Optimizing WiFi Network Performance

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November 21, 2024

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Overview of the Problem

- **Goal**: Optimize WiFi network performance by efficiently allocating power and bandwidth across access points, minimizing interference, and ensuring required Quality of Service (QoS).
- Why?
 - Improve overall network performance.
 - Minimize interference and optimize resource usage.
- Challenge: Balancing power allocation, minimizing interference, and ensuring QoS across the network.

Core Components of the Model

Variables:

- P_i : Power allocated to access point i, influencing coverage.
- B_i : Bandwidth allocated to access point i, affecting throughput.
- C_i : Number of clients connected to access point i, affecting load.

Parameters:

- P_{max} : Maximum power limit to prevent interference.
- B_{max} : Maximum bandwidth allocation per access point.
- Q_i : QoS requirement (throughput/latency) for access point i.
- I_{ij} : Interference factor between access points i and j.

Additional Considerations:

• C_B: Cost of bandwidth allocation.



Objective Function and Constraints

Objective: Minimize interference and allocation costs:

$$Cost = \sum_{i=1}^{N} \left(I_{ii} + \sum_{j \neq i} I_{ij} \right) + \sum_{i=1}^{N} C_i \cdot P_i + C_B \cdot B_i$$

Constraints:

- Power: $0 \le P_i \le P_{\text{max}}$.
- Bandwidth: $0 \le B_i \le B_{\text{max}}$.
- QoS: $Q_i \leq QoS_i$, where QoS_i defines the required quality for access point i.
- Non-Negativity: $P_i, B_i, C_i \geq 0$.

Convexity

- The objective function is convex, ensuring that any local minimum is also a global minimum, which is crucial for efficient optimization and guarantees optimality.
- Constraints are linear, forming a convex feasible region, which makes the problem well-suited for methods like linear programming.
- Decision variables P_i , B_i , and C_i are in a **finite-dimensional vector space**, supporting the application of efficient optimization algorithms such as linear programming and gradient-based methods (e.g., gradient descent).
- Implication: The convexity of the problem ensures that optimization algorithms will converge to a global solution, even in large-scale networks, allowing for efficient solutions.

Mathematical Tools for Optimization

- Linear Programming (LP): Solvers like Gurobi or CBC are used to handle the linear components of the model, ensuring that resource allocation and interference terms are efficiently optimized.
- Quadratic Programming (QP): Used to solve problems involving quadratic terms, such as interference models, where the relationship between variables is non-linear but still convex.
- Gradient-Based Solvers: Suitable for convex functions, where methods like Sequential Quadratic Programming (SQP) can be used to iteratively find the optimal allocation of power and bandwidth across the network.

Solution Scheme and Scalability

Optimization Methods:

- Linear Programming (LP): Efficient solvers like Gurobi handle large-scale LP for linear models.
- Metaheuristics: Genetic Algorithms or Simulated Annealing address complex, non-linear models.
- Convex Optimization: Gradient-based solvers, such as SQP, work for smooth convex models.

Scalability:

- Heuristics balance solution quality and computation time as network size grows.
- Real-time optimization adjusts to dynamic networks and traffic.
- Decomposition or parallel computation helps with large networks.

Solution Approach:

- Define decision variables and formulate the objective function and constraints.
- Use solvers or heuristics based on model complexity.

Expected Results

- Optimal Resource Allocation: Power and bandwidth are efficiently allocated across the network, reducing resource waste, improving overall network performance, and ensuring scalability as the system expands.
- Improved QoS: All access points meet or exceed the required QoS thresholds, ensuring reliable, high-quality connectivity with minimal latency and optimal throughput for all users, regardless of network load.
- Minimized Interference: Interference between access points is minimized, resulting in improved signal-to-noise ratios, better coverage, and enhanced user experience in dense network environments.

Conclusion and Applications

 Optimizing WiFi networks is a complex yet rewarding challenge. The proposed solution provides a scalable and efficient approach, leading to improved performance through better resource allocation and reduced interference.

• Applications:

- Enterprise WiFi Networks: Optimize resource allocation in large office buildings and campuses to ensure efficient connectivity for employees and visitors.
- **Smart Cities:** Efficiently allocate bandwidth in public WiFi systems to support IoT devices, such as smart street lights, sensors, and cameras.
- **Hospital Networks:** Ensure quality of service for medical devices and critical infrastructure requiring low-latency and high reliability.
- Public WiFi Hotspots: Minimize interference and ensure consistent performance for users in crowded locations like airports, malls, or public parks.