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- Alligation: It is the rule which enables us to find the ratio in which two or more ingredients at given prices must be mixed to produce a mixture of a desired price. (mixing / linking)
- **Mean Price**: The cost price of a unit quantity of mixture is called the mean price.
- **Dearer**: The more expensive ingredient
- Note:

Always maintain the order in which problem is given else answer gets changed

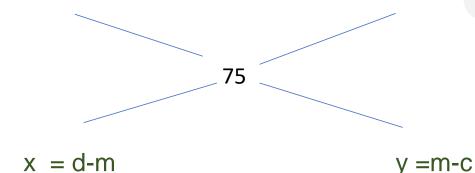


Type 1 oranges at Rs.60 per kg and Type 2 oranges at Rs.120 per kg and when mixed cost is Rs.75 per kg. Find the ratio in which Type 1 and Type 2 oranges are mixed.

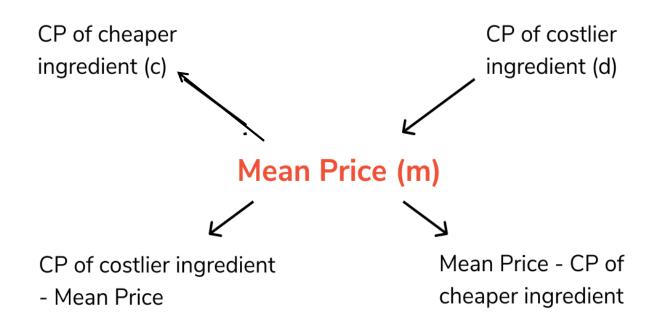
#### Soln:

Type 1 60

Type 2 120



$$\frac{x}{y} = \frac{d-m}{m-c} = \frac{120-75}{75-60} = \frac{45}{15} = \frac{3}{1} = 3:1$$



 $\frac{\text{Quantity of cheaper ingredient}}{\text{Quantity of costlier ingredient}} = \frac{d - m}{m - c}$ 



Mean

```
= (C.P. of Higher) - (Mean Price)
Quantity of Lower
Quantity of Higher
                         (Mean Price) – (C.P. of Lower)
                                   CPh - CPm
            <u>Q</u>|
            Qh
                                   CPm - CPI
                                   (CPh-CPm): (CPm-CPI)
(Qty Low) : (Qty High)
                 Low
                                                           High
                 Rate
                                                            Rate
                                     Mean Rate
                 High-
                                                           Mean-
```



Low

Q. In what ratio must a grocer mix two varieties of pulses costing Rs. 15 and Rs. 20 per kg respectively so as to get a mixture worth Rs. 16.50 per kg?

A. 3:7

B. 5:7

C. 7:3

D. 7:5

Ans: C



Q. CP of rice A is Rs. 15/kg and CP of rice B is Rs.20/kg. If both A and B are mixed in the ratio 2:3. Then find the price per kg of the mixed rice.

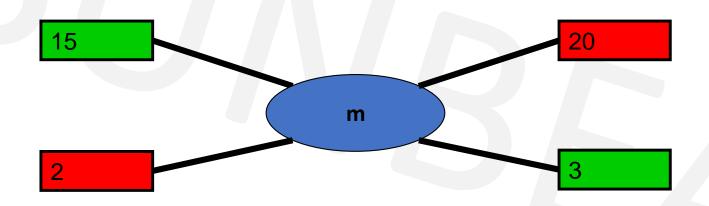
A. Rs. 28

B. Rs. 17

C. Rs. 18

D. Rs. 48

#### Soln:



$$\frac{x}{y} = \frac{d-m}{m-c}$$

$$2 \qquad 20-n$$

$$\frac{2}{3} = \frac{20-m}{m-15}$$

$$m = \frac{90}{5} = Rs.18$$

Ans: C



Q. In what ratio must a grocer mix two varieties of dal worth Rs. 60/kg & Rs. 65/kg, so that selling the mixture at 68.20/kg, he may gain 10%.

#### Soln:

- Mean price is always CP
- Steps-
- 1. m=?
- 2. m = cost price(CP)
- 3. SP = given
- 4. find x/y=?



In what ratio must a grocer mix two varieties of dal worth Rs. 60/kg & Rs. 65/kg, so that selling the mixture at 68.20/kg, he may gain 10%.

A. 3:2

B. 2:3

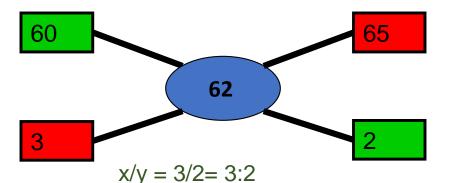
C. 3:4

D. 4:3

- SP of 1 kg of mixture = Rs. 68.20
- Gain =10%
- In case of profit,  $SP = \frac{C.P. x (100 + \%gain)}{100}$
- CP of 1kg of mixture = Rs  $(\frac{100}{100+10} \times 68.2)$

Mean price =Rs. 62

- By the rule of alligation, we have:
- C.P. of 1kg dal of 1<sup>st</sup> kind C.P. of 1kg dal of 2<sup>nd</sup> kind



Ans: A

Q. A person blends two varieties of tea, one cost Rs. 160/kg and other cost Rs. 200/kg in the ratio 5 : 4. He sells the blended variety at Rs.192/kg. Find the profit %.

A. 6%

B. 8%

C. 7%

D. 9%

#### Soln:

$$\frac{x}{y} = \frac{d-m}{m-c}$$

$$\frac{5}{4} = \frac{200 - m}{m - 160}$$

$$5m - 800 = 800 - 4m$$

$$9m = 1600$$

$$m = \frac{1600}{9}$$

SP=Rs.192(given), CP =mean price

Profit% = 
$$\frac{SP-CP}{CP} \times 100$$
  
=  $\frac{192 - \frac{1600}{9}}{1600} = \frac{17}{2}$ 

$$= \frac{192 - \frac{1600}{9}}{\frac{1600}{9}} = \frac{1728 - 1600}{1600} = \frac{128}{16} = 8\%$$

cheaper price

dearer price



Ans: B



Q. What quantity of sugar costing Rs 6.10 per kg must be mixed with 126 kg of sugar priced at Rs 2.85 per kg so that 20% may be gained by selling mix at Rs 4.80/kg?

A. 65 kg

B. 69 kg

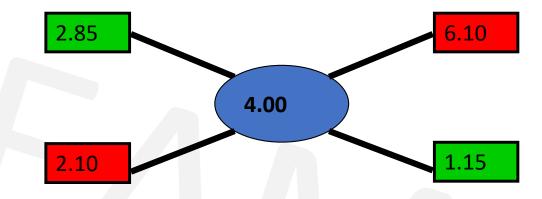
C. 66 kg

D. 64 kg

#### Soln:

$$SP = \frac{C.P. \times (100 + \%gain)}{100}$$

- CP (Mean) =  $4.8 \times 100/120 = 4.0$
- Qty of Low : Qty of High = 210/115 = 42/23
- 126 / Qh = 42/23
- $QI = 126 \times 23/42 = 69$
- Ans B





Q. Acid and water are mixed in a vessel A in the ratio of 5:2 and in the vessel B in the ratio of 8:5. In what ratio mixtures from two vessels should be mixed to get a new mixture in which the acid and water will be in the ratio of 9:4?

A. 7:2

B. 2:7

C. 7:4

D. 2:3

**Soln**: For these type of questions consider 1 ingredient out of the two ingredients and represent as fraction of one.

Α

В

a:w

a:w

5:2

8:5

C

a:w

9:4

We consider acid here, so fraction of acid,

 $\frac{A}{\frac{5}{}} = \frac{5}{5}$ 

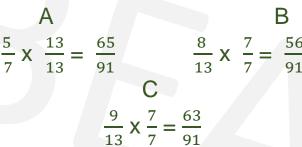
В

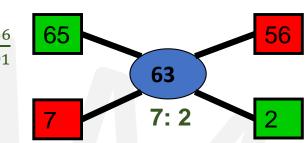
$$\frac{8}{8+5} = \frac{8}{13}$$

 $\frac{9}{9+4} = \frac{9}{13}$ 

Ans: A

To make calculations easier, convert all denominator into common one So, find LCM(7,13,13) = 91





forget denominators,

By rule of Alligation,

- Final concentration = Initial  $(1-\frac{R}{Initial})^n$
- where,
- Final concentration is the amount of concentration remaining after the process
- n is the number of times the process is done and
- R is the replaced quantity.
- Initial is the initial concentration



Q. A container contains 60 litres of milk. From this container 6 litres of milk was taken out and replaced by water. This process was repeated further two times. How much milk is now contained by the container?

A. 38.52 litres

B. 43.74 litres

C. 42.68 litres

D. 39.85 litres

#### Ans: B

The volume of milk remaining after the three processes is,

• V=N(1- $\frac{R}{N}$ )<sup>n</sup> = 60(1- $\frac{6}{60}$ )<sup>3</sup> = 60(1- $\frac{1}{10}$ )<sup>3</sup> = 60(0.729)

= 43.74 litres

where,

N is the original amount of milk, n is the number of processes and R is the replaced quantity.

Q. A container contains 100 L of milk. From this container 10 L of milk was taken out and replaced by water. This process was further repeated three times. How much milk does the container have now?

A. 72.9 litres

B. 65.61 litres

C. 34.39 litres

D. 81 litres

Ans: B

Final concentration = Initial concentration (1-Replaced/Initial)n



Q. The ratio of milk to water in 80 litres of a mixture is 7:3. The water (in litres) to be added to it to make the ratio 2:1 is?

A. 4 litres

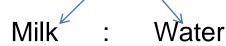
B. 5 litres

C. 6 litres

D. 8 litres

#### Soln:

Mixture = 80 litres



$$= 7+3 = 10(total parts of mixture)$$

Quantity of Milk = 
$$\frac{7}{10}$$
 x 80 = 56 litres

Quantity of Water = 
$$\frac{3}{10}$$
 x 80 = 24 litres

Let quantity of water added be 'x' litres

$$\frac{56}{24+x} = \frac{2}{1}$$

$$56 = 48 + 2x$$

$$x = 4$$
 litres of water is to be added.

Let, Milk = 
$$7x$$
 and Water =  $3x$ 

$$7x + 3x = 80$$
 litres

$$10x = 80$$

$$x = 8$$
litres

$$Milk = 7x = 7x8 = 56$$
 litres

Water = 
$$3x = 3x = 24$$
 litres

$$\frac{56}{24+x} = \frac{2}{1}$$
 56 = 48 + 2x

$$56 = 48 + 2x$$

x = 4 litres of water is to be added.



Q. How many kg of sugar costing Rs. 9 per kg must be mixed with 27kg of sugar costing Rs. 7 per kg, so that there maybe a gain of 10% by selling the mix at 9.24 per kg?

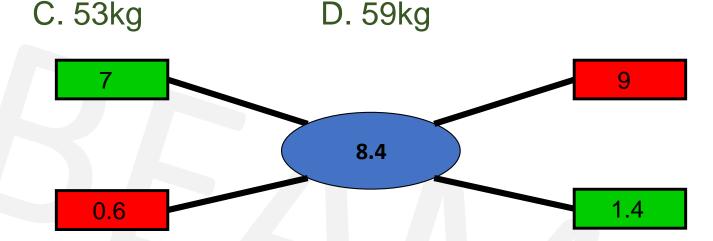
A. 62kg

B. 63kg

#### Soln:

$$SP = \frac{C.P. x (100 + \%gain)}{100}$$

 $CP (Mean) = 9.24 \times 100/110 = 8.4$ 



- Qty of Low: Qty of High = 0.6/1.4 = 6/14 = 3/7
- 27 / QH = 3/7
- $QH = 27 \times 7/3 = 63 \text{ kg}$

Ans: B



Q. The cost of two varieties of tea is ₹300 and ₹375 respectively. If both the varieties of tea are mixed together in the ratio 3 : 2, then what should be the price of mixed variety of tea per kg?

A. Rs. 340

B. Rs.330

C. Rs. 350

D. Rs. 360

Ans: B



Q. What quantity of sugar costing Rs 21.20 per kg must be mixed with 144 kg of sugar priced at Rs 26.20 per kg so that 10% may be gained by selling mix at Rs 25.30/kg?

A. 256 kg

B. 265 kg

C. 244 kg

D. 144 kg

Ans: A



Q. What ratio must a grocer mix tea at Rs. 60/kg and Rs. 65/kg, so that by selling the mixture at Rs. 69.30/kg, he may gain 10%

A. 2:3

B. 4:3

C. 3:2

D. 2:1

Ans: A



Q. Find the ratio in which the contains of 2 jars A & B containing spirit & water in the ratio 1:3 & 3:2 respectively must be mixed so that resulting mixture contains 45% spirit?

A. 2:3

B. 3:5

C. 3:2

D. 3:4

Ans D



Q. Two solutions have milk: water ratio of 2:3 and 4:5. In what ratio must they be mixed such that the resultant solution has milk: water ratio of 3:4? A. 8:3 B. 3:8 C. 5:9 D. 9:5

Ans: C



Q. In what ratio rice at Rs. 9.30/kg be mixed with rice at Rs. 10.80/kg. So that the mixture be worth Rs. 10/kg.

A. 6:5

B. 8:7

C. 3:7

D. 6:1

Ans: B



Q. The ratio, in which tea costing Rs. 192 per kg is to be mixed with tea costing Rs. 150 per kg so that the mixed tea when sold for Rs. 194.40 per kg, gives a profit of 20%.

A. 2:5

B. 3:5

C. 5:3

D. 5:2

Ans: A



Q. In what ratio must a mixture of 30% alcohol strength be mixed with that of 50% alcohol strength so as to get a mixture of 45% alcohol strength?

A. 1:2

B. 1:3

C. 2:1

D. 3:1

Ans: B



Q. A mixture of 70 litres of alcohol and water contains 10% of water. How much water must be added to the above mixture to make the water 12.5% of the resulting mixture?

A. 1 litre

B. 1.5 litres C. 2 litres

D. 2.5 litres

#### Ans: C

- Water=10% of 70 lit=7 lit,
- alcohol=90% of 70 lit=63 lit.
- Let, x lit water must be added. (7+x)\_ 12.5% 87.5%
- 7 + x = 787.5/87.57 + x = 9
- x=2 litres

Q. In what ratio should two qualities of coffee powder having the rates of ₹47 per kg and ₹32 per kg be mixed in order to get a mixture that would have a rate of ₹37 per kg?

A. 1:2

B. 4:1

C. 1:3 D. 3:1

E. 1:4

Ans: A



Q. How many kilograms of tea worth Rs. 3. 60 per kg. must be mixed with 8 kg. of tea worth Rs. 4.20 per kg. so that by selling the mixture at Rs. 4.40 per kg. There may be a of 10%.

A) 4 kg

B) 3 kg.

C) 6 kg.

D) 8 kg.

Ans: A



Q. The ratio of milk to water in 20 litres of a mixture is 3:1. The Milk (in litres) to be added to the mixture so as to have milk and water in the ratio 4:1 is?

A. 7 litres

B. 4 litres

C. 5 litres

D. 6 litres

Ans: C



Q. In what ratio must water be mixed with milk costing Rs. 12 per litre to obtain a mixture worth of Rs. 8 per litre?

A. 1:2

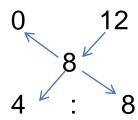
B. 2:1

C. 2:3

D. 3:2

#### Ans: A

By the rule of alligation:



Ratio of water to milk

= 4:8

= 1:2

Q. Two jars A and B contain milk and water in the ratio 7:5 and 17:7 respectively. In what ratio mixtures from two vessels should be mixed to get a new mixture containing milk and water in the ratio 5:3?

A. 2:1

B. 1:2

C. 2:3

D. 3:4

#### Soln:

For these type of questions consider 1 ingredient out of the two ingredients and represent as fraction of one.

Α

В

m:w

m:w

7:5

17:7

m:w

5:3

C

We consider milk here, so fraction of milk,

$$\frac{7}{7+5} = \frac{7}{12}$$

$$\frac{17}{17+7} = \frac{17}{24}$$

$$\frac{5}{5+3} = \frac{5}{8}$$

Ans: A

To make calculations easier, convert all denominator into common one

So, find LCM(12,24,8) = 24

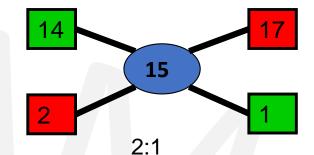
$$\frac{7}{12}$$
 X  $\frac{2}{2} = \frac{14}{24}$ 

В

$$\frac{5}{8}$$
 x  $\frac{3}{3}$  =  $\frac{15}{24}$ 

forget denominators,

By rule of Alligation,



Q. Two vessels A and B contain spirit and water mixed in the ratio 5:2 and 7:6 respectively. Find the ratio in which these mixtures are mixed to obtain a new mixture in vessel C containing spirit and water in the ratio 8:5?

A. 4:3

B. 3:4

C. 5:6

D. 7:9

Ans: D



Q. A container contains 40 litres of milk. From this container 4 litres of milk was taken out and replaced by water. This process was repeated further two times. How much milk is now contained by the container?

A. 26.34 litres

B. 27.36 litres

C. 28 litres

D. 29.16 litres

#### Ans: D

• The volume of milk remaining after the three processes is,

• V=N(1- $\frac{R}{N}$ )n = 40(1- $\frac{4}{40}$ )<sup>3</sup> = 40(1- $\frac{1}{10}$ )<sup>3</sup> = 40(0.729) =29.16

where,

N is the original amount of milk, n is the number of processes and R is the replaced quantity.

#### Basics

Profit (Gain) = (S.P - C.P)

Loss =(C.P - S.P)

% gain =  $(Gain / C.P) \times 100$ 

% loss =  $(Loss / C.P) \times 100$ 

#### Multipliers to find S.P

In Case of Profit: S.P. = C.P.  $\times$  (100 +%gain)/100

In Case of Loss : S.P. = C.P. x (100 - %loss)/100

i.e For sale at 25% profit S.P. = 125 % of C.P.

For sale at 25% loss S.P. = 75% of C.P.



Q. A man bought certain no of oranges at the rate of 5 for Rs 4 and sold them at the rate of 4 for Rs 5. Find his overall profit/loss percentage?

A. 25.5% Pr

B. 36.5% Pr C. 56.2% Pr

D. 64.5% Pr

#### Soln

Cost Price

Selling Price

Oranges → Rs Oranges →

Rs

 $20 \rightarrow 16 20 \rightarrow$ 

25

SP>CP, so profit

 $P\% = (SP - CP)/CP \times 100$ 

 $= (25-16)/16 \times 100$ 

= 225/4 = 56.20%

Ans: C

**Cost Price** Oranges → Rs

Selling Price Oranges > Rs

SP>CP, so profit  $P\% = (SP - CP)/CP \times 100$ 

Q. A man bought banana at the rate of 8 for Rs 34 and sold them at the rate of 12 for Rs 57 How many banana should be sold to earn a net profit of Rs. 45?

A. 90

B. 100

C. 135

D. 150

#### Soln:-

**Cost Price** 

banana >

Rs

Selling Price

banana ->

12

Rs

57

- SP>CP, so profit
- Profit = (SP CP)

$$= \frac{19}{4} - \frac{17}{4} = \frac{1}{2}$$

No. of banana to make a profit of Rs.45

$$= \frac{\text{Profit total}}{\text{Pofit one}} = \frac{45}{1/2} = 90 \text{ banana}$$

Ans: A



Q. When a article is sold for Rs.116, the profit percent is thrice as much as when it is sold for Rs. 92. The cost price of article is –

A. Rs. 68

B. Rs. 72 C. Rs. 78

D. Rs. 80

#### Soln:

• %P when SP is 116  $= 3 \times \%$ P when SP is 92

• 
$$\frac{116-CP}{CP}$$
 x 100

• 
$$\frac{116-CP}{CP} \times 100 = 3 \times \frac{92-CP}{CP} \times 100$$

• 116 - CP = 276 - 3CP

• 2CP =160

• CP =Rs. 80

Ans: D

## **Profit & Loss**

Q. By selling 90 ball pens for Rs.160, a person loses 20%. How many ball pens should be sold for Rs.96, so as to have a profit of 20%?

A. 20

B. 30

C. 36

D. 26

Ans: C

Soln:

SP =Rs. 160 ,loss =20%

 $CP = \frac{100}{100-20} \times 160 = Rs.200$ 

SP =Rs. 96 ,profit =20%

 $CP = \frac{100}{100+20} \times 96 = Rs.80$ 

Rs.200 CP of = 90 ball pens

Rs. 80 CP of = ?  $\frac{90 \times 80}{200}$  = 36 ball pens

## **Profit & Loss**

Q. If selling price is doubled, the profit triples. Find the profit %.

A. 
$$66\frac{2}{3}\%$$

B. 100%

C. 
$$105\frac{1}{3}\%$$

D. 120%

#### Soln:

Let, 
$$CP = C$$
,  $SP=S$ 

As they ask profit %, we know profit = SP - CP

As per given,

$$3(S-C) = 2S-C$$

$$3S - 3C = 2S - C$$

$$S = 2C$$

But, Profit = 
$$S - C = 2C - C = C$$

Profit % = 
$$\frac{\text{profit}}{\text{CP}} \times 100 = \frac{\text{C}}{\text{C}} \times 100 = 100\%$$



## **Combination**

Q. A merchant has 1000 kg of sugar, part of which he sells at 8% profit and rest at 18% profit. he gains 14% on the whole. What is the quantity sold at 18% profit?

A. 300 kg

B. 700 kg

C. 600 kg

D. 400 kg

Ans: C



## **Combination**

Q. A man has 80 pens. He sells some of these at 15% profit and the rest at 10%loss. Overall he gets a profit of 10%. Find how many pens were sold at 15% profit?

A. 16

B. 64

C. 40

D. 72

Ans: B



## **Mixtures & Alligation**

Q. A person blends two varieties of tea, one cost Rs. 160/kg and other cost Rs. 200/kg in the ratio 5 : 4. He sells the blended variety at Rs.192/kg. Find the profit %.

A. 6%

B. 8%

C. 7%

D. 9%

### Soln:

$$\frac{x}{y} = \frac{d-m}{m-c}$$

$$\frac{5}{4} = \frac{200 - m}{m - 160}$$

$$5m - 800 = 800 - 4m$$

$$9m = 1600$$

$$m = \frac{1600}{9}$$

SP=Rs.192(given), CP =mean price

Profit% = 
$$\frac{SP-CP}{CP} \times 100$$
  
=  $\frac{192 - \frac{1600}{9}}{1600} = \frac{17}{2}$ 

$$= \frac{192 - \frac{1600}{9}}{\frac{1600}{9}} = \frac{1728 - 1600}{1600} = \frac{128}{16} = 8\%$$

cheaper price

dearer price



Ans: B



If gain is half of SP, the gain percentage is \_\_\_\_\_?

A. 50%

B. 33.33%

C. 25%

D. 100%

### Soln:

we know profit = SP - CP

As per given,

1/2SP = SP-CP

CP = SP - 1/2SP

SP = 2CP

But, Profit = SP - CP = 2CP - CP = CP

Profit % =  $\frac{\text{profit}}{\text{CP}}$  x 100 =  $\frac{\text{CP}}{\text{CP}}$  x 100 = 100%

Ans: D



Q. If the cost price of 6 pencils is equal to the selling price of 5 pencils, then the gain per cent is

```
A. 10%
```

B. 20%

C. 15%

D. 25%

#### Soln:

Let the cost price of one pencil be Rs.1. CP of 5 pencils =Rs. 5

CP of 6 pencils =Rs. 6

as, SP of 5 pencils = CP of 6 pencils

SP of 5 pencils = Rs.6 if, SP > CP so it's a profit profit = SP - CP = 6 - 5= 1 Profit % = profit/cp x 100 =  $1/5 \times 100$ 

= 20%

SP=CP + gain 6 times CP is equal to 5 times SP

6CP=5SP 6CP=5(CP + gain) 6CP=5CP+5gain CP=5 gain

Gain % = gain/CP x100 = 1/5 x 100 = 20%





Q. Ram bought 1600 eggs at the rate of Rs. 3.75 per dozen. He sold 900 of them at 2 eggs for Rs. 1 and the remaining at 5 eggs for Rs. 2. Find his loss or gain per cent.

A. 4%

B. 45%

C. 42%

D. 46%

#### Ans: D

Price of 12 eggs = Rs. 3.75

Price of 1 egg = 3.75/12 = Rs.0.3125

Price of 1600 eggs = Rs.  $(0.3125 \times 1600) = Rs.500$ 

 $CP ext{ of eggs} = Rs. 500$ 

Selling price of 2 eggs = Rs. 1

Selling price of 900 eggs =

Selling price of 5 eggs = Rs. 2

Selling price of remaining (1600 - 900 = 700) eggs

Total SP of eggs = Rs. 450 + 280 = Rs.730.

### $SP > CP \rightarrow profit/gain$

Gain = SP - CP = Rs. 730 - 500 = Rs. 230.

 $%Gain = 230/500 \times 100 = 46\%$ 



Q. A shopkeeper purchases 11 sword for Rs.10 and sells them at the rate of 10 sword for Rs. 11. He earns a profit % of?

A. 11%

B. 15%

C. 20%

D. 21%

Ans: D



Q. A bookseller sells 84 books at the cost of 72 books. Find his profit or loss%

A. 14.28%

B. 28.24%

C. 20.4%

D. 12.86%

Ans: A



Q. By selling 100 pencils, a shopkeeper gains the selling price of 20 pencils. His gain per cent is

A) 25

B) 20

C) 15

D) 12

Ans: A

SP – CP = gain here gain = SP of 20 pencils

S.P. of 100 pencils – C.P. of 100 pencils = S.P. of 20 pencils

S.P. of 80 pencils = C.P. of 100 pencils

Let C.P. of 1 pencil = Rs. 1

S.P. of 80 pencils = Rs. 100

C.P. of 80 pencils = Rs. 80

Profit  $\% = \frac{100-80}{80} \times 100 = 25\%$ 

Q. A man bought a horse & carriage together for Rs 15600 & sold them together, the horse at 36% profit & the carriage at 15% loss. If selling price of both is equal. Find the cost of the carriage?

A.Rs.6000

B. Rs.7600

C. Rs.3600

D. Rs.9600

- · Soln
- Let CP of horse be H & Carriage be C → H+C= 15600
- SP of both is equal
- So, comparing the CPs
- 136H/100 = 85C/100

• H

= 5C/8

• 5C/8 + C

= 15600

• 13C/8

= 15600

• (

 $= 1200 \times 8$ 

• C

= 9600

Q. A vendor bought 6 oranges for Re 10 and sold them at 4 for Re 6. Find his loss or gain percent.

A. 8% gain

B. 10% gain

C. 8% loss

D. 10% loss

Ans: D



Q. A shopkeeper sells his goods at 10% loss but uses a weight of 750gms instead of 1kg. Find profit %

A. 20% Pr

B. 14.28% Pr C. 30% Pr

D. 25% Ls

Ans: A



Q. A fruit seller buys oranges at 4 for Rs. 3 and sells them at 3 for Rs. 4. Find its profit percent.

A. 43.75% Pr B. 77.7% Pr C. 75% Pr

D. 65.7% Ls

Ans: B



Q. A man buys a cycle for Rs. 1400 and sells it at a loss of 15%. What is the selling price of the cycle?

A. Rs. 1090

B. Rs. 1160

C. Rs. 1190

D. Rs. 1202

Ans: C



Q. 100 oranges are bought at the rate of Rs. 350 and sold at the rate of Rs. 48 per dozen. The percentage of profit or loss is:

A. 14 2/7% gain B. 15% gain

C. 14 2/7% loss

D. 15 % loss

Ans: A



Q. A shopkeeper sells his goods at 20% profit and to make an extra profit he gives only 800 gm per kg. Find his profit %

A. 25% Pr B. 33.33% Pr C. 50% Pr D. 25% Ls

Soln

CP SP Profit

100 120 20

80 120 40

% Profit =  $40/80 \times 100$ 

 $= 1/2 \times 100$ 

= 50%

Ans: C



Percentage is a fraction whose denominator is 100(per 100)

Fract ion	% <b>+100</b>	Fracti on	%	Fracti on	%	Fracti on	%	Fracti on	%
x100				1/1	100%	1/6	16.66	1/11	9.09
3/4	75%	5/4	125%				%		%
4/5	80%	3/2	150%	1/2	50%	1/7	14.28 %	1/12	8.33 %
2/3	66.66	1/16	6.25%	1/3	<b>33.33</b> %	1/8	12.5 %	1/13	<b>7.69</b> %
5/6	83.33			1/4	25%	1/9	11.11 %	1/14	<b>7.14</b> %
6/5	120%			1/5	20%	1/10	10%	1/15	6.66 %



Q. x is 83.33% of y. So y is \_\_\_\_\_% of x

### **Solution:**

$$x = 83.33y$$

$$x = \frac{5}{6} y$$

So, 
$$y = \frac{6}{5}x$$

y = 120% (from chart)

Fraction x100	% 100	Fraction	%
3/4	<b>75</b> %	5/4	125%
4/5	80%	3/2	150%
2/3	66.66	1/16	6.25%
5/6	83.33		
6/5	120%		



**Q.** x is 80% of y. So y is \_\_\_\_\_% of x

### Solution:

$$x = 80y$$

$$X = \frac{4}{5} y$$

$$x = \frac{4}{5}y$$
So,  $y = \frac{5}{4}x$ 

$$y = 125\%$$

Q. A number x is increased by 20% then the number is decreased by 20%. Find the net % change.

- <u>Soln</u>:
- If a number is increased / decreased by x% then there is always a loss of  $-(x/10)^2$
- Net % Change =  $-(20/10)^2 = -(400/100) = -4\%$  (loss)
- OR
- Let the number be 100
- 100 ↑ by 20% =120
- So  $20\% \downarrow$  of 120 = 96
- 10012096
  - -4% = net change



Q. A number x is increased by 50% then the number is increased by 20% and again by 10%. Find the net % change

#### Soln:

- Let the number be 100
- 100 by 50% = 150
- Again,  $150 \uparrow$  by 20% = 30, So 150 + 30 = 180
- 10% of 180 = 18, So, 180 + 18 = 198

100150180198

98% = net change

### Two Step change of Percentage

In first step if number is changed by a% and the result is again changed by b% the net percentage change of original number is given by

Net % Change in Number = a + b + ab/100 (+ve or -ve)



Q. If a number is increased by 12 % & then decreased by 18% then the net % change in number is

#### Soln:

Net % Change in Number = a + b + ab/100 (+ve or -ve)

% Change = 
$$12 - 18 + (12 \times -18)/100$$
  
=  $-6 - 2.16$   
=  $-8.16\%$ 



- Expenditure = Price x Consumption
- $P \propto \frac{1}{\text{Consumption}}$
- So, for expenditure to remain constant, when one quantity increases the other quantity should decrease proportionally.
- Eg: If the price of a commodity is decreased by 20% and its consumption is increased by 20%, what will be the increase or decrease in expenditure on the commodity?
- Soln:

Net % Change = 
$$a + b + ab/100$$
 (+ve or -ve)  
% Change =  $-20 + 20 + (-20 \times 20)/100$   
=  $0 - 4 = -4\%$ 

#### <u>OR</u>

100 === 20%↓(Decrease in Price) ===> 80 === 20%↑(Increase in Consumption) ===> 96. Thus, there is a decrement of 4%



Q. Two numbers are respectively 40% and 60% more than a third number. The ratio of the two numbers is:

A. 7:8 B. 3:5

C.4:5

D. 6:7

Soln:-

- Let the third number be 100
- First number = 40% more than 100 = 100 + 40% of 100 = 100 + 40 = 140
- Second number = 60% more than 100 = 100 + 60% of 100 = 100 + 60 = 160

• Ratio = 
$$\frac{\text{first number}}{\text{second number}} = \frac{140}{160} = \frac{7}{8} = 7:8$$

Ans: A

## Percentage using x

Q. Two numbers are respectively 40% and 60% more than a third number. The ratio of the two numbers is:

A. 7:8

B. 3:5

C.4:5

D. 6:7

Soln:-

• Let the third number be x.

• First number = 40% more than x = x + 40% of  $x = x + \frac{40}{100}x = \frac{100x + 40x}{100} = \frac{140x}{100}$ 

• Second number = 60% more than x = x + 60% of  $x = x + \frac{60}{100}x = \frac{100x + 60x}{100} = \frac{160x}{100}$ 

• Ratio = 
$$\frac{\text{first number}}{\text{second number}} = \frac{\frac{7x}{5}}{\frac{8x}{5}} = \frac{7}{8} = 7:8$$

Ans: A

Q. If the price of sugar increases by 25%, by what percent will a housewife have to reduce her consumption to leave total expenditure on sugar unchanged?

A. 25%

B. 35%

C. 20%

D. 15%

Ans: C



Q. If the radius of a circle is decreased by 50%, find the percentage decrease in its area.

• A. 55%

- B. 65%
- C. 75%

D. 85%

- · Soln:
- Area of a circle =  $\pi r^2$  where r is the radius => Area is directly proportional to  $r^2$
- Assume the old radius is = r1=100
- $A_1 = \pi \times 100^2 = 10000\pi$

Assume the new radius is = r2=50

$$A_2 = \pi \times 50^2 = 2500\pi$$

Decrease in area =  $10000\pi - 2500\pi = 7500\pi$ 

Percentage decrease in area =  $\frac{difference}{old}$  x100 =  $\frac{7500\pi}{10000\pi}$  x 100 = 75%

• Ans : C



Q. 1.14 expressed as a per cent of 1.9 is:

A. 6%

B. 10%

C. 60%

D. 90%

Ans: C



Q. A number x is increased by 20% then the number is increased by 10% and again by 50%. Find the net % change.

A. 77%

B. 75%

C. 88%

D. 98%

E. 99%

Ans: D



Q. If the altitude of a triangle increases by 5% and the base of the triangle increases by 7%, by what percent will the area of the triangle increase?

A. 12.25% B. 12.35%

C. 6.00%

D. 5.25%

Ans B



Q. The length and breadth of a room are increased by 25% and 40% respectively. While the height is decreased by 20%. Find % change.

A. 16%

B. 40%

C. 60%

D. 30%

Ans B



Q. If the length of a rectangle is increased by 37.5% and its breadth is decreased by 20%, find the change in its area.

A. 15% increase B. 13% decrease C. 10% increase D. 10% decrease

Ans: C



Q. The ratio 5: 4 expressed as a percent equals:

A. 125%

B. 80%

C. 40%

D. 12.5%

Ans: A

Required  $\% = 5/4 \times 100 = 125\%$ 



# Percentage(Assignment)

Q. 12% of 5000 = ?

A. 600

B. 620

C. 680

D. 720



# Percentage(Assignment)

Q. 280% of 3940 = ?

A. 10132

B. 11032

C. 11230

D. 11320

Ans: B



### Percentage(Assignment)

Q. 15% of 578 + 22.5% of 644 = ?

A. 231.4

B. 231.6

C. 231.8

D. 233.6

Ans: B



- How likely an event is supposed to happen.
- Probability =  $\frac{\text{Favourable outcome}}{\text{Total number of outcomes}}$
- AND → multiply(x) e.g:- 1green and 1 blue ball in a box
- OR → Add (+) e.g:- 1 red or 1 blue ball in a box
- 1 bag has 3 balls, what is the probability of you picking up 2 balls?

Total no. of balls the bag contains

Out of which how many balls
We need to choose
(tells number of times 3 has to be reduces)

Probability = 
$$\frac{\text{Favourable outcome}}{\text{Total number of outcomes}}$$



### **Points to Remember**

- The **probability** of an event will not be less **than** 0.
- This is because 0 is impossible (sure that something will not happen).
- The **probability** of an event will not be **more than 1**. This is because **1** is certain that something will happen.
- The probability of an event is a number describing the chance that the event will happen.
- An event that is certain to happen has a probability of 1.
- An event that cannot possibly happen has a probability of 0.
- If there is a chance that an event will happen, then its probability is between 0 & 1.



- Atleast min to max
- Eg:- 2 bags out of 3 min max

So various probabilities to be done is 2 and 3

- Atmost max to min
- Eg:- A bag has 3 balls out of which probability to pick up 2 balls

atmost 2  $\rightarrow$  max 2, 1, 0 (min)



Q. A bag contains 2 red, 3 green and 2 blue balls. Two balls are drawn at random. What is the probability that none of the balls drawn is blue?

A. 10/21

B. 11/21

C. 2/7

D. 5/7

- · Soln-
- Total balls = 2+3+2=7 balls in the bag
- None = blue (neglect whichever color is written after none)
- Draw = 2 balls

• Probability = 
$$\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{2\text{R or } (1\text{R and } 1\text{ G}) \text{ or } 2\text{G}}{7\text{C}_2} = \frac{2\text{C}_2 + (2\text{C}_1 \times 31) + 3\text{C}_2}{7\text{C}_2} = \frac{10}{21}$$

Q. In a box, there are 8 red, 7 blue and 6 green balls. One ball is picked up randomly. What is the probability that it is neither red nor green?

A. 1/3

B. 3/4

C. 7/19

D. 8/21

E. 9/21

### Soln:

- Total balls = 8+7+6 = 21 balls in the box
- Neither red nor green means only blue
- Draw =1 ball

• Probability = 
$$\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{\text{1blue out of total 7}}{21C_1} = \frac{7C_1}{21C_1} = \frac{7}{21} = \frac{1}{3}$$

Q. In a class, there are 15 boys and 10 girls. Three students are selected at random. The probability that 1 girl and 2 boys are selected, is:

A. 21/46

B. 25/117

C. 1/50

D. 3/25

### Soln:

- Total students = 15 + 10 = 25 students in a class
- Draw = 3 students

Probability = 
$$\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{10C_1 \times 15C_2}{25C_3} = \frac{21}{46}$$



Q. What is the probability of getting a sum 5 from two throws of a dice?

A. 1/9

B. 1/8 C. 1/7 D. 1/6

Soln-

Dice =6 faces = 6 possibilities

So in two throws of dice, total possibilities = 6 x 6= 36

Sum =5,so favourable outcomes are -  $\{(1,4), (4,1), (2,3), (3,2)\}$ 

Probability = 
$$\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{4}{36} = \frac{1}{9}$$



Q. Three unbiased coins are tossed. What is the probability of getting utmost two heads?

A.  $\frac{3}{4}$ 

B. 1/4

C. 3/8

D. 7/8

· Soln-

• Total possibilities = {TTT, TTH, THT, HTT, THH, HTH, HHT, HHH}

Event of getting utmost 2 heads = max 2H or 1H or 0H

• Possibility of getting 2 H = {TTT, TTH,THT, HTT, THH, HTH, HHT}

• Probability =  $\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{7}{8}$ 

Ans: D

- A Standard deck of playing cards consist of 52 cards, among them there are 4 subgroups/suits –
- The four suits with there names, symbols and color –

1. The suit of Hearts



26 red cards

2. The suit of Diamonds



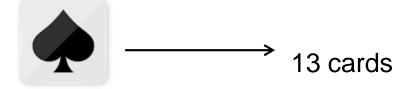
13 cards

3. The suit of Clubs

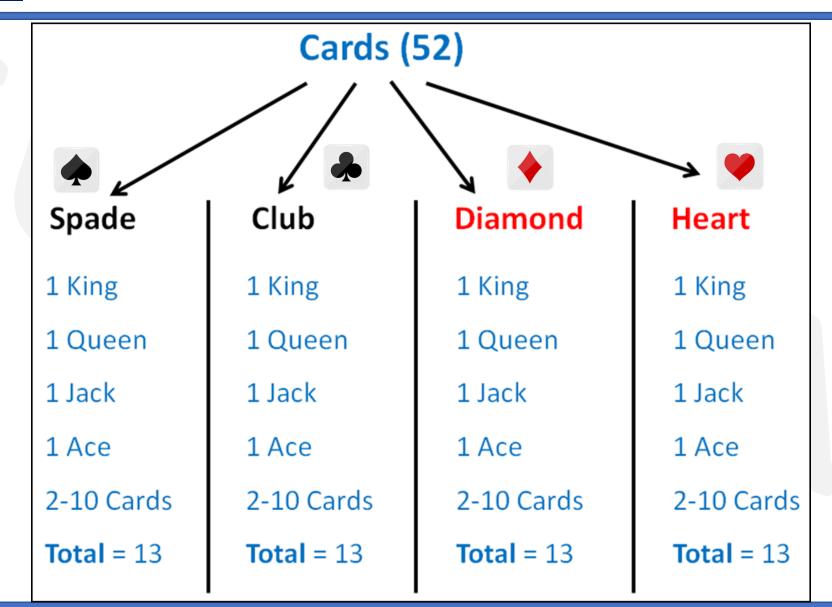


26 black cards

4. The suit of Spades









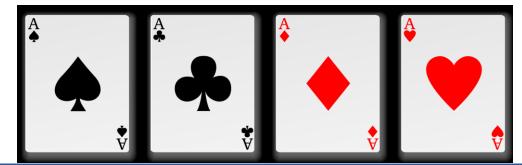
- King, Queen and Jack (or Knaves) are face cards. So, there are 12 face cards in the deck of 52 playing cards.
- Jokers are not normally considered to be face cards







- Aces
- There are 4 Aces in every deck, 1 of every suit.





Q. From a pack of 52 cards, two cards are drawn together at random. What is the probability of both the cards being kings?

A. 1/15

B. 25/57

C. 35/256

D. 1/221

- · Soln-
- Total cards in a pack =52
- Total kings in a pack = 4
- Drawn =2

• Probability =  $\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{4C_2}{52C_2} = \frac{1}{221}$ 

Ans: D

Q. Out of 450 students of a school 325 play football,175 play cricket and 50 neither play football nor cricket. How many students play both football and cricket?

A. 50

B. 75

C. 100

D. 225

#### Soln:

- AUB is used for the set that contains those elements that are either in A or in B, or in both.
- A∩B is used for the largest set which contains all the elements that are common to both the sets.
- $n(A \cap B) = n(A) + n(B) n(A \cup B)$   $\rightarrow$  addition theorem of probability.
- Total students who play either Cricket or football or both cricket and football
- =  $n(A \cup B) = 450 50 = 400$
- students who play cricket, n(A) = 325 and students who play football, n(B) = 175
- Students who play both football and Cricket = n(A∩B) = 325 + 175 400 = 100
- Ans: C



Q. Two dice are rolled. Find the probability of getting a sum of 8 or 11 on both the dices.

A. 5/36

B. 9/36

C. 7/36

D. 11/36

- Favorable outcomes for sum of 8 or 11 on both the dices are-
- (2,6),(3,5),(4,4),(5,3),(6,2),(5,6),(6,5)
- Number of favorable outcomes = 7
- Probability =  $\frac{7}{36}$

A man tossed two dice. What is the probability that the total score is a prime number?

A. 5/12

B. 5/14

C. 5/20

D. 5/24

- · Soln-
- Dice =6 faces = 6 possibilities
- 2 Dice =  $6 \times 6 = 36$  possibilities
- Sum = prime number
- So favourable outcomes are { (1,1), (1,2), (1,4), (1,6), (2,1), (2,3), (2,5), (3,2), (3,4), (4,1), (4,3), (5,2), (5,6), (6,5), (6,1) }
- Probability =  $\frac{\text{Favourable outcome}}{\text{Total number of outcomes}} = \frac{15}{36} = \frac{5}{12}$



Q. A brother and sister appear for an interview against two vacant posts in an office. The probability of the brother's selection is 1/5 and that of the sister's selection is 1/3. What is the probability that one of them is selected?

A. 1/5

B. 2/5

C. 1/3

D) 2/3

Soln: -

(brother is selected and sister is not selected) OR (brother is not selected and sister is selected)

Probability = 
$$\frac{1}{5} \times \frac{2}{3} + \frac{4}{5} \times \frac{1}{3}$$
  
=  $\frac{6}{15}$ 

sister not selected = 1 – prob. of sister selected = 1- $\frac{1}{3}$ =  $\frac{2}{3}$ 

 $=\frac{2}{5}$ 

Ans: B

brother not selected = 1 – prob. of brother selected = 1- $\frac{1}{5}$ =  $\frac{4}{5}$ 

Q. Probability of occurrence of event A is 0.5 and that of event B is 0.2. the probability of occurrence of both A and B is 0.1. what is the probability that none of A and B occur?

A. 0.4

B. 0.5

C. 0.2

D. 0.1

#### Soln:

probability of sure event = 1

- Given P(A) = 0.5 and P(B) = 0.2
- $P(A \text{ or } B) = P(A \cup B) = P(A) + P(B) P(A \cap B)$ = 0.5 + 0.2 - 0.1 = 0.6
- And P(neither A nor B) =  $P(A' \cap B') = 1 P(A \cup B) = 1 0.6 = 0.4$ .

- Note: P(A∪B) = P(A) + P(B) P(A∩B)
- This is also known as the addition theorem of probability.



Q. A bag contains 4 white, 5 red and 6 blue balls. Three balls are drawn at random from the bag. The probability that all of them are red, is?

A. 1/22

B. 3/22

C. 2/91

D. 2/77



Q. What is the probability of getting a sum 9 from two throws of a dice?

A. 1/6

B. 1/8

C. 1/9

D. 1/12



Q. A bag contains 6 black and 8 white balls. One ball is drawn at random. What is the probability that the ball drawn is white?

A.  $\frac{3}{4}$ 

B. 4/7

C. 1/8

D. 3/7

Ans: B



Q. A bag contains 6 blue balls, 3 white balls and 4 green balls. If two balls are drawn at random what is the possibility that they are not of the same color?

A. 6/13

B. 7/13

C. 9/13

D. 10/13



Q. One card is drawn at random from a pack of 52 cards. What is the probability that the card drawn is a face card (Jack, Queen and King only)?

A. 1/13

B. 1/4

C. 3/13

D. 9/52



Q. One card is drawn at random from a pack of 52 cards. What is the probability that the card drawn is not a face card (Jack, Queen and King only)?

A. 5/13

B. 10/13

C. 1/13

D. 1/26

Ans: B



Q. A basket contains 6 apples ,4 pears and 3 oranges. If two fruits are picked up at random, what is the probability that both are pears?

A. 4/13

B. 1/13

C. 2/13

D. 3/26

Ans: B



### **Partnership**

Q.A started business with Rs. 45,000 and B joined afterwards with 30,000. If the profit at the end of a year was divided in the ratio 2: 1 respectively, then B would have joined A for business after.

A. 1 month

B. 2 months

C. 3 months

D. 4 months

Soln:

• Capital of A = Rs. 45,000

Capital of B = Rs. 30,000

- Ratio of P1:P2=2:1
- using formula,

• In this type, the time period is 12 months i.e. one year

• 
$$\frac{45000 \times 12}{30000 \times T2}$$
 =  $\frac{2}{1}$ 

- T2=9
- B would join business after (12 9) = 3 months
- Ans: C

### **Partnership**

Q. If 4 (A's capital) = 6 (B's capital) = 10 (C's capital), then out of a profit of Rs. 4650, C will receive \_

A) Rs.700

B) Rs.800

C) Rs.900

D) Rs.1000

### Soln:

$$4A = 6B = 10C$$
 $A = 10/4C = 5/2C$  and  $B = 10/6C = 5/3C$ 
 $A + B + C = 4650$ 
 $5/2C + 5/3C + C = 4650$ 
 $C = 900$ 

Share of C or C will receive Rs.900



### **Partnership**

Q. A, B & C enter into a partnership with total of Rs 8,200. A's capital is Rs 1000 more than B's & Rs 2000 less than C's. What is B's share of annual profit of Rs 2,460?

A. Rs 1320

B. Rs 720

C. Rs 420

D. Rs 520



Q. A started a business by investing Rs. 32000. After 4 months B joined him with some investments. At the end of the year the total profit was divided in the ratio 6:5. How much capital was invested by B?

A. Rs. 30,000

B. Rs. 28000

C. Rs. 40000

D. Rs. 19000



Q. Three persons stared a placement business with a capital of Rs. 3000. B invests Rs. 600 less than A and C invests Rs. 300 less than B. What is B's share in a profit of Rs. 886?

A. Rs. 443

B. Rs. 354.40

C. Rs. 265.80

D. Rs. 177.20



Q. Anand and Deepak started a business investing Rs.22,500 and Rs.35,000 respectively. Out of a total profit of Rs. 13,800. Deepak's share is

A. Rs 9600

B. Rs 8500

C. Rs 8450

D. Rs 8400

Ans: D

Ratio of their shares-

= 22500 : 35000

= 9:14

Deepak's share =  $Rs.(13800 \times 14/23)$ 

= Rs. 8400



Q. A started a business with Rs. 21,000 and is joined afterwards by B with Rs. 36,000. After how many months did B join if the profits at the end of the year are divided equally?

A. 4

B. 5

C. 6

D. 7

Ans: B

• Capital of A = Rs. 21000

Capital of B = Rs. 36000

- Ratio of P1:P2=1:1
- using formula,

$$\cdot \frac{\text{C1T1}}{\text{C2T2}} = \frac{\text{P}'}{\text{P}'}$$

• In this type, the time period is 12 months i.e. one year

• 
$$\frac{21000 \times 12}{36000 \times T2}$$
 =  $\frac{1}{1}$ 

- T2=7
- B would join business after (12 7) = 5 months

Q. A,B,C subscribes Rs. 50000 for a buisness. A subscribes Rs. 4000 more than B and B Rs. 5000 more than C. Out of a total profit of Rs. 35000, A receives :

A. Rs. 8400

B. Rs. 11900

C. Rs. 13600

D. Rs. 14700

Ans: D



- Three partners A, B, C start a business. B's Capital is four times C's capital and twice A's capital is equal to thrice B's capital. If the total profit is Rs 16500 at the end of a year ,Find out B's share in it.
- A. Rs. 4000 B. Rs. 5000

C. Rs. 6000

D. Rs. 7000

- Ans: C
- A: B = 3:2
- B : C = 4 : 1
- A:B:C = 12:8:2(using inverted N)
- A:B:C = 6:4:1

Share of B =  $16500 \times 4/11 = 6000/-$ 



