More Functions

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Lazy Evaluation

Arguments to functions are evaluated *lazily*, so they are evaluated only as needed.

```
f <- function(a, b) {
        a^2
}
f(2)
```

This function never actually uses the argument `b`, so calling `f(2)` will not produce an error because the 2 gets positionally matched to `a`.

Lazy Evaluation

Another example

```
f <- function(a, b) {
        print(a)
        print(b)
}

> f(45)
[1] 45
Error in print(b) : argument "b" is missing, with no default
>
```

Notice that “45” got printed first before the error was triggered. This is because `b` did not have to be evaluated until after `print(a)`. Once the function tried to evaluate `print(b)` it had to throw an error.

The "..." Argument

The `...` argument indicate a variable number of arguments that are usually passed on to other functions.

- `...` is often used when extending another function and you don't want to copy the entire argument list of the original function

```
myplot <- function(x, y, type = "l", ...) {
        plot(x, y, type = type, ...)
}
```

- Generic functions use `...` so that extra arguments can be passed to methods (more on this later).

```
> mean
function (x, ...)
UseMethod("mean")
```

The "..." Argument

The `...` argument is also necessary when the number of arguments passed to the function cannot be known in advance.

```
> args(paste)
function (..., sep = " ", collapse = NULL)

> args(cat)
function (..., file = "", sep = " ", fill = FALSE,
    labels = NULL, append = FALSE)
```

Arguments Coming After the "..." Argument

One catch with ... is that any arguments that appear *after* ... on the argument list must be named explicitly and cannot be partially matched.

```
> args(paste)
function (..., sep = " ", collapse = NULL)

> paste("a", "b", sep = ":")
[1] "a:b"

> paste("a", "b", se = ":")
[1] "a b :"
```

A Diversion on Binding Values to Symbol

How does R know which value to assign to which symbol? When I type

```
> lm <- function(x) { x * x }
> lm
function(x) { x * x }
```

how does R know what value to assign to the symbol `lm`? Why doesn't it give it the value of `lm` that is in the **stats** package?

A Diversion on Binding Values to Symbol

When R tries to bind a value to a symbol, it searches through a series of `environments` to find the appropriate value. When you are working on the command line and need to retrieve the value of an R object, the order is roughly

1. Search the global environment for a symbol name matching the one requested.
2. Search the namespaces of each of the packages on the search list

The search list can be found by using the `search` function.

```
> search()
[1] ".GlobalEnv"        "package:stats"     "package:graphics"
[4] "package:grDevices" "package:utils"     "package:datasets"
[7] "package:methods"   "Autoloads"         "package:base"
```

Binding Values to Symbol

- The *global environment* or the user's workspace is always the first element of the search list and the **base** package is always the last.
- The order of the packages on the search list matters!
- User's can configure which packages get loaded on startup so you cannot assume that there will be a set list of packages available.
- When a user loads a package with `library` the namespace of that package gets put in position 2 of the search list (by default) and everything else gets shifted down the list.
- Note that R has separate namespaces for functions and non-functions so it's possible to have an object named `c` and a function named `c`.

Scoping Rules

The scoping rules for R are the main feature that make it different from the original S language.

- The scoping rules determine how a value is associated with a free variable in a function
- R uses *lexical scoping* or *static scoping*. A common alternative is *dynamic scoping*.
- Related to the scoping rules is how R uses the *search list* to bind a value to a symbol
- Lexical scoping turns out to be particularly useful for simplifying statistical computations

Lexical Scoping

Consider the following function.

```
f <- function(x, y) {
        x^2 + y / z
}
```

This function has 2 formal arguments `x` and `y`. In the body of the function there is another symbol `z`. In this case `z` is called a *free variable*.
The scoping rules of a language determine how values are assigned to free variables. Free variables are not formal arguments and are not local variables (assigned insided the function body).

Lexical Scoping

Lexical scoping in R means that

> *the values of free variables are searched for in the environment in which the function was defined.*

What is an environment?

- An *environment* is a collection of (symbol, value) pairs, i.e. `x` is a symbol and `3.14` might be its value.
- Every environment has a parent environment; it is possible for an environment to have multiple “children”
- the only environment without a parent is the empty environment
- A function + an environment = a *closure* or *function closure*.

Lexical Scoping

Searching for the value for a free variable:

- If the value of a symbol is not found in the environment in which a function was defined, then the search is continued in the *parent environment*.
- The search continues down the sequence of parent environments until we hit the *top-level environment*; this usually the global environment (workspace) or the namespace of a package.
- After the top-level environment, the search continues down the search list until we hit the *empty environment*.
- If a value for a given symbol cannot be found once the empty environment is arrived at, then an error is thrown.

Lexical Scoping

Why does all this matter?

- Typically, a function is defined in the global environment, so that the values of free variables are just found in the user's workspace
- This behavior is logical for most people and is usually the “right thing” to do
- However, in R you can have functions defined *inside other functions*
    - Languages like C don't let you do this
- Now things get interesting — In this case the environment in which a function is defined is the body of another function!

Lexical Scoping

```
make.power <- function(n) {
        pow <- function(x) {
                x^n
        }
        pow
}
```

This function returns another function as its value.

```
> cube <- make.power(3)
> square <- make.power(2)
> cube(3)
[1] 27
> square(3)
[1] 9
```

Exploring a Function Closure

What's in a function's environment?

```
> ls(environment(cube))
[1] "n"   "pow"
> get("n", environment(cube))
[1] 3

> ls(environment(square))
[1] "n"   "pow"
> get("n", environment(square))
[1] 2
```

Lexical vs. Dynamic Scoping

```
y <- 10

f <- function(x) {
        y <- 2
        y^2 + g(x)
}

g <- function(x) {
        x * y
}
```

What is the value of

```
f(3)
```

Lexical vs. Dynamic Scoping

- With lexical scoping the value of `y` in the function `g` is looked up in the environment in which the function was defined, in this case the global environment, so the value of `y` is 10.
- With dynamic scoping, the value of `y` is looked up in the environment from which the function was *called* (sometimes referred to as the *calling environment*).
    - In R the calling environment is known as the *parent frame*

  So the value of `y` would be 2.

Lexical vs. Dynamic Scoping

When a function is *defined* in the global environment and is subsequently *called* from the global environment, then the defining environment and the calling environment are the same. This can sometimes give the appearance of dynamic scoping.

```
> g <- function(x) {
+          a <- 3
+          x + a + y
+ }
> g(2)
Error in g(2) : object "y" not found
> y <- 3
> g(2)
[1] 8
```

Other Languages

Other languages that support lexical scoping

- Scheme
- Perl
- Python
- Common Lisp (all languages converge to Lisp)

Consequences of Lexical Scoping

- In R, all objects must be stored in memory
- All functions must carry a pointer to their respective defining environments, which could be anywhere

Application: Optimization

Why is any of this information useful?

- Optimization routines in R like `optim`, `nlm`, and `optimize` require you to pass a function whose argument is a vector of parameters (e.g. a log-likelihood)
- However, an object function might depend on a host of other things besides its parameters (like *data*)
- When writing software which does optimization, it may be desirable to allow the user to hold certain parameters fixed

Maximizing a Normal Likelihood

Write a "constructor" function

```
make.NegLogLik <- function(data) {
        function(mu) {
                -sum(dnorm(data, mean = mu, sd = 1, log = TRUE))
        }
}
```

Note: Optimization functions in R *minimize* functions, so you need to use the negative log-likelihood.

Maximizing a Normal Likelihood

```
> set.seed(1)
> x <- rnorm(100, 6)
> nLL <- make.NegLogLik(x)
> nLL

function(mu) {
                -sum(dnorm(data, mean = mu, sd = 1, log = TRUE))
        }
<environment: 0x7fe78543f540>
```

Estimating Parameters

```
> nLL(3)

[1] 615.0876

> nLL(5)

[1] 193.3101

> nLL(10)

[1] 888.8665

> optimize(nLL, c(1, 10))

$minimum
[1] 6.108887
```

Plotting the (Negative) Log-Likelihood

One problem is that the `nLL()` function is not *vectorized*

```
> nLL(1:5)

[1] 718.8763
```

This is easily solved with the `Vectorize()` function!

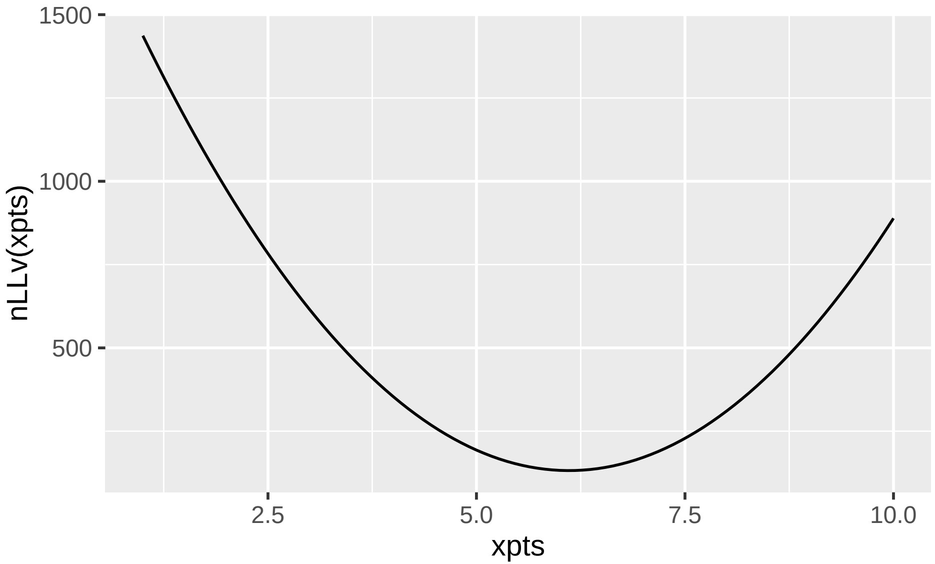
```
> nLLv <- Vectorize(nLL)
> nLLv(1:5)

[1] 1436.8651  975.9763  615.0876  354.1989  193.3101
```

Now we can plot

```
> xpts <- seq(1, 10, len = 100)
> library(ggplot2)
> qplot(xpts, nLLv(xpts), geom = "line")
```

Plotting the (Negative) Log-Likelihood



Lexical Scoping Summary

- Objective functions can be "built" which contain all of the necessary data for evaluating the function
- No need to carry around long argument lists — useful for interactive and exploratory work.
- Code can be simplified and cleand up
- Reference: Robert Gentleman and Ross Ihaka (2000). "Lexical Scope and Statistical Computing," *JCGS*, 9, 491–508.