

# Assignment 2

## Overview

This assignment satisfies the following learning objectives of the course:

- Develop inductive definitions based on mathematical induction
- Construct finite automata and grammars for regular languages

This assignment contains 6 questions and 40 points.

## Rules and Deliverables

- This is an individual assignment.
- Cheating of any kind is NOT tolerated! Assignments will be checked against each other, and illegal collaboration will be treated based on the University dishonesty policy.
- The due date will be **Saturday 9/28/2024 at 11:59pm.**
- Submitting the assignment 24 hours after the due date will result in a deduction of 20% from the student's grade.
- Each student should submit:
  1. The answers document in a PDF format.
  2. The complete name and EUID of students must be written within the document.
- The assignment must be submitted only through Canvas.

## Assignment Description

1. Find an inductive definition for each set S. In this question, N is the set of Natural numbers and includes 0. (4 points)

a)  $S: \{1, 5, 13, 29, 61, \dots\}$

b)  $S: \{a^{2n} \mid n \in \mathbb{N}\} \cup \{a^{2n+1} \mid n \in \mathbb{N}\}$

2. Define a grammar for each of the following languages: (6 points)

a)  $L = \{bb, bab, baab, baaab, \dots\}$

b)  $\{a^n \mid n \in \mathbb{N}\} \cup \{bc^n \mid n \in \mathbb{N}\}$       \* N is the set of Natural numbers and includes

c)  $aa^*cbb^*d$        $\Sigma = \{a,b,c,d\}$

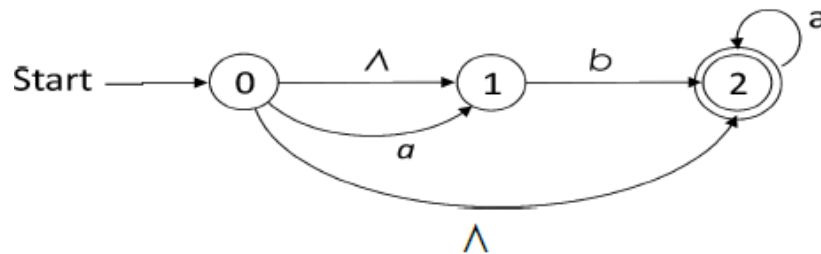
3. Construct an NFA for the following languages. (6 points)

i.  $(a + b)^*a$

ii.  $(ab + abc)^*$

4. **(A)** Convert the following NFA to equivalent DFA. **(B)** Show the steps for the conversion. (10 points)

Over alphabet  $\{a, b\}$ . Hint: Symbol  $\Lambda$  is another notation for empty string ( $\epsilon$ )



5. What is the NFA of the following regular grammar? (4 points)

$S \rightarrow abS \mid aS \mid ba$

6. Convert the following NFA to an equivalent Regular Expression using **GNFA method**. Please first delete state B, then state S, and finally state A. (10 points)

