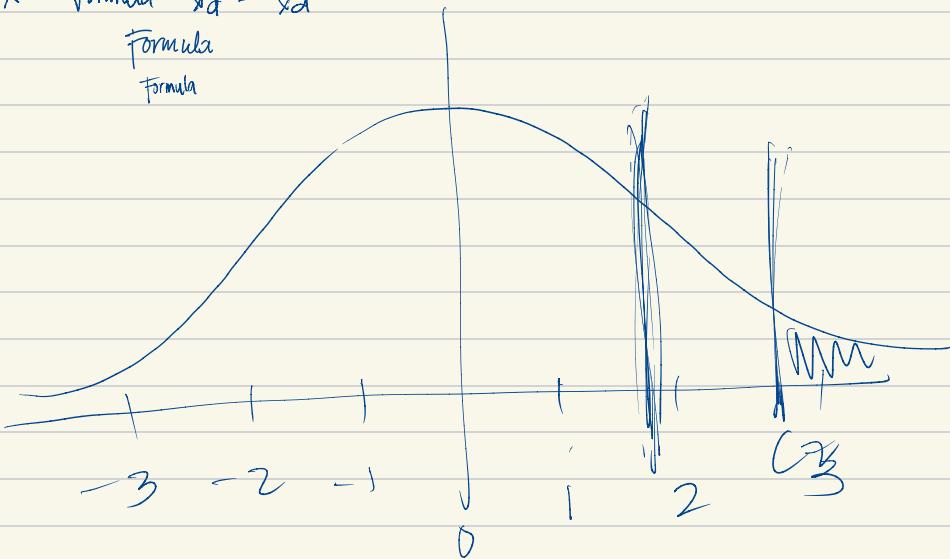
$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

$$t = \frac{\bar{x}_d - 0}{s_{eo}} =$$

$x - \bar{x}$ - formula $x_d - \bar{x}_d$

Formula

Formula



Quizzes > Lesson05: Lecture Activity

Lesson05: Lecture Activity

Last updated at 8:57am

Instructions

The following questions:

The following descriptive statistics were obtained from a study (Bardal, O'Quigley et al., Journal of Rehabilitation Research and Development, vol. 40, 2003) that aimed to compare the weight of Kuwaiti men with Swedish men between the ages of 20 to 29 years.

Group size	Mean weight	Standard deviation
Kuwaiti men	15	61.57
Swedish men	15	70.73

Interpret and explain what (if any) effect a country has on the mean weight of its men. Use a 95% confidence level.

Next >

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① $n_1 = 15$

$n_2 = 15$

②

Test for Independence

- ↳ cross-tab, Contingency table
- ↳ Variables are either dependent or not
- ↳ Chi-squared test (χ^2)

Lung Cancer

Smoking	Present	Absent	Column Total
Smoker	605 t_1	185 t_2	790
Non-Smoker	122 F_1	312 F_2	434
Row Total	727	497	1224

$$\begin{aligned} \textcircled{1} \quad x(\text{cause}) &= \text{smoking} \\ y(\text{effect}) &= \text{lung cancer} \\ \alpha &= 0.05 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad H_0: \text{smoking} &\perp\!\!\!\perp \text{lung cancer} \\ H_a: \text{smoking} &\pm \text{lung cancer} \end{aligned}$$

$$t_{1,1} = \frac{727 + 790}{1224} = 469.22 = 469$$

$$t_{1,2} = \frac{497 + 790}{1224} = 320.78 = 321$$

$$t_{2,1} = \frac{727 + 434}{1224} = 257.78 = 258$$

$$t_{2,2} = \frac{497 * 434}{1224} = 176.22 = 176$$

Lung Cancer

Smoking	Present	Absent	Column Total
Smoker	469 E_1	321 E_2	790
Non-Smoker	238 F_1	176 F_2	414
Raw Total	727	497	1224

$$\textcircled{2} \quad \chi^2 = \sum \frac{oc - ec}{ec}$$

oc = Observed count
ec = Expected count

$$= \frac{(185 - 469)^2}{469} + \frac{(185 + 321)^2}{321} + \frac{(122 - 238)^2}{238} + \frac{(312 - 176)^2}{176}$$

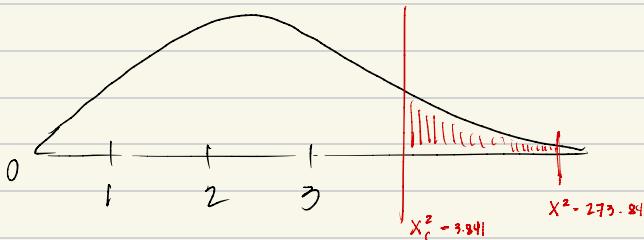
$$= 273.84$$

$$\textcircled{4} \quad df = (r-1) \times (c-1)$$

$$= (2-1) \times (2-1)$$

$$= 1$$

$r = \# \text{ of rows}$ $\chi^2_c = 3.841$
 $c = \# \text{ of columns}$



∴ Reject the H_0 , that states that the variables smoking and lung cancer are independent, therefore we accept that σ and λ are associated

for Research:

- * Use Storrs
- * methods learned on CC8 and CC12 only
- * Descriptive vs. Inferential
 - describe within \odot assumption about outside the \odot
 - measures of central tendencies

POP

