

Underlying:

S_0

$$dS = S(\mu dt + \sigma dW_t), \quad W_t - \text{Wiener process}$$

Base option:

payoff: $\max(S_T - K, 0)$, K - strike,
 T - expiry

$V(t, S_t)$ - option price

Compound option:

payoff: $\max(V(T', S_{T'}) - K', 0)$,
 K' - strike
 T' - expiry, $T' \leq T$

$VC(t, S_t)$ - compound option price

Find: VC

Input parameters: $S_0, \mu, \sigma, T, K, T', K'$

Aux: change $\max \rightarrow \min$