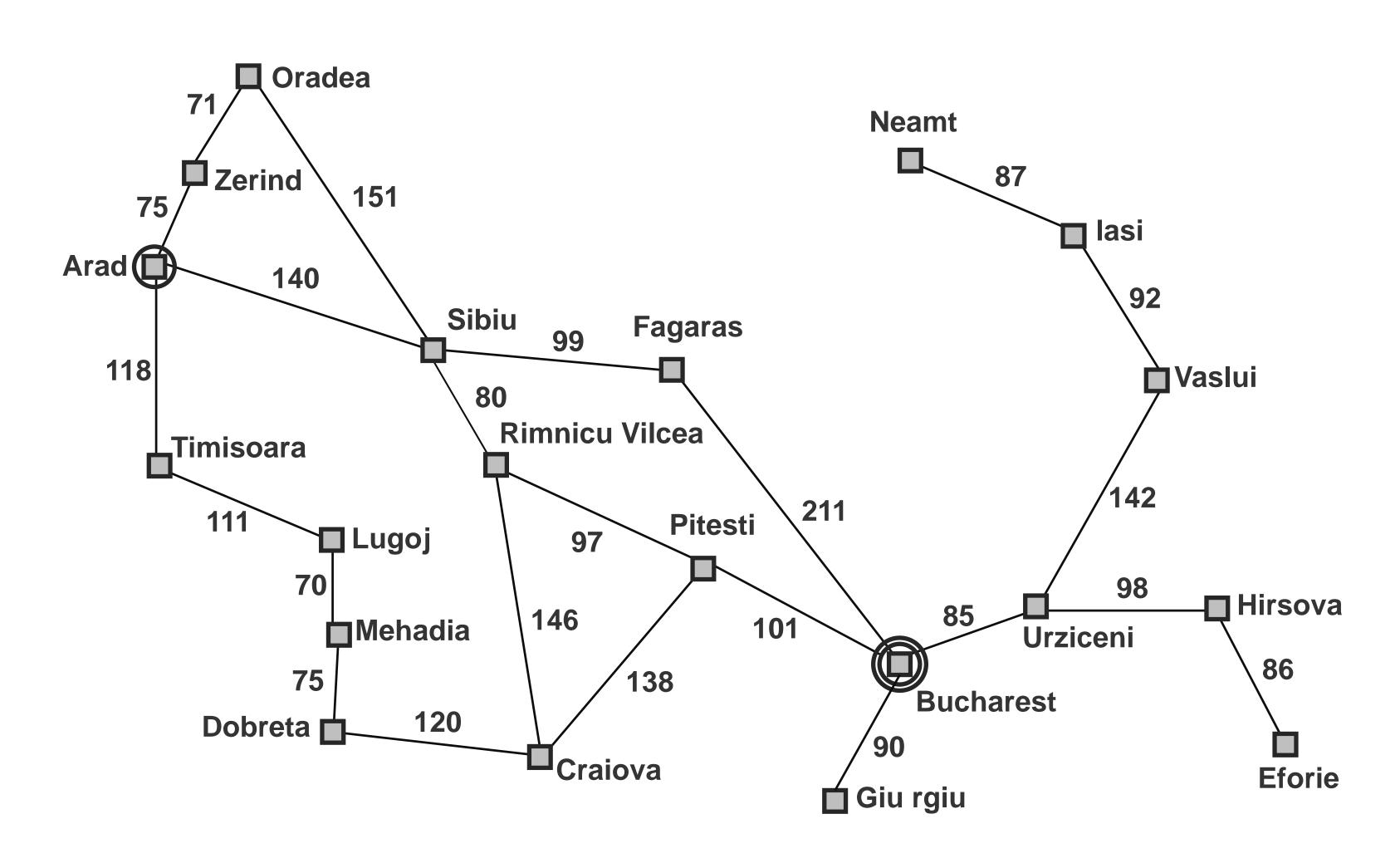
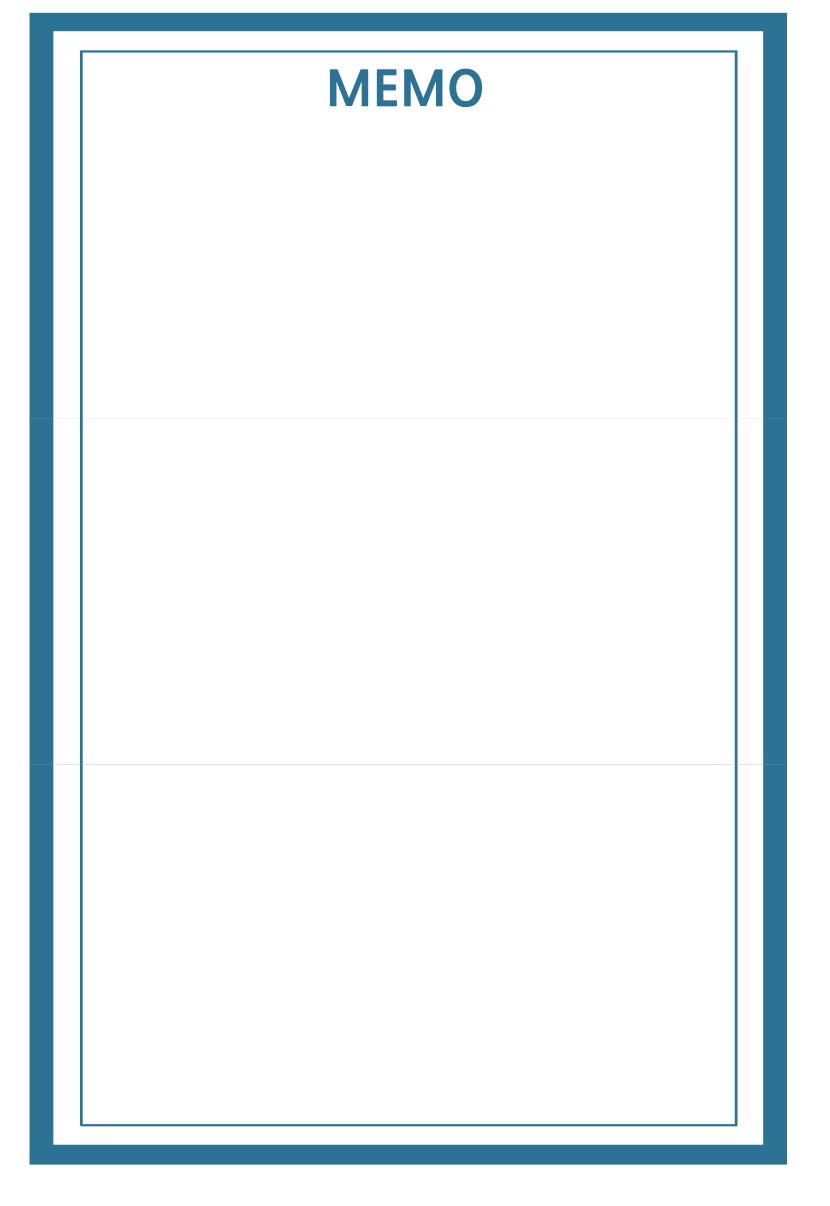




Example: Romania

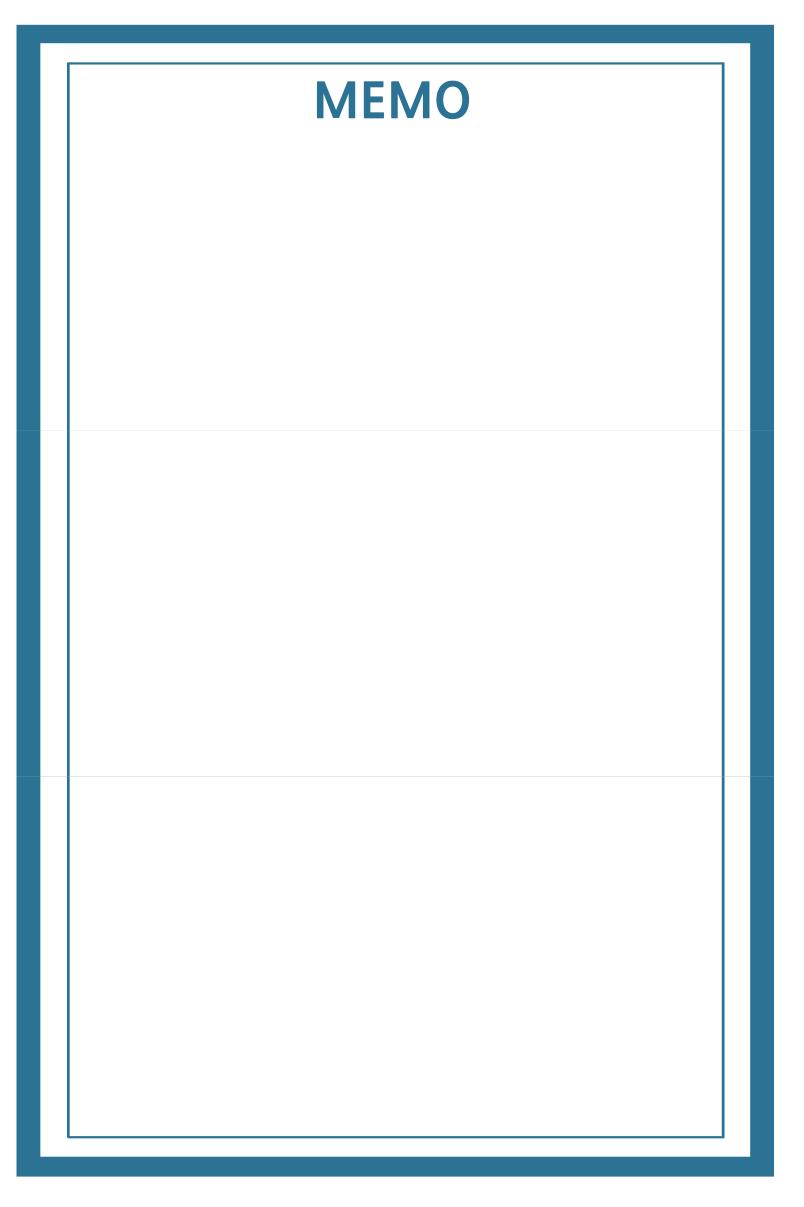






Example: Romania

- On holiday in Romania, the flight leaves tomorrow from Bucharest
- Formulate initial state and goal
 - ► Currently in Arad, and be in Bucharest
- Formulate problem:
 - ► States: various cities
 - ► Actions: drive between cities
- Find solution:
 - ► A sequence of cities, e.g., Arad, Sibiu, Fagaras, Bucharest



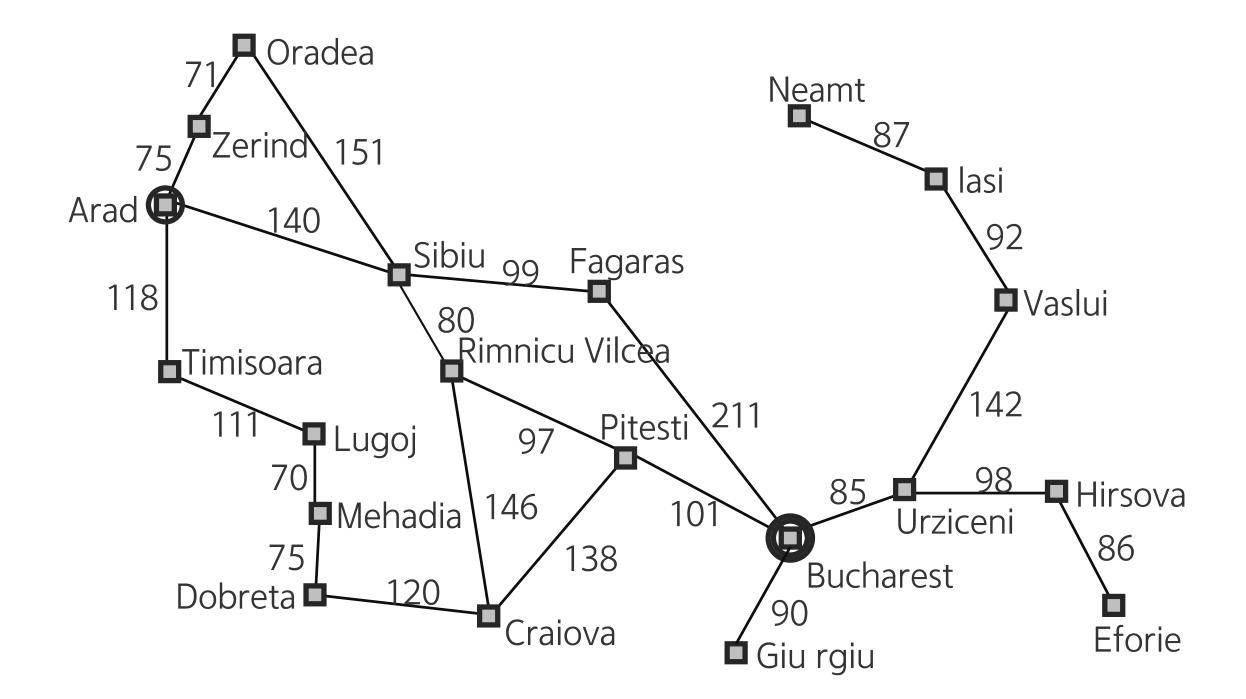


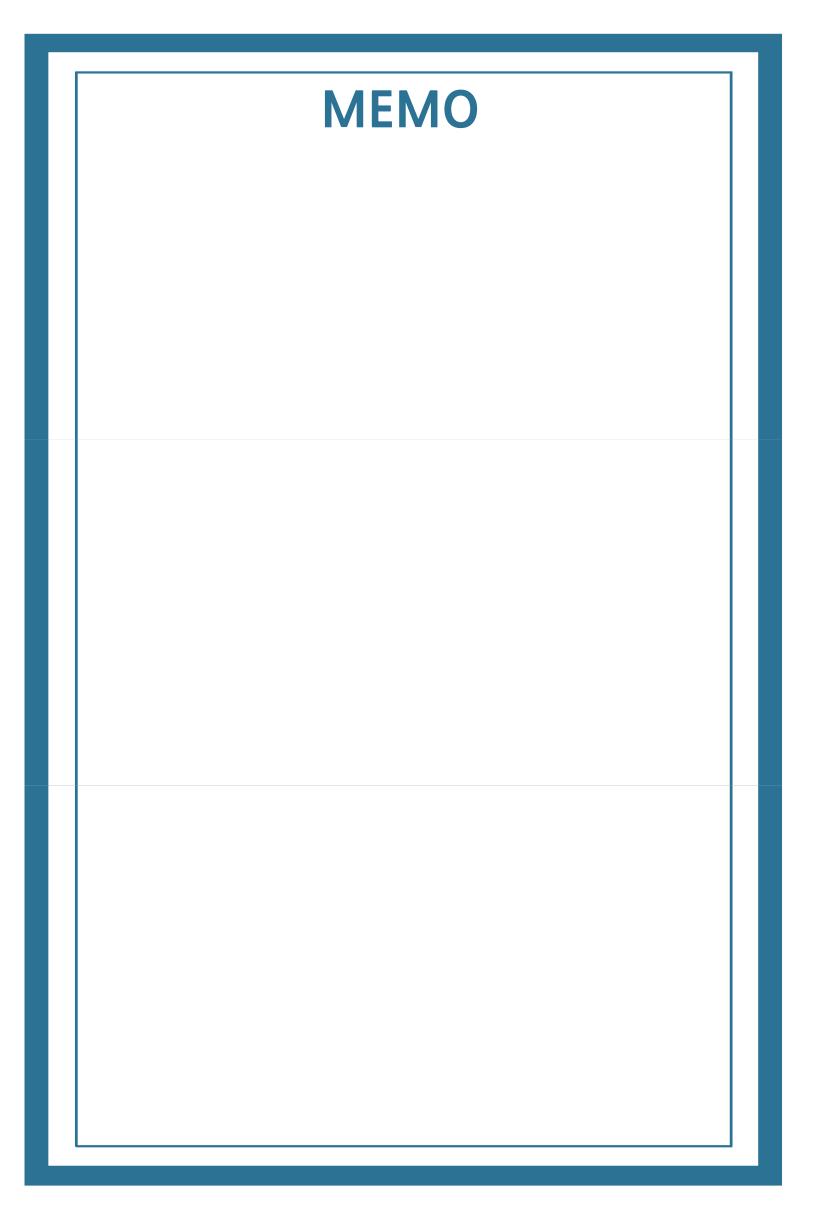
Search as Problem Solving

Need to search a space of possible solutions

► There are many sequences of actions, each with their own utility

We want to find, or search for, the best one







Problem

Formally defined by four components

- 1. Initial state
 - The state that the agent starts in
 - e.g. at Arad
- 2. Possible actions
 - Successor function successor_fn(x): given a state x, return a set of (action, successor) ordered pairs
 - e.g. $S(Arad) = \{\langle Arad \rightarrow Zerind, Zerind \rangle, \dots \}$



Problem

Formally defined by four components

- 3. Goal test
 - Determines whether a given state is a goal state
 - Explicit, e.g., x = "at Bucharest"
 - Implicit, e.g., Checkmate(x)
- 4. Path cost
 - Assigns a numeric cost to each path
 - Step cost $c(x, a, y) \ge 0$: a cost of taking action a to go from x to y
 - e.g., sum of distances, number of actions executed, etc.

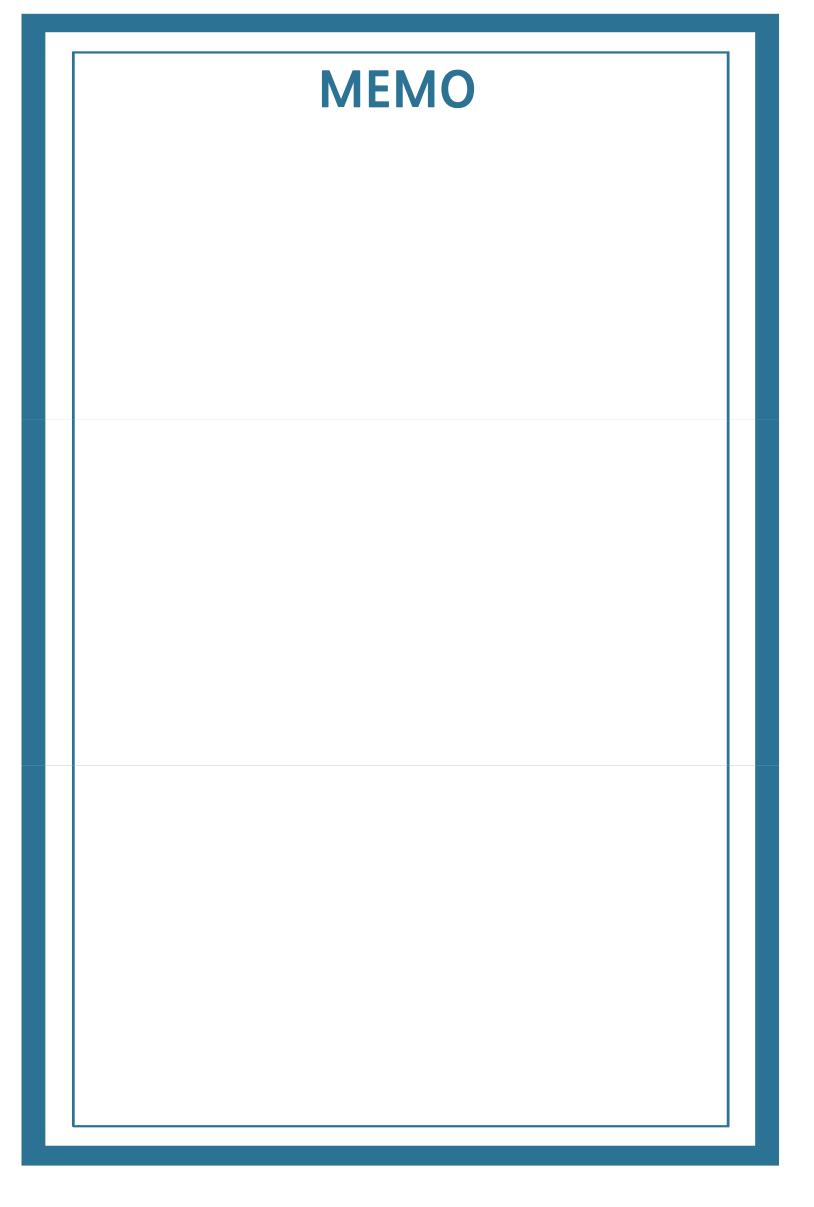
Solution: a sequence of actions leading from the initial state to a goal state

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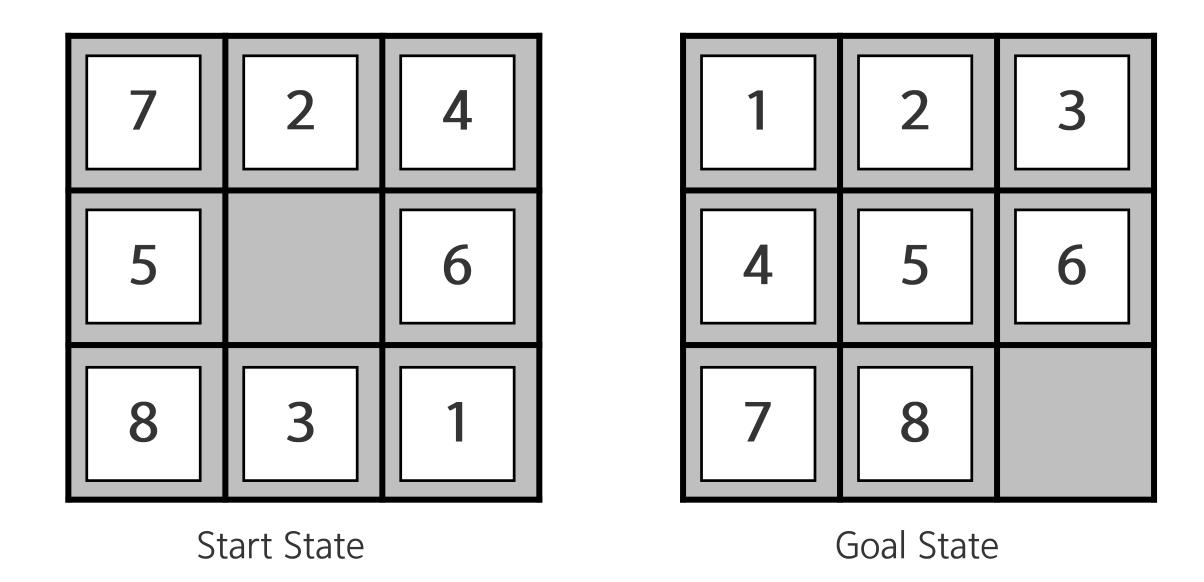


Selecting a State Space

- - ► (Abstract) state = a set of real states
 - ► (Abstract) action = a complex combination of real actions
 - ▶ e.g., "Arad → Zerind" represents a complex set of possible routes, detours, rest stops, etc.
 - ► (Abstract) solution = a set of real paths that are solutions in the real world
- Each abstract action should be <u>easier</u> than the original problem







[Note: an optimal solution of n-Puzzle family is NP-hard]

- States? Locations of tiles
- Actions? Move blank left, right, up, down
- Goal test? Goal state (given)
- Path cost? 1 per move



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Tree Search Algorithms

Basic idea

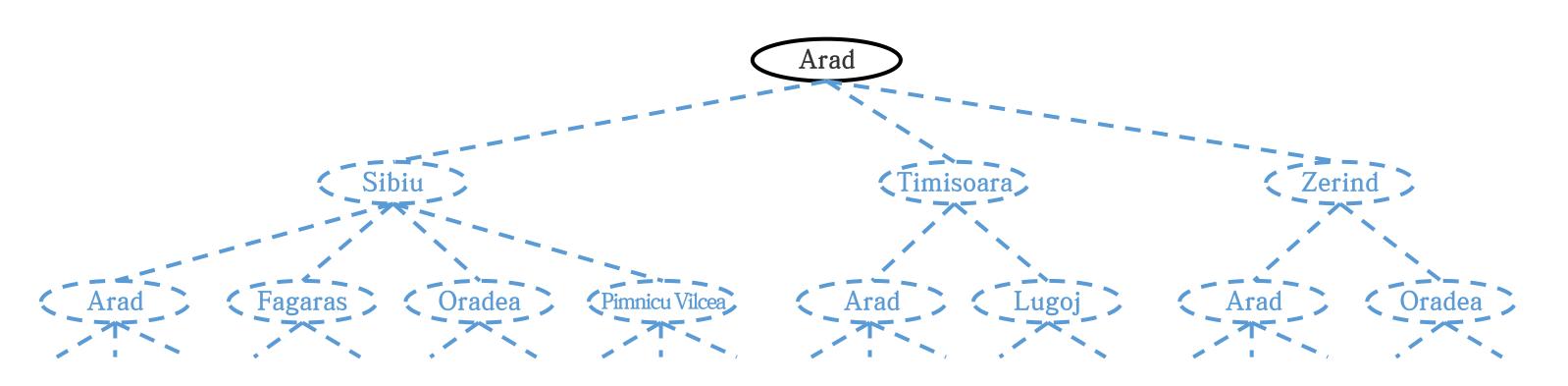
- ► Exploration of state space by generating successors of already-explored states (a.k.a. ~ expanding states)
- ► Every state is evaluated: is it a goal state?

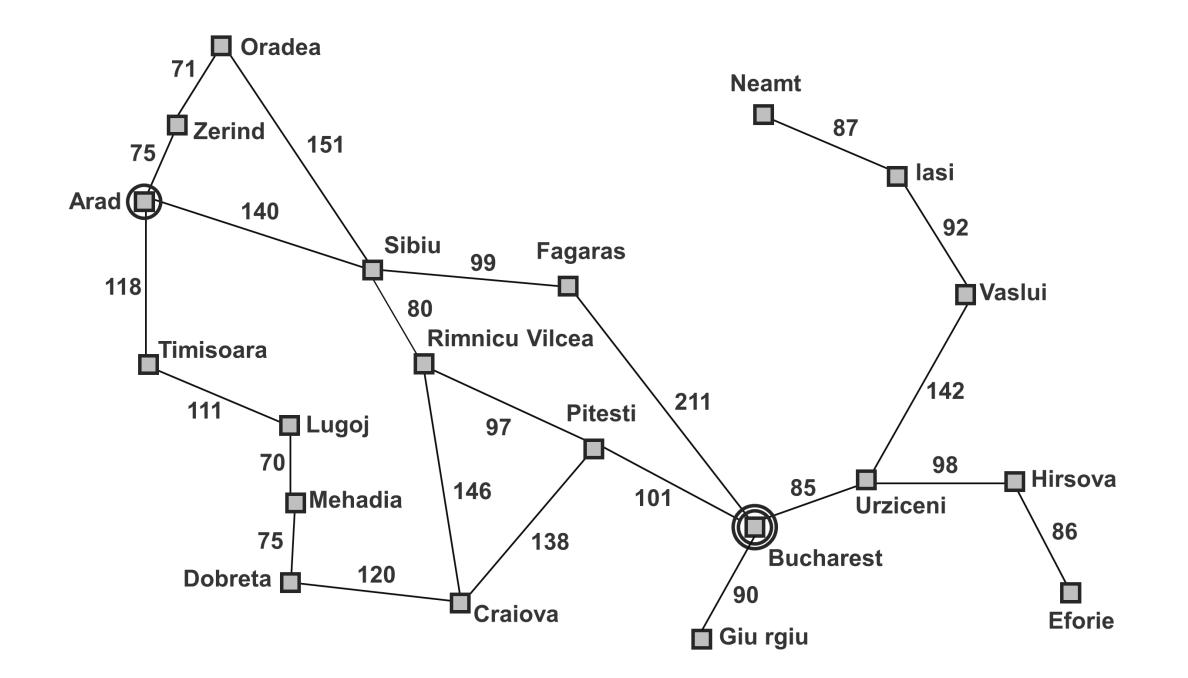


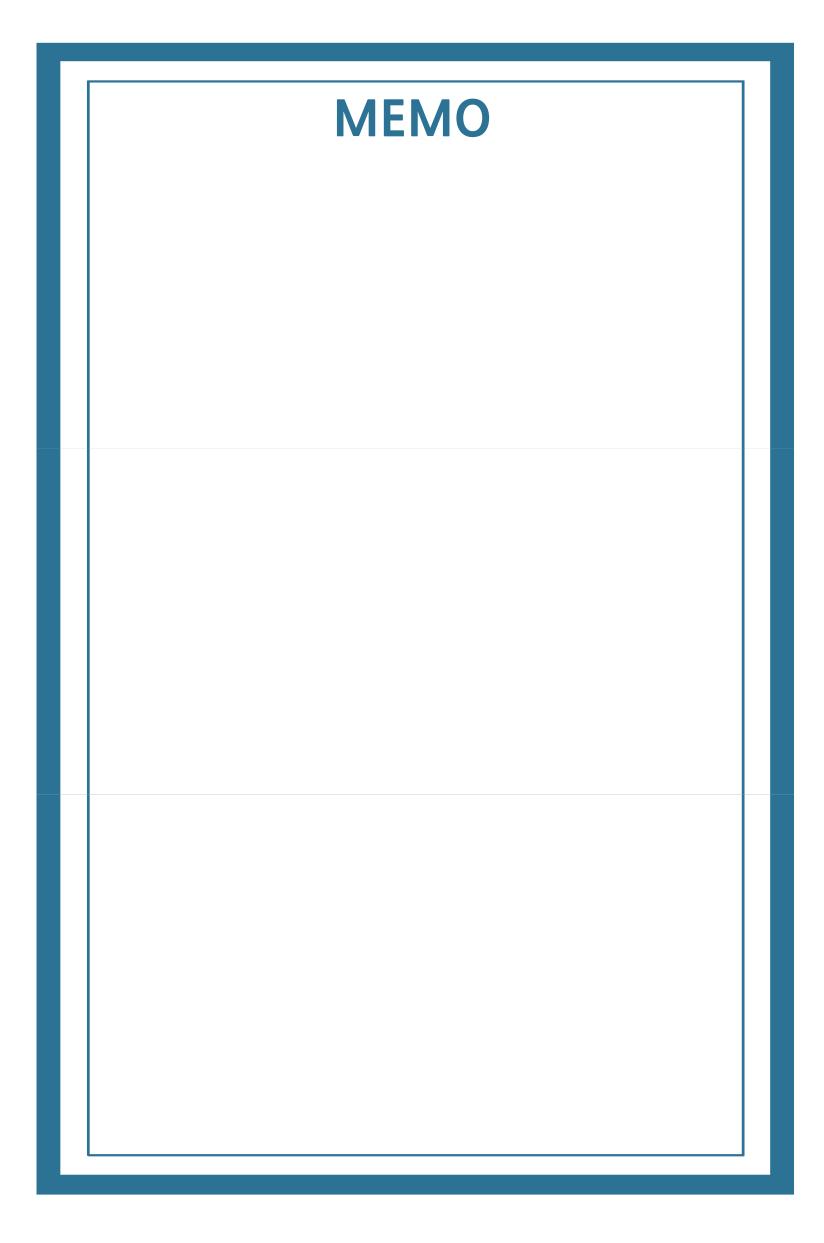
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Tree Search Example

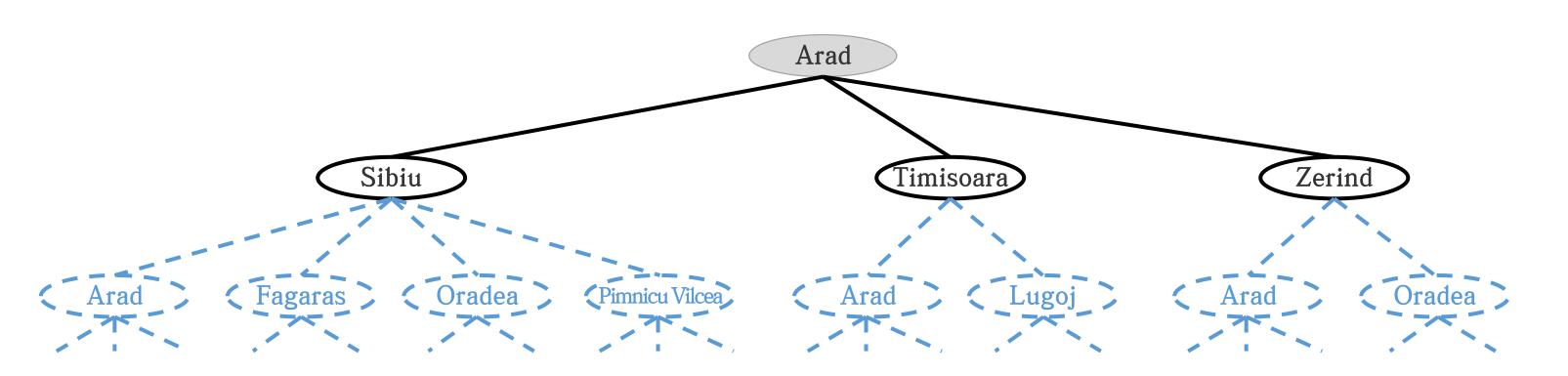


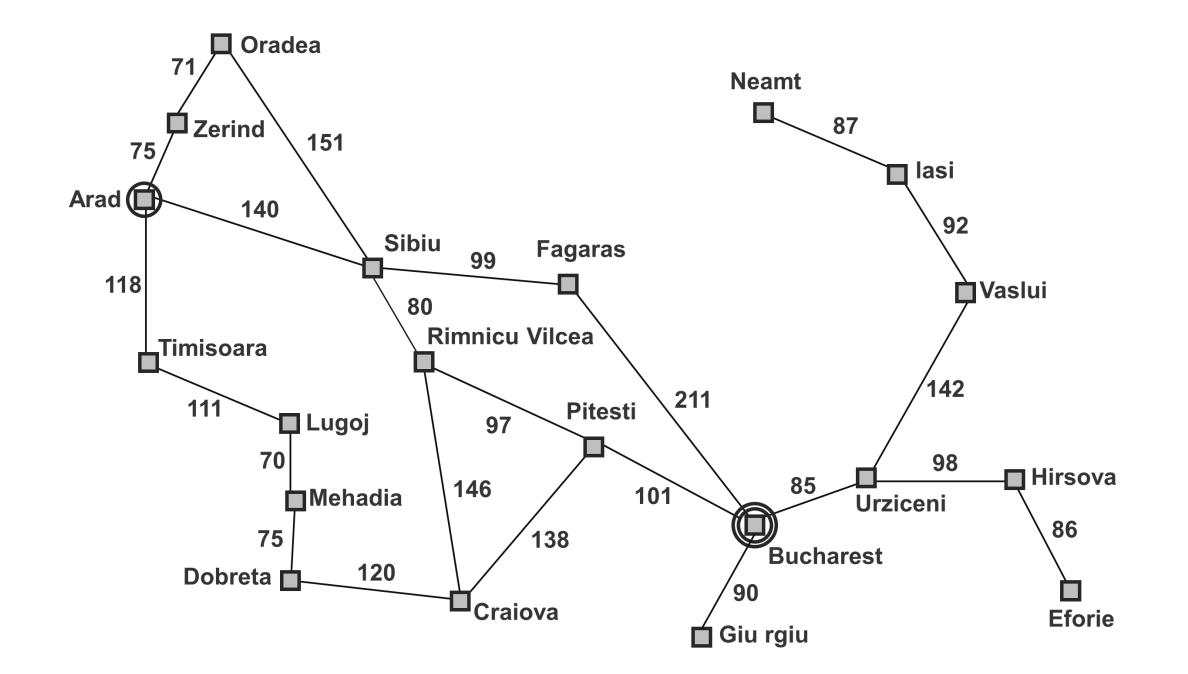


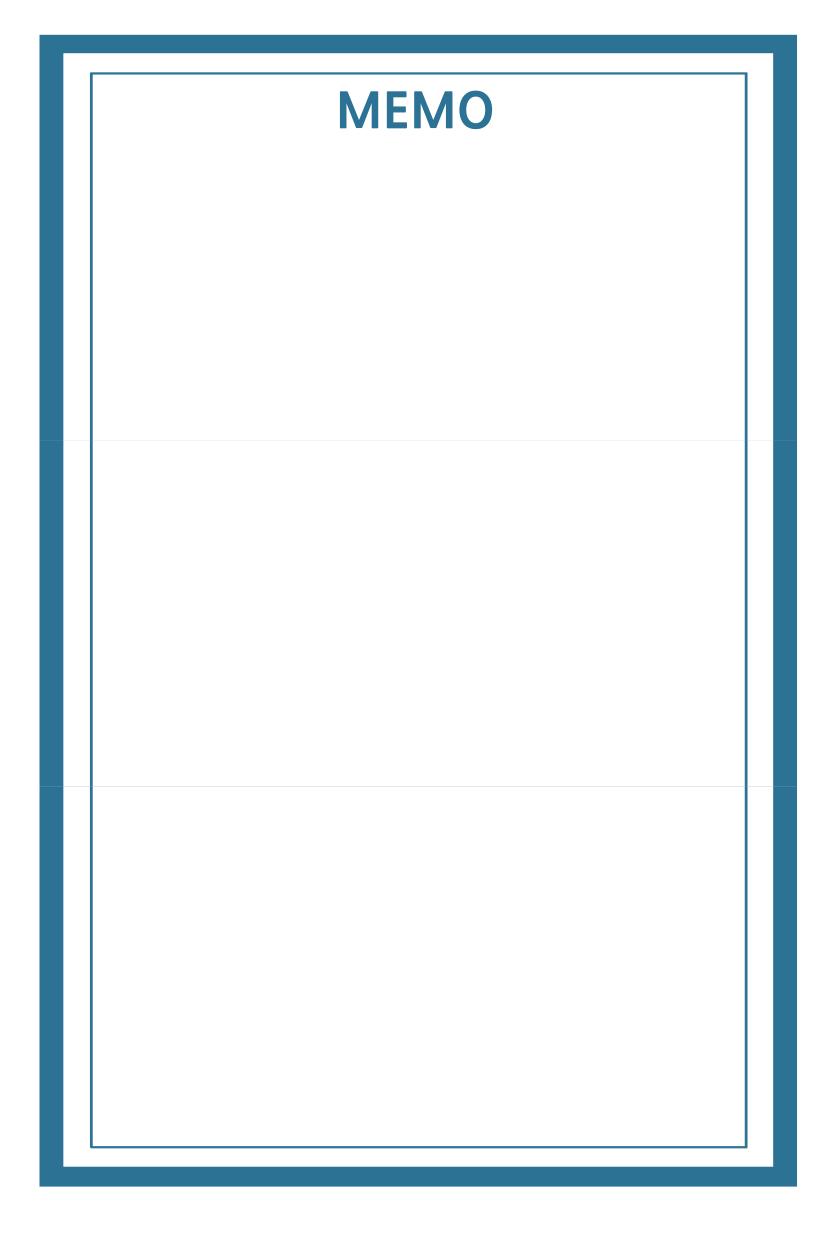




Tree Search Example

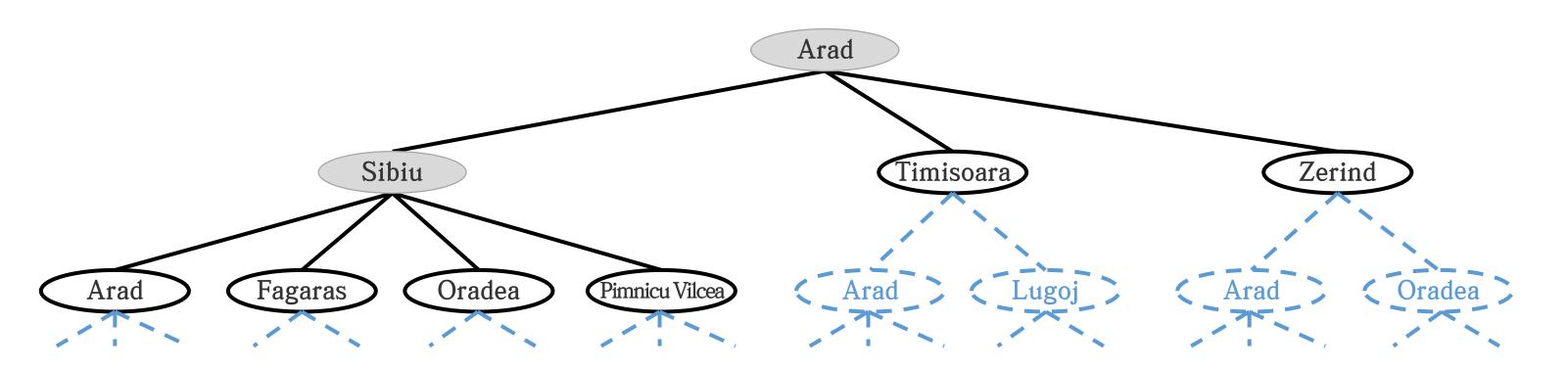




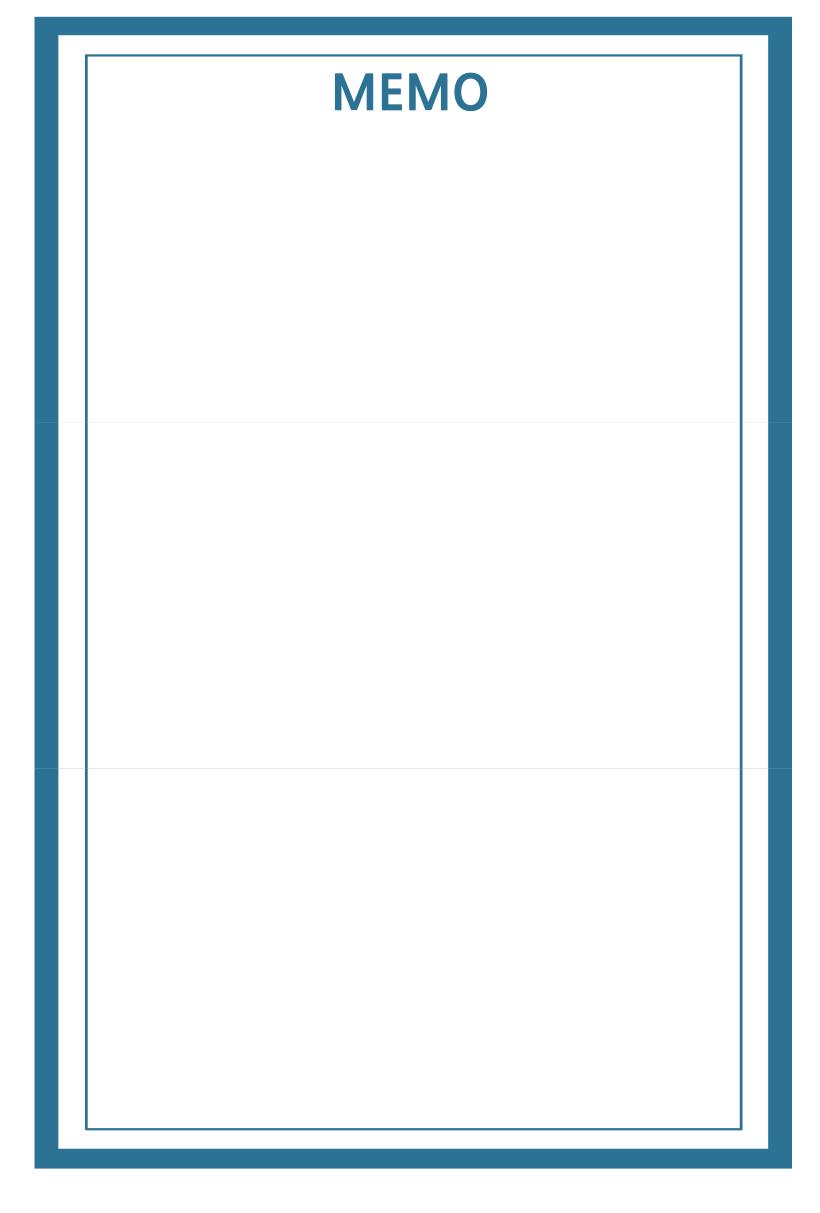




Tree Search Example



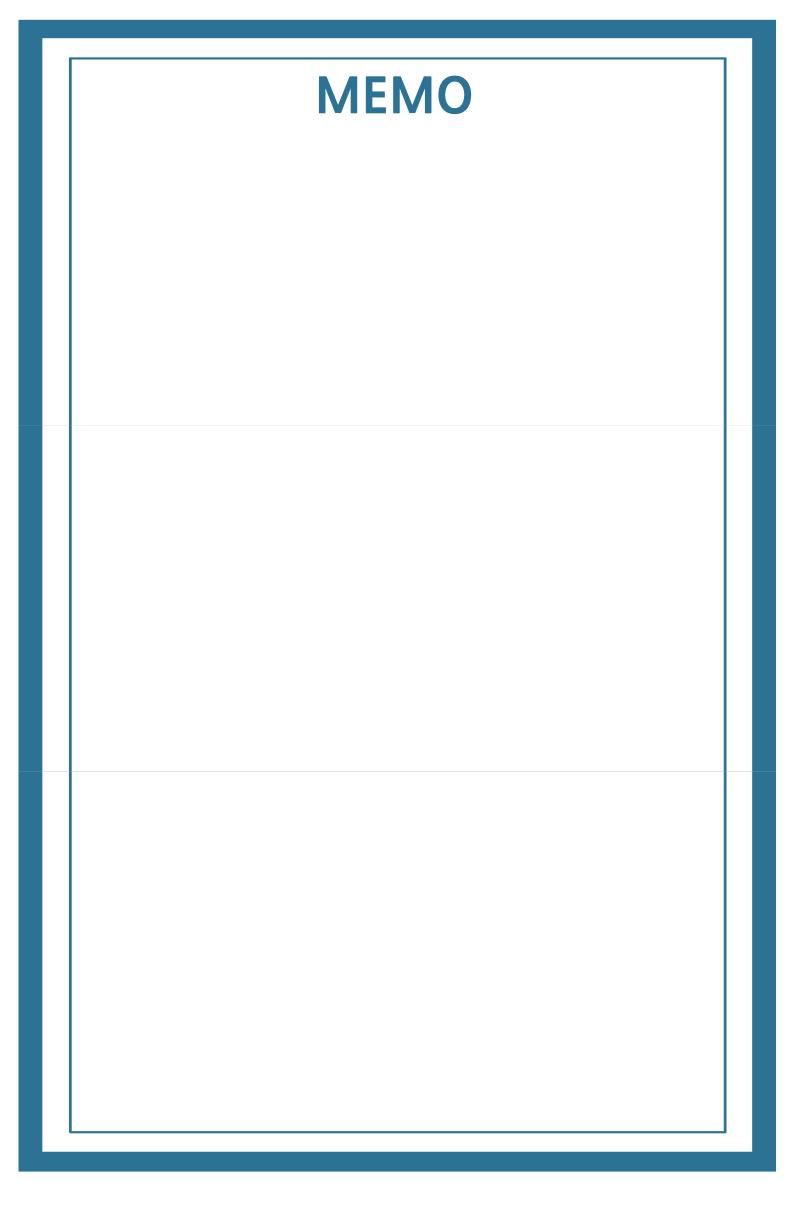
- State space forms a tree structure
 - ► Root = start state
 - ► Each node represents a state
 - ► Actions are branches, children are all possible next-states
- Search involves expanding a <u>frontier</u> of potential next states





Search Strategies

- A search strategy is defined by picking the order of node expansion
- Strategies are evaluated along the following dimensions
 - ► Completeness: does it always find a solution if one exists?
 - ► Time complexity: number of nodes generated
 - ► Space complexity: maximum number of nodes in memory
 - ► Optimality: does it always find a least-cost solution?





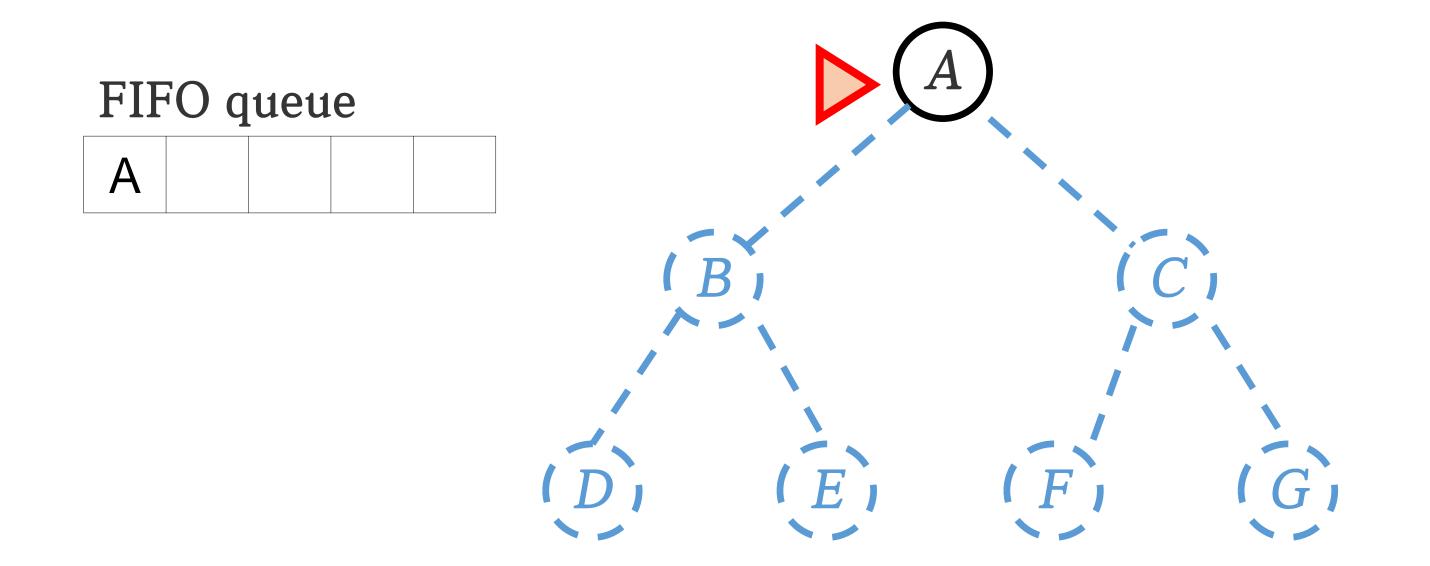
- Uninformed search strategies use only the information available in the problem definition
 - ► Breadth-first search
 - ▶ Uniform-cost search
 - ▶ Depth-first search
 - ▶ Depth-limited search
 - ► Iterative deepening search



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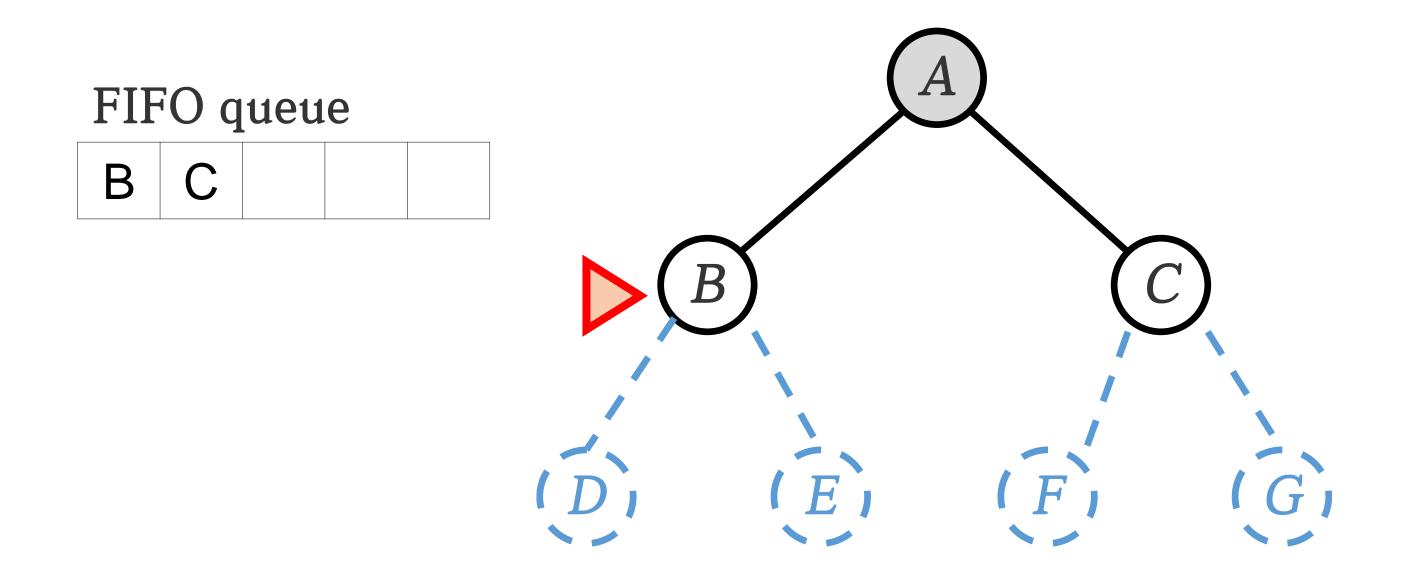
- Expand shallowest unexpanded node
- Implementation:
 - ► Fringe = FIFO queue, i.e., new successors go at end search



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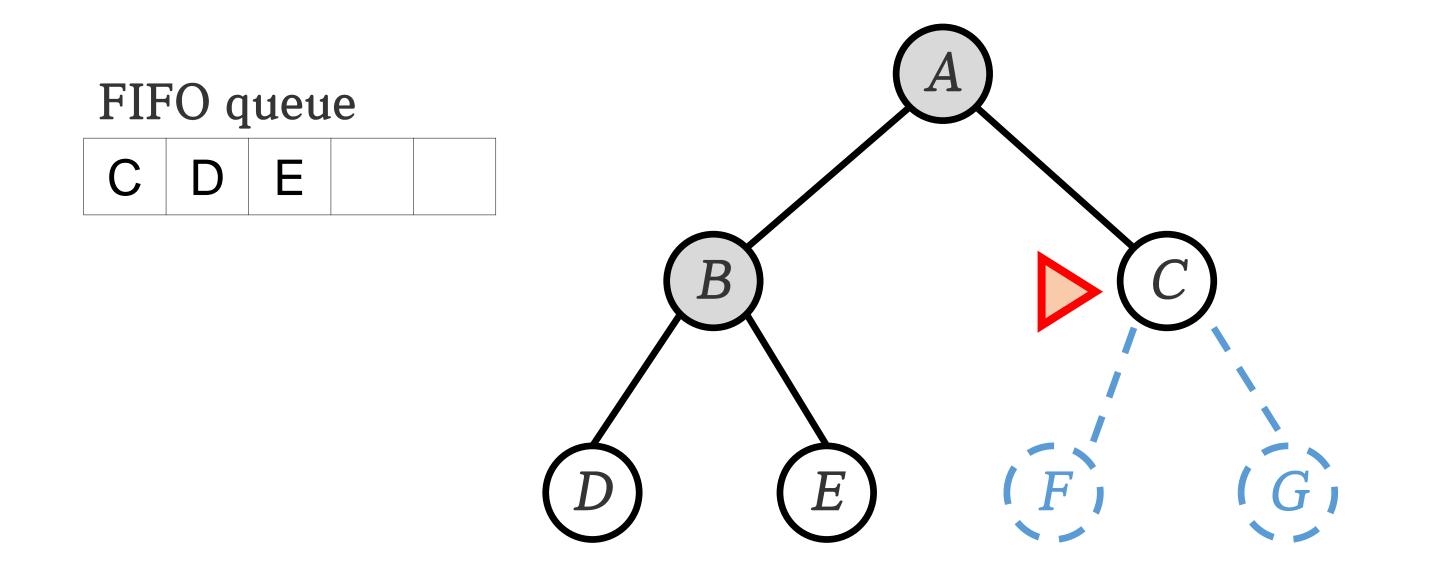
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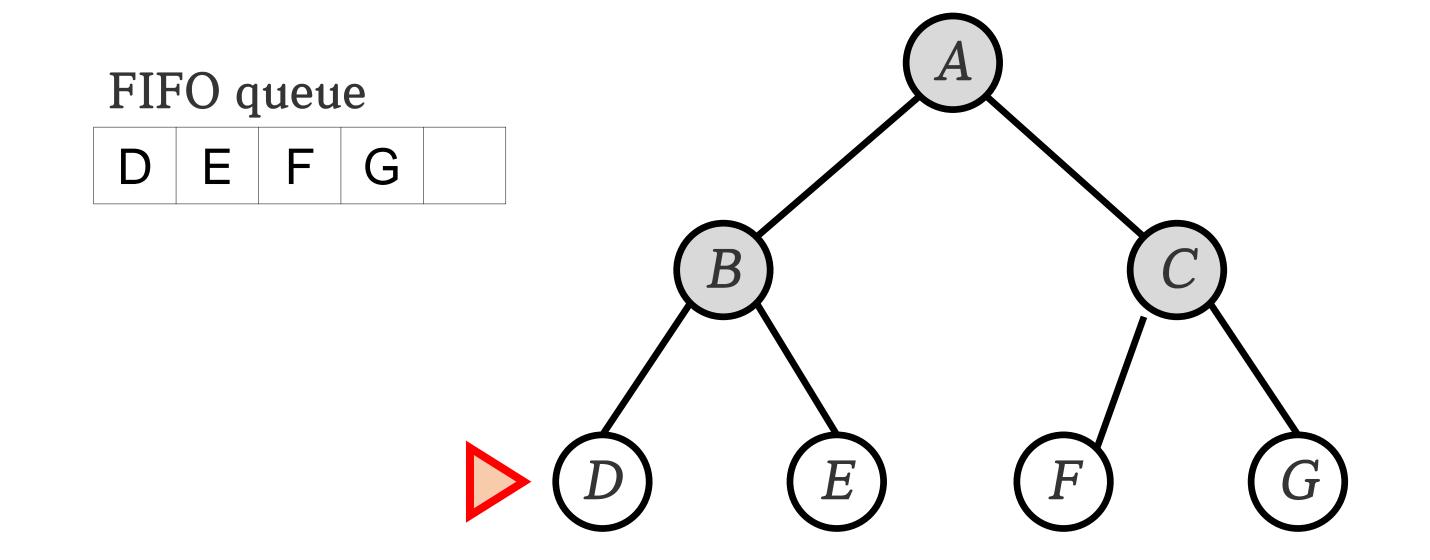
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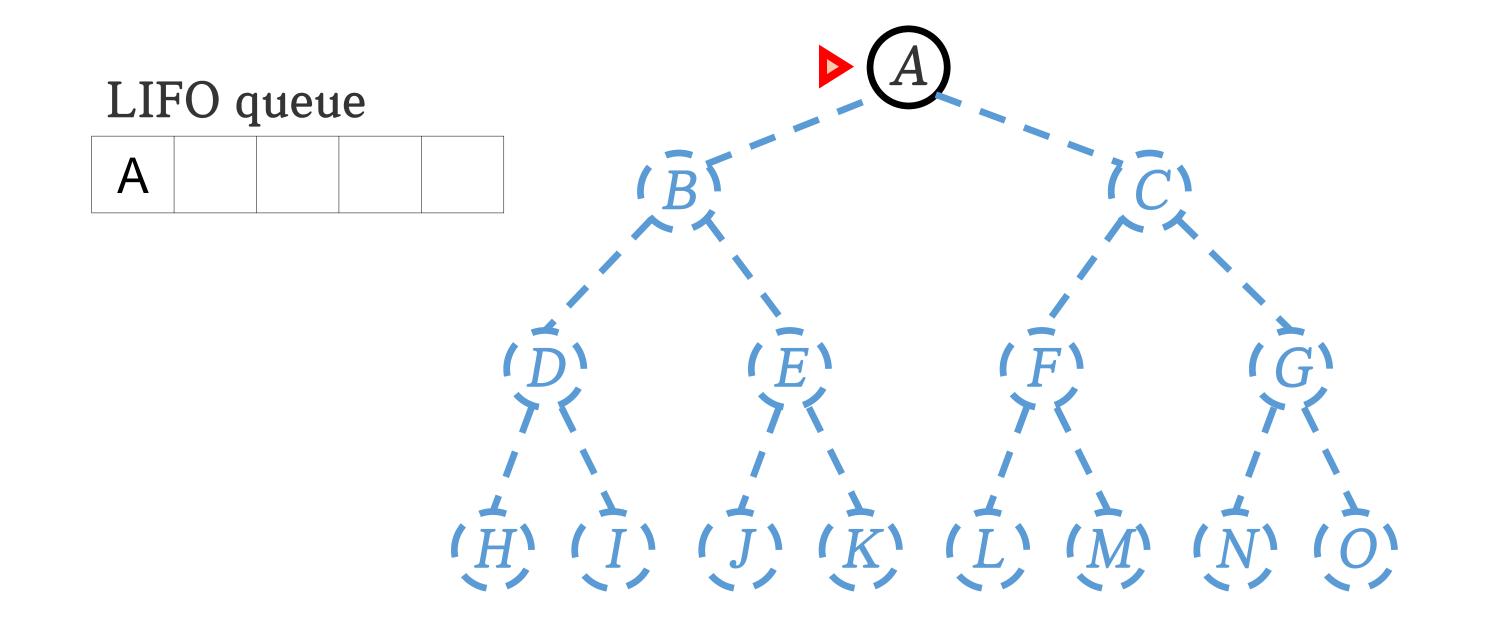


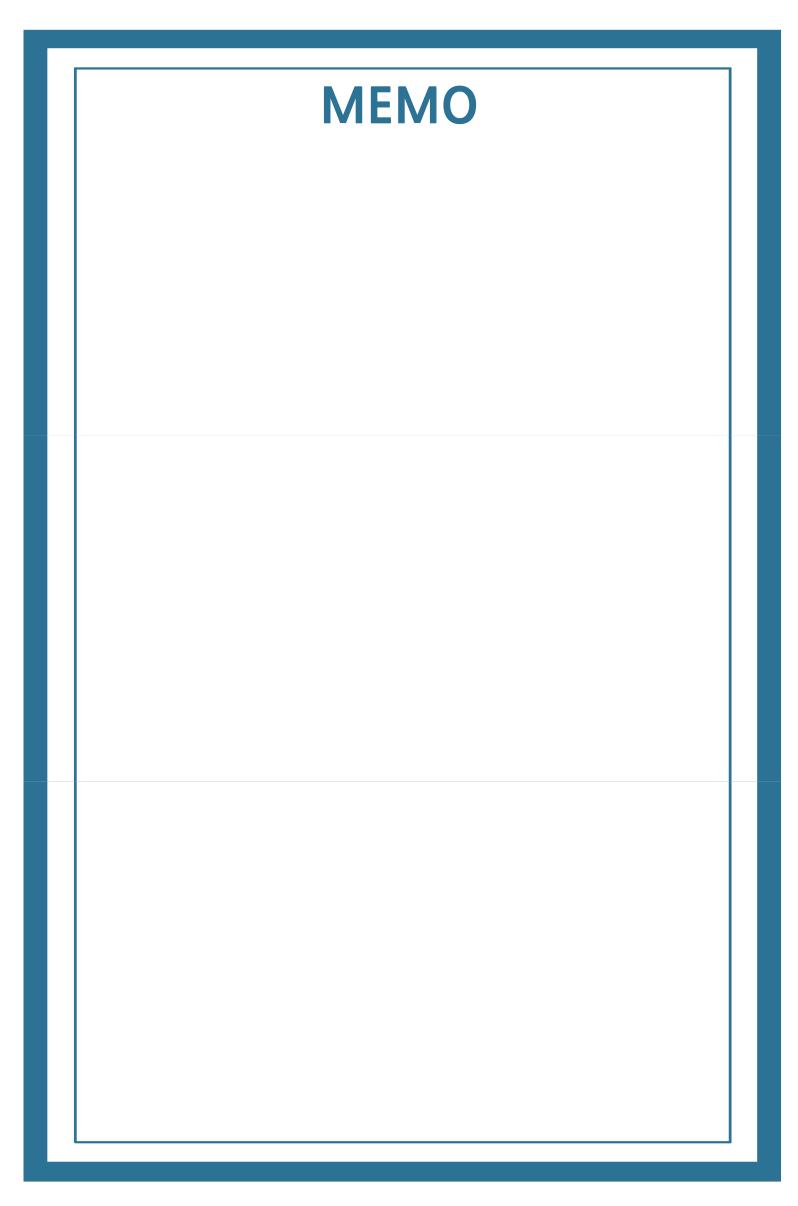
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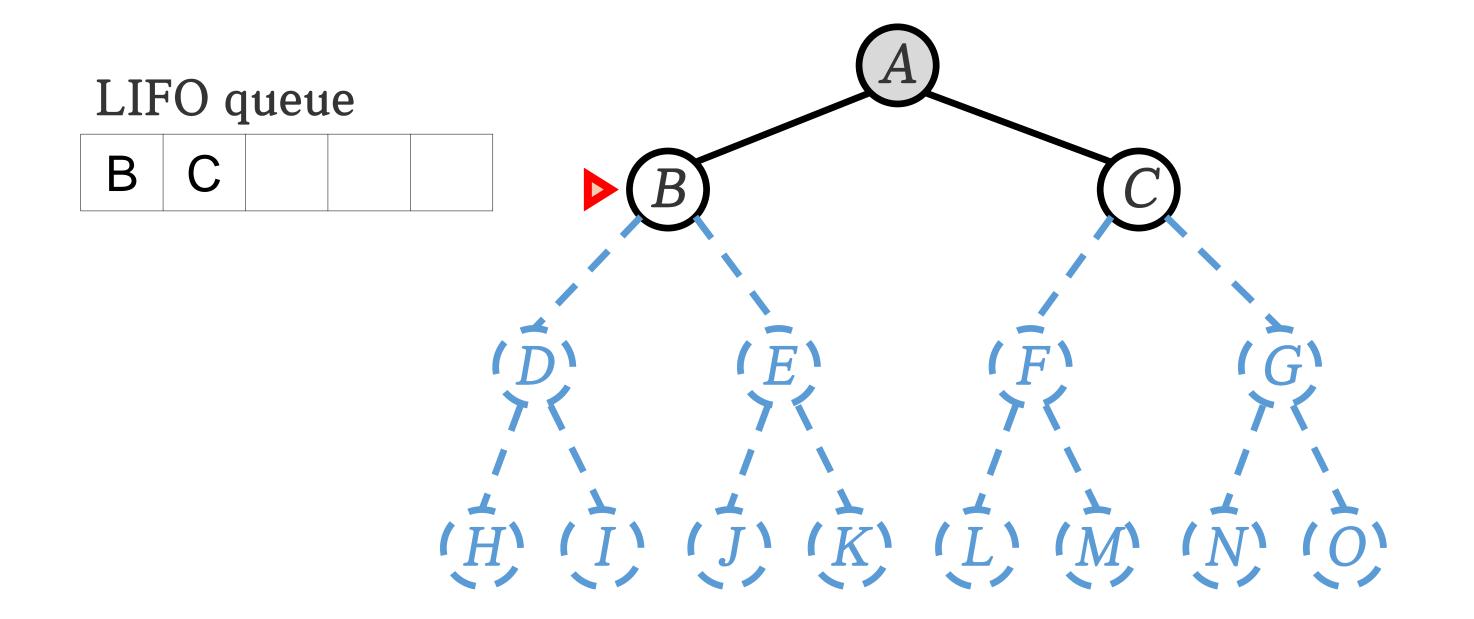
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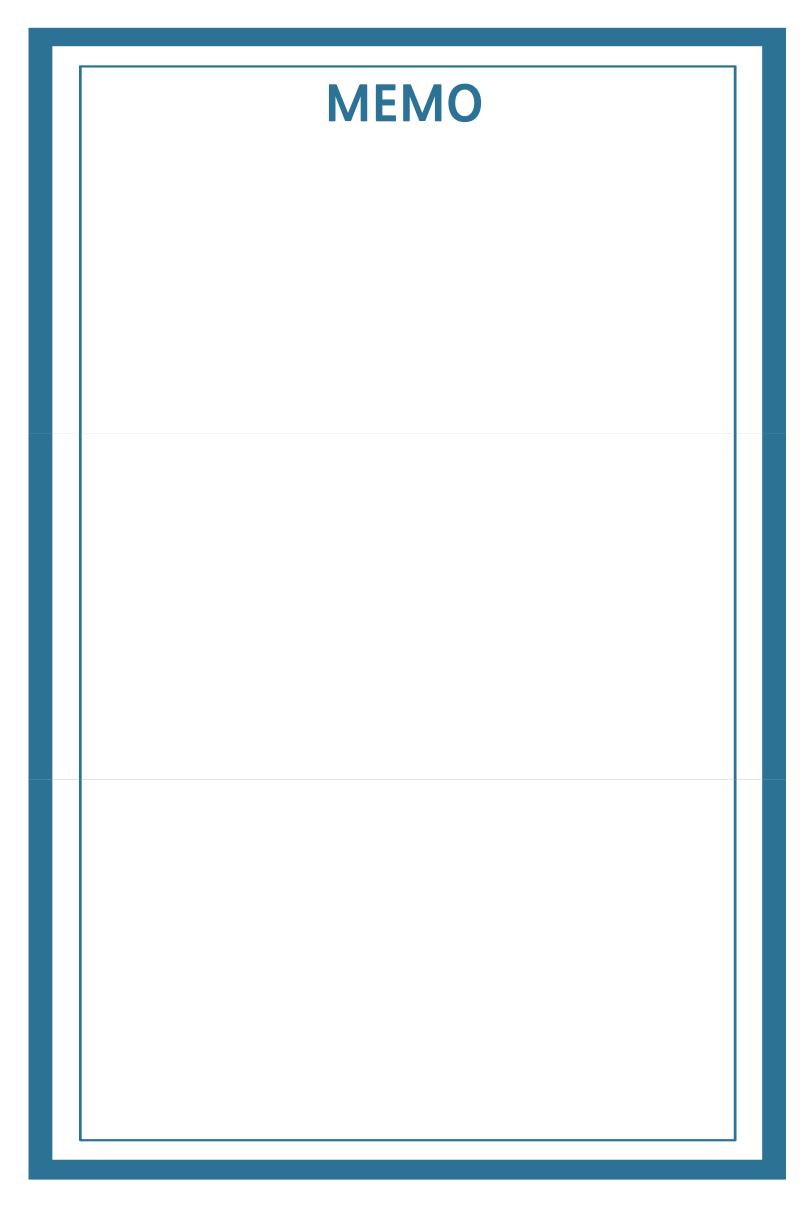






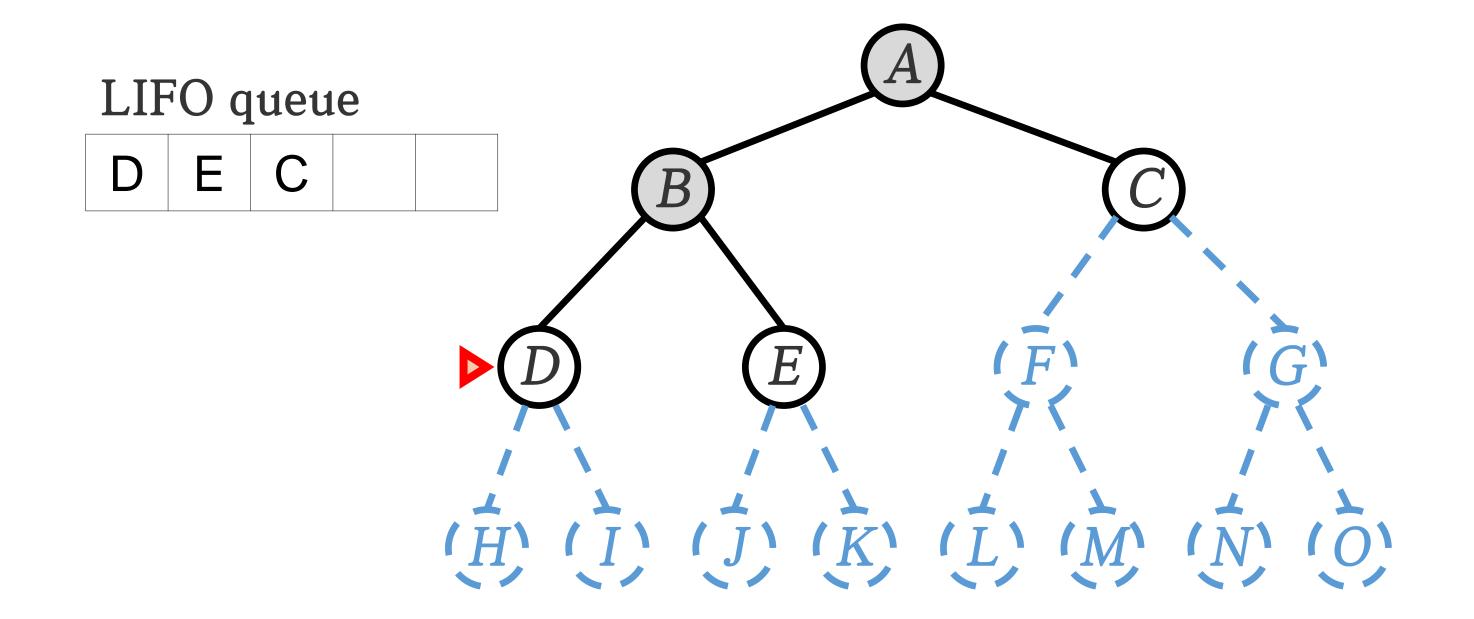
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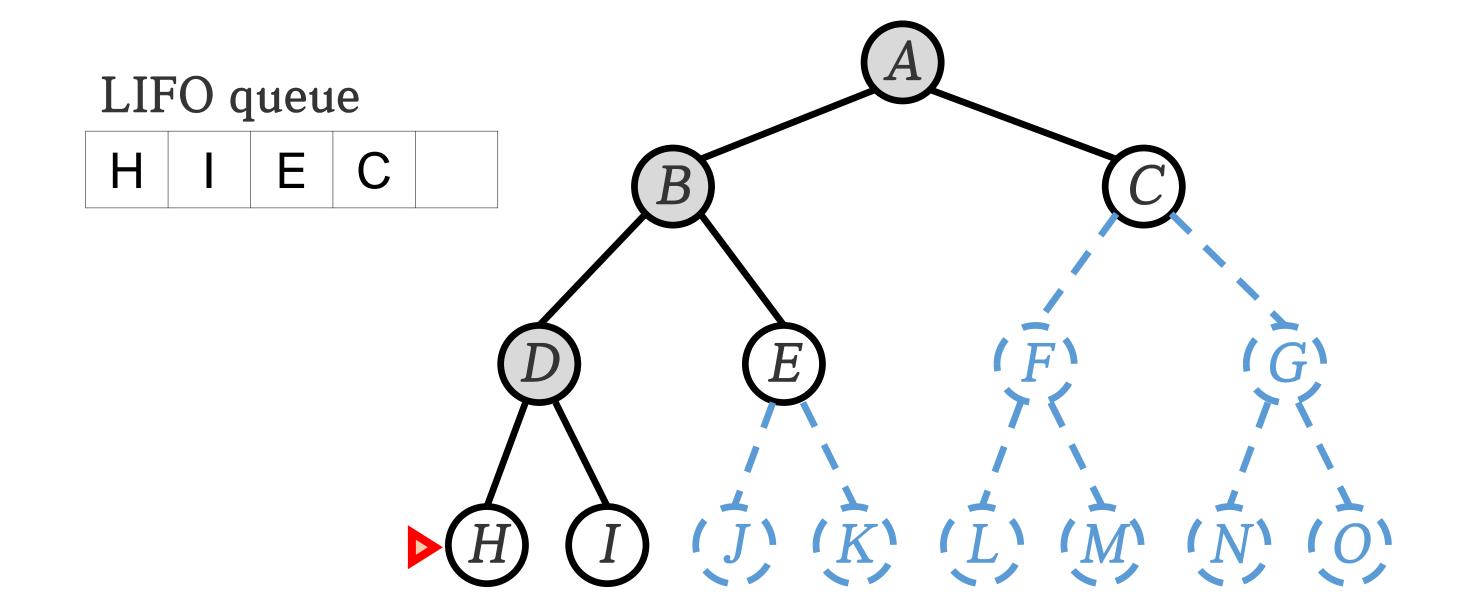


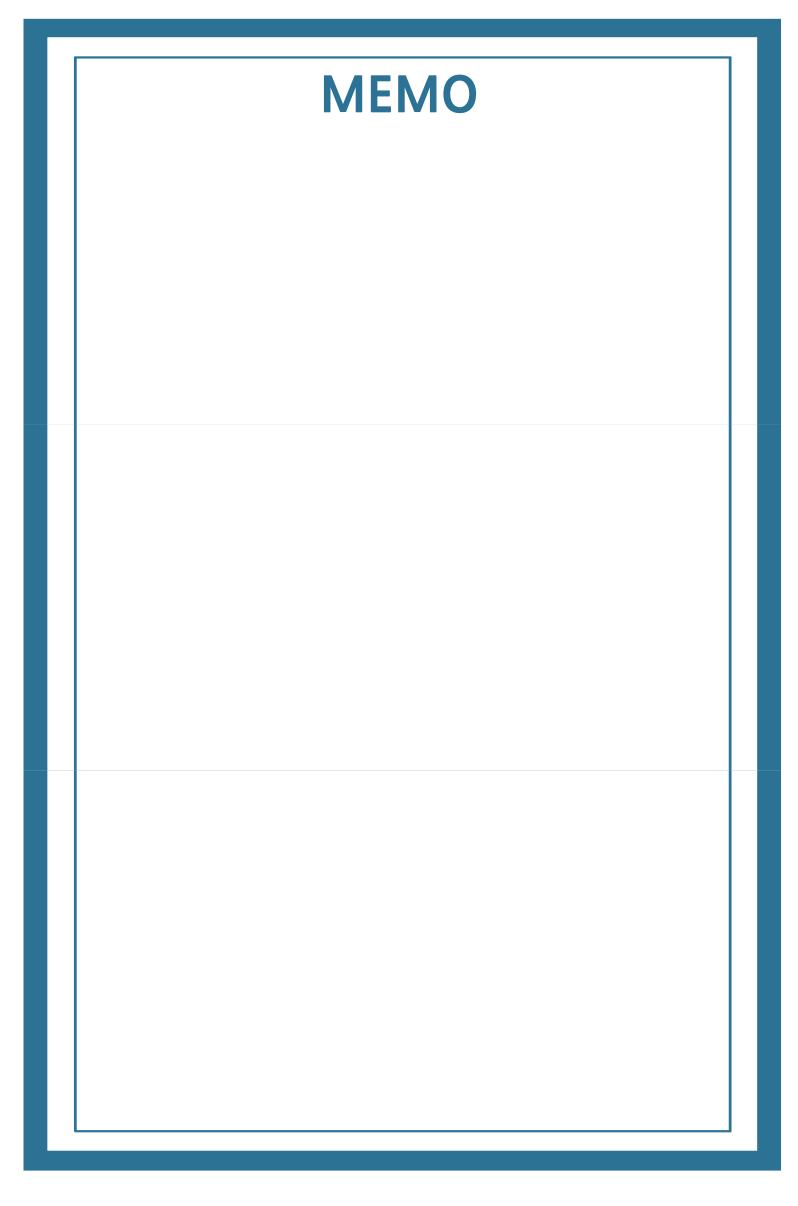
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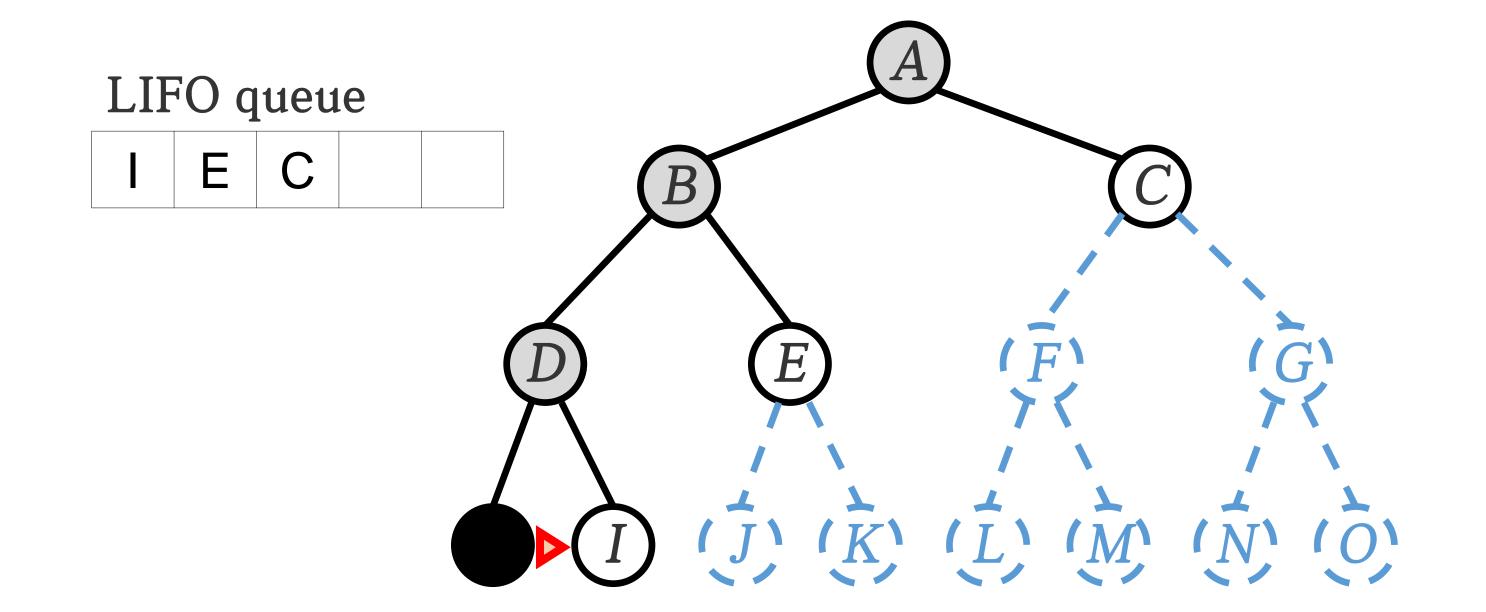
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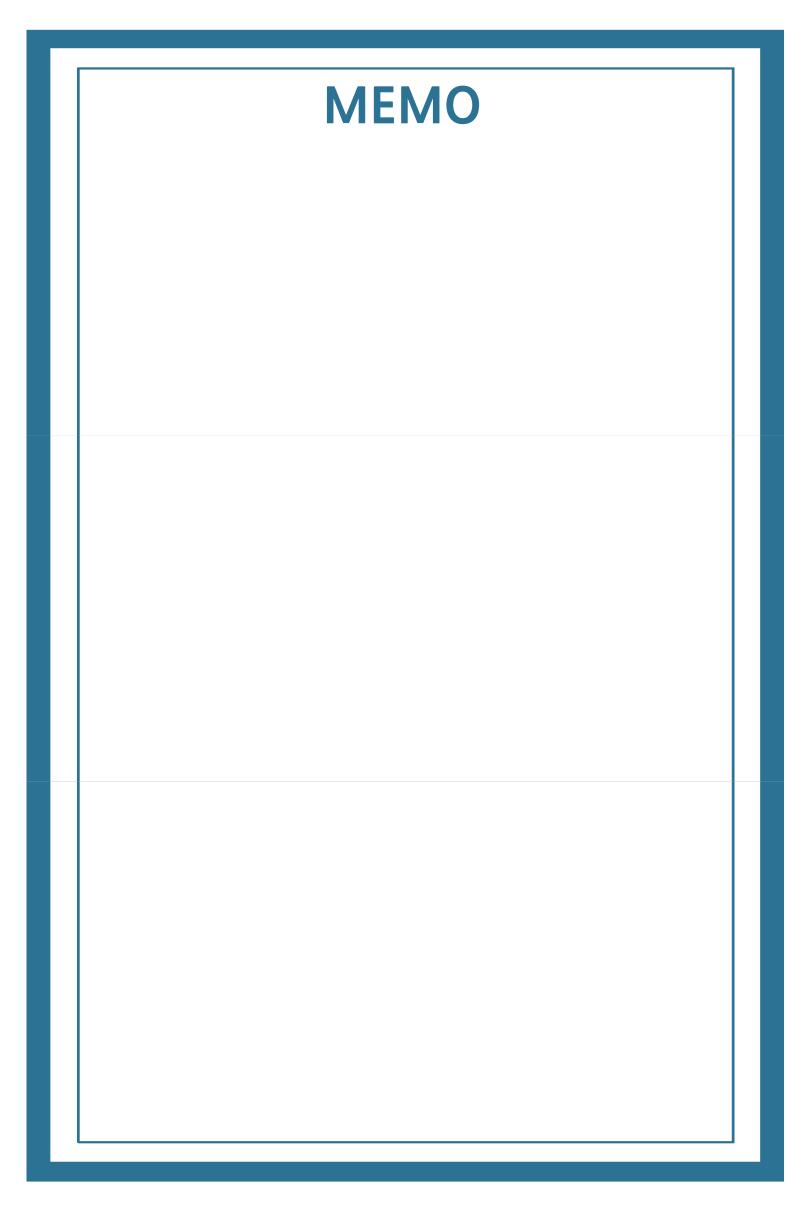






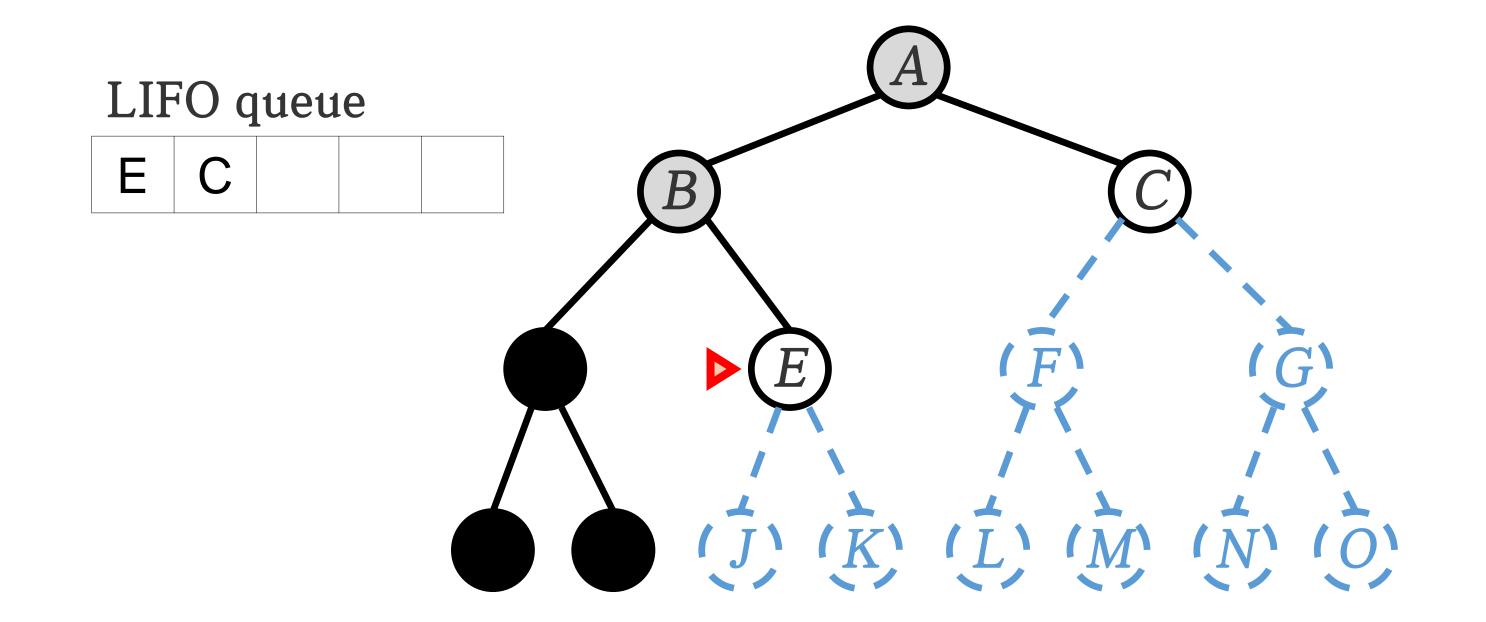
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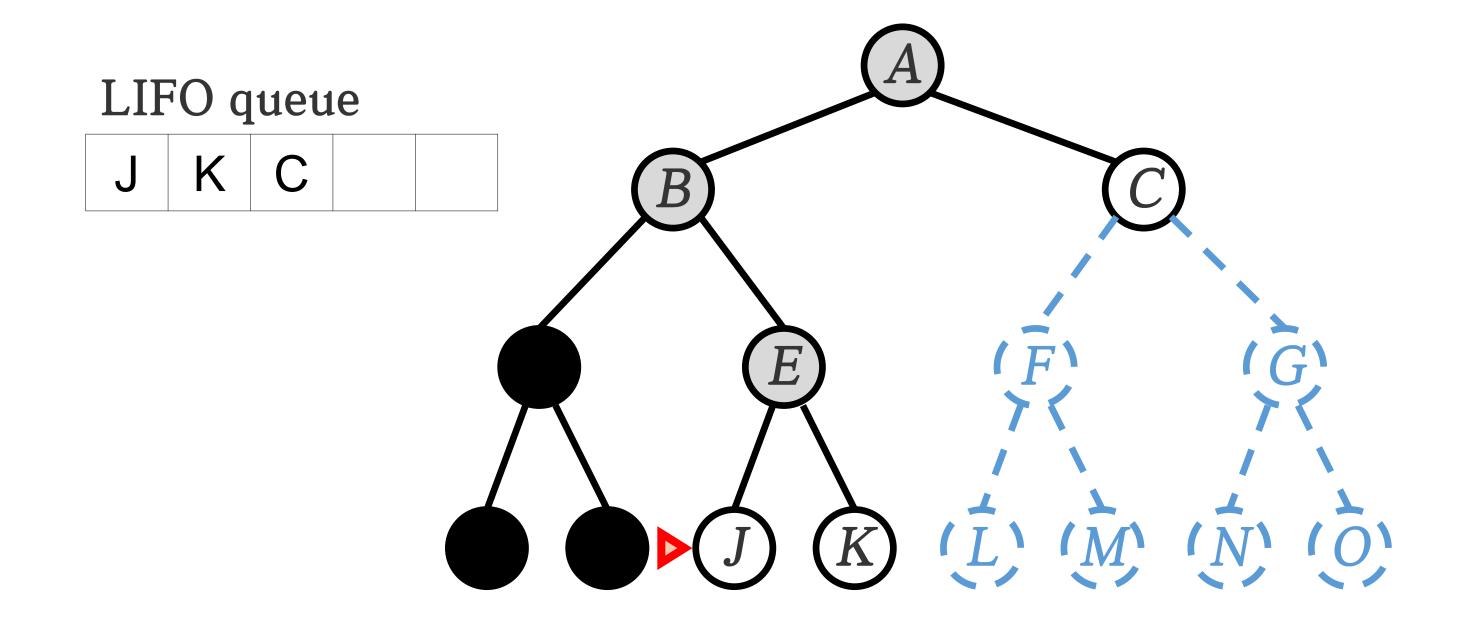


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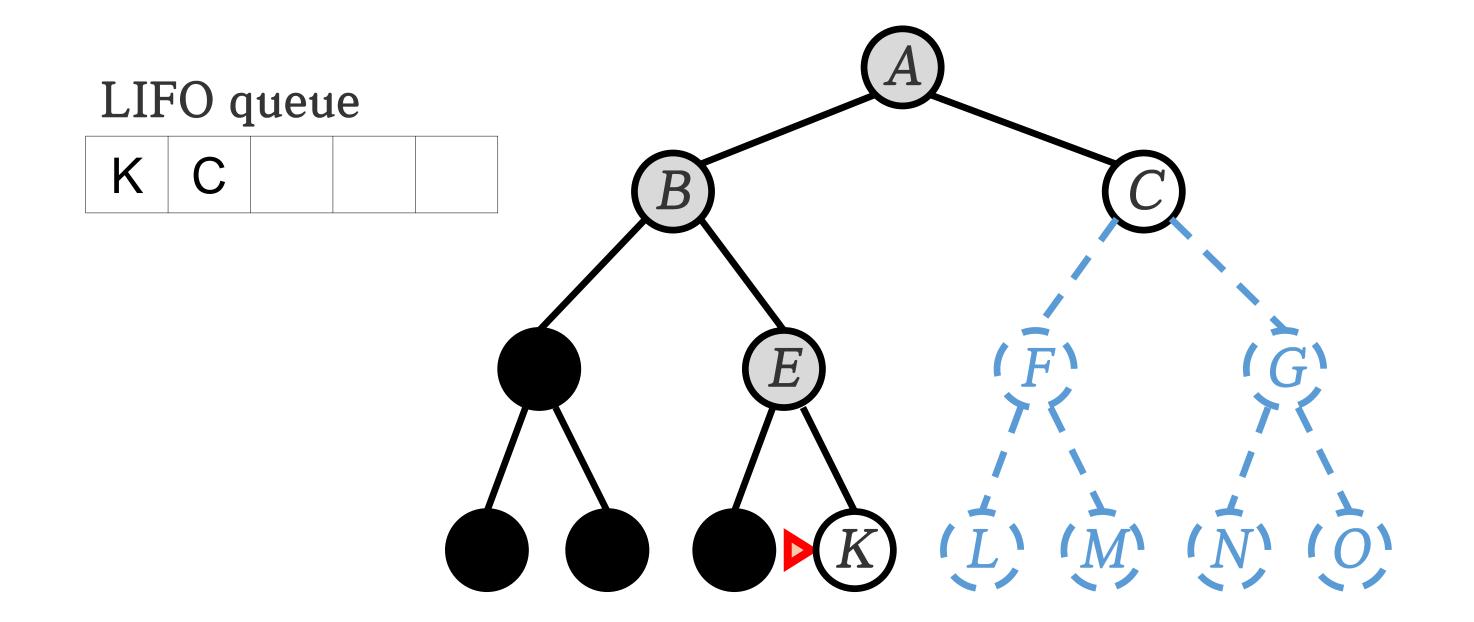


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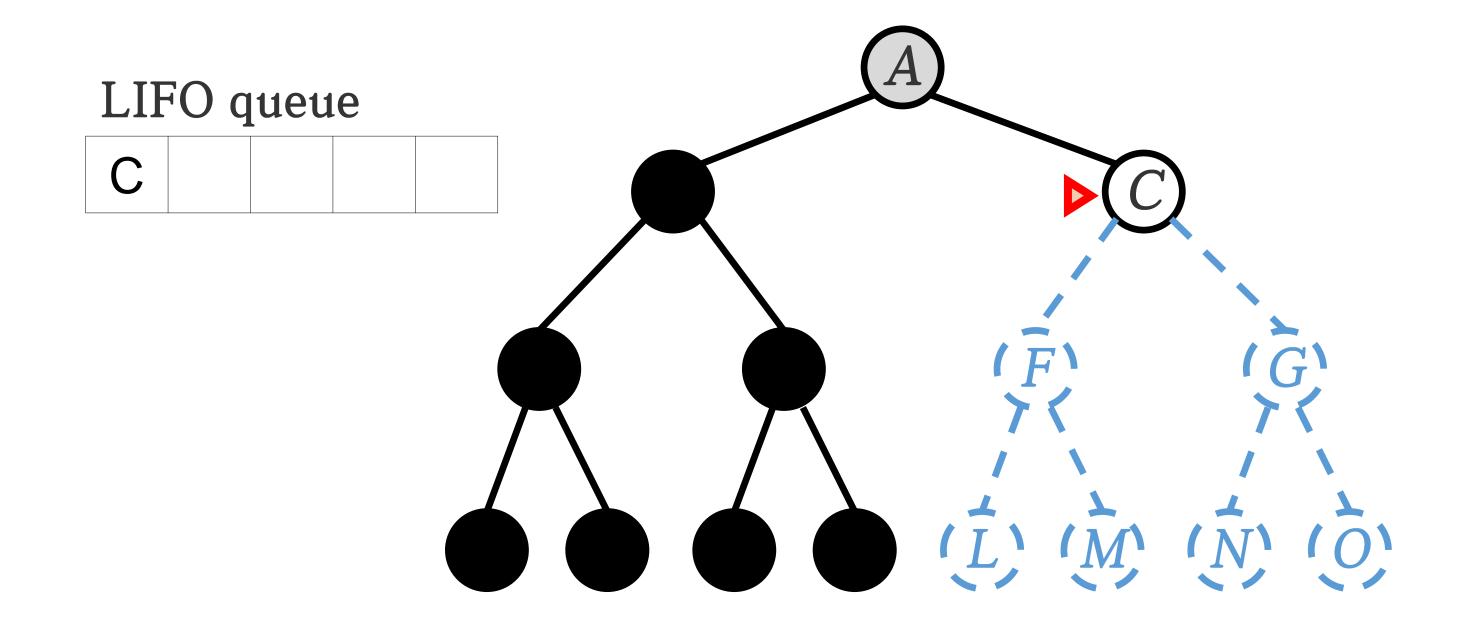


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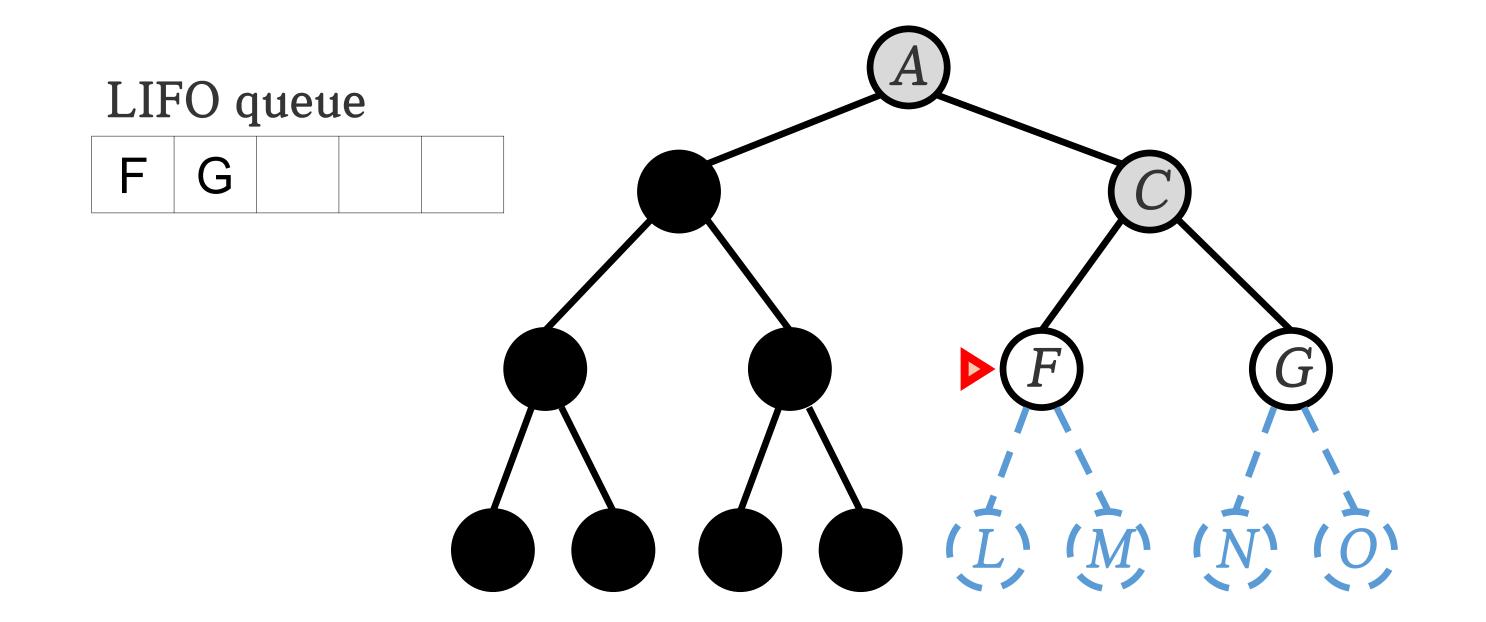


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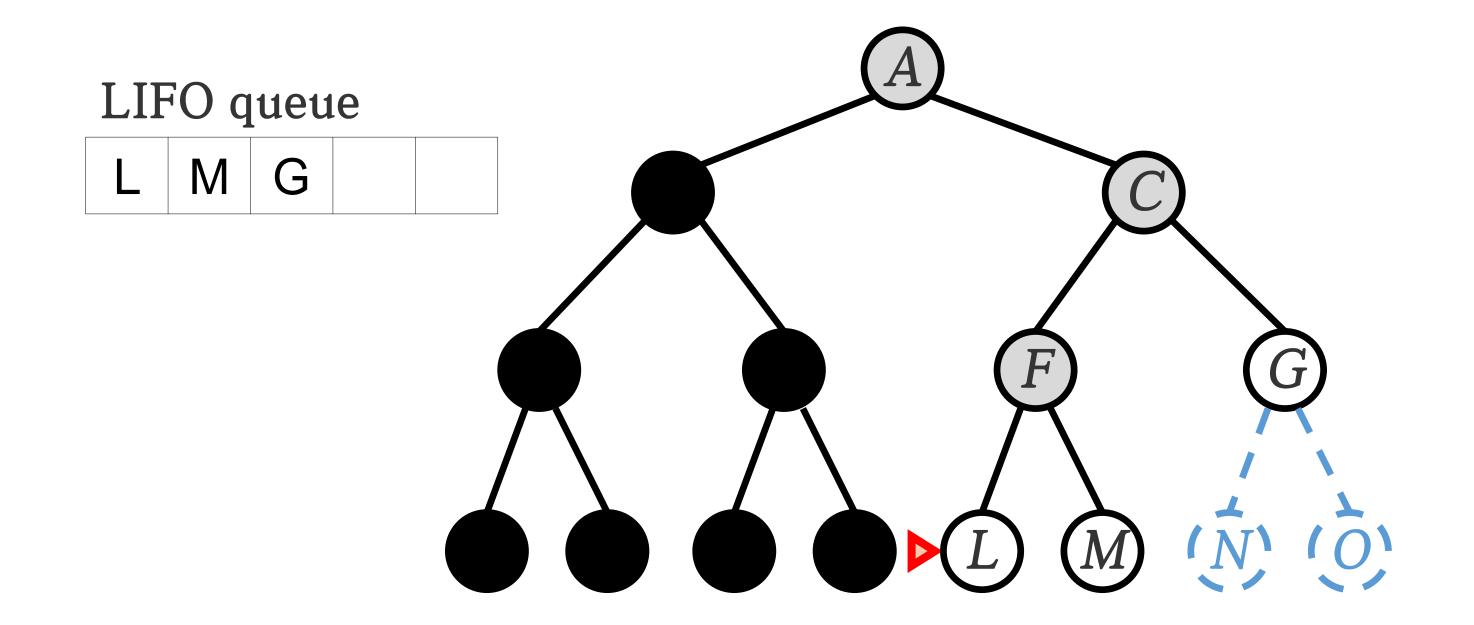


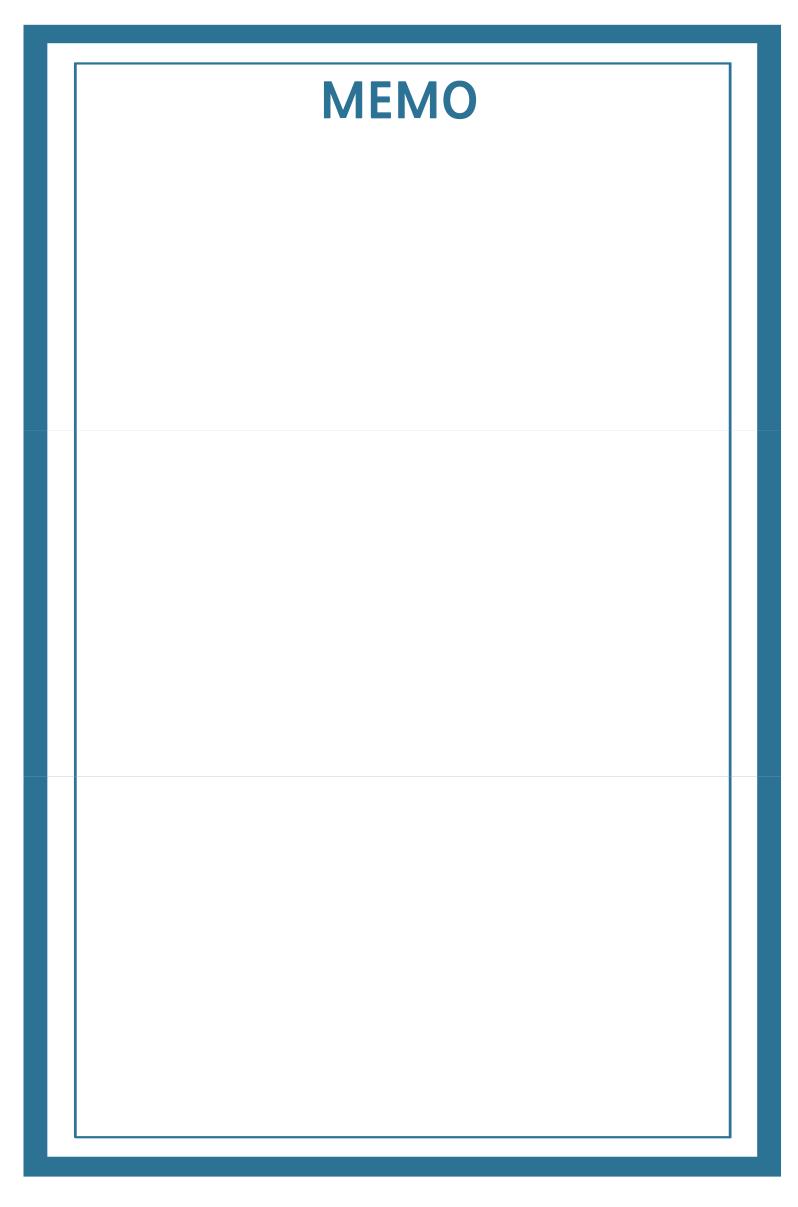
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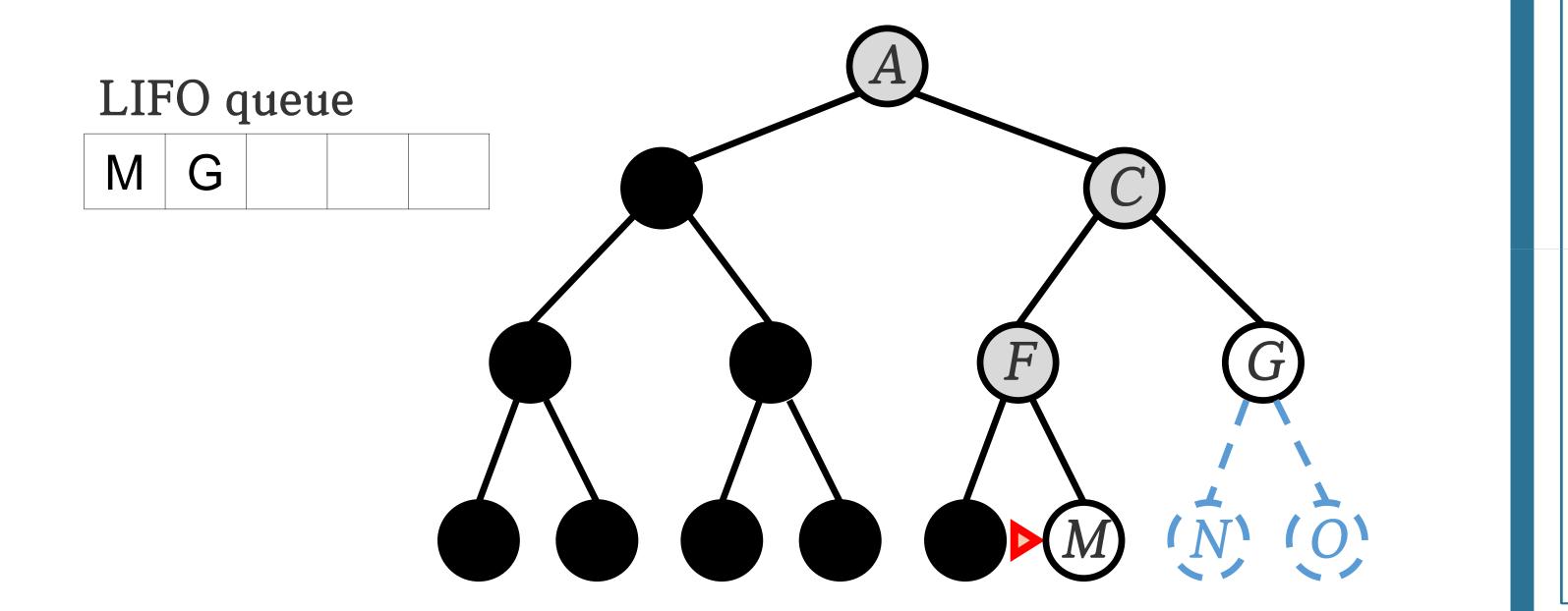
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Summary of BFS and DFS

© Comparison

| Criterion | BFS | DFS |
|-----------|--------------|----------|
| Complete? | Yes | No |
| Time | $O(b^{d+1})$ | $O(b^m)$ |
| Space | $O(b^{d+1})$ | O(bm) |
| Optimal? | Yes | No |

- ▶ Breadth-first search is complete but expensive
- ► Depth-first search is cheap but incomplete
- © Can't we do better than this?



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