

Question	Answer	Marks	Guidance
10(a)	Gradient of $AB = \frac{-5-3}{8-4} [= -2]$	M1*	
	Midpoint $AB = \left(\frac{8+4}{2}, \frac{-5+3}{2}\right) [(6, -1)]$	M1	
	Gradient of normal $= -\frac{1}{-2} \left[= \frac{1}{2} \right]$ and an attempt to find the required equation	DM1	Must be used to find equation of perpendicular through <i>their</i> (6, -1).
	Equation of perpendicular bisector is $y+1 = \frac{1}{2}(x-6)$, so $y = \frac{1}{2}x - 4$	A1	WWW AG – working involving the perpendicular bisector must be seen.
	Alternative Method for Question 10(a)		
	$AC^2 = (a-4)^2 + (b-3)^2$, $BC^2 = (a-8)^2 + (b+5)^2$ both expanded	M1*	
	Solving $AC = BC$ [= 10]	DM1	Only allow a single sign error.
	Eliminating a^2 and b^2	DM1	May be awarded before the previous DM1.
	$a = 2b + 8$, concluding $y = \frac{x}{2} - 4$	A1	WWW
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Question	Answer	Marks	Guidance
10(b)	Using the centre as $\left(a, \frac{1}{2}a - 4\right)$	M1	May see centre as $(2y + 8, y)$ OE. May be seen in an incorrect equation.
	$(4 - a)^2 + (3 - 0.5a + 4)^2 = 100$	M1	Sub in $(4, 3)$ or $(8, -5)$. Could use circle with $(6, -1)$ and $r = \sqrt{80}$.
	$1.25a^2 - 15a - 35 [=0] \Rightarrow a^2 - 12a - 28 [=0] \text{ (or } b^2 + 2b - 15 [=0])$	DM1	Obtain a 3-term quadratic in <i>their</i> x or y .
	$[(a - 14)(a + 2) = 0] \Rightarrow a = 14, a = -2$	A1	Or $[(b - 3)(b + 5) = [0]] \Rightarrow b = 3, b = -5$.
	$\Rightarrow (x - 14)^2 + (y - 3)^2 = 100 \text{ and } (x + 2)^2 + (y + 5)^2 = 100$	A1	
	Alternative Method 1 for the first 3 marks:		
	Make a or b the subject from a circle centre (a, b) using A or B	M1	E.g. $b = \sqrt{100 - (y - 3)^2} + 4$ from circle through A . These equations may have been found in part (a).
	Form an equation in a or b only	M1	Substitute <i>their</i> a or b into their second circle equation.
	Simplify to a quadratic in a or b	DM1	Expect $a^2 - 12a - 28 = 0$ or $b^2 + 2b - 15 = 0$, OE.
	Alternative Method 2 for the first 3 marks:		
	Obtaining CM (C , centre; M , mid-point of AB)	M1	Expect $\sqrt{80}$. Must be clear this is CM , not AB .
	Using the triangle CMT , where CT is parallel to the x -axis, to find the vertical distance of C from M , MT	DM1	Expect $MT = 4$.
	Using the triangle CMT , where MT is parallel to the y -axis, to find the horizontal distance of C from M , CT	DM1	Expect $CT = 8$.
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