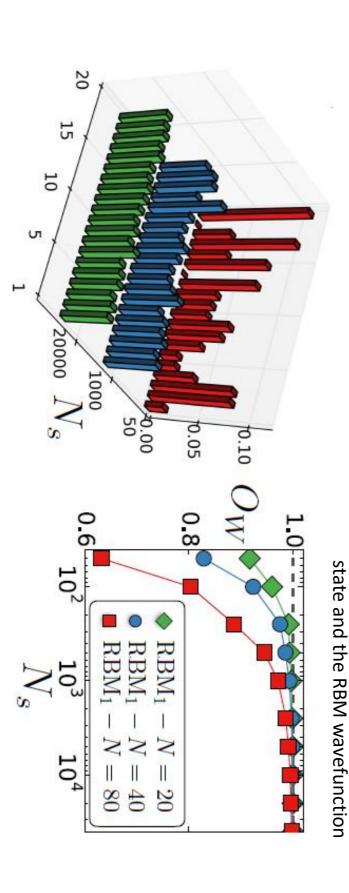
### Many body quantum state tomography with neural networks

Sim Jun Yan

Numerical result

#### W state

Overlap (fidelity) between W

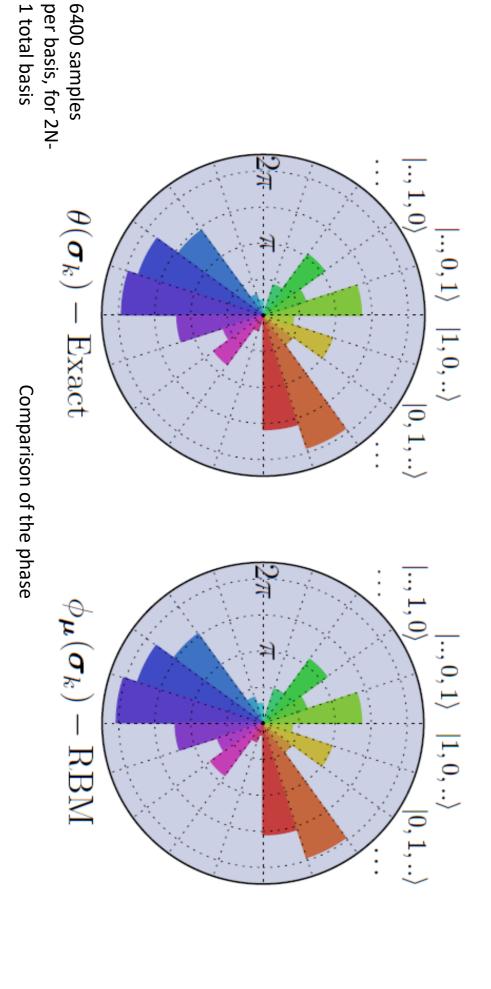


 $N_{\rm S}$  is the number of

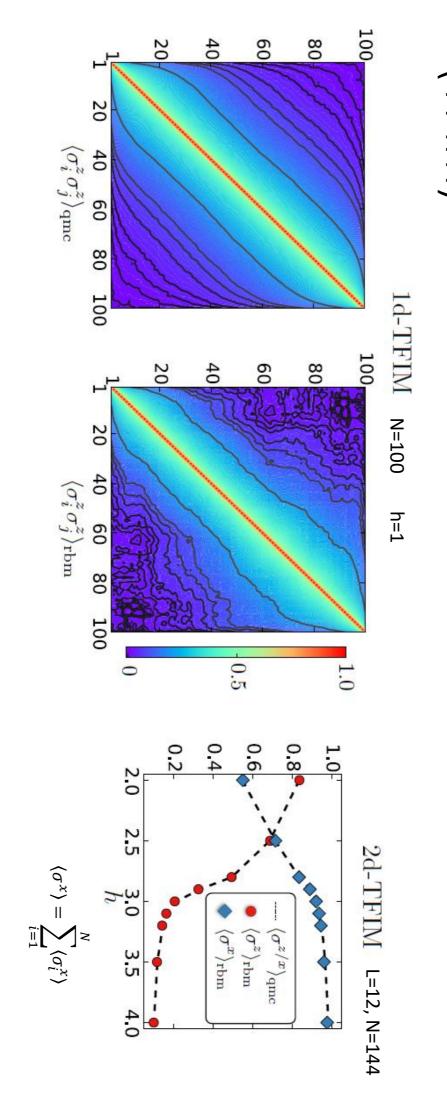
training samples

For N=20, fidelity=0.99 with  $N_{\rm S}=300$  Cf. MPS: fidelity=0.96 with  $N_{\rm S}=400$ 

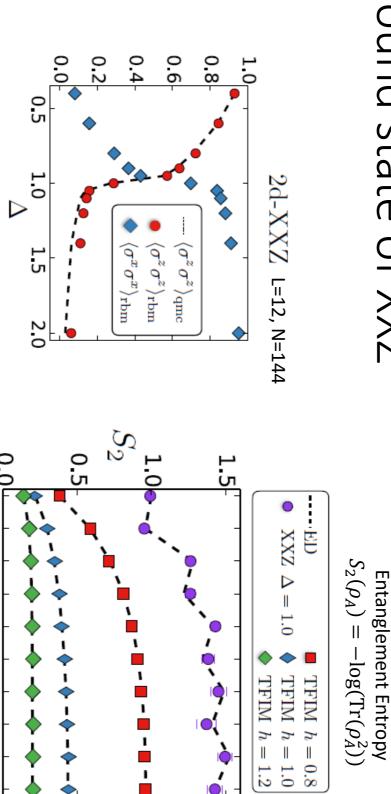
# W state with random local phase shifts (N=20)



## (TFIM) Ground state of Transverse Field Ising Model



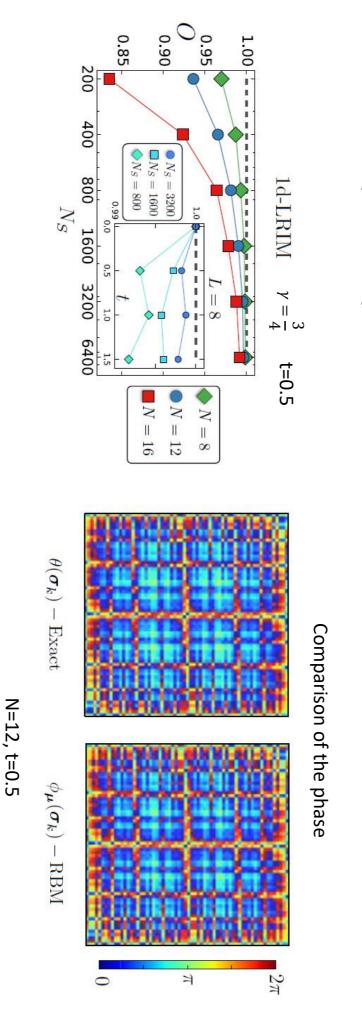
## Ground state of XXZ



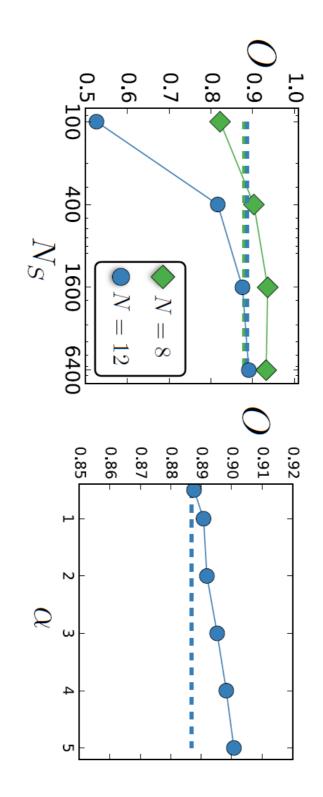
N=20

 $\ell$  is the size of the subsystem  $ho_A$ 

## Quantum dynamics of Long Range Ising Model (LRIM)



#### Random State



example, consider an unstructured wavefunction, i.e. a randomly chosen state. The wavefunction in the previous example all have some kind of structure which explains the good performance. In this

In the first figure, the overlap saturates rather quickly.

units increase to 5. Whereas previous examples shows pretty good result with  $\frac{1}{4} \le \alpha \le 1$ . In the second figure, the overlap shows little improvement even when lpha which is the ratio of hidden units to the visible

Applications of machine learning technique generally fails when there is little structure in the wavefunction.

## Representational power and limitations of RBM

List from Z.-A. Jia, B. Yi, R. Zhai, Y.-C. Wu, G.-C. Guo, and G.-P. Guo, "Quantum Neural Network States," arxiv: 1808.10601

#### States that can be efficiently represented by RBM:

- $\mathbb{Z}_2$ -toric code states<sup>23</sup>;
- Graph states<sup>25</sup>;
- Stabilizer states with generators of pure type,  $\mathbf{S}_X, \mathbf{S}_Y, \mathbf{S}_Z$  and their arbitrary union<sup>24</sup>;
- Perfect surface code states, surface code states with boundary, defect and twist<sup>24</sup>;
- Kitaev's  $D(\mathbb{Z}_d)$  quantum double ground states<sup>24</sup>;

## States that cannot be efficiently represented by RBM:

universal quantum computational states, PEPS, and ground states of k-local Hamiltonians

### States that can be efficiently represented by Deep Boltzmann Machine (DBM):

- Any *n*-qubit quantum states generated by a quantum circuit of depth T, the number of hidden neurons is  $O(nT)^{25}$ ;
- Tensor network states consist of n-local tensors with bound dimension D and maximum coordination number d, the number of hidden neurons is  $O(nD^{2d})^{25}$ ;
- The ground states of Hamiltonian with gap  $\Delta$ , the number of hidden neurons is  $O(\frac{m^2}{\Delta}(n-\log \epsilon))$  where  $\epsilon$  is the representational error<sup>25</sup>;

D.-L. Deng, X. Li, and S. Das Sarma, "Machine learning topological states," Phys. Rev. B 96, 195145 (2017).

Z.-A. Jia, Y.-H. Zhang, Y.-C. Wu, G.-C. Guo, and G.-P. Guo, "Efficient machine learning representations of surface code with boundaries, defects, domain walls and twists," arXiv preprint arXiv:1802.03738 (2018)

X. Gao and L.-M. Duan, "Efficient representation of quantum many-body states with deep neural networks," Nature Communications 8, 662 (2017).