Note Set 3

A	is defined as any activity or phenomenon that meets the following conditions.
1.	
2.	
3.	
<b>J.</b>	
Examples of Experime	nts
cannot be predicted.	: The process through which some type of observation is obtained. An outcome is produced that
·	: one basic outcome of an experiment
	: A form of representation which presents the collection of all possible sample points.
Basic Probability Rule	s for Sample Points:
<b>1.</b> The probability of or	ne single sample point occurring must be between 0 and 1 inclusive.
2. The sum of all proba	abilities of sample points within a single sample space must sum to 1.
Event:	
	: Calculated through summing probabilities of simple events within the sample space.
Example 1: Rolling a d	ie
Experiment:	
Sample point:	
Sample space:	
Example 2:	
Experiment:	
Sample point:	
Sample space:	
Event:	

# **Classical Probability**

Using the classical approach to probability, the probability of an event A, denoted P(A), is given by

### **Relative Frequency**

If an experiment is performed *n* times, under identical conditions, and the event *A* happens *k* times, the **relative frequency** of *A* is given by the following expression.

Understanding Events
: Two events are said to be independent if the occurrence or non occurrence of one event does not change the probability associated with the other event.
event does not change the probability associated with the other event.
: Two events are dependent if they are not independent, essentially one event occurri or not occurring affects the probability associated with the other event.
: Two events are mutually exclusive if the occurrence of one event prohibits the
occurrence of the other. The events cannot both occur. (strongest case of dependent events)
: The union of two events represents the event in which either event A occurs, event B occurs, or they both occu
: The intersection of two events represents the event in which both event A and event B occur.
: Two events whose probabilities reference the same event, sum to one, and represent all possibilities of the event
The Addition Rule
For any two events A and B
Mutually Exclusive Events
If Events A and B are mutually exclusive then
Conditional Probability

#### **Multiplicative Probability Rule:**

If two events A and B are independent then the probability of events A and B is

The conditional probability of A, given that B has already occurred is

2.		
3.		
4. probability of success remains the same	for each trial	
Binomial Probability	Binomial Probability Formula	
Where		
p: probability of success on a single trial		
q: 1-p or probability of failure		
n: number of trials	Combination Formula	
x: number of successes in <i>n</i> trials		
Example 5		
For a binomial with $n = 5$ and $p = .25$ , find the $P($	< = 1).	
Example 6		
For a binomial with $n = 5$ and $p = .25$ , find the $P($	< = 2).	
Example 7		
For a binomial with $n = 5$ and $p = .25$ , find the $P($	( = 3).	
Random Variables and Probability Distributions		
A is a numerical outcor	ne of a random process.	
Ais a modall possible probabilities connected to the value	el that describes a specific kind of random process. A distribution displaying of a random value.	3
Random variables can be either	or	
A discrete random variable is a random variable	which has anumber of possible outcomes.	
A continuous random variable is a random varia of values in an interval.	ole whosecan assume any one of a countless num	эeı
or	of the discrete random variable x is	
of a discrete random v	ariable x is	

A **binomial experiment** has the following characteristics:

1.

#### **Example 8**

Given the probability distribution below find the **expected value**, **variance**, **and standard deviation**.

х	1	2	3	4
p(x)	.4	.54	.02	.04

A test contains five multiple choice questions, each with 4 possible answers. If a student guesses at all five questions, use the binomial probability formula to find the probability of the following:

The probability of	
getting 0 correct	

The probability of
getting 3 correct

Х	0	1	2	3	4	5
P(X)						

Find the mean, variance, and standard deviation for the binomial distribution.

#### Example 9

Suppose the probability that a patient will recover from some blood disease is .30. Assuming that this situation has all the characteristics for a binomial probability and that it is known that 15 people have this disease find each of the following.

- a. The probability no one recovers from the disease
- b. the probability that exactly 4 people will recover from the disease
- c. the probability at least one person recovers from the disease
- d. The mean  $\mu$  or expected number of people who will recover
- e. The variance or  $\sigma^2$  for the number of people who will recover.
- f. The standard deviation or  $\sigma$  for the number of people who will recover

#### Probability Distribution for the Blood Disease Example

$$P(X=0) = P(X=4) = H$$

$$P(X = 8) = P(X = 12) =$$

$$P(X=1) = P(X=5) =$$

$$P(X = 9) =$$

$$P(X = 13) =$$

$$P(X = 2) =$$

$$P(X = 6) =$$

$$P(X = 10) =$$

$$P(X = 14) =$$

$$P(X = 3) =$$

$$P(X = 7) =$$

$$P(X = 11) =$$

$$P(X = 15) =$$

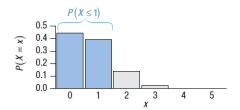
Х	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
P(X)																

Х	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
∑P(X)																

## E

# **Cumulative Binomial Probabilities**

Numerical entries represent  $P(X \le x)$ .



		_				p				
n	X	0.1	0.2	0.3	0.4	0.5	0.6	0.7	8.0	0.9
1	0	0.9000	0.8000	0.7000	0.6000	0.5000	0.4000	0.3000	0.2000	0.1000
	1	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
2	0	0.8100	0.6400	0.4900	0.3600	0.2500	0.1600	0.0900	0.0400	0.0100
	1	0.9900	0.9600	0.9100	0.8400	0.7500	0.6400	0.5100	0.3600	0.1900
	2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	0	0.7290	0.5120	0.3430	0.2160	0.1250	0.0640	0.0270	0.0080	0.0010
	1	0.9720	0.8960	0.7840	0.6480	0.5000	0.3520	0.2160	0.1040	0.0280
	2	0.9990	0.9920	0.9730	0.9360	0.8750	0.7840	0.6570	0.4880	0.2710
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

# **Cumulative Binomial Probabilities** (cont.)

						p				
n	X	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
8	0	0.4305	0.1678	0.0576	0.0168	0.0039	0.0007	0.0001	0.0000	0.0000
	1	0.8131	0.5033	0.2553	0.1064	0.0352	0.0085	0.0013	0.0001	0.0000
	2	0.9619	0.7969	0.5518	0.3154	0.1445	0.0498	0.0113	0.0012	0.0000
	3	0.9950	0.9437	0.8059	0.5941	0.3633	0.1737	0.0580	0.0104	0.0004
	4	0.9996	0.9896	0.9420	0.8263	0.6367	0.4059	0.1941	0.0563	0.0050
	5	1.0000	0.9988	0.9887	0.9502	0.8555	0.6846	0.4482	0.2031	0.0381
	6	1.0000	0.9999	0.9987	0.9915	0.9648	0.8936	0.7447	0.4967	0.1869
	7	1.0000	1.0000	0.9999	0.9993	0.9961	0.9832	0.9424	0.8322	0.5695
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
9	0	0.3874	0.1342	0.0404	0.0101	0.0020	0.0003	0.0000	0.0000	0.0000
	1	0.7748	0.4362	0.1960	0.0705	0.0195	0.0038	0.0004	0.0000	0.0000
	2	0.9470	0.7382	0.4628	0.2318	0.0898	0.0250	0.0043	0.0003	0.0000
	3	0.9917	0.9144	0.7297	0.4826	0.2539	0.0994	0.0253	0.0031	0.0001
	4	0.9991	0.9804	0.9012	0.7334	0.5000	0.2666	0.0988	0.0196	0.0009
	5	0.9999	0.9969	0.9747	0.9006	0.7461	0.5174	0.2703	0.0856	0.0083
	6	1.0000	0.9997	0.9957	0.9750	0.9102	0.7682	0.5372	0.2618	0.0530
	7	1.0000	1.0000	0.9996	0.9962	0.9805	0.9295	0.8040	0.5638	0.2252
	8	1.0000	1.0000	1.0000	0.9997	0.9980	0.9899	0.9596	0.8658	0.6126
	9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

	_	_				р				
n	X	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
15	0	0.2059	0.0352	0.0047	0.0005	0.0000	0.0000	0.0000	0.0000	0.0000
	1	0.5490	0.1671	0.0353	0.0052	0.0005	0.0000	0.0000	0.0000	0.0000
	2	0.8159	0.3980	0.1268	0.0271	0.0037	0.0003	0.0000	0.0000	0.0000
	3	0.9444	0.6482	0.2969	0.0905	0.0176	0.0019	0.0001	0.0000	0.0000
	4	0.9873	0.8358	0.5155	0.2173	0.0592	0.0093	0.0007	0.0000	0.0000
	5	0.9978	0.9389	0.7216	0.4032	0.1509	0.0338	0.0037	0.0001	0.0000
	6	0.9997	0.9819	0.8689	0.6098	0.3036	0.0950	0.0152	0.0008	0.0000
	7	1.0000	0.9958	0.9500	0.7869	0.5000	0.2131	0.0500	0.0042	0.0000
	8	1.0000	0.9992	0.9848	0.9050	0.6964	0.3902	0.1311	0.0181	0.0003
	9	1.0000	0.9999	0.9963	0.9662	0.8491	0.5968	0.2784	0.0611	0.0022
	10	1.0000	1.0000	0.9993	0.9907	0.9408	0.7827	0.4845	0.1642	0.0127
	11	1.0000	1.0000	0.9999	0.9981	0.9824	0.9095	0.7031	0.3518	0.0556
	12	1.0000	1.0000	1.0000	0.9997	0.9963	0.9729	0.8732	0.6020	0.1841
	13	1.0000	1.0000	1.0000	1.0000	0.9995	0.9948	0.9647	0.8329	0.4510
	14	1.0000	1.0000	1.0000	1.0000	1.0000	0.9995	0.9953	0.9648	0.7941
	15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

Х	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
∑P(X)																

Law of Large Numbers: