

1)

$$a) a^*(ba)a^*(ba+a^*)a^*.$$

$$\mathcal{L} = \{xbyz:$$

$$\mathcal{L} = \{x_1 b a x_2 y x_3 : x_1, x_2, x_3 \in \{a\}^* \wedge y \in \{ba, a^*\}\}$$

$$*) c) (00+1)^*(0+11)^*$$

$$\mathcal{L} = \{xy : x \in \{00, 1\}^* \wedge y \in \{0, 11\}^*\}$$

2)

$$a) \mathcal{L} = \{w \in \{a, b, c\}^* : |w|_a > 0 \wedge |w|_b \geq 0 \wedge |w|_c > 0.\}$$

$$(a+b+c)^*(a(b+c)^*b(a+c)^*c + a(b+c)^*c(a+b)^*b.$$

$$b(a+c)^*a(b+c)^*c + b(a+c)^*c(a+b)^*a.$$

$$c(a+b)^*a(b+c)^*b + c(a+b)^*b(a+c)^*a).$$

$$b) \mathcal{L} = \{a^{2n}b^{2m+1} : m, n \in \mathbb{N}\}$$

$$(aa)^*(bb)^*b$$

$$d) \mathcal{L} = \{w \in \{a, b\}^* : |w|_3 = 0.\}$$

$$((a+b)(a+b)(a+b))^*$$

Date:

3)

$$a) \mathcal{L} = \{x1y : x, y \in \{0,1\}^* \wedge |y| = 4\}$$
$$(0+1)^* 1 (0+1)(0+1)(0+1)(0+1)$$

$$b) \mathcal{L} = \{x1 : x \in \{0,1\}^* \wedge 00 \notin w\}$$
$$((10)^* + (11)^* + (01)^* + (0(0)^* + 1(01)^*)) 1$$
$$= ((11)^* + (\epsilon + 1)(01)^* + (\epsilon + 0)(10)^*) 1$$

$$e) \{w \in \{0,1\}^* : |w_0| \equiv_e 1\}$$
$$(1^* 0 1^* 0 1^*)^* 1 0 1^*$$

$$f) c) w \in \mathcal{L} = \{w \in \{0,1\}^* : |w_0| \equiv_5 0\}$$
$$(\cancel{1^* 0 1^* 0 1^* 0 1^* 0 1^* 0 1^*})^*$$
$$(1^* 0 1^* 0 1^* 0 1^* 0 1^*)^*$$

A)

a) $\forall w \in \{a, b\}^*$: aaa xuất hiện duy nhất 1 lần trong w
 $(ab + aab + b)^* aaa (ba + baa + b)^*$.

b) $\mathcal{L} = \{w \in \{a, b\}^* \text{ mọi cặp } aa \text{ đều xuất hiện trước } bb\}$
 $(ba)^* (ab)^* (aa)^* (bb)^* (ab)^* (ba)^*$

c) $\mathcal{L} = \{w \in \{a, b, c\}^* : \text{chiều dài các chuỗi con chứa } a : 3\}$
 $(b+c)^* + (ab(a+b+c)(a+b+c) + (a+b+c)a(a+b+c) + (a+b+c)(a+b+c)a)^*$

Errata: chiều dài các chuỗi con chỉ chứa $a : 3$.

$(a+b+c)^* ((b+c)(a+b+c)^*) + (aaa)^*$