

CSCE 5400 Formal Languages, Automata, and Computability - Fall 2024

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Assignment-3

1. Find grammar for the following languages:

- $L = \{a^n b^m c^k \mid n = k + m \text{ and } n \geq 0, m \geq 0, k \geq 0\}$ (3 points)
- $L = \{(ab)^n (cd)^n : n \geq 1\}$ (3 points)
- Language whose 3rd symbol from last is b. over $\{a, b\}$ (3 point)

Ans:

a.

$$\begin{cases} S \rightarrow aSc \mid B \\ B \rightarrow aBb \mid \text{epsilon} \end{cases}$$

b.

$$\begin{cases} S \rightarrow abScd \mid abcd \end{cases}$$

c.

$$\begin{cases} S \rightarrow AbBB \\ A \rightarrow aA \mid bA \mid \text{epsilon} \\ B \rightarrow a \mid b \end{cases}$$

2. What is the language of the following CFG? (5 points)

$$\begin{cases} S \rightarrow AB \mid \varepsilon \\ A \rightarrow 1A \mid S \\ B \rightarrow 0B \mid S \end{cases}$$

Ans: This grammar can generate any combination of 0 and 1 including epsilon.

$$L(G) = \{0,1\}^*$$

3. Remove the ε -Productions: (3 points)

$$\left\{ \begin{array}{l} S \rightarrow AaB \mid aaB \\ A \rightarrow \varepsilon \\ B \rightarrow aaA \mid \varepsilon \end{array} \right.$$

Ans:
$$\left\{ \begin{array}{l} S \rightarrow aB \mid aaB \mid a \mid aa \\ B \rightarrow aa \end{array} \right.$$

4. Convert the following CFG into an equivalent CFG in Chomsky Normal Form: (3 points)

$$\left\{ \begin{array}{l} A \rightarrow BAB \mid B \mid \varepsilon \\ B \rightarrow 00 \mid \varepsilon \end{array} \right.$$

Ans:

Remove epsilon productions:

$$\left\{ \begin{array}{l} A \rightarrow BAB \mid B \mid BB \mid AB \mid BA \mid A \mid \text{epsilon} \\ B \rightarrow 00 \end{array} \right.$$

Remove unit productions

$$\left\{ \begin{array}{l} A \rightarrow BAB \mid 00 \mid BB \mid AB \mid BA \mid \text{epsilon} \\ B \rightarrow 00 \end{array} \right.$$

$$\left\{ \begin{array}{l} A \rightarrow BAB \mid XX \mid BB \mid AB \mid BA \mid \text{epsilon} \\ B \rightarrow XX \\ X \rightarrow 0 \end{array} \right.$$

$$\left\{ \begin{array}{l} A \rightarrow BY \mid XX \mid BB \mid AB \mid BA \mid \text{epsilon} \\ B \rightarrow XX \\ X \rightarrow 0 \\ Y \rightarrow AB \end{array} \right.$$

5. i) Find the grammar for the following language. (5 points)

$$L = \{ a^n b^n c^m d^m \mid n \geq 1, m \geq 1 \} \cup \{ a^n b^m c^m d^n \mid n \geq 1, m \geq 1 \}$$

ii) Convert the generated Context Free Grammar to Greibach Normal Form. (3 points)

iii) Is the grammar for language L ambiguous? Why? (2 points)

Ans:

i.

$$\left\{ \begin{array}{l} S \rightarrow A \mid B \\ A \rightarrow XY \\ X \rightarrow aXb \mid ab \\ Y \rightarrow cYd \mid cd \\ B \rightarrow aBd \mid aKd \\ K \rightarrow bKc \mid bc \end{array} \right.$$

ii.

$$\left\{ \begin{array}{l} S \rightarrow A \mid B \\ A \rightarrow XY \\ X \rightarrow aXM \mid aM \\ Y \rightarrow cYN \mid cN \\ B \rightarrow aBN \mid aKN \\ K \rightarrow bKO \mid bO \\ M \rightarrow b \\ N \rightarrow d \\ O \rightarrow c \end{array} \right.$$

$$\begin{array}{l}
 S \rightarrow aXMY \mid aMY \mid aBN \mid aKN \\
 A \rightarrow aXMY \mid aMY \\
 X \rightarrow aXM \mid aM \\
 Y \rightarrow cYN \mid cN \\
 B \rightarrow aBN \mid aKN \\
 K \rightarrow bKO \mid bO \\
 M \rightarrow b \\
 N \rightarrow d \\
 O \rightarrow c
 \end{array}$$

iii. Yes, the grammar for language L is ambiguous because we can derive a string by different ways.

Ex: String "abcd" can be derived in 2 ways.

Method 1: $S \rightarrow A \rightarrow XY \rightarrow Xcd \rightarrow abcd$

Method 2: $S \rightarrow B \rightarrow aKd \rightarrow abcd$
