

```
In [88]: import pandas as pd
from scipy.stats import linregress
import seaborn as sns
import matplotlib.pyplot as plt

df = pd.read_csv('activity7.csv').set_index('Country')
```

**1. Use Excel to find the summation of  $x$ ,  $y$ ,  $xy$ ,  $x^2$ , and  $y^2$ .**

```
In [89]: sumX= df['Birth Rate'].sum()
sumY = df['Life Expectancy'].sum()
print("Sum of x: " + str(sumX) + '\nSum of y: ' + str(sumY))
sumXY = 0
sumX2 = 0
sumY2 = 0
for _,row in df.iterrows():
    sumXY += row.iloc[0]*row.iloc[1]
    sumX2 += row.iloc[0] ** 2
    sumY2 += row.iloc[1] ** 2

print("Sum of xy: "+str(sumXY) + "\nSum of x^2: " + str(sumX2) + "\nSum of y
```

```
Sum of x: 466
Sum of y: 1788
Sum of xy: 34382
Sum of x^2: 9736
Sum of y^2: 133512
```

**2. Use Excel to find the covariance  $S_{xy}$ .**

```
In [90]: cov = df.cov()['Birth Rate'].iloc[1]
print(cov)
```

```
-14.565217391304348
```

**Covariance of xy is -14.562**

**3. Use Excel to calculate  $S_x$ ,  $S_y$ , and the correlation coefficient.**

```
In [91]: sx = df['Birth Rate'].std()
sy = df['Life Expectancy'].std()
print('x deviation: ' + str(sx))
print("y deviation: " + str(sy))
corrCoef = df.corr()['Birth Rate'].iloc[1]
print("Correlation coeffecient: " + str(corrCoef))
```

```
x deviation: 5.468619304856508
y deviation: 3.647512553245973
Correlation coeffecient: -0.7302011028563675
```

**4. Use Excel to calculate the coefficient of determination.**

```
In [92]: print("Coefficient of determination: " + str(corrCoef**2))
```

Coefficient of determination: 0.5331936506126554

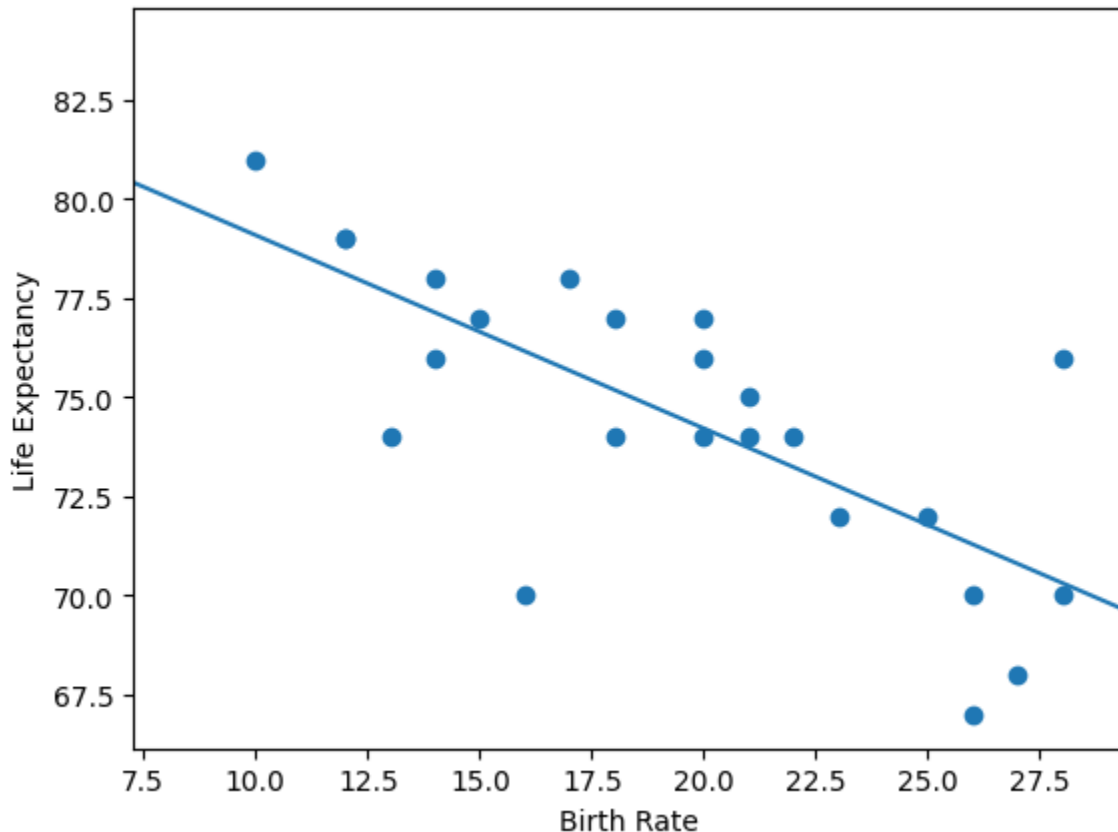
**5. Use Excel to calculate  $b_1$ ,  $x$ ,  $y$ , and  $b_0$ .**

```
In [93]: b1 = cov / sx**2
b0 = df['Life Expectancy'].mean() - (b1*df['Birth Rate'].mean())
print('slope: ' + str(b1) + ' intercept: ' + str(b0))
print(f"Model:  $\hat{y}={b0:.3f}+({b1:.3f})x$ ")

fig, ax= plt.subplots()
ax.set_xlabel('Birth Rate')
ax.set_ylabel('Life Expectancy')
ax.axline((0,b0), slope = b1)
scatter = plt.scatter(df['Birth Rate'], df['Life Expectancy'])
ax.set_xlim(df['Birth Rate'].min()-df['Birth Rate'].std()/2)
plt.show()
```

slope: -0.48703658832081403 intercept: 83.9566270898958

Model:  $\hat{y}=83.957+(-0.487)x$



**6. Given the scatterplot and regression equation you created in Excel and the information you have found up to this point, do you think there is a linear relationship between birthrate and life expectancy?**

**ANSWER:** Yes, it seems linear

**7. Given the regression equation above, what is the general trend for life expectancy given a country's birthrate? Is this a positive or negative association?**

**ANSWER:** There seems to be a negative relationship

**8. Notice that Paraguay had a birth rate of 28 per 1000 and a life expectancy of 76 years. Find Paraguay's expected life expectancy and the residual. Do you think the model accurately predicted the life expectancy for Paraguay?**

```
In [94]: predParaguay = b0 + b1*28
print(f"predicted expectancy: {predParaguay: .3f}, Life expectancy standard deviation: {b1*28: .3f}")
```

predicted expectancy: 70.320, Life expectancy standard deviation: 3.647512553245973

**ANSWER:** The model predicts 70 years of life expectancy vs. 76 measured, that is not within a standard deviation of what has been measured. Not a good prediction

**9. Find another country that the model poorly predicted the life expectancy of. Find the expected life expectancy of the country and the residual**

```
In [95]: yStd = df['Life Expectancy'].std()
print("Bad predictions (outside 1 standard deviation), life expectancy, and residual")
for index, row in df.iterrows():
    y = row['Life Expectancy']
    pred = b0 + b1*row['Birth Rate']
    lowStd = y - yStd
    highStd = y + yStd
    if pred < lowStd or pred > highStd:
        print(f"{index}: predicted life expectancy: {round(pred,3)}, residual: {round(y - pred,3)}")
```

Bad predictions (outside 1 standard deviation), life expectancy, and residual:

Bahamas: predicted life expectancy: 76.164, residual: -6.164  
Bolivia: predicted life expectancy: 71.294, residual: -4.294  
Paraguay: predicted life expectancy: 70.32, residual: 5.68

**10. Notice that Nicaragua had a birth rate of 23 per 1000 and a life expectancy of 72 years (23, 72). Find Nicaragua's expected life expectancy and the residual. Do you think the model accurately predicted the life expectancy for Nicaragua?**

```
In [96]: pred = b0 + b1*23
y = 72
lowStd = y - yStd
highStd = y + yStd
print(f"Predicted life expectancy: {pred:.3f}. \nStandard deviation interval from prediction: ({lowStd:.3f}, {highStd:.3f})")
```

Predicted life expectancy: 72.755.  
Standard deviation interval from prediction: (76.4, 69.1)

**ANSWER:** Yes, measured expected life expectancy is within 1 standard deviation of predicted.

**11. Find another country that the model accurately predicted the life expectancy of. Find the expected life expectancy of the country and the residual.**

```
In [97]: print("Good predictions (within 1 standard deviation of prediction): \n")
for index, row in df.iterrows():
    y = row.iloc[1]
    pred = b0 + b1*row.iloc[0]
    lowStd = y - yStd
    highStd = y + yStd
    if pred > lowStd and pred < highStd:
        print(f"{index}: predicted life expectancy: {round(pred,3)}, residual: {round(y - pred,3)}")
```

Good predictions (within 1 standard deviation of prediction):

Argentina: predicted life expectancy: 75.19, residual: 1.81  
Barbados: predicted life expectancy: 77.625, residual: -3.625  
Belize: predicted life expectancy: 70.807, residual: -2.807  
Canada : predicted life expectancy: 79.086, residual: 1.914  
Chile: predicted life expectancy: 76.651, residual: 0.349  
Colombia: predicted life expectancy: 75.19, residual: -1.19  
Costa Rica: predicted life expectancy: 75.677, residual: 2.323  
Dominican Republic: predicted life expectancy: 73.242, residual: 0.758  
Ecuador: predicted life expectancy: 73.729, residual: 1.271  
El Salvador: predicted life expectancy: 71.781, residual: 0.219  
Guatemala: predicted life expectancy: 70.32, residual: -0.32  
Honduras: predicted life expectancy: 71.294, residual: -1.294  
Jamaica: predicted life expectancy: 74.216, residual: -0.216  
Mexico: predicted life expectancy: 74.216, residual: 1.784  
Nicaragua: predicted life expectancy: 72.755, residual: -0.755  
Panama: predicted life expectancy: 74.216, residual: 2.784  
Puerto Rico: predicted life expectancy: 78.112, residual: 0.888  
United States: predicted life expectancy: 77.138, residual: 0.862  
Uruguay: predicted life expectancy: 77.138, residual: -1.138  
Venezuela : predicted life expectancy: 73.729, residual: 0.271  
Virgin Islands: predicted life expectancy: 78.112, residual: 0.888