# Social network Graph Link Prediction - Facebook Challenge

#### **Problem statement:**

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

#### **Data Overview**

Taken data from facebook's recruting challenge on kaggle <a href="https://www.kaggle.com/c/FacebookRecruiting">https://www.kaggle.com/c/FacebookRecruiting</a>

data contains two columns source and destination eac edge in graph

```
Data columns (total 2 columns):source_node int64destination node int64
```

### Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos :
  - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
  - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf

- https://kaggle2.blob.core.windows.net/forum-messageattachments/2594/supervised link prediction.pdf
- https://www.youtube.com/watch?v=2M77Hgy17cg

#### **Business objectives and constraints:**

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

#### **Performance metric for supervised learning:**

- Both precision and recall is important so F1 score is good choice
- Confusion matrix

```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xgboost: pip3 install xgboost
```

```
import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
In [2]: #reading graph
        if not os.path.isfile('data/after eda/train woheader.csv'):
            traincsv = pd.read csv('data/train.csv')
            print(traincsv[traincsv.isna().any(1)])
            print(traincsv.info())
            print("Number of diplicate entries: ",sum(traincsv.duplicated()))
            traincsv.to csv('data/after eda/train woheader.csv',header=False,in
        dex=False)
            print("saved the graph into file")
        else:
            g=nx.read edgelist('data/after eda/train woheader.csv',delimiter=
        ',',create using=nx.DiGraph(),nodetype=int)
            print(nx.info(g))
        Name:
        Type: DiGraph
        Number of nodes: 1862220
        Number of edges: 9437519
        Average in degree:
                             5.0679
        Average out degree: 5.0679
              Displaying a sub graph
In [3]: if not os.path.isfile('train woheader sample.csv'):
            pd.read csv('data/train.csv', nrows=50).to csv('train woheader samp
        le.csv',header=False,index=False)
        subgraph=nx.read edgelist('train woheader sample.csv',delimiter=',',cre
```

```
ate_using=nx.DiGraph(),nodetype=int)
# https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with
-networkx-and-matplotlib

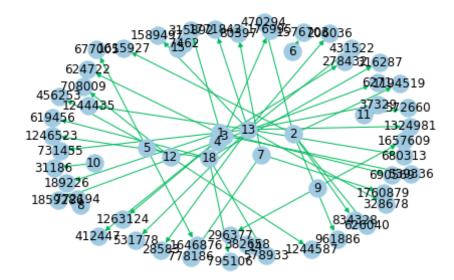
pos=nx.spring_layout(subgraph)
nx.draw(subgraph,pos,node_color='#A0CBE2',edge_color='#00bb5e',width=1,
edge_cmap=plt.cm.Blues,with_labels=True)
plt.savefig("graph_sample.pdf")
print(nx.info(subgraph))
```

Name:

Type: DiGraph

Number of nodes: 66 Number of edges: 50

Average in degree: 0.7576 Average out degree: 0.7576



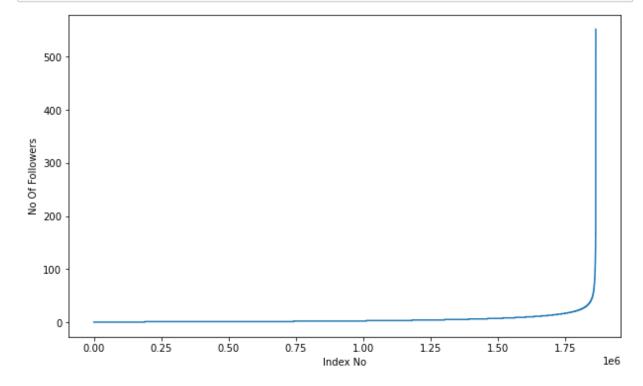
# 1. Exploratory Data Analysis

```
In [4]: # No of Unique persons
print("The number of unique persons",len(g.nodes()))
```

The number of unique persons 1862220

## 1.1 No of followers for each person

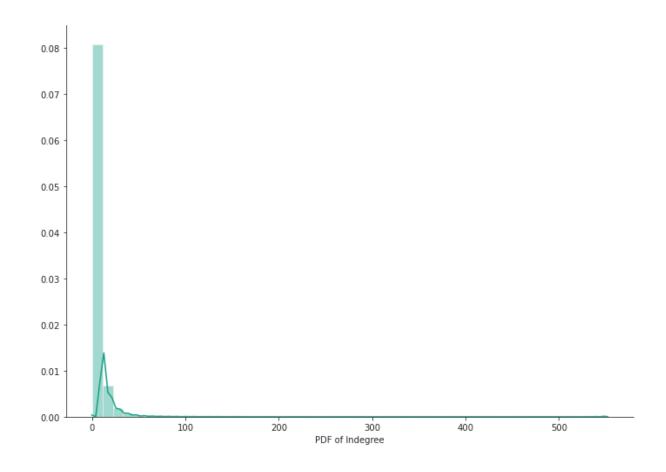
```
In [5]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
```



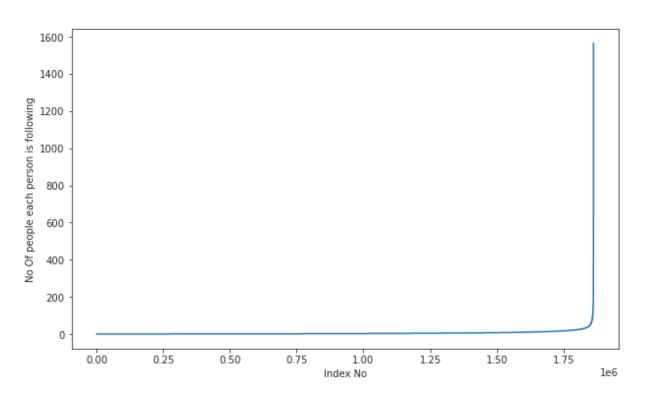
```
In [6]: | indegree_dist = list(dict(g.in_degree()).values())
         indegree_dist.sort()
         plt.figure(figsize=(10,6))
         plt.plot(indegree_dist[0:1500000])
         plt.xlabel('Index No')
         plt.ylabel('No Of Followers')
         plt.show()
            7
            6
            5
          No Of Followers
            2
            1
            0
                                                            1.0
                                                                     1.2
                         0.2
                                  0.4
                                          0.6
                                                   0.8
                                                                              1.4
                0.0
                                                                                     1e6
                                               Index No
In [7]: plt.boxplot(indegree_dist)
         plt.ylabel('No Of Followers')
         plt.show()
```

```
In [8]: ### 90-100 percentile
        for i in range(0,11):
            print(90+i, 'percentile value is', np.percentile(indegree dist, 90+i))
        90 percentile value is 12.0
        91 percentile value is 13.0
        92 percentile value is 14.0
        93 percentile value is 15.0
        94 percentile value is 17.0
        95 percentile value is 19.0
        96 percentile value is 21.0
        97 percentile value is 24.0
        98 percentile value is 29.0
        99 percentile value is 40.0
        100 percentile value is 552.0
        99% of data having followers of 40 only.
In [9]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is', np.percentile(indegree dist,
        99+(i/100))
```

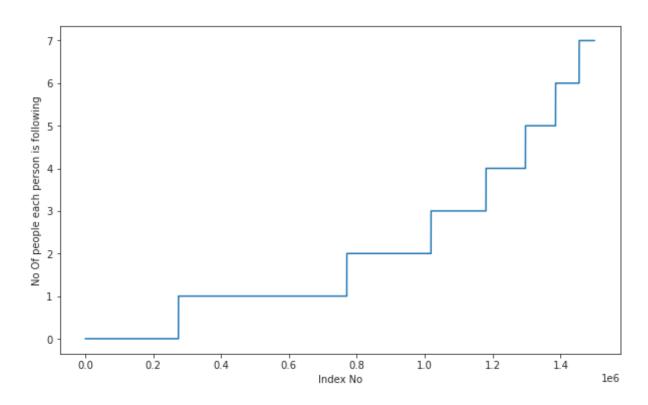
```
99.1 percentile value is 42.0
         99.2 percentile value is 44.0
         99.3 percentile value is 47.0
         99.4 percentile value is 50.0
         99.5 percentile value is 55.0
         99.6 percentile value is 61.0
         99.7 percentile value is 70.0
         99.8 percentile value is 84.0
         99.9 percentile value is 112.0
         100.0 percentile value is 552.0
In [10]: %matplotlib inline
         sns.set style('ticks')
         fig, ax = plt.subplots()
         fig.set size inches(11.7, 8.27)
         sns.distplot(indegree_dist, color='#16A085')
         plt.xlabel('PDF of Indegree')
         sns.despine()
         #plt.show()
```



# 1.2 No of people each person is following



```
In [12]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(outdegree_dist[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following')
    plt.show()
```

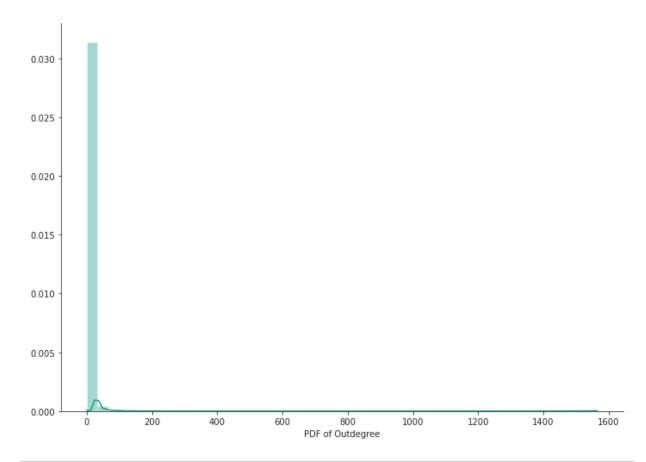


```
In [13]: plt.boxplot(indegree_dist)
   plt.ylabel('No Of people each person is following')
   plt.show()
```

```
No Of people each person is following 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200 - 200
```

```
In [14]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is', np.percentile(outdegree dist, 90+i
         ))
         90 percentile value is 12.0
         91 percentile value is 13.0
         92 percentile value is 14.0
         93 percentile value is 15.0
         94 percentile value is 17.0
         95 percentile value is 19.0
         96 percentile value is 21.0
         97 percentile value is 24.0
         98 percentile value is 29.0
         99 percentile value is 40.0
         100 percentile value is 1566.0
In [15]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(outdegree_dist
          ,99+(i/100)))
         99.1 percentile value is 42.0
         99.2 percentile value is 45.0
```

```
99.3 percentile value is 48.0
99.4 percentile value is 52.0
99.5 percentile value is 56.0
99.6 percentile value is 63.0
99.7 percentile value is 73.0
99.8 percentile value is 90.0
99.9 percentile value is 123.0
100.0 percentile value is 1566.0
In [16]: sns.set_style('ticks')
fig, ax = plt.subplots()
fig.set_size_inches(11.7, 8.27)
sns.distplot(outdegree_dist, color='#16A085')
plt.xlabel('PDF of Outdegree')
sns.despine()
```



No of persons those are not following anyone are 274512 and \$ is 14.741 115442858524

No of persons having zero followers are 188043 and % is 10.097786512871

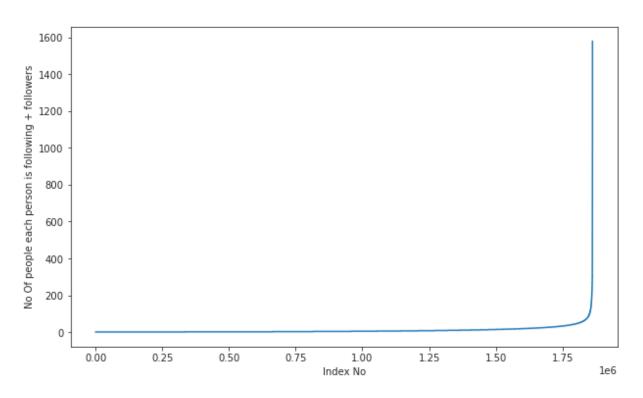
734

No of persons those are not not following anyone and also not having an y followers are  $\boldsymbol{\theta}$ 

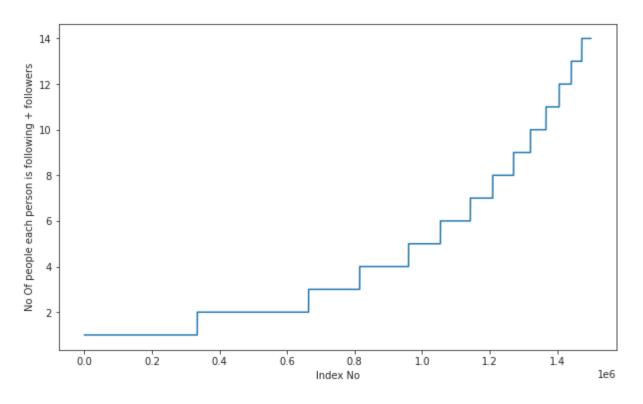
## 1.3 both followers + following

```
In [20]: from collections import Counter
dict_in = dict(g.in_degree())
dict_out = dict(g.out_degree())
d = Counter(dict_in) + Counter(dict_out)
in_out_degree = np.array(list(d.values()))
```

```
In [21]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [22]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [23]: ### 90-100 percentile
for i in range(0,11):
     print(90+i, 'percentile value is',np.percentile(in_out_degree_sort,9
     0+i))

90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
```

```
In [24]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(in out degree
         sort,99+(i/100))
         99.1 percentile value is 83.0
         99.2 percentile value is 87.0
         99.3 percentile value is 93.0
         99.4 percentile value is 99.0
         99.5 percentile value is 108.0
         99.6 percentile value is 120.0
         99.7 percentile value is 138.0
         99.8 percentile value is 168.0
         99.9 percentile value is 221.0
         100.0 percentile value is 1579.0
In [25]: print('Min of no of followers + following is',in out degree.min())
         print(np.sum(in out degree==in out degree.min()),' persons having minim
         um no of followers + following')
         Min of no of followers + following is 1
         334291 persons having minimum no of followers + following
In [26]: print('Max of no of followers + following is',in out degree.max())
         print(np.sum(in out degree==in out degree.max()),' persons having maxim
         um no of followers + following')
         Max of no of followers + following is 1579
         1 persons having maximum no of followers + following
In [271:
         print('No of persons having followers + following less than 10 are',np.
         sum(in out degree<10))</pre>
         No of persons having followers + following less than 10 are 1320326
In [28]: print('No of weakly connected components', len(list(nx.weakly connected
         components(g))))
         count=0
         for i in list(nx.weakly connected components(q)):
```

```
if len(i)==2:
    count+=1
print('weakly connected components wit 2 nodes',count)
```

No of weakly connected components 45558 weakly connected components wit 2 nodes 32195

## 2. Posing a problem as classification problem

# 2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
In [29]: %%time
         ###generating bad edges from given graph
         import random
         if not os.path.isfile('data/after eda/missing edges final.p'):
             #getting all set of edges
             r = csv.reader(open('data/after eda/train woheader.csv','r'))
             edges = dict()
             for edge in r:
                 edges[(edge[0], edge[1])] = 1
             missing edges = set([])
             while (len(missing edges)<9437519):
                 a=random.randint(1, 1862220)
                 b=random.randint(1, 1862220)
                 tmp = edges.get((a,b),-1)
                 if tmp == -1 and a!=b:
                     try:
                         if nx.shortest path length(g,source=a,target=b) > 2:
```

```
missing edges.add((a,b))
                         else:
                              continue
                     except:
                             missing edges.add((a,b))
                 else:
                      continue
             pickle.dump(missing edges,open('data/after eda/missing edges final.
         p','wb'))
         else:
             missing edges = pickle.load(open('data/after eda/missing edges fina
         l.p','rb'))
         CPU times: user 2.04 s, sys: 2.31 s, total: 4.35 s
         Wall time: 4.34 s
In [30]: len(missing edges)
Out[30]: 9437519
```

## 2.2 Training and Test data split:

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

```
In []: from sklearn.model_selection import train_test_split
   if (not os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and (
        not os.path.isfile('data/after_eda/test_pos_after_eda.csv')):
        #reading total data df
        df_pos = pd.read_csv('data/train.csv')
        df_neg = pd.DataFrame(list(missing_edges), columns=['source_node',
        'destination_node'])

        print("Number of nodes in the graph with edges", df_pos.shape[0])
        print("Number of nodes in the graph without edges", df_neg.shape[0])
])
```

```
#Trian test split
    #Spiltted data into 80-20
    #positive links and negative links seperatly because we need positi
ve training data only for creating graph
    #and for feature generation
    X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_spli
t(df pos,np.ones(len(df pos)),test size=0.2, random state=9)
    X train neg, X test neg, y train neg, y test neg = train test spli
t(df neg,np.zeros(len(df neg)),test size=0.2, random state=9)
    print('='*60)
    print("Number of nodes in the train data graph with edges", X train
pos.shape[0], "=", y train pos.shape[0])
    print("Number of nodes in the train data graph without edges", X tr
ain neg.shape[0], "=", y train neg.shape[0])
    print('='*60)
    print("Number of nodes in the test data graph with edges", X test p
os.shape[0], "=", y test pos.shape[0])
    print("Number of nodes in the test data graph without edges", X tes
t neg.shape[0], "=", y test neg.shape[0])
    #removing header and saving
    X train pos.to csv('data/after eda/train pos after eda.csv',header=
False, index=False)
    X test pos.to csv('data/after eda/test pos after eda.csv',header=Fa
lse. index=False)
    X train neg.to csv('data/after eda/train neg after eda.csv',header=
False, index=False)
    X test neg.to csv('data/after eda/test neg after eda.csv',header=Fa
lse. index=False)
else:
    #Graph from Traing data only
    del missing edges
Number of nodes in the graph with edges 9437519
Number of nodes in the graph without edges 9437519
Number of nodes in the train data graph with edges 7550015 = 7550015
Number of nodes in the train data graph without edges 7550015 = 7550015
```

```
Number of nodes in the test data graph with edges 1887504 = 1887504
        Number of nodes in the test data graph without edges 1887504 = 1887504
In [ ]: if (os.path.isfile('data/after eda/train pos after eda.csv')) and (os.p
        ath.isfile('data/after eda/test pos after eda.csv')):
            train graph=nx.read edgelist('data/after eda/train pos after eda.cs
        v',delimiter=',',create using=nx.DiGraph(),nodetype=int)
            test graph=nx.read edgelist('data/after eda/test pos after eda.csv'
         ,delimiter=',',create using=nx.DiGraph(),nodetype=int)
            print(nx.info(train graph))
            print(nx.info(test graph))
            # finding the unique nodes in the both train and test graphs
            train nodes pos = set(train graph.nodes())
            test nodes pos = set(test graph.nodes())
            trY teY = len(train nodes pos.intersection(test nodes pos))
            trY teN = len(train nodes pos - test nodes pos)
            teY trN = len(test nodes pos - train nodes pos)
            print('no of people common in train and test -- ',trY teY)
            print('no of people present in train but not present in test -- ',t
        rY teN)
            print('no of people present in test but not present in train -- ',t
        eY trN)
            print(' % of people not there in Train but exist in Test in total T
        est data are {} %'.format(teY trN/len(test nodes pos)*100))
        Name:
        Type: DiGraph
        Number of nodes: 1780722
        Number of edges: 7550015
        Average in degree:
                             4.2399
        Average out degree: 4.2399
        Name:
        Type: DiGraph
        Number of nodes: 1144623
        Number of edges: 1887504
        Average in degree:
```

```
Average out degree: 1.6490
no of people common in train and test -- 1063125
no of people present in train but not present in test -- 717597
no of people present in test but not present in train -- 81498
% of people not there in Train but exist in Test in total Test data ar
e 7.1200735962845405 %
```

we have a cold start problem here

```
In [ ]: #final train and test data sets
        if (not os.path.isfile('data/after eda/train after eda.csv')) and \
        (not os.path.isfile('data/after eda/test after eda.csv')) and \
        (not os.path.isfile('data/train y.csv')) and \
        (not os.path.isfile('data/test y.csv')) and \
        (os.path.isfile('data/after eda/train pos after eda.csv')) and \
        (os.path.isfile('data/after eda/test pos after eda.csv')) and \
        (os.path.isfile('data/after eda/train neg after eda.csv')) and \
        (os.path.isfile('data/after eda/test neg after eda.csv')):
            X train pos = pd.read csv('data/after eda/train pos after eda.csv',
         names=['source node', 'destination node'])
            X test pos = pd.read csv('data/after eda/test pos after eda.csv', n
        ames=['source node', 'destination node'])
            X train neg = pd.read csv('data/after eda/train neg after eda.csv',
         names=['source node', 'destination node'])
            X test neg = pd.read csv('data/after eda/test neg after eda.csv', n
        ames=['source node', 'destination node'])
            print('='*60)
            print("Number of nodes in the train data graph with edges", X train
        pos.shape[0])
            print("Number of nodes in the train data graph without edges", X tr
        ain neg.shape[0])
            print('='*60)
            print("Number of nodes in the test data graph with edges", X test p
        os.shape[0])
```

```
print("Number of nodes in the test data graph without edges", X tes
t neg.shape[0])
    X train = X train pos.append(X train neg,ignore index=True)
    y_train = np.concatenate((y_train_pos,y train neg))
    X test = X test pos.append(X test neg,ignore index=True)
    y test = np.concatenate((y test pos,y test neg))
    X train.to csv('data/after eda/train after eda.csv',header=False,in
dex=False)
    X test.to csv('data/after eda/test after eda.csv',header=False,inde
x=False)
    pd.DataFrame(y train.astype(int)).to csv('data/train y.csv',header=
False.index=False)
    pd.DataFrame(y test.astype(int)).to csv('data/test y.csv',header=Fa
lse.index=False)
Number of nodes in the train data graph with edges 7550015
Number of nodes in the train data graph without edges 7550015
```

Number of nodes in the test data graph with edges 1887504 Number of nodes in the test data graph without edges 1887504

```
In [ ]: print("Data points in train data",X_train.shape)
    print("Data points in test data",X_test.shape)
    print("Shape of traget variable in train",y_train.shape)
    print("Shape of traget variable in test", y_test.shape)
```

Data points in train data (15100030, 2)
Data points in test data (3775008, 2)
Shape of traget variable in train (15100030,)
Shape of traget variable in test (3775008,)

# Social network Graph Link Prediction - Facebook Challenge

```
In [1]: #Importing Libraries
```

```
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import csv
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xqboost as xqb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore,DataFrame
from pandas import read hdf
from scipy.sparse.linalg import svds, eigs
import qc
from tqdm import tqdm
```

## 1. Reading Data

```
In [2]:
    if os.path.isfile('data/after_eda/train_pos_after_eda.csv'):
        train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.cs
    v',delimiter=',',create_using=nx.DiGraph(),nodetype=int)
```

```
print(nx.info(train_graph))
else:
    print("please run the FB_EDA.ipynb or download the files from driv
e")
```

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

# 2. Similarity measures

#### 2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

$$j = rac{|X \cap Y|}{|X \cup Y|}$$

```
In [4]: #one test case
        print(jaccard for followees(273084,1505602))
        0.0
In [5]: #node 1635354 not in graph
        print(jaccard for followees(273084,1505602))
        0.0
In [6]: #for followers
        def jaccard for followers(a,b):
            try:
                if len(set(train graph.predecessors(a))) == 0 | len(set(g.pred
        ecessors(b))) == 0:
                    return 0
                sim = (len(set(train graph.predecessors(a)).intersection(set(tr
        ain graph.predecessors(b))))/\
                                         (len(set(train_graph.predecessors(a)).
        union(set(train graph.predecessors(b)))))
                return sim
            except:
                return 0
In [7]: print(jaccard for followers(273084,470294))
        0
In [8]: #node 1635354 not in graph
        print(jaccard for followees(669354,1635354))
        0
```

## 2.2 Cosine distance

```
CosineDistance = rac{|X \cap Y|}{|X| \cdot |Y|}
```

```
In [9]: #for followees
         def cosine_for_followees(a,b):
             try:
                 if len(set(train graph.successors(a))) == 0 | len(set(train gr
         aph.successors(b))) == 0:
                     return 0
                 sim = (len(set(train graph.successors(a)).intersection(set(trai
         n graph.successors(b))))/\
                                             (math.sqrt(len(set(train graph.succ
         essors(a)))*len((set(train graph.successors(b))))))
                 return sim
             except:
                 return 0
In [10]: print(cosine_for_followees(273084,1505602))
         0.0
In [11]: print(cosine_for_followees(273084,1635354))
         0
In [12]: def cosine for followers(a,b):
             try:
                 if len(set(train graph.predecessors(a))) == 0 | len(set(train
         graph.predecessors(b)) == 0:
                     return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(tr
         ain graph.predecessors(b))))/\
                                              (math.sqrt(len(set(train graph.pre
         decessors(a))))*(len(set(train graph.predecessors(b)))))
                 return sim
```

```
except:
    return 0

In [13]: print(cosine_for_followers(2,470294))
    0.02886751345948129

In [14]: print(cosine_for_followers(669354,1635354))
    0
```

## 3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link analysis.pagerank alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

## 3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

# 4. Other Graph Features

## 4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [18]: #if has direct edge then deleting that edge and calculating shortest pa
th

def compute_shortest_path_length(a,b):
    p=-1
    try:
    if train_graph.has_edge(a,b):
        train_graph.remove_edge(a,b)
```

## 4.2 Checking for same community

```
In [21]: #getting weekly connected edges from graph
         wcc=list(nx.weakly connected components(train graph))
         def belongs to same wcc(a,b):
             index = []
             if train_graph.has_edge(b,a):
                 return 1
             if train graph.has edge(a,b):
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if (b in index):
                         train graph.remove_edge(a,b)
                         if compute shortest path length(a,b)==-1:
                             train graph.add edge(a,b)
                              return 0
                         else:
```

```
train_graph.add_edge(a,b)
    return 1

else:
    return 0

else:

for i in wcc:
    if a in i:
        index= i
        break

if(b in index):
    return 1

else:
    return 0
```

```
In [22]: belongs_to_same_wcc(861, 1659750)
Out[22]: 0
In [23]: belongs_to_same_wcc(669354,1635354)
Out[23]: 0
```

### 4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x,y) = \sum_{u \in N(x) \cap N(y)} rac{1}{log(|N(u)|)}$$

```
In [24]: #adar index
def calc_adar_in(a,b):
    sum=0
    try:
        n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors(b))))
    if len(n)!=0:
```

```
for i in n:
                         sum=sum+(1/np.log10(len(list(train_graph.predecessors(i
         ))))))
                     return sum
                 else:
                     return 0
             except:
                 return 0
In [25]: calc adar in(1,189226)
Out[25]: 0
In [26]: calc adar in(669354,1635354)
Out[26]: 0
         4.4 Is persion was following back:
In [27]: def follows back(a,b):
             if train graph.has edge(b,a):
                 return 1
             else:
                 return 0
In [28]: follows_back(1,189226)
Out[28]: 1
In [29]: follows back(669354,1635354)
Out[29]: 0
```

4.5 Katz Centrality:

#### https://en.wikipedia.org/wiki/Katz\_centrality

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/ Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

$$x_i = lpha \sum_j A_{ij} x_j + eta,$$

where A is the adjacency matrix of the graph G with eigenvalues

 $\lambda$ 

.

The parameter

 $\beta$ 

controls the initial centrality and

$$\alpha < rac{1}{\lambda_{max}}$$

#### 4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS\_algorithm

```
In [33]: if not os.path.isfile('data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, n
    ormalized=True)
        pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
    else:
        hits = pickle.load(open('data/fea_sample/hits.p','rb'))

In [34]: print('min',hits[0][min(hits[0], key=hits[0].get)])
    print('max',hits[0][max(hits[0], key=hits[0].get)])
    print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
    max 0.004868653378780953
    mean 5.615699699344123e-07
```

## 5. Featurization

### 5. 1 Reading a sample of Data from both train and test

```
In [35]: import random
if os.path.isfile('data/after_eda/train_after_eda.csv'):
    filename = "data/after_eda/train_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file
```

```
name
             # here we have hardcoded the number of lines as 15100030
             # n train = sum(1 for line in open(filename)) #number of records in
          file (excludes header)
             n train = 15100028
             s = 100000 #desired sample size
             skip train = sorted(random.sample(range(1,n train+1),n train-s))
             #https://stackoverflow.com/a/22259008/4084039
In [36]: if os.path.isfile('data/after eda/train after eda.csv'):
             filename = "data/after eda/test after eda.csv"
             # you uncomment this line, if you don't know the lentgh of the file
          name
             # here we have hardcoded the number of lines as 3775008
             # n test = sum(1 for line in open(filename)) #number of records in
          file (excludes header)
             n test = 3775006
             s = 50000 #desired sample size
             skip test = sorted(random.sample(range(1,n test+1),n test-s))
             #https://stackoverflow.com/a/22259008/4084039
In [37]: print("Number of rows in the train data file:", n train)
         print("Number of rows we are going to elimiate in train data are",len(s
         kip train))
         print("Number of rows in the test data file:", n test)
         print("Number of rows we are going to elimiate in test data are",len(sk
         ip test))
         Number of rows in the train data file: 15100028
         Number of rows we are going to elimiate in train data are 15000028
         Number of rows in the test data file: 3775006
         Number of rows we are going to elimiate in test data are 3725006
In [38]: df final train = pd.read_csv('data/after_eda/train_after_eda.csv', skip
         rows=skip train, names=['source node', 'destination node'])
         df final train['indicator link'] = pd.read csv('data/train y.csv', skip
         rows=skip train, names=['indicator link'])
```

```
print("Our train matrix size ",df_final_train.shape)
df_final_train.head(2)
```

Our train matrix size (100002, 3)

### Out[38]:

	source_node	destination_node	indicator_link
0	273084	1505602	1
1	365429	1523458	1

```
In [39]: df_final_test = pd.read_csv('data/after_eda/test_after_eda.csv', skipro
    ws=skip_test, names=['source_node', 'destination_node'])
    df_final_test['indicator_link'] = pd.read_csv('data/test_y.csv', skipro
    ws=skip_test, names=['indicator_link'])
    print("Our test matrix size ",df_final_test.shape)
    df_final_test.head(2)
```

Our test matrix size (50002, 3)

### Out[39]:

L		source_node	destination_node	indicator_link	
	0	848424	784690	1	
	1	1562045	1824397	1	

# **5.2 Adding a set of features**

we will create these each of these features for both train and test data points

- 1. jaccard\_followers
- 2. jaccard\_followees
- 3. cosine\_followers
- 4. cosine followees
- 5. num\_followers\_s
- 6. num\_followees\_s

```
8. num followees d
          9. inter followers
          10. inter followees
In [40]: if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
             #mapping jaccrd followers to train and test data
             df final train['jaccard followers'] = df final train.apply(lambda r
         OW:
                                                      jaccard for followers(row[
          'source node'], row['destination node']), axis=1)
             df final test['jaccard followers'] = df final test.apply(lambda row
                                                      jaccard for followers(row[
          'source node'],row['destination node']),axis=1)
             #mapping jaccrd followees to train and test data
             df final train['jaccard followees'] = df final train.apply(lambda r
         OW:
                                                      jaccard for followees(row[
          'source node'],row['destination node']),axis=1)
             df final test['jaccard followees'] = df final test.apply(lambda row
                                                      jaccard for followees(row[
          'source node'], row['destination node']), axis=1)
                 #mapping jaccrd followers to train and test data
             df final train['cosine followers'] = df final train.apply(lambda ro
                                                      cosine for followers(row['s
         ource node'],row['destination node']),axis=1)
             df final test['cosine followers'] = df final test.apply(lambda row:
                                                       cosine for followers(row['s
         ource node'],row['destination node']),axis=1)
             #mapping jaccrd followees to train and test data
             df final train['cosine followees'] = df final train.apply(lambda ro
```

7. num followers d

```
W:
                                                      cosine for followees(row['s
         ource_node'],row['destination_node']),axis=1)
             df final test['cosine followees'] = df final test.apply(lambda row:
                                                      cosine for followees(row['s
         ource node'],row['destination node']),axis=1)
In [41]: def compute features stage1(df final):
             #calculating no of followers followees for source and destination
             #calculating intersection of followers and followees for source and
          destination
             num followers s=[]
             num followees s=[]
             num followers d=[]
             num followees d=[]
             inter followers=[]
             inter followees=[]
             for i,row in df final.iterrows():
                 try:
                     s1=set(train graph.predecessors(row['source node']))
                     s2=set(train graph.successors(row['source node']))
                 except:
                     s1 = set()
                     s2 = set()
                 try:
                     d1=set(train graph.predecessors(row['destination node']))
                     d2=set(train graph.successors(row['destination node']))
                 except:
                     d1 = set()
                     d2 = set()
                 num followers s.append(len(s1))
                 num followees s.append(len(s2))
                 num followers d.append(len(d1))
                 num followees d.append(len(d2))
                 inter followers.append(len(s1.intersection(d1)))
                 inter followees.append(len(s2.intersection(d2)))
```

```
return num_followers_s, num_followers_d, num_followees_s, num_follo
wees_d, inter_followers, inter_followees
```

```
In [42]: if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
             df final train['num followers s'], df final train['num followers d'
         ], \
             df final train['num followees s'], df final train['num followees d'
         ], \
             df final train['inter followers'], df final train['inter followees'
         ]= compute features stage1(df final train)
             df final test['num followers s'], df final test['num followers d'],
             df final test['num followees s'], df final test['num followees d'],
             df final test['inter followers'], df final test['inter followees']=
          compute features stage1(df final test)
             hdf = HDFStore('data/fea sample/storage sample stage1.h5')
             hdf.put('train df', df final train, format='table', data columns=Tru
         e)
             hdf.put('test df', df final test, format='table', data columns=True)
             hdf.close()
         else:
             df final train = read hdf('data/fea sample/storage sample stage1.h
         5', 'train df', mode='r')
             df final test = read hdf('data/fea sample/storage sample stage1.h5'
          , 'test df', mode='r')
         df final train.head()
```

#### Out[42]:

Ī		source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
	0	273084	1505602	1	0	0.000000	0
	1	365429	1523458	1	0	0.023077	0
	2	1122952	720171	1	0	0.071429	0
	3	201818	992764	1	0	0.100000	0
ı							_

4 1160801 | 71690 | 1 | 0 | 0.000000 | 0

In [43]: df\_final\_train.head()

Out[43]:

source\_node | destination\_node | indicator\_link | jaccard\_followers | jaccard\_followees | c **0** 273084 0.000000 1505602 0 1 365429 1523458 0 0.023077 **2** 1122952 720171 0 0.071429 **3** 201818 0 992764 0 0.100000 **4** 1160801 0 71690 0 0.000000

# 5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
#mapping followback or not on train
    df final train['follows back'] = df final train.apply(lambda row: f
ollows back(row['source node'], row['destination node']), axis=1)
   #mapping followback or not on test
    df final test['follows back'] = df final test.apply(lambda row: fol
lows back(row['source node'], row['destination node']), axis=1)
   #mapping same component of wcc or not on train
    df final train['same comp'] = df final train.apply(lambda row: belo
ngs to same wcc(row['source node'], row['destination node']), axis=1)
   ##mapping same component of wcc or not on train
    df final test['same comp'] = df final test.apply(lambda row: belong
s to same wcc(row['source node'],row['destination node']),axis=1)
    #-----
   #mapping shortest path on train
    df final train['shortest path'] = df final train.apply(lambda row:
compute shortest path length(row['source node'],row['destination node'
1),axis=1)
   #mapping shortest path on test
    df final test['shortest path'] = df final test.apply(lambda row: co
mpute shortest path length(row['source node'],row['destination node']),
axis=1)
   hdf = HDFStore('data/fea sample/storage sample stage2.h5')
   hdf.put('train df', df final train, format='table', data columns=Tru
e)
   hdf.put('test df',df final test, format='table', data columns=True)
    hdf.close()
else:
    df final train = read hdf('data/fea sample/storage sample stage2.h
5', 'train df',mode='r')
    df final test = read hdf('data/fea sample/storage sample stage2.h5'
, 'test df',mode='r')
```

# **5.4 Adding new set of features**

we will create these each of these features for both train and test data points

- 1. Weight Features
  - weight of incoming edges
  - · weight of outgoing edges
  - weight of incoming edges + weight of outgoing edges
  - weight of incoming edges \* weight of outgoing edges
  - 2\*weight of incoming edges + weight of outgoing edges
  - weight of incoming edges + 2\*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities\_s of dest

#### **Weight Features**

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1 + |X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
In [45]: #weight for source and destination of each link
         Weight in = \{\}
         Weight out = \{\}
         for i in tqdm(train graph.nodes()):
             s1=set(train graph.predecessors(i))
             w in = 1.0/(np.sqrt(1+len(s1)))
             Weight in[i]=w in
             s2=set(train graph.successors(i))
             w out = 1.0/(np.sqrt(1+len(s2)))
             Weight out[i]=w out
         #for imputing with mean
         mean weight in = np.mean(list(Weight_in.values()))
         mean weight out = np.mean(list(Weight out.values()))
                        | 1780722/1780722 [00:15<00:00, 113411.28it/s]
In [46]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
             #mapping to pandas train
             df final train['weight in'] = df final train.destination node.apply
         (lambda x: Weight in.get(x,mean weight in))
             df final train['weight out'] = df final train.source node.apply(lam
         bda x: Weight out.get(x,mean weight out))
             #mapping to pandas test
             df final test['weight in'] = df final test.destination node.apply(l)
         ambda x: Weight in.get(x,mean weight in))
             df final test['weight out'] = df final test.source node.apply(lambd
         a x: Weight out.get(x, mean weight out))
             #some features engineerings on the in and out weights
             df final train['weight f1'] = df final train.weight in + df final t
         rain.weight out
             df final train['weight f2'] = df final train.weight in * df final t
```

```
rain.weight out
                               df final train['weight f3'] = (2*df final train.weight in + 1*df fi
                     nal train.weight out)
                               df final train['weight f4'] = (1*df final train.weight in + 2*df fi
                      nal train.weight out)
                               #some features engineerings on the in and out weights
                               df final test['weight f1'] = df final test.weight in + df final tes
                      t.weight out
                               df final test['weight f2'] = df final test.weight in * df final tes
                      t.weiaht out
                               df final test['weight f3'] = (2*df final test.weight in + 1*df final test.weight in 
                      l test.weight out)
                               df final test['weight f4'] = (1*df final test.weight in + 2*df fina
                      l test.weight out)
In [47]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
                               #page rank for source and destination in Train and Test
                               #if anything not there in train graph then adding mean page rank
                               df final train['page rank s'] = df final train.source node.apply(la
                     mbda x:pr.get(x,mean pr))
                               df final train['page rank d'] = df final train.destination node.app
                      ly(lambda x:pr.get(x,mean pr))
                               df final test['page rank s'] = df final test.source node.apply(lamb
                      da x:pr.get(x,mean pr))
                               df final test['page rank d'] = df final test.destination node.apply
                      (lambda x:pr.get(x,mean pr))
                               #Katz centrality score for source and destination in Train and test
                               #if anything not there in train graph then adding mean katz score
                               df final train['katz s'] = df final train.source node.apply(lambda
                      x: katz.get(x,mean katz))
                               df final train['katz d'] = df final train.destination node.apply(la
                     mbda x: katz.get(x,mean katz))
```

```
df final test['katz s'] = df final test.source node.apply(lambda x:
katz.get(x,mean katz))
    df final test['katz d'] = df final test.destination node.apply(lamb
da x: katz.get(x,mean katz))
    #Hits algorithm score for source and destination in Train and test
    #if anything not there in train graph then adding 0
    df final train['hubs s'] = df final train.source node.apply(lambda
x: hits[0].get(x,0)
    df final train['hubs d'] = df final train.destination node.apply(la
mbda x: hits[0].get(x,0)
    df final test['hubs s'] = df final test.source node.apply(lambda x:
hits[0].qet(x,0)
    df final test['hubs d'] = df final test.destination node.apply(lamb
da x: hits[0].get(x,0))
    #Hits algorithm score for source and destination in Train and Test
    #if anything not there in train graph then adding 0
    df final train['authorities s'] = df final train.source node.apply(
lambda x: hits[1].get(x,0))
    df final train['authorities d'] = df final train.destination node.a
pplv(lambda x: hits[1].get(x.0))
    df final test['authorities s'] = df final test.source node.apply(la
mbda x: hits[1].get(x,0))
    df final test['authorities d'] = df final test.destination node.app
ly(lambda x: hits[1].get(x,0))
    hdf = HDFStore('data/fea sample/storage sample stage3.h5')
    hdf.put('train df',df final train, format='table', data columns=Tru
e)
    hdf.put('test df',df final test, format='table', data columns=True)
```

```
hdf.close()
else:
    df_final_train = read_hdf('data/fea_sample/storage_sample_stage3.h
5', 'train_df',mode='r')
    df_final_test = read_hdf('data/fea_sample/storage_sample_stage3.h5'
, 'test_df',mode='r')
```

In [48]: df\_final\_train.head()

Out[48]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	273084	1505602	1	0	0.000000	0
1	365429	1523458	1	0	0.023077	0
2	1122952	720171	1	0	0.071429	0
3	201818	992764	1	0	0.100000	0
4	1160801	71690	1	0	0.000000	0

5 rows × 31 columns

# **Assignments:**

- Add another feature called Preferential Attachment with followers and followees data of vertex. you can check about Preferential Attachment in below link <a href="http://be.amazd.com/link-prediction/">http://be.amazd.com/link-prediction/</a>
- 2. Add feature called svd\_dot. you can calculate svd\_dot as Dot product between sourse node svd and destination node svd features. you can read about this in below pdf

https://storage.googleapis.com/kaggle-forum-message-attachments/2594/supervised\_link\_prediction.pdf

3. Tune hyperparameters for XG boost with all these features and check the error metric.

### **Add new feature Preferential Attachement**

#### **Preferential Attachement for Followers**

```
In [49]: #pa= preferential attachment, for train data
    pa_src=np.array(df_final_train['num_followers_s'])
    pa_des=np.array(df_final_train['num_followers_d'])
    pa_followers=[]
    for i in range(len(pa_src)):
        pa_followers.append(pa_des[i]*pa_src[i])
    df_final_train['Pref_Attach_followers']= pa_followers
    df_final_train.head()
```

### Out[49]:

		source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
	0	273084	1505602	1	0	0.000000	0
	1	365429	1523458	1	0	0.023077	0
2	2	1122952	720171	1	0	0.071429	0
;	3	201818	992764	1	0	0.100000	0
,	4	1160801	71690	1	0	0.000000	0

5 rows × 32 columns

```
In [50]: df final train.shape
Out[50]: (100002, 32)
In [51]: df final train.columns
Out[51]: Index(['source node', 'destination node', 'indicator link',
                 'jaccard followers', 'jaccard followees', 'cosine followers',
                 'cosine_followees', 'num_followers_s', 'num_followers_d',
                 'num followees s', 'num followees d', 'inter followers',
                 'inter followees', 'adar index', 'follows back', 'same comp',
                 'shortest path', 'weight in', 'weight out', 'weight fl', 'weight
         _f2',
                 'weight f3', 'weight f4', 'page rank s', 'page rank d', 'katz
         s',
                 'katz d', 'hubs s', 'hubs d', 'authorities s', 'authorities d',
                'Pref Attach followers'],
               dtype='object')
In [52]: #pa= preferential attachment , for test data
         pa src=np.array(df final test['num followers s'])
         pa des=np.array(df final test['num followers d'])
         pa followers=[]
         for i in range(len(pa src)):
             pa followers.append(pa des[i]*pa src[i])
         df final test['Pref Attach followees']= pa followers
         df final test.head()
Out[52]:
            source node destination node indicator link jaccard followers jaccard followees c
          0 848424
                        784690
                                                   0
                                                                   0.000000
                                                                                   0
          1 1562045
                                                   0
                                                                                   0
                        1824397
                                                                   0.000000
```

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
2	1432006	1842942	1	0	0.000000	0
3	1718418	37205	1	0	0.068966	0
4	911169	392490	1	0	0.238095	0

5 rows × 32 columns

```
←
```

```
In [53]: df_final_test.shape
```

Out[53]: (50002, 32)

### **Preferential Attachement for Followees**

```
In [54]: #pa= preferential attachment for train data
    pa_src=np.array(df_final_train['num_followees_s'])
    pa_des=np.array(df_final_train['num_followees_d'])
    pa_followees=[]
    for i in range(len(pa_src)):
        pa_followees.append(pa_des[i]*pa_src[i])
    df_final_train['Pref_Attach_followees']= pa_followees
    df_final_train.head()
```

Out[54]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	273084	1505602	1	0	0.000000	0
1	365429	1523458	1	0	0.023077	0

	sour	rce_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
2	1122	952	720171	1	0	0.071429	0
;	2018	318	992764	1	0	0.100000	0
4	1160	)801	71690	1	0	0.000000	0

5 rows × 33 columns

```
←
```

```
In [55]: df_final_train.shape
```

Out[55]: (100002, 33)

```
In [56]: #pa= preferential attachment for test data
    pa_src=np.array(df_final_test['num_followees_s'])
    pa_des=np.array(df_final_test['num_followees_d'])
    pa_followees=[]
    for i in range(len(pa_src)):
        pa_followees.append(pa_des[i]*pa_src[i])
    df_final_test['Pref_Attach_followees']= pa_followees
    df_final_test.head()
```

Out[56]:

		source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
	0	848424	784690	1	0	0.000000	0
	1	1562045	1824397	1	0	0.000000	0
7	2	1432006	1842942	1	0	0.000000	0

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
3	1718418	37205	1	0	0.068966	0
4	911169	392490	1	0	0.238095	0

5 rows × 33 columns

## 5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [59]: def svd(x, S):
```

```
try:
                  z = sadj dict[x]
                  return S[z]
              except:
                   return [0,0,0,0,0,0]
 In [60]: #for svd features to get feature vector creating a dict node val and in
          edx in svd vector
          sadj col = sorted(train graph.nodes())
          sadj dict = { val:idx for idx,val in enumerate(sadj col)}
 In [61]: Adj = nx.adjacency matrix(train graph, nodelist=sorted(train graph.nodes
          ())).asfptype()
 In [62]: U, s, V = svds(Adj, k = 6)
          print('Adjacency matrix Shape', Adj.shape)
          print('U Shape', U.shape)
          print('V Shape', V.shape)
          print('s Shape',s.shape)
          Adjacency matrix Shape (1780722, 1780722)
          U Shape (1780722, 6)
          V Shape (6, 1780722)
          s Shape (6,)
In [117]: if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
              df final train[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4',
           'svd u s 5', 'svd u s 6']] = \
              df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Seri
          es)
              df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4',
           'svd u d 5', 'svd u d 6']] = \
              df final train.destination node.apply(lambda x: svd(x, U)).apply(pd
           .Series)
```

```
df final train[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4',
'svd v s 5', 'svd v s 6',11 = \
    df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Se
ries)
    df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4',
 'svd v d 5', 'svd v d 6']] = \setminus
    df final train.destination node.apply(lambda x: svd(x, V.T)).apply(
pd.Series)
   df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4',
'svd u s 5', 'svd u s 6'11 = \
    df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Serie
s)
    df final test[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4',
'svd u d 5','svd u d 6']] = \
   df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.
Series)
    df final test[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4',
'svd v s 5', 'svd v s 6',]] = \
    df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Ser
ies)
    df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4',
'svd v d 5', 'svd v d 6']] = \
    df final test.destination node.apply(lambda x: svd(x, V.T)).apply(p
d.Series)
```

```
hdf = HDFStore('data/fea_sample/storage_sample_stage4.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=Tru
e)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
```

# Add new feature svd\_dot

```
In [118]: #SVD train data
          s1,s2,s3,s4,s5,s6=df final train['svd u s 1'],df final train['svd u s
          2'], df final train['svd u s 3'], df final train['svd u s 4'], df final tr
          ain['svd u s 5'],df final train['svd u s 6']
          s7,s8,s9,s10,s11,s12=df final train['svd v s 1'],df final train['svd v
          s 2'], df final train['svd v s 3'], df final train['svd v s 4'], df final
          train['svd v s 5'],df final train['svd v s 6']
          d1,d2,d3,d4,d5,d6=df final train['svd u d 1'],df final train['svd u d
          2'], df final train['svd u d 3'], df final train['svd u d 4'], df final tr
          ain['svd u d 5'],df final train['svd u d 6']
          d7,d8,d9,d10,d11,d12=df final train['svd v d_1'],df_final_train['svd_v_
          d 2'],df final train['svd v d 3'],df final train['svd v d 4'],df final
          train['svd v d 5'], df final train['svd v d 6']
In [119]: svd dot=[]
          for i in range(len(np.array(s1))):
              d 1=[]
              d 2=[1]
              d 1.append(np.array(s1[i]))
              d 1.append(np.array(s2[i]))
              d 1.append(np.array(s3[i]))
              d 1.append(np.array(s4[i]))
              d 1.append(np.array(s5[i]))
              d 1.append(np.array(s6[i]))
              d 1.append(np.array(s7[i]))
              d 1.append(np.array(s8[i]))
```

```
d 1.append(np.array(s9[i]))
    d 1.append(np.array(s10[i]))
    d 1.append(np.array(s11[i]))
    d 1.append(np.array(s12[i]))
    d 2.append(np.array(d1[i]))
    d 2.append(np.array(d2[i]))
    d_2.append(np.array(d3[i]))
    d 2.append(np.array(d4[i]))
    d 2.append(np.array(d5[i]))
    d 2.append(np.array(d6[i]))
    d 2.append(np.array(d7[i]))
    d 2.append(np.array(d8[i]))
    d 2.append(np.array(d9[i]))
    d 2.append(np.array(d10[i]))
    d 2.append(np.array(d11[i]))
    d 2.append(np.array(d12[i]))
    svd dot.append(np.dot(d 1,d 2))
df final train['svd dot'] = svd dot
#https://www.tutorialspoint.com/numpy/numpy dot.htm
```

In [120]: df\_final\_train.head()

Out[120]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	273084	1505602	1	0	0.000000	0
1	365429	1523458	1	0	0.023077	0
2	1122952	720171	1	0	0.071429	0
3	201818	992764	1	0	0.100000	0
4	1160801	71690	1	0	0.000000	0

```
5 rows × 58 columns
In [121]: #SVD test data
          s1,s2,s3,s4,s5,s6=df final test['svd u s 1'],df final test['svd u s 2'
          ],df final test['svd u s 3'],df final test['svd u s 4'],df final test[
           'svd u s 5'],df final test['svd u s 6']
          s7,s8,s9,s10,s11,s12=df final test['svd v s 1'],df final test['svd v s
          2'], df final test['svd v s 3'], df final test['svd v s 4'], df final test
          ['svd v s 5'], df final test['svd v s 6']
          d1,d2,d3,d4,d5,d6=df final test['svd u d 1'],df final test['svd u d 2'
          ],df final test['svd u d 3'],df final test['svd u d 4'],df final test[
           'svd u d 5'],df final test['svd u d 6']
          d7.d8.d9.d10,d11,d12=df final test['svd v d 1'],df final test['svd v d
          2'], df final test['svd v d 3'], df final test['svd v d 4'], df final test
           ['svd v d 5'], df final test['svd v d 6']
In [122]: svd dot=[]
          for i in range(len(np.array(s1))):
              d 1=[]
              d 2=[1]
              d 1.append(np.array(s1[i]))
              d 1.append(np.array(s2[i]))
              d 1.append(np.array(s3[i]))
              d 1.append(np.arrav(s4[i]))
              d 1.append(np.array(s5[i]))
              d 1.append(np.array(s6[i]))
              d 1.append(np.array(s7[i]))
              d 1.append(np.array(s8[i]))
              d 1.append(np.array(s9[i]))
              d 1.append(np.array(s10[i]))
              d 1.append(np.array(s11[i]))
              d 1.append(np.array(s12[i]))
              d 2.append(np.array(d1[i]))
              d 2.append(np.array(d2[i]))
              d 2.append(np.array(d3[i]))
```

```
d_2.append(np.array(d4[i]))
d_2.append(np.array(d5[i]))
d_2.append(np.array(d6[i]))
d_2.append(np.array(d7[i]))
d_2.append(np.array(d8[i]))
d_2.append(np.array(d9[i]))
d_2.append(np.array(d10[i]))
d_2.append(np.array(d11[i]))
d_2.append(np.array(d12[i]))
svd_dot.append(np.dot(d_1,d_2))
df_final_test['svd_dot']=svd_dot
#https://www.tutorialspoint.com/numpy/numpy_dot.htm
```

In [123]: df\_final\_test.head()

Out[123]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	848424	784690	1	0	0.000000	0
1	1562045	1824397	1	0	0.000000	0
2	1432006	1842942	1	0	0.000000	0
3	1718418	37205	1	0	0.068966	0
4	911169	392490	1	0	0.238095	0

5 rows × 58 columns

```
In [124]: hdf = HDFStore('data/fea_sample/storage_sample_stage4.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
```

```
hdf.put('test df',df final test, format='table', data columns=True)
        hdf.close()
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xgboost: pip3 install xgboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import HDFStore,DataFrame
        from pandas import read hdf
        from scipy.sparse.linalg import svds, eigs
        import qc
        from tgdm import tgdm
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1 score
```

```
In [2]: #reading
    from pandas import read_hdf
    df_final_train = read_hdf('data/fea_sample/storage_sample_stage4.h5',
        'train_df',mode='r')
    df_final_test = read_hdf('data/fea_sample/storage_sample_stage4.h5', 't
        est_df',mode='r')
```

### In [3]: df\_final\_train.head()

### Out[3]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	273084	1505602	1	0	0.000000	0
1	365429	1523458	1	0	0.023077	0
2	1122952	720171	1	0	0.071429	0
3	201818	992764	1	0	0.100000	0
4	1160801	71690	1	0	0.000000	0

5 rows × 58 columns

In [4]: df final test.head()

### Out[4]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
0	848424	784690	1	0	0.000000	0

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	С
1	1562045	1824397	1	0	0.000000	0
2	1432006	1842942	1	0	0.000000	0
3	1718418	37205	1	0	0.068966	0
4	911169	392490	1	0	0.238095	0

5 rows × 58 columns

```
In [5]: df final train.columns
Out[5]: Index(['source node', 'destination node', 'indicator link',
                'jaccard followers', 'jaccard followees', 'cosine followers',
               'cosine followees', 'num followers s', 'num followers d',
               'num followees_s', 'num_followees_d', 'inter_followers',
               'inter followees', 'adar index', 'follows back', 'same comp',
               'shortest path', 'weight in', 'weight out', 'weight fl', 'weight
        _f2',
               'weight f3', 'weight f4', 'page rank s', 'page rank d', 'katz
        s',
               'katz d', 'hubs s', 'hubs d', 'authorities s', 'authorities d',
               'Pref Attach followers', 'Pref Attach followees', 'svd u s 1',
               'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6',
               'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5',
               'svd u d 6', 'svd v s 1', 'svd v s 2', 'svd v s 3', 'svd v s 4',
               'svd v s 5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3',
               'svd v d 4', 'svd v d 5', 'svd v d 6', 'svd dot'],
              dtvpe='object')
In [6]: y train = df final train.indicator link
        y test = df final test.indicator link
```

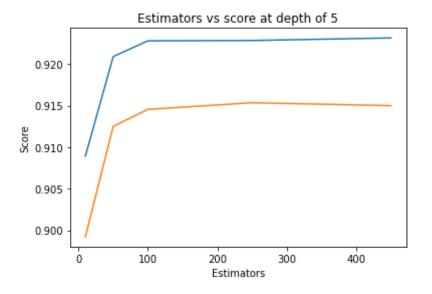
```
In [7]: df_final_train.drop(['source_node', 'destination_node','indicator_link'
],axis=1,inplace=True)
    df_final_test.drop(['source_node', 'destination_node','indicator_link'
],axis=1,inplace=True)
```

### **Random Forest**

```
In [132]: estimators = [10,50,100,250,450]
          train scores = []
          test scores = []
          for i in estimators:
              clf = RandomForestClassifier(bootstrap=True, class weight=None, cri
          terion='gini',
                      max depth=5, max features='auto', max leaf nodes=None,
                      min impurity decrease=0.0, min impurity split=None,
                      min samples leaf=52, min samples split=120,
                      min weight fraction leaf=0.0, n estimators=i, n jobs=-1,ran
          dom state=25,verbose=0,warm start=False)
              clf.fit(df final train,y train)
              train sc = f1 score(y train,clf.predict(df final train))
              test sc = f1 score(y test,clf.predict(df final test))
              test scores.append(test sc)
              train scores.append(train sc)
              print('Estimators = ',i,'Train Score',train sc,'test Score',test sc
          plt.plot(estimators, train scores, label='Train Score')
          plt.plot(estimators, test scores, label='Test Score')
          plt.xlabel('Estimators')
          plt.ylabel('Score')
          plt.title('Estimators vs score at depth of 5')
          Estimators = 10 Train Score 0.9089390658830807 test Score 0.8992434449
          165717
          Estimators = 50 Train Score 0.9208917767850635 test Score 0.9125044427
          254292
          Estimators = 100 Train Score 0.9227863292460214 test Score 0.914545683
          2571596
```

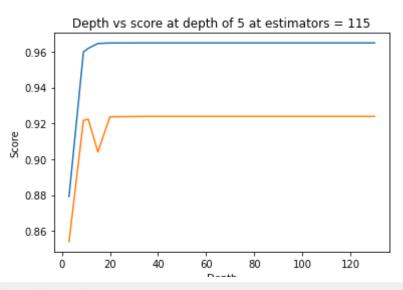
Estimators = 250 Train Score 0.9228264273040393 test Score 0.915345247 084487 Estimators = 450 Train Score 0.9231363864282132 test Score 0.914993700 1259973

### Out[132]: Text(0.5, 1.0, 'Estimators vs score at depth of 5')



```
train_scores.append(train_sc)
    print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
plt.plot(depths,train_scores,label='Train Score')
plt.plot(depths,test_scores,label='Test Score')
plt.xlabel('Depth')
plt.ylabel('Score')
plt.title('Depth vs score at depth of 5 at estimators = 115')
plt.show()
```

depth = 3 Train Score 0.8792637051439198 test Score 0.8540307824776666
depth = 9 Train Score 0.9598138186569221 test Score 0.9216800050678885
depth = 11 Train Score 0.9618488628026413 test Score 0.922326818354510
6
depth = 15 Train Score 0.964521384928717 test Score 0.9039907212509127
depth = 20 Train Score 0.9648295460332658 test Score 0.923661543658165
9
depth = 35 Train Score 0.9648520649793757 test Score 0.923882298307088
2
depth = 50 Train Score 0.9648520649793757 test Score 0.923882298307088
2
depth = 70 Train Score 0.9648520649793757 test Score 0.923882298307088
2
depth = 130 Train Score 0.9648520649793757 test Score 0.923882298307088



Deptn

```
In [134]: from sklearn.metrics import f1 score
          from sklearn.ensemble import RandomForestClassifier
          from sklearn.metrics import f1 score
          from sklearn.model selection import RandomizedSearchCV
          from scipy.stats import randint as sp randint
          from scipy.stats import uniform
          param dist = {"n estimators":sp randint(105,125),
                        "max depth": sp randint(10,15),
                        "min samples split": sp randint(110,190),
                        "min samples leaf": sp randint(25,65)}
          clf = RandomForestClassifier(random state=25,n jobs=-1)
          rf random = RandomizedSearchCV(clf, param distributions=param dist,
                                             n iter=5,cv=10,scoring='f1',random s
          tate=25)
          rf random.fit(df final train,y train)
          mean test scores [0.96302753 0.96303605 0.96161726 0.96309172 0.9646340
          mean train scores [0.96439527 0.96416869 0.96211981 0.96383528 0.965866
          33]
In [135]: print(rf random.best estimator )
          RandomForestClassifier(max depth=14, min samples leaf=28, min samples s
          plit=111,
                                 n estimators=121, n jobs=-1, random state=25)
In [136]: clf = RandomForestClassifier(bootstrap=True, class weight=None, criteri
          on='gini',
                      max depth=14, max features='auto', max leaf nodes=None,
                      min impurity decrease=0.0, min impurity split=None,
                      min samples leaf=28, min samples split=111,
                      min weight fraction leaf=0.0, n estimators=121, n jobs=-1,
```

```
oob score=False, random state=25, verbose=0, warm start=Fal
          se)
In [137]: clf.fit(df final train,y train)
          y train pred = clf.predict(df final train)
          y test pred = clf.predict(df final test)
In [138]: from sklearn.metrics import fl score
          print('Train f1 score', f1 score(y train, y train pred))
          print('Test f1 score', f1 score(y test, y test pred))
          Train f1 score 0.9662007986309185
          Test f1 score 0.9244187274301523
  In [8]: from sklearn.metrics import confusion matrix
          def plot confusion matrix(test y, predict y):
              C = confusion matrix(test y, predict y)
              A = (((C.T)/(C.sum(axis=1))).T)
              B = (C/C.sum(axis=0))
              plt.figure(figsize=(20,4))
              labels = [0,1]
              # representing A in heatmap format
              cmap=sns.light palette("blue")
              plt.subplot(1, 3, 1)
              sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels
           , vticklabels=labels)
              plt.xlabel('Predicted Class')
              plt.ylabel('Original Class')
              plt.title("Confusion matrix")
              plt.subplot(1, 3, 2)
              sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels
           , vticklabels=labels)
              plt.xlabel('Predicted Class')
              plt.ylabel('Original Class')
```

```
plt.title("Precision matrix")

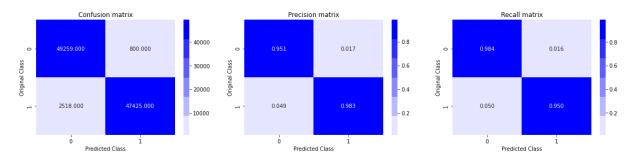
plt.subplot(1, 3, 3)
# representing B in heatmap format
sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels
, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Recall matrix")

plt.show()
```

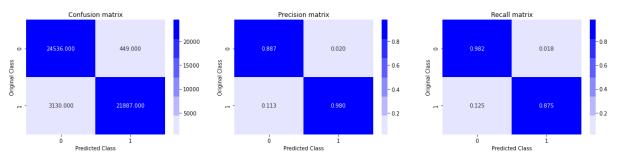
### In [140]:

```
print('Train confusion_matrix')
plot_confusion_matrix(y_train,y_train_pred)
print('Test confusion_matrix')
plot_confusion_matrix(y_test,y_test_pred)
```

### Train confusion\_matrix



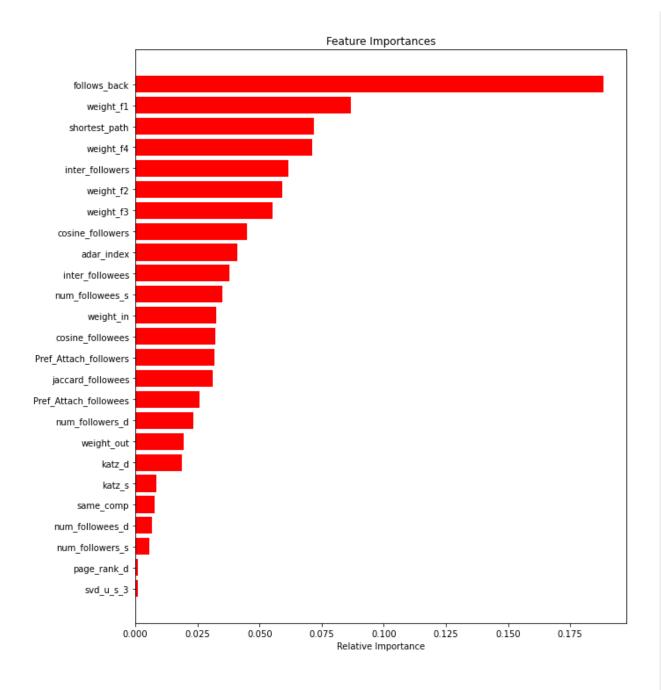
### Test confusion\_matrix



### 

```
In [142]: features = df_final_train.columns
   importances = clf.feature_importances_
   indices = (np.argsort(importances))[-25:]
   plt.figure(figsize=(10,12))
   plt.title('Feature Importances')
   plt.barh(range(len(indices)), importances[indices], color='r', align='c
```

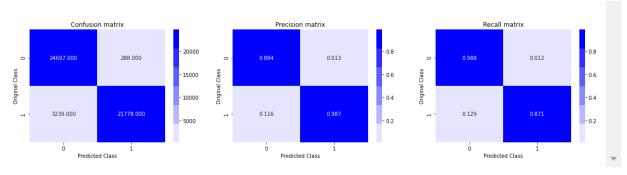
```
enter')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```



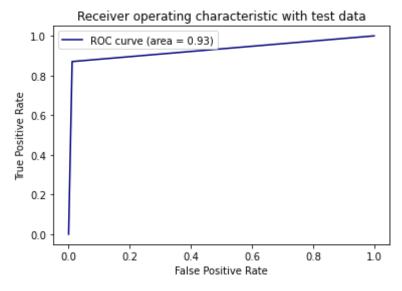
### **Applying XGBOOST**

```
In [27]: import xgboost as xgb
         from sklearn.metrics import f1 score
         from sklearn.ensemble import RandomForestClassifier
         from sklearn.metrics import f1 score
         from sklearn.model selection import RandomizedSearchCV
         from scipy.stats import randint as sp randint
         from scipy.stats import uniform
         clf = xqb.XGBClassifier()
         param dist = {"n estimators":sp randint(105,125),
                       "max depth": sp randint(10,15)
         model = RandomizedSearchCV(clf, param distributions=param dist,n iter=5
         ,cv=3,scoring='f1',random state=25, return train score=True).fit(df fin
         al train, y train)
In [28]: print(model.best estimator )
         XGBClassifier(base score=0.5, booster='gbtree', colsample bylevel=1,
                       colsample bynode=1, colsample bytree=1, gamma=0, gpu id=-
         1,
                       importance type='gain', interaction constraints='',
                       learning rate=0.300000012, max delta step=0, max depth=1
         0,
                       min child weight=1, missing=nan, monotone_constraints
         ='()',
                       n estimators=109, n jobs=0, num parallel tree=1, random s
         tate=0,
                       reg alpha=0, reg lambda=1, scale pos weight=1, subsample=
         1,
                       tree method='exact', validate parameters=1, verbosity=Non
         e)
In [29]: clf=xgb.XGBClassifier(base score=0.5, booster='gbtree', colsample bylev
         el=1,
                colsample bytree=1, gamma=0, learning rate=0.1, max delta step=0
```

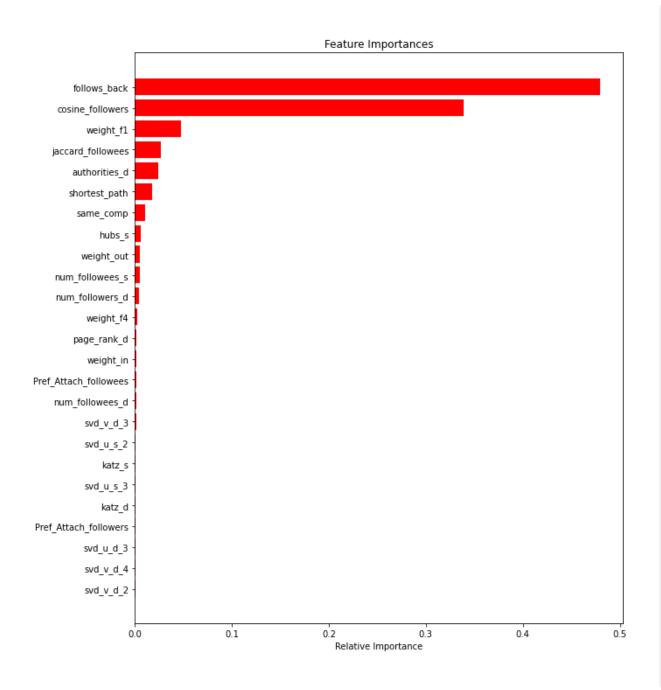
```
max depth=10, min child weight=1, missing=None, n estimators=109
                  n jobs=1, nthread=None, objective='binary:logistic', random stat
          e=0,
                  reg alpha=0, reg lambda=1, scale pos weight=1, seed=None,
                  silent=True, subsample=1)
         clf.fit(df final train,y train)
In [221:
          y train pred = clf.predict(df final train)
          y test pred = clf.predict(df final test)
In [31]: from sklearn.metrics import fl score
          print('Train f1 score', f1 score(y train, y train pred))
          print('Test fl score',fl score(y test,y test pred))
          Train fl score 0.9931026161796939
          Test f1 score 0.9250897351485675
In [32]: print('Train confusion matrix')
          plot confusion matrix(y train,y train pred)
          print('Test confusion matrix')
          plot confusion matrix(y test,y test pred)
          Train confusion_matrix
                  Confusion matrix
                                              Precision matrix
                                                                         Recall matrix
                         129.000
                                                    0.003
                                                                                0.003
                                 - 30000
                                 - 20000
                557.000
                                           0.011
                                                                       0.011
                                                            - 0.2
                                 - 10000
                   Predicted Class
                                                                         Predicted Class
          Test confusion matrix
```



```
In [33]: from sklearn.metrics import roc_curve, auc
fpr,tpr,ths = roc_curve(y_test,y_test_pred)
auc_sc = auc(fpr, tpr)
plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc_sc)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic with test data')
plt.legend()
plt.show()
```



```
In [34]: features = df_final_train.columns
    importances = clf.feature_importances_
    indices = (np.argsort(importances))[-25:]
    plt.figure(figsize=(10,12))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='r', align='c
    enter')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```



### Conclusion