



# Advanced analytic methods for neutron spectra unfolding and pulse shape discrimination

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## Motivation and Introduction

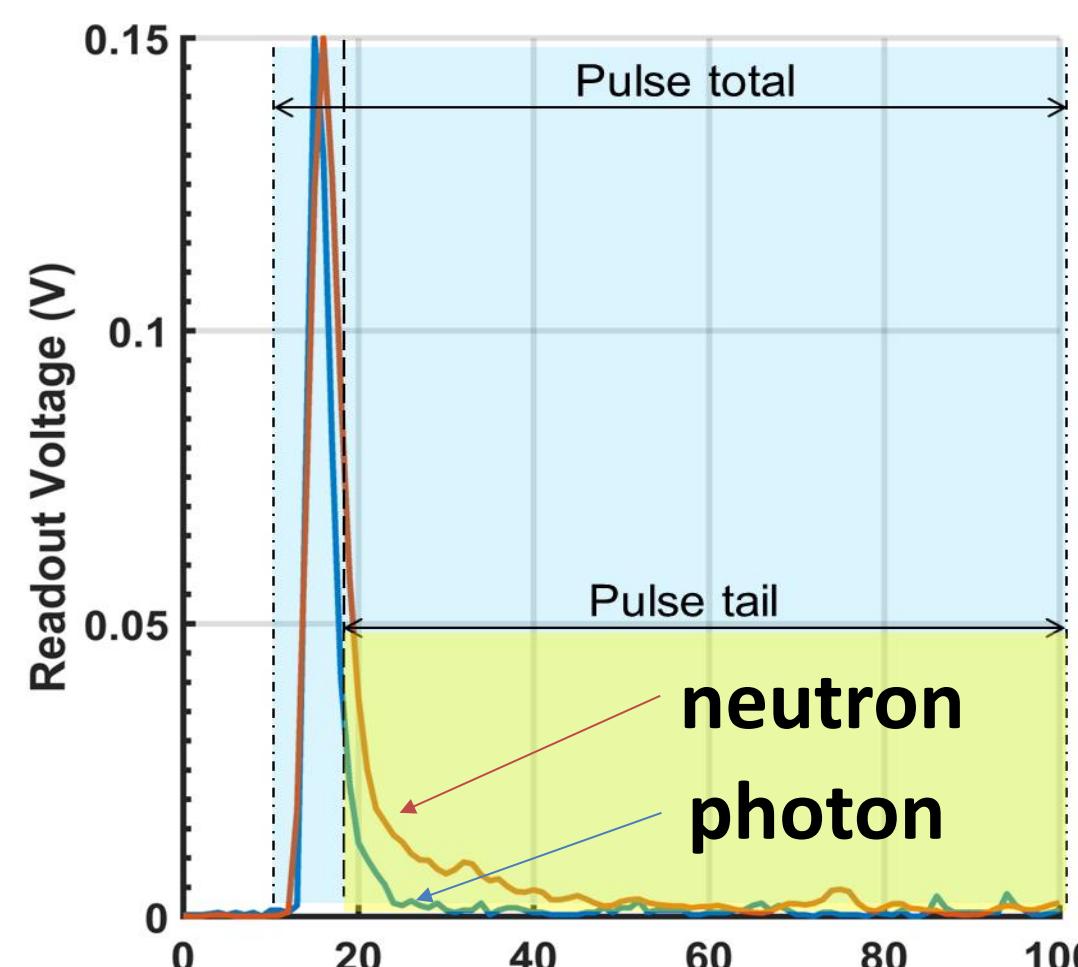
- Neutron spectrometry without time-of-flight** can be extremely useful in safeguards and nonproliferation applications, e.g. neutron imaging for material accountancy and verification (Fig. 1), to discriminate between fissile material and other neutron emitting sources.
- Organic scintillators are intrinsically able to reconstruct the incident neutron spectrum, by unfolding the measured pulse-height distribution with the known response of the scintillator to monoenergetic neutrons.**
- The use of organic scintillators is well established for the measurement of neutron spectra above several hundred keV.
- Pulse-height spectrum results from energy deposited both by proton recoils, produced by neutron interactions with H-1 nuclei in the scintillator, and electron recoils, generated by gamma-rays via Compton scattering.
- Improved algorithms are needed both to maximize gamma-neutron discrimination capability and increase fidelity of neutron spectrometry and thus decrease the neutron energy detection threshold.**

Fig. 1 Radiation Inspection System [1].

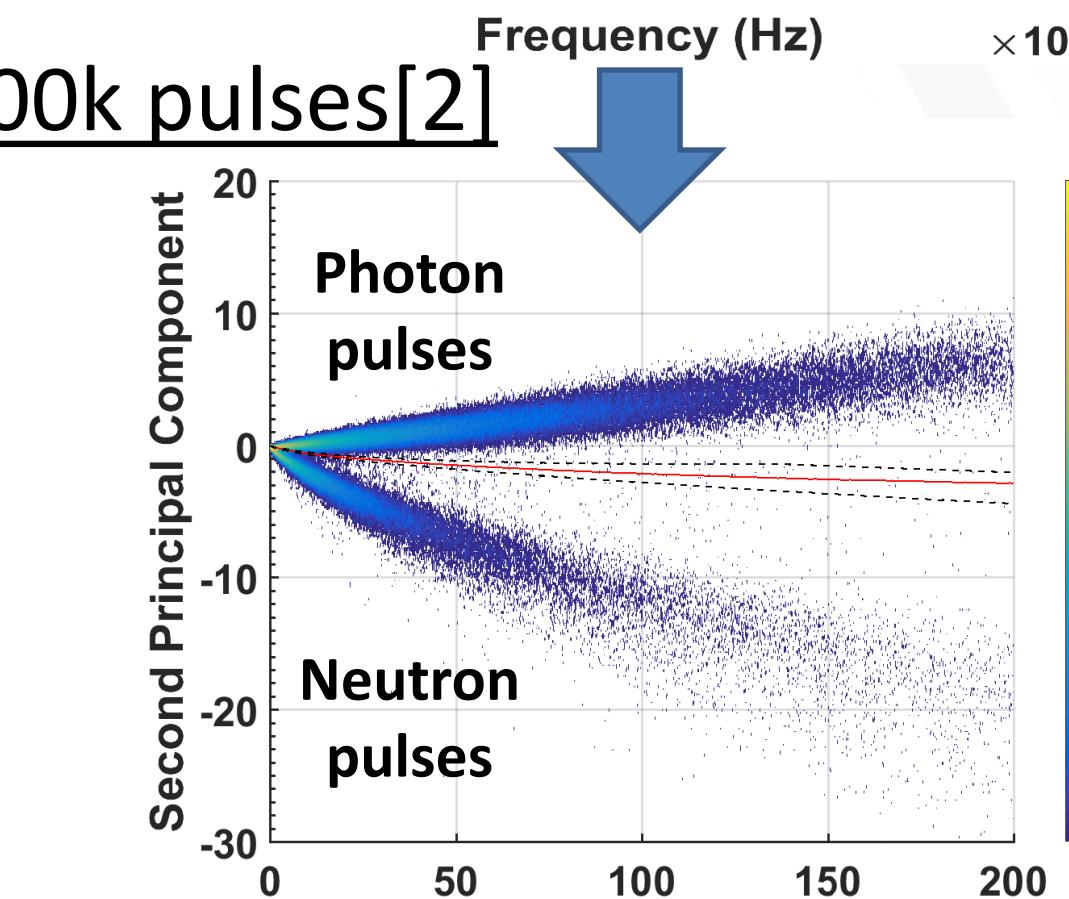
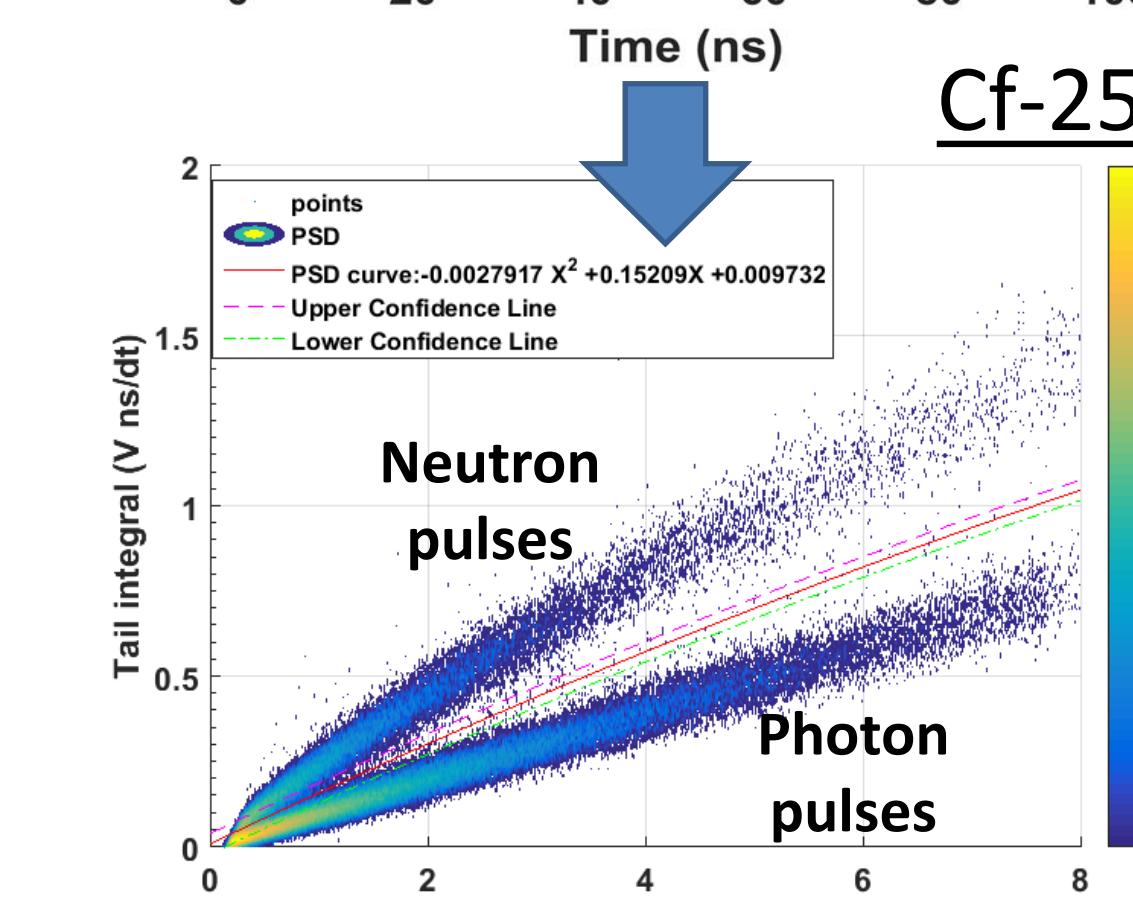
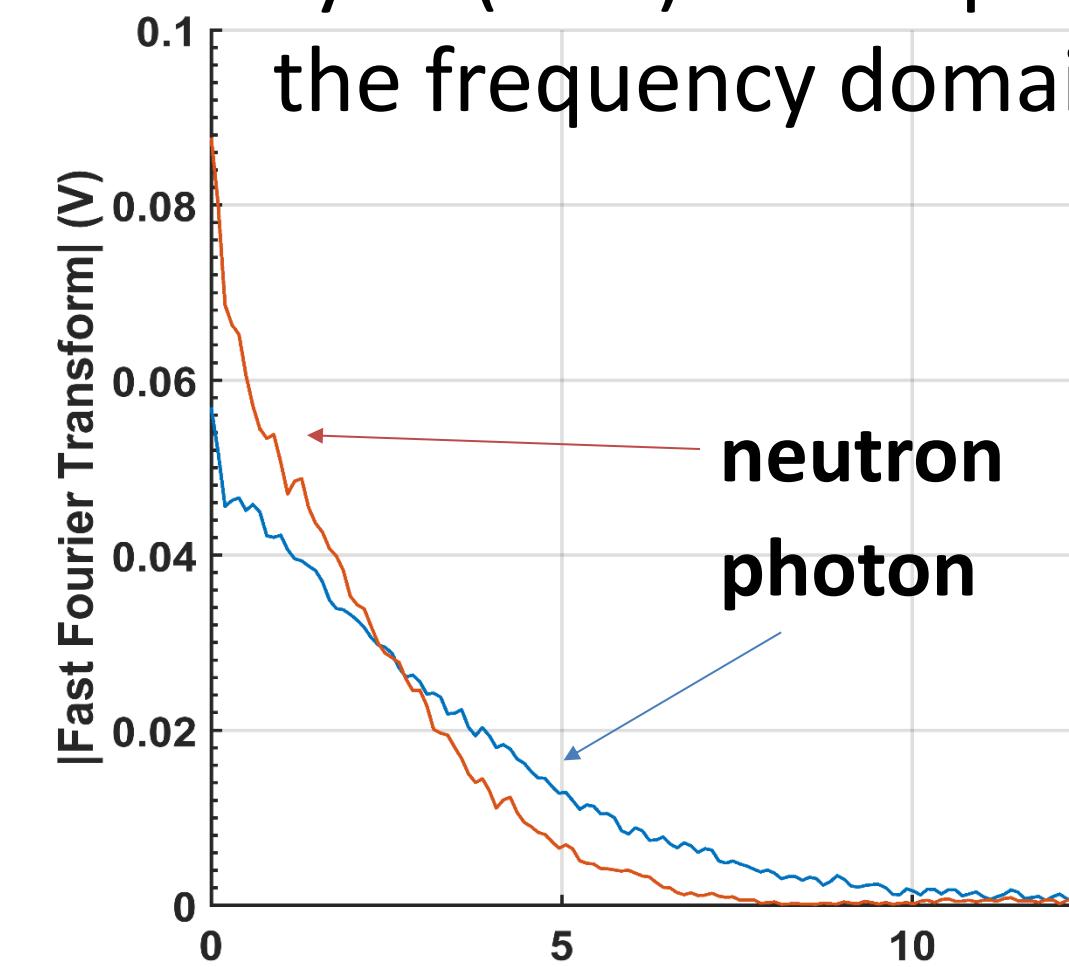
## Pulse shape discrimination

### GAMMA-NEUTRON DISCRIMINATION

Charge Integration (CI) of the pulse in the time domain



Principal component analysis (PCA) of the pulse in the frequency domain



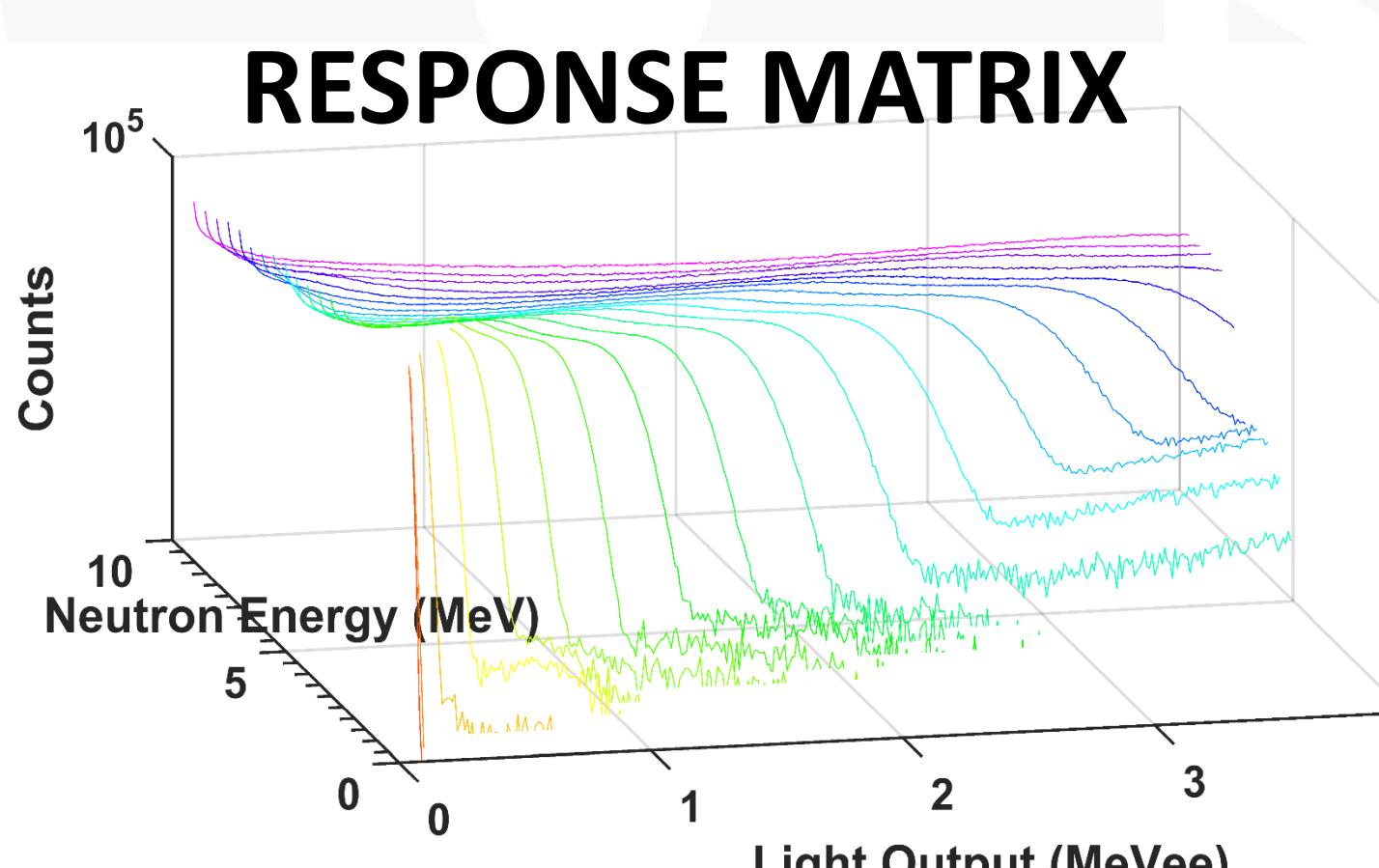
## Neutron spectra unfolding

### UNFOLDING

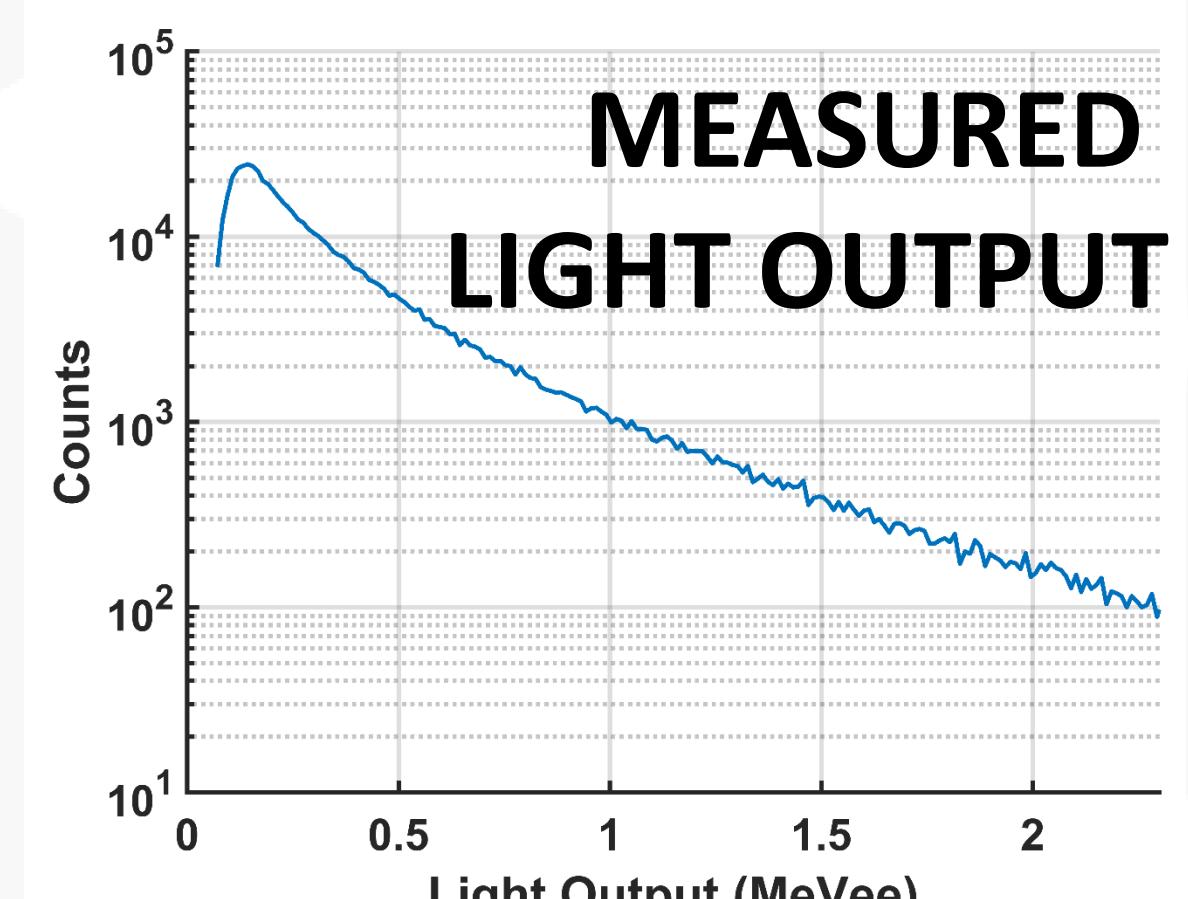
$$z_{0i} + e_i = \sum_j R_{ij} F_j \quad (i = 1 \dots M)$$

$z_{0i}$  light output spectrum  
 $M$  is the number of detection channels  
 $R_i(E)$  is the detector response  
 $\Phi(E)$  Neutron spectrum flux  $\text{cm}^{-2}$

### RESPONSE MATRIX



### MEASURED LIGHT OUTPUT



### Approach A (new!!!):

Poisson unfolding, for discrete events

• Convex optimization technique:

SPIRAL [4]

• Markov chain Monte Carlo :

automatic adjustment of the regularization parameters + a posteriori measures of uncertainty

### UNFOLDING ALGORITHM

### NEUTRON SPECTRUM

Approach B:  
MAXED [2] solves a regularized weighted least squares problem incorporating prior information

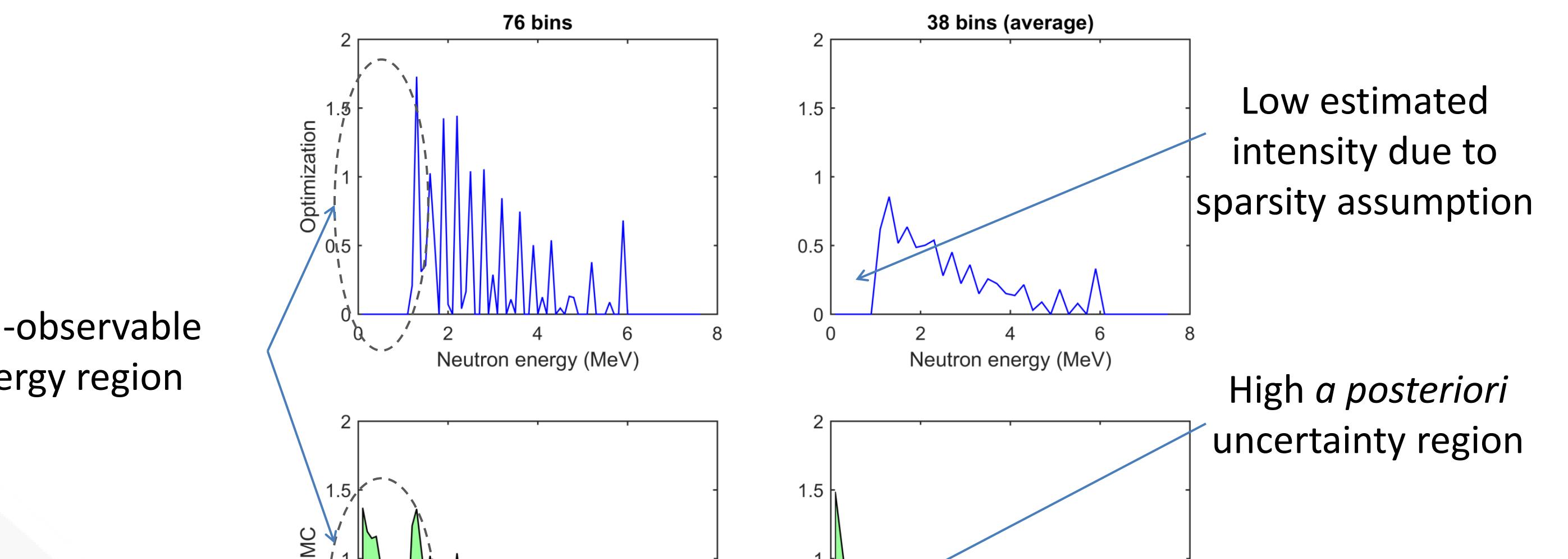


Fig. 4: Cf-252 neutron energy spectra unfolded by SPIRAL [1] (top) and the proposed MCMC method (bottom)

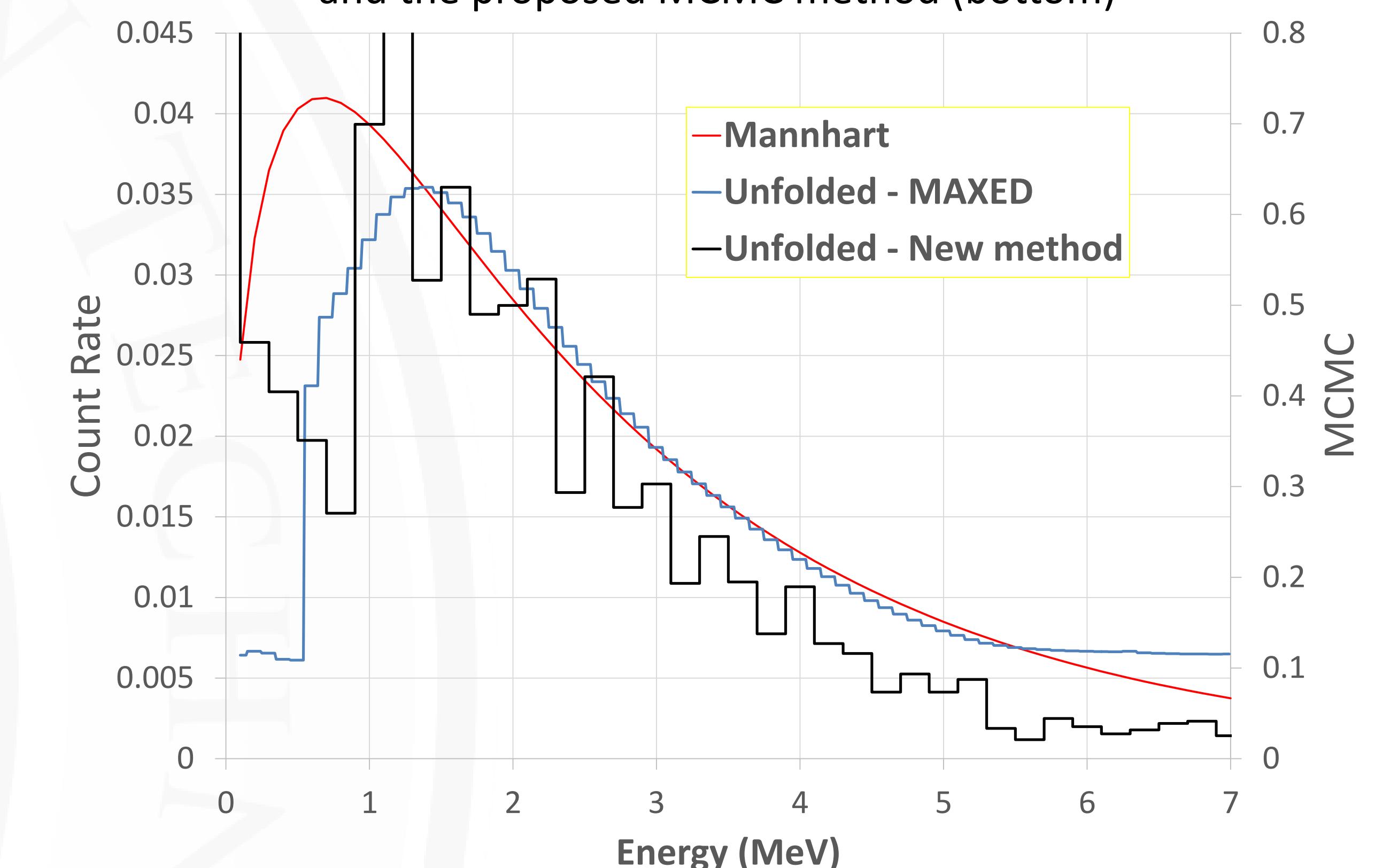


Fig. 5. Unfolded neutron energy spectrum from Cf-252 detected with an EJ-309 liquid scintillator; the Watt spectrum from Mannhart is shown for reference.

## Conclusions and Future Work

### PCA

- Principal component analysis does not require parameter optimization to perform the classification.
- Domain transformation mitigates the effect of temporal delays.

### Unfolding

- Novel unfolding algorithm to be used for neutron energy reconstruction using a single liquid scintillator (ill-conditioned response matrix).
- Trend of the reconstructed neutron spectrum compares well with analytic spectrum function → uncertainty compensation needed.

Incorporate the pulse shape discrimination to the unfolding algorithm to improve fidelity at low energies.



### References

- [1] "Technology R&D for Arms Control", Office of Nonproliferation Research and Engineering, Spring 2001.
- [2] A. C. Kaplan, et al., "EJ-309 pulse shape discrimination performance with a high gamma-ray-to-neutron ratio and low threshold," Nucl. Instr. Meth. A, **729**, (2013)
- [3] Reginatto, M. "Spectrum unfolding, sensitivity analysis and propagation of uncertainties with the maximum entropy deconvolution code MAXED," Nucl. Instr. Meth. A, **476**, 242 (2002).
- [4] Harmany, Z. T. et al., "This is SPIRAL-TAP: Sparse Poisson Intensity Reconstruction Algorithms—Theory and Practice", IEEE Trans. Image Process., 2012

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