

Programming #3

CS 545: Machine Learning

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Algorithm #1: K-Means clustering

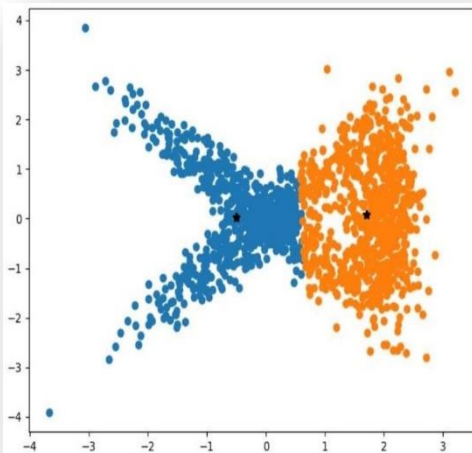
In this experiment, standard version of k-means algorithm is implemented. The initial centers(centroids) of 'k' clusters are randomly chosen from the dataset.

For a fixed 'k' value, This algorithm runs for 'r' number of times. For each of this 'r' we randomly chosen 'k' number of points (initial cluster centers). The sum-square-error is calculated for each 'r' and finally we select one model that gives minimum sum-square-error, for that 'k'. (here r value is taken as 10)

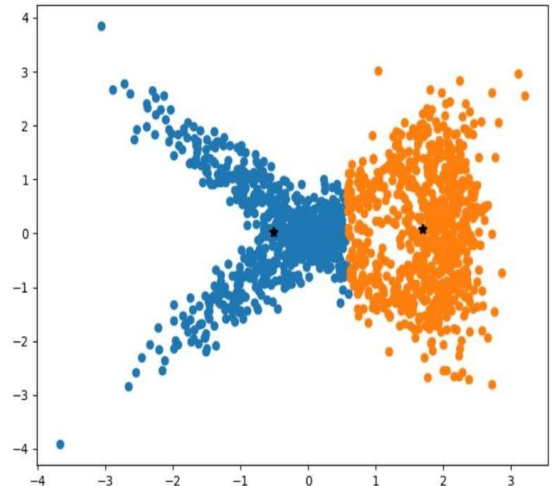
Observations:

1. Number of Clusters (k) = 2:

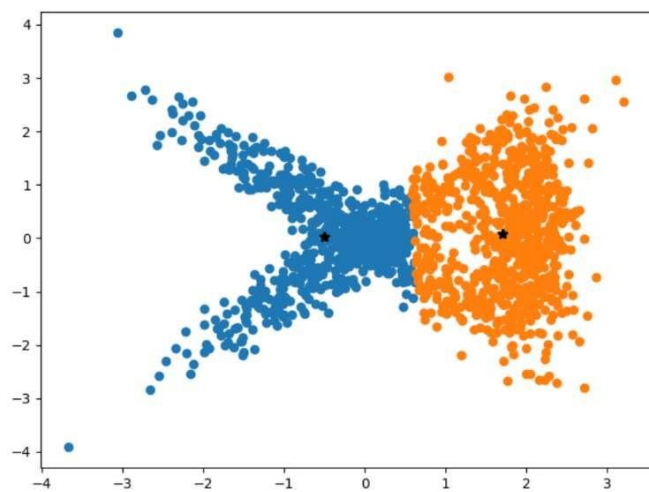
r=1



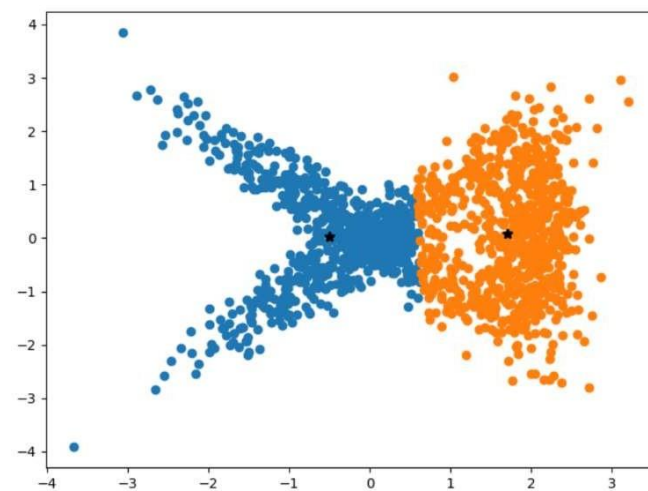
r=2



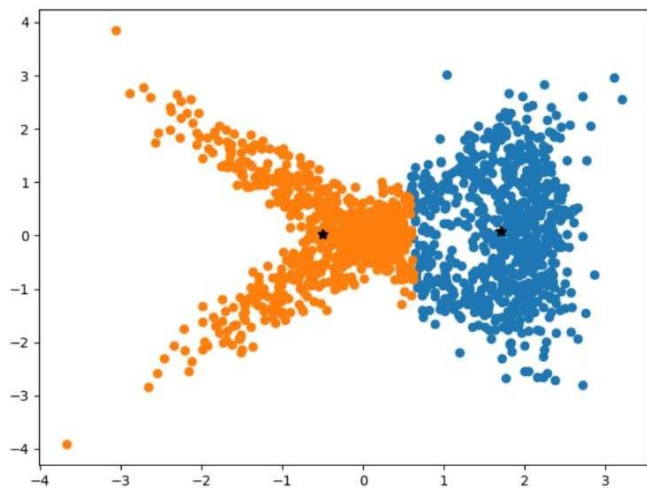
$r = 3$



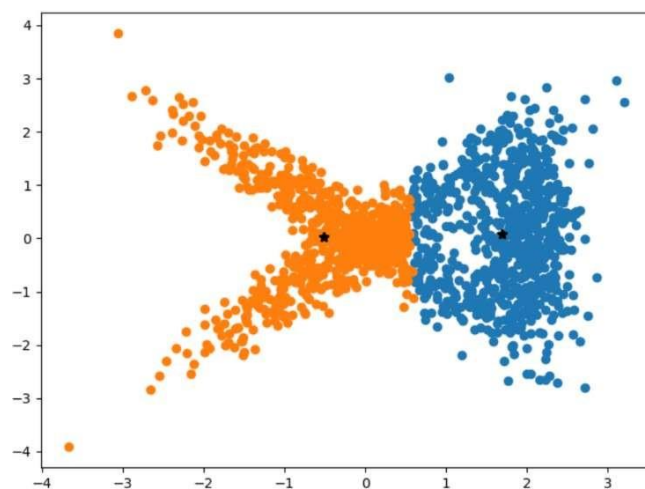
$r = 4$



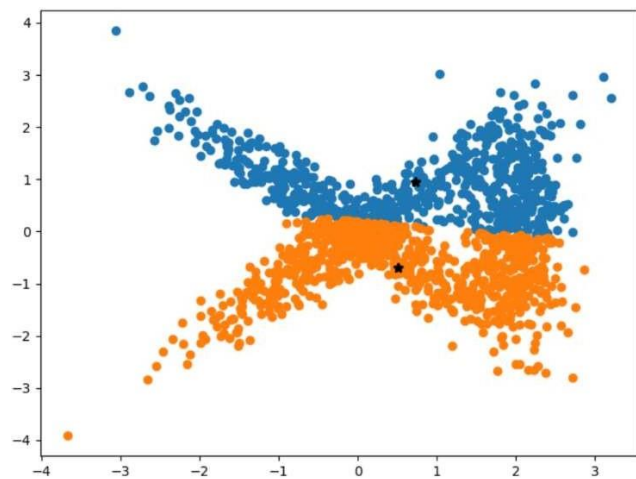
$r = 5$



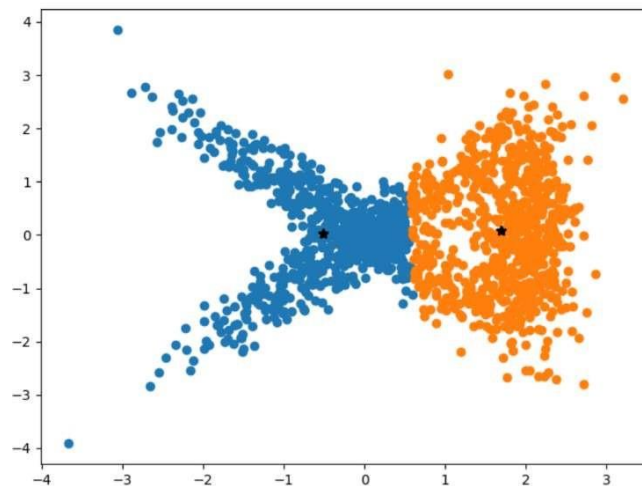
$r = 6$



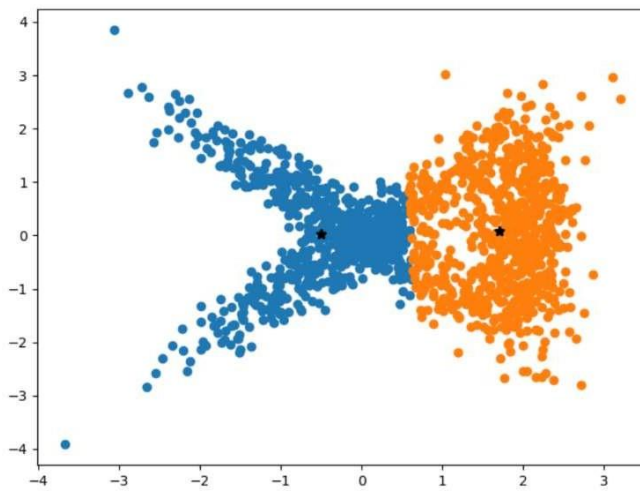
$r = 7$



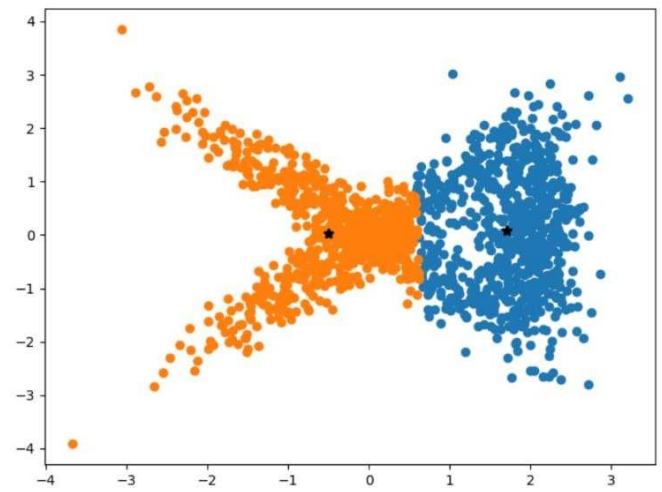
$r = 8$



r = 9



r = 10

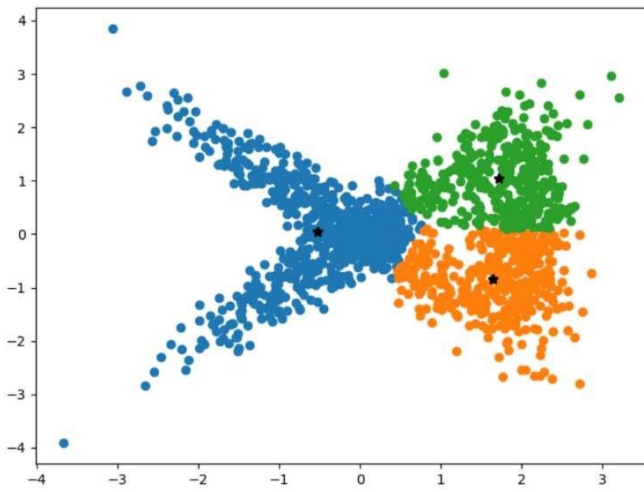


Errors for K=2

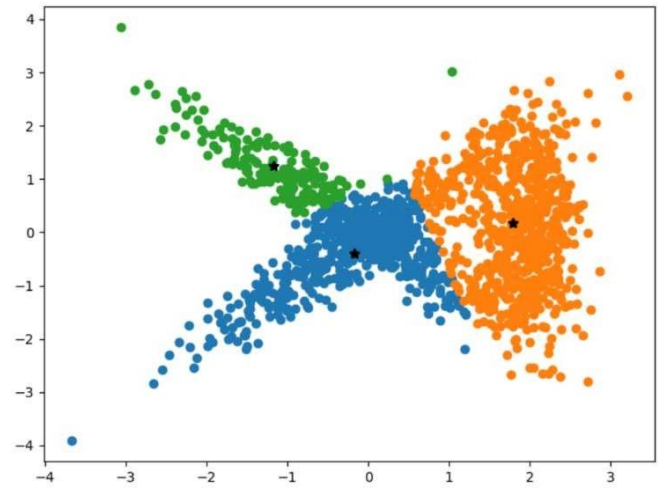
```
errors = [2168.2788438938355, 2171.001969681453, 2171.001969681462, 2171.001969681453, 2171.001969681453, 2168.278843893843,  
2171.001969681462, 2171.001969681453, 2171.001969681453, 2171.001969681453]  
min error when r = 1  
error = 2168.2788438938355
```

2. Number of Clusters $K = 3$

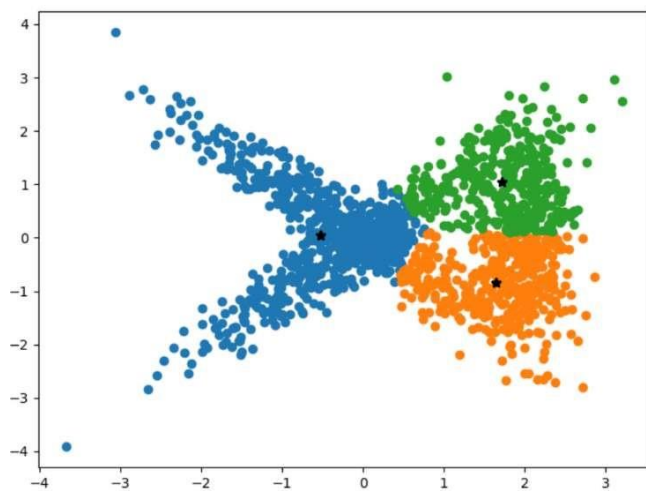
$r = 1$



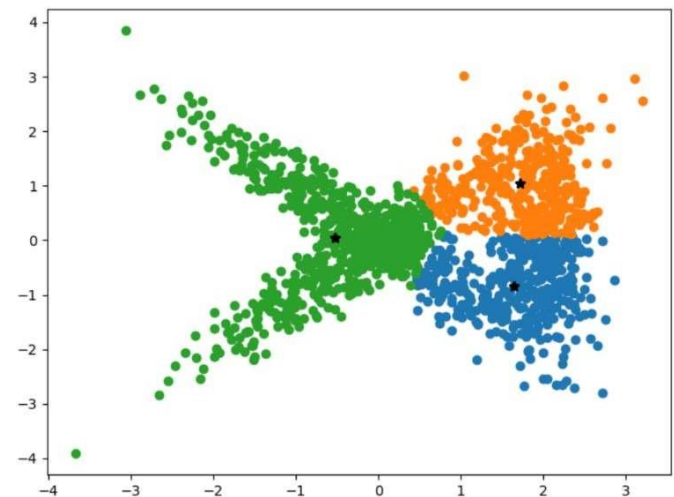
$r = 2$



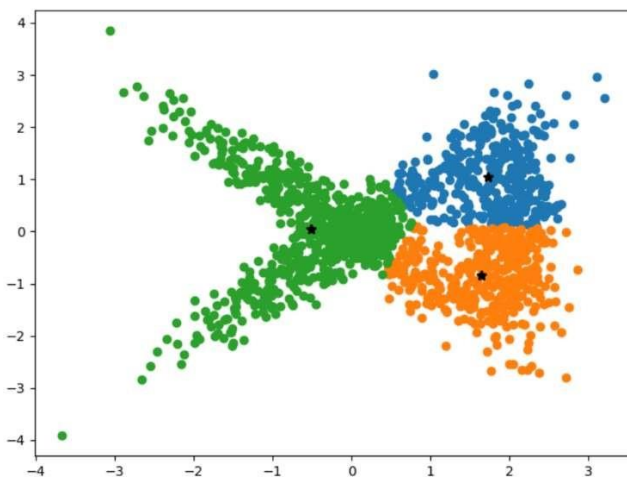
$r = 3$



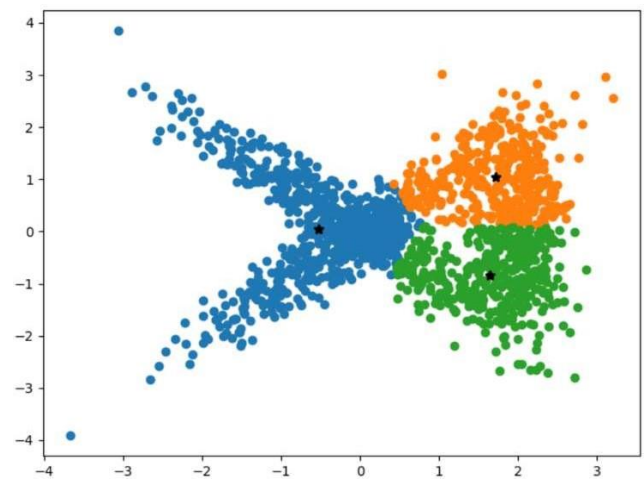
$r = 4$



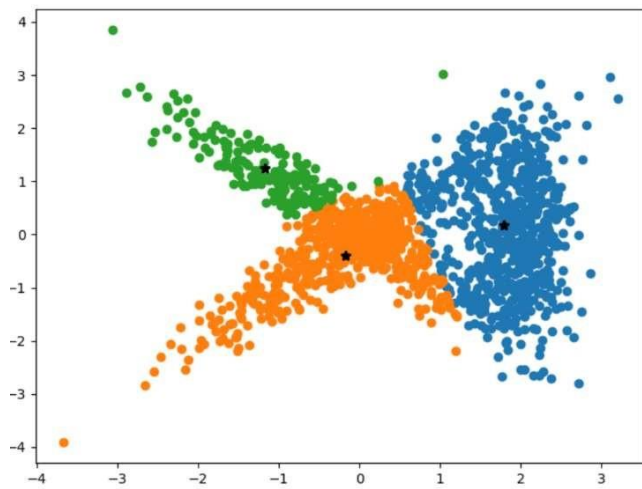
$r = 5$



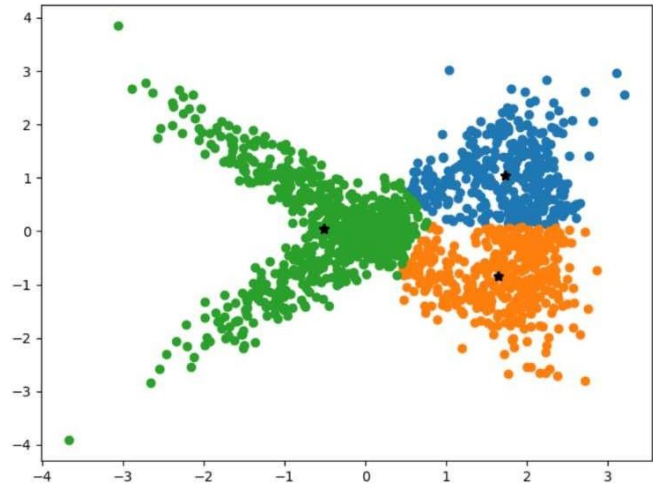
$r = 6$



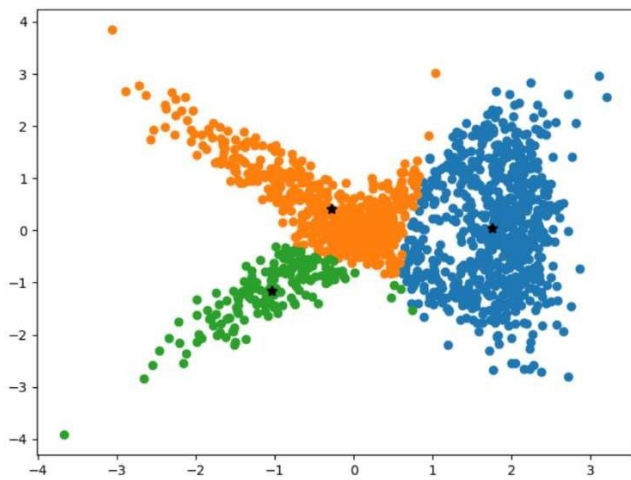
r = 7



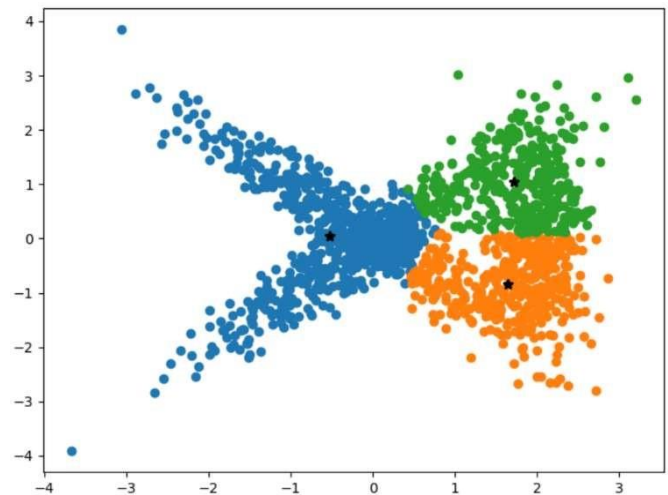
r = 8



r = 9



r = 10



Errors for K=3

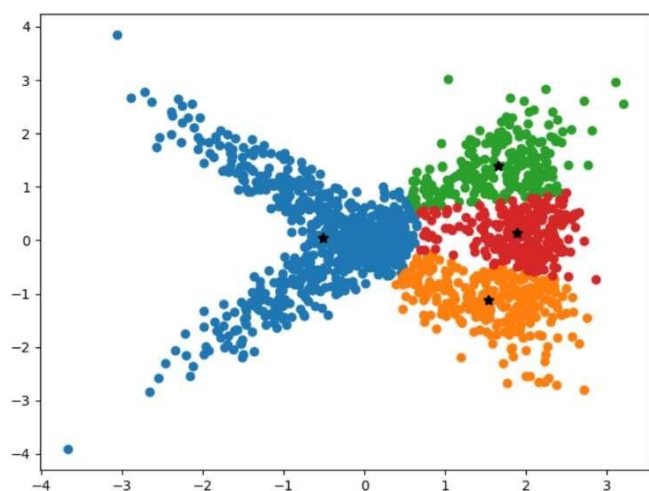
errors = [1912.9394977223042, 1479.5970650234513, 1478.4278229881193, 1912.939497722299, 1603.7708155559499, 1915.8717614424424, 1478.4278229881165, 1478.4278229881143, 1479.5970650234558, 1912.939497722298]

min error when r = 8

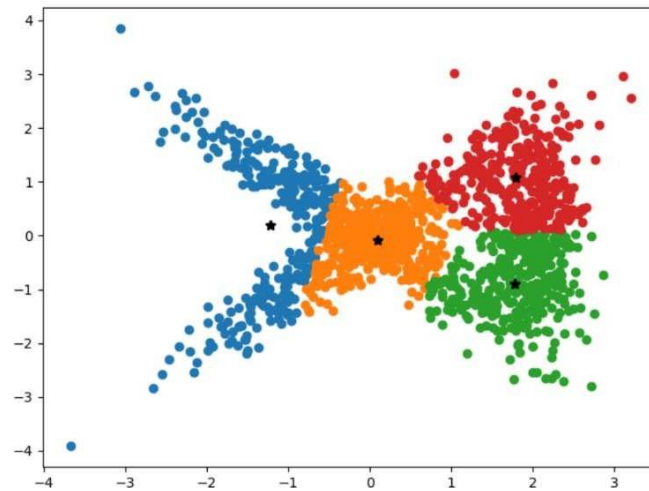
error = 1478.4278229881143

3) Number of clusters $K = 4$

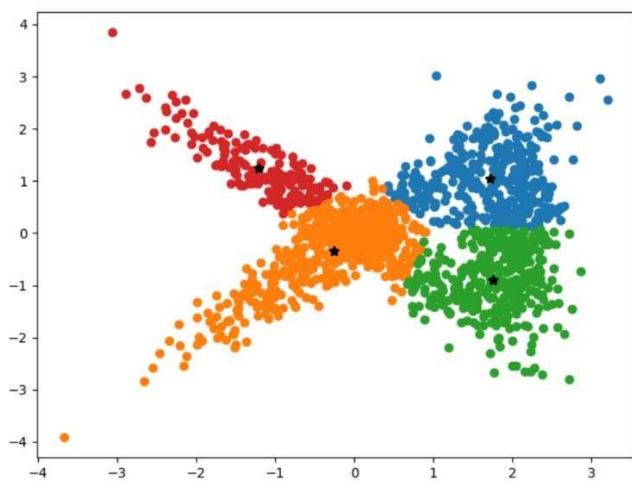
$r = 1$



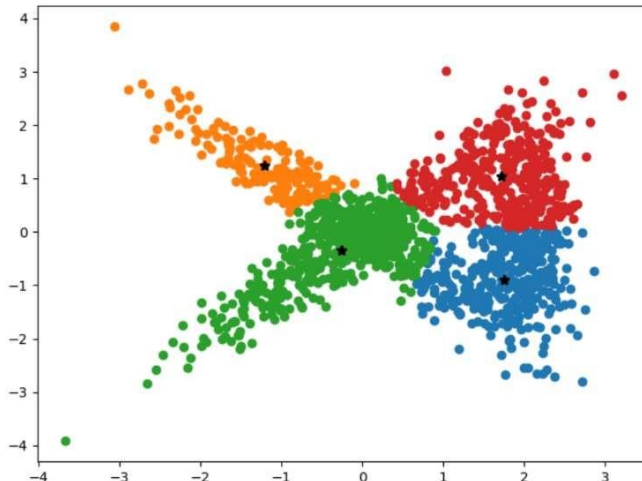
$r = 2$



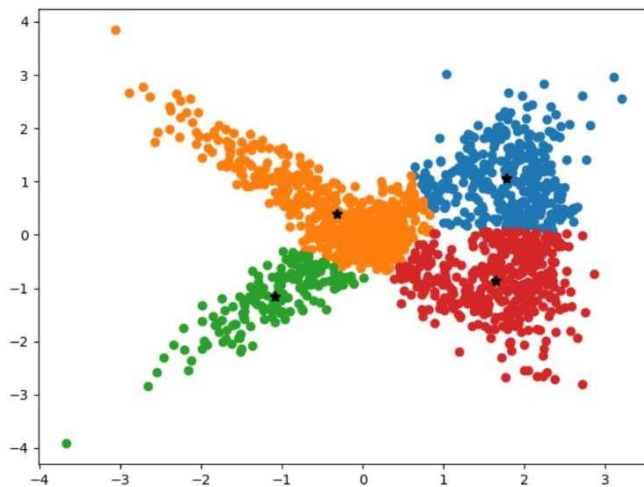
$r = 3$



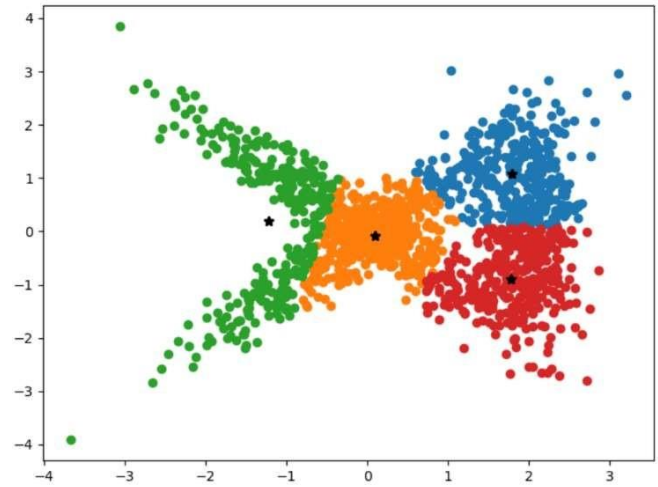
$r = 4$



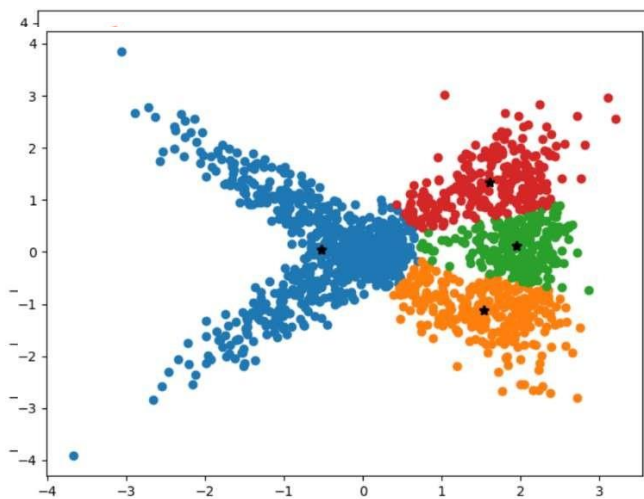
r = 5



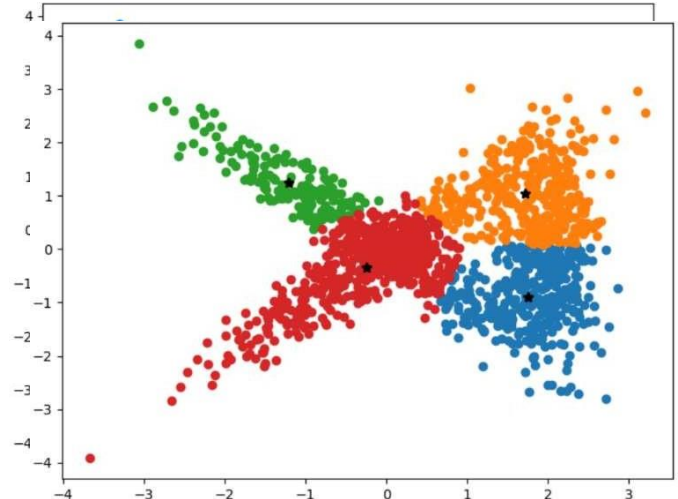
r = 6



r = 7



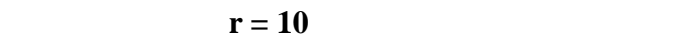
r = 8



r = 9



r = 10



Errors for K=4

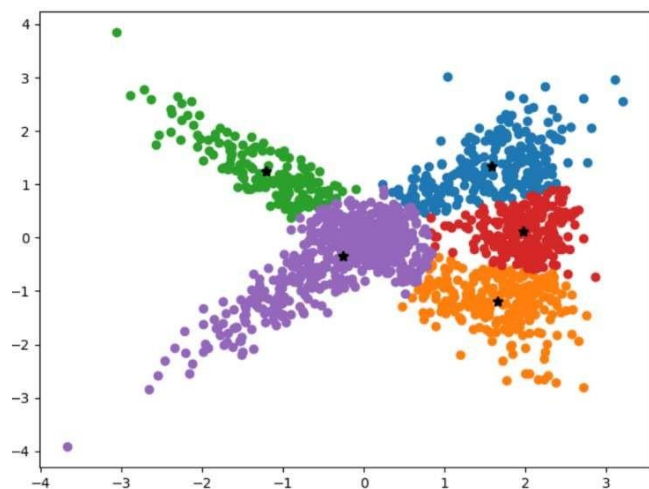
```
errors = [1324.9651675045973, 1324.9651675045986, 1422.177645088136, 1420.470317927065, 1422.177645088134, 1293.5101463478609, 1295.423959311399, 1325.0257551100406, 1422.177645088134, 1303.828957173732]
```

min error when r = 6

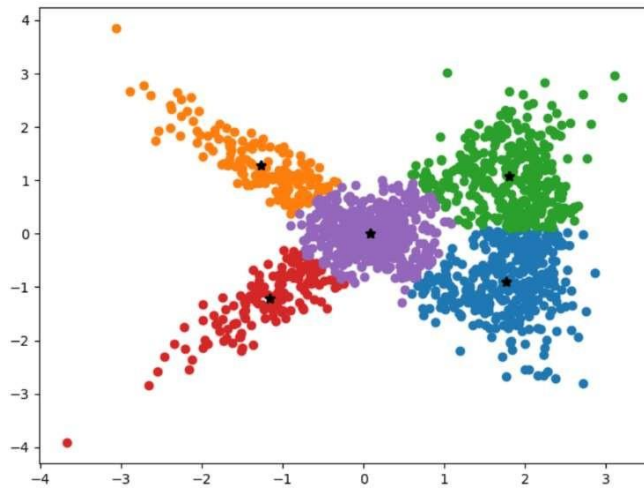
error = 1293.5101463478609

4) Number of Clusters $k = 5$

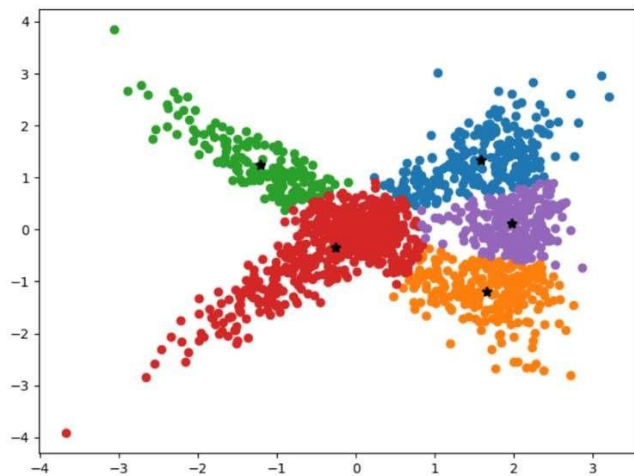
$r = 1$



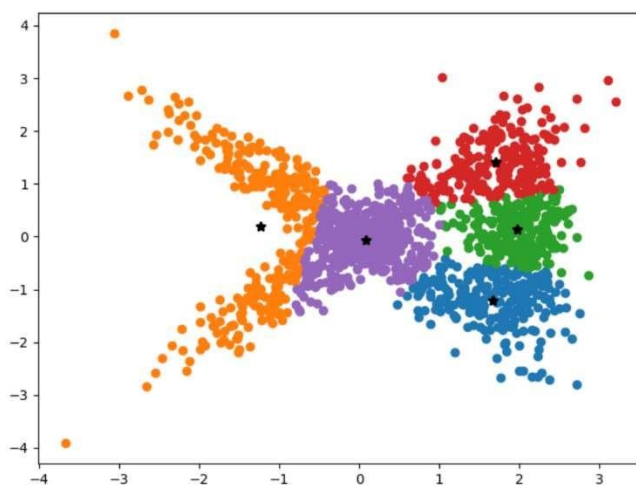
$r = 2$



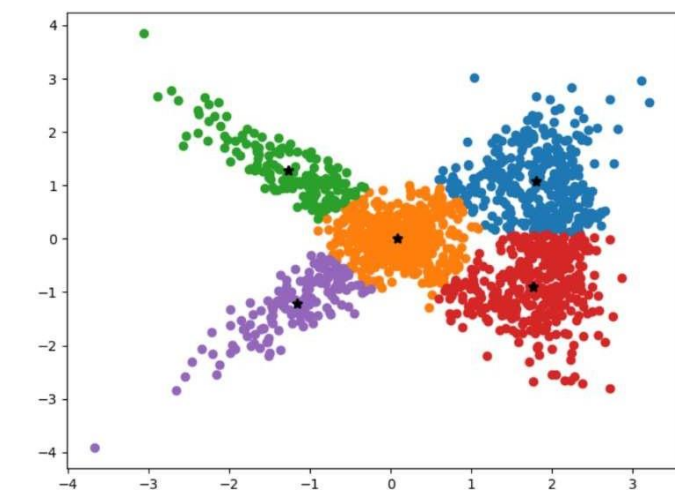
$r = 3$



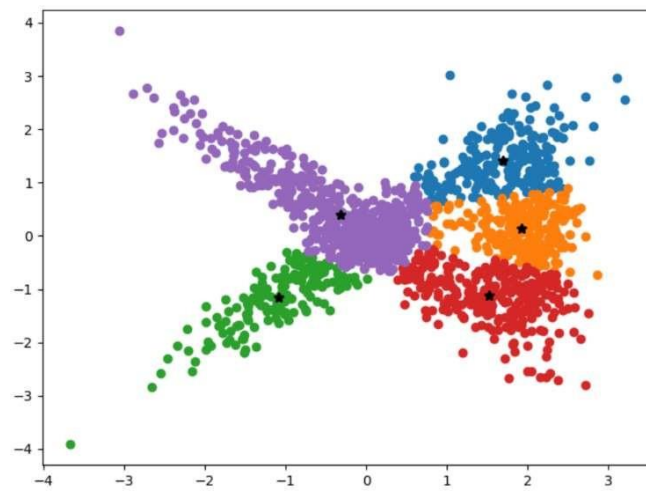
$r = 4$



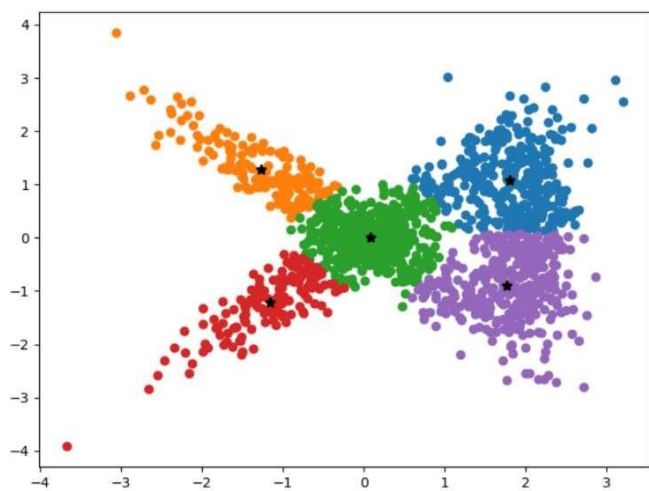
$r = 5$



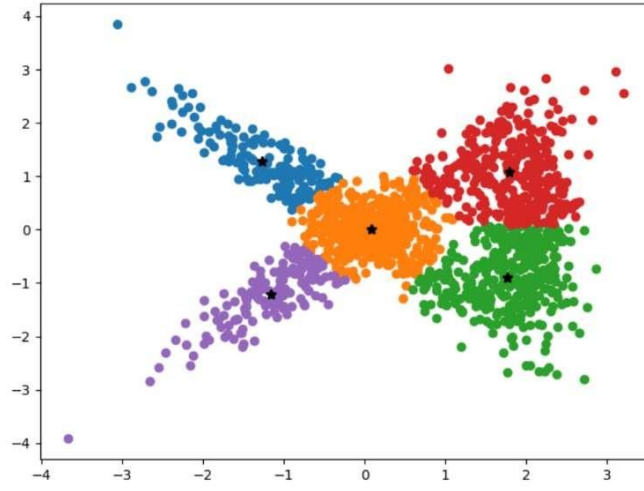
$r = 6$



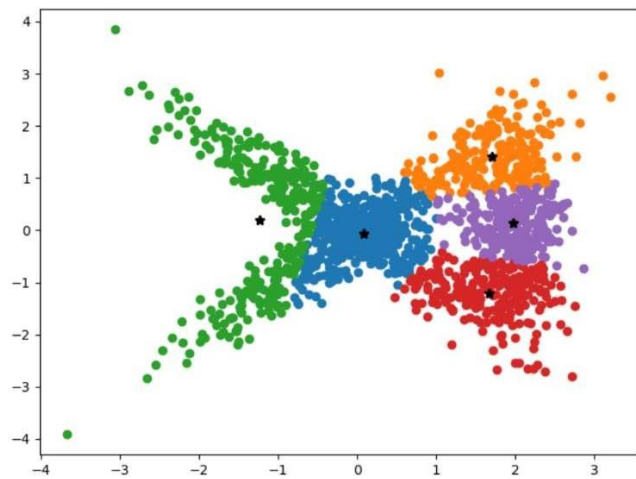
$r = 7$



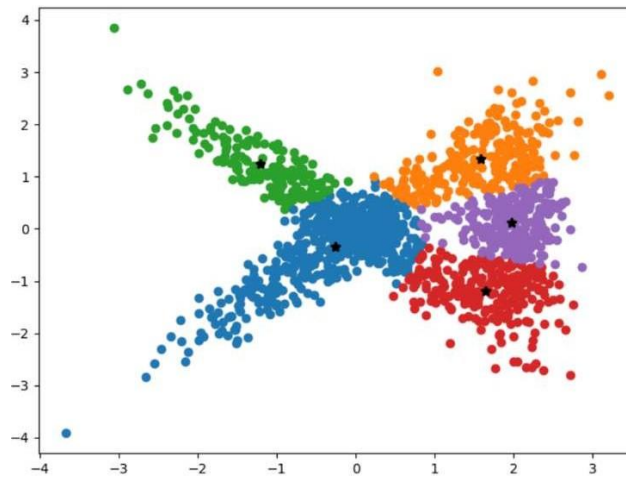
$r = 8$



$r = 9$



$r = 10$



Errors for K=5

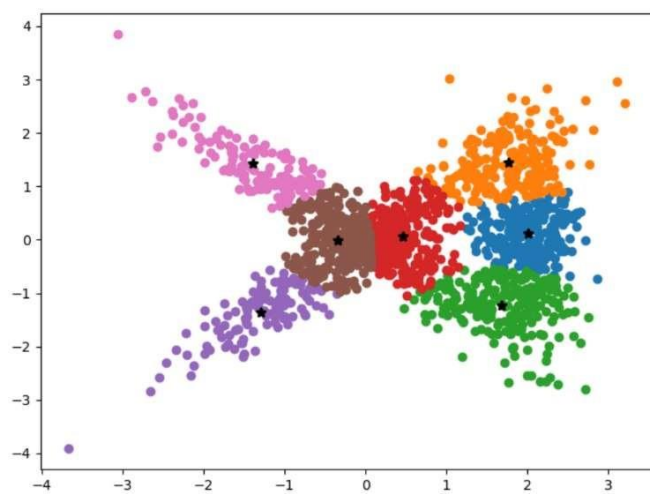
```
errors = [638.2989423487169, 1147.533249115753, 780.235642801088, 780.2356428010883, 1147.533249115754, 638.298942348717, 779.9152903382285, 1147.5332491157521, 1288.4819711122952, 1147.5332491157512]
```

```
min error when r = 1
```

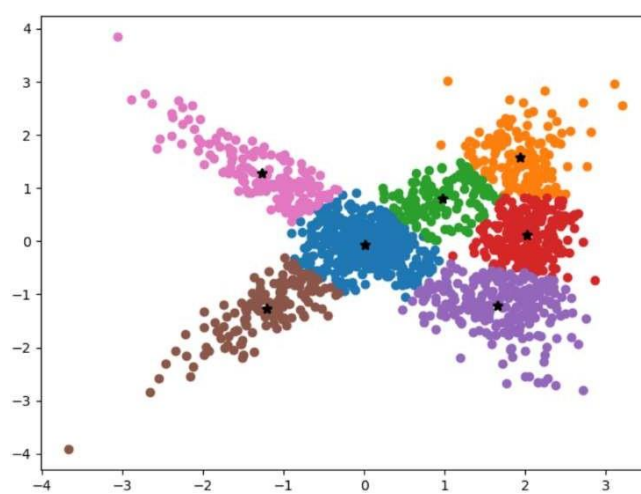
```
error = 638.2989423487169
```

5) Number of clusters $k = 7$

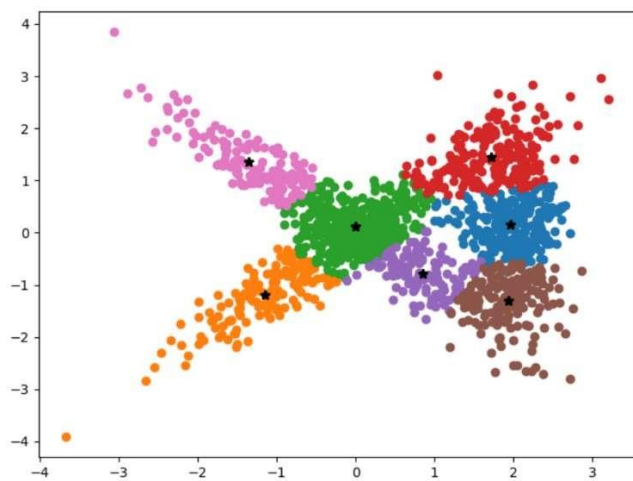
$r = 1$



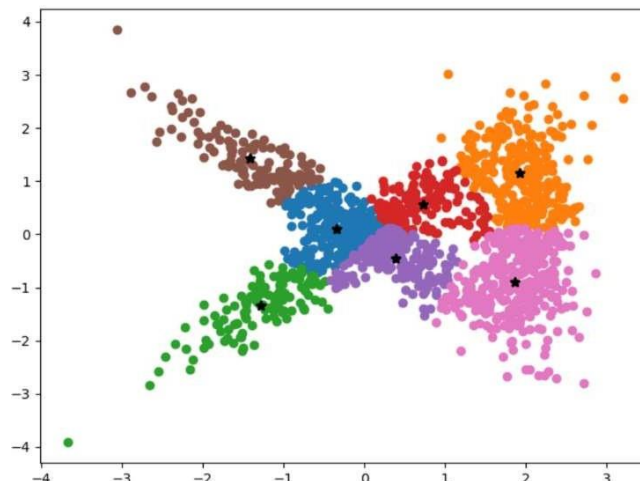
$r = 2$



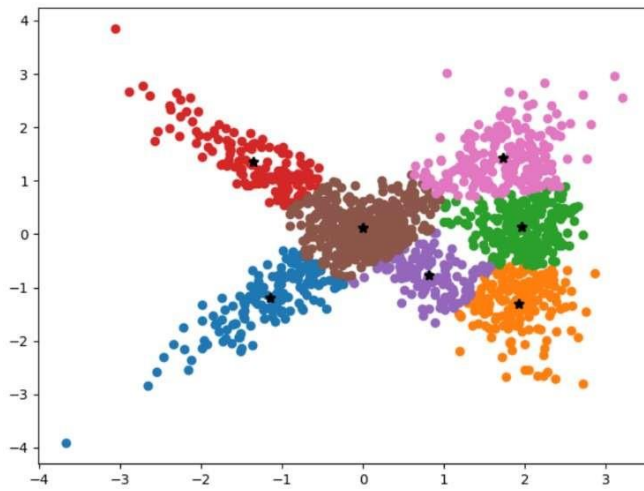
$r = 3$



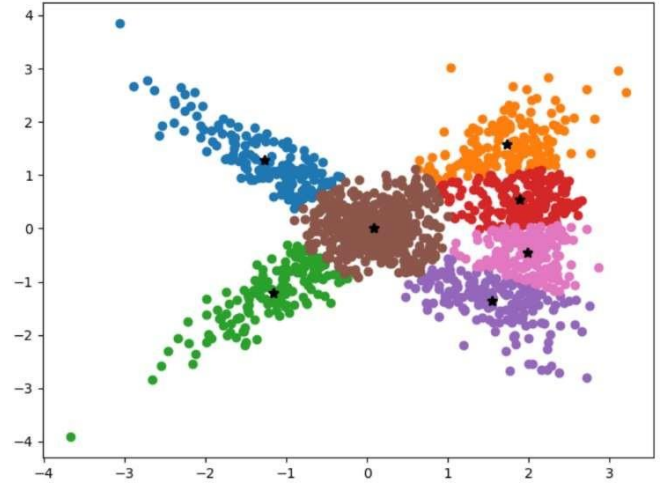
$r = 4$



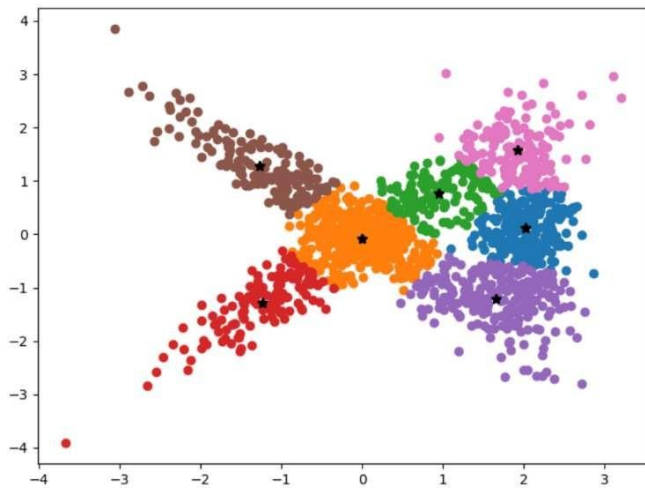
$r = 5$



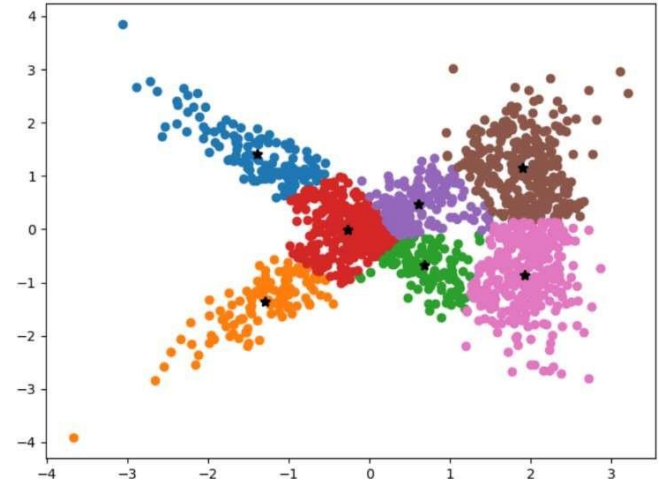
$r = 6$



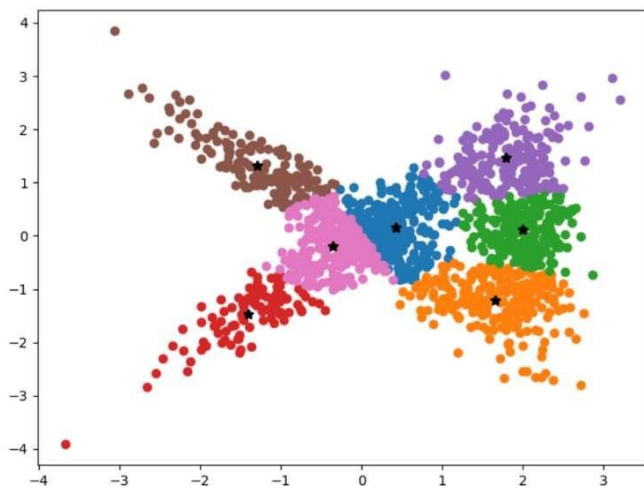
$r = 7$



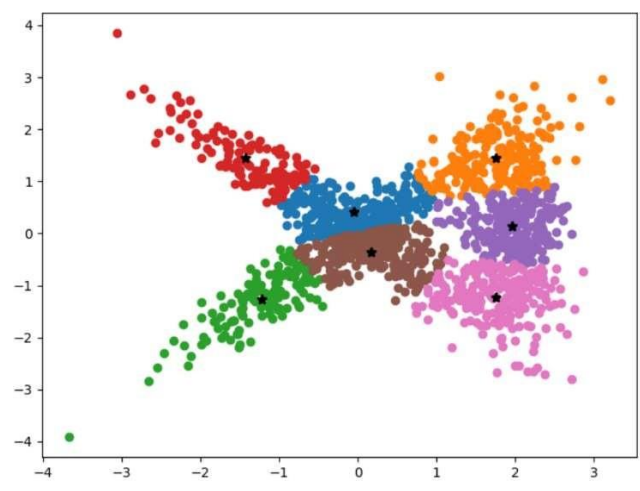
$r = 8$



$r = 9$



$r = 10$



Errors for K=7

```
errors = [501.7170080682313, 613.35147061806, 566.8367585057923, 501.2878001639502, 617.7675609600572, 617.751406587475, 500.66599491088806, 610.4280482387062, 617.4867824312614, 617.751406587476]  
min error when r = 7  
error = 500.66599491088806
```

For different 'K' values (k = 2 to 7). And for each 'k' value it is run for 'r' (10)times. Below table shows selected models sum-square-error for each 'k' value and 'r' value at which that model occurred.

K Value	Minimum Sum-Square Error	Model occurred at 'r'
K = 2	2168.278	5
K = 3	1478.427	1
K = 4	810.717	5
K = 5	638.298	6
K = 6	627.896	4
K = 7	500.78	7