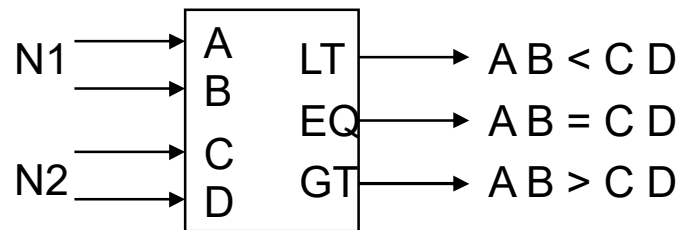


Comparator

Two-Bit Comparator



block diagram
and
truth table

A	B	C	D	LT	EQ	GT
0	0	0	0	0	1	0
		0	1	1	0	0
		1	0	1	0	0
		1	1	1	0	0
0	1	0	0	0	0	1
		0	1	0	1	0
		1	0	1	0	0
		1	1	1	0	0
1	0	0	0	0	0	1
		0	1	0	0	1
		1	0	0	1	0
		1	1	1	0	0
1	1	0	0	0	0	1
		0	1	0	0	1
		1	0	0	0	1
		1	1	0	1	0

we'll need a 4-variable Karnaugh map
for each of the 3 output functions

Two-Bit Comparator (cont'd)

			A		
	0	0	0	0	
	1	0	0	0	D
C	1	1	0	1	
	1	1	0	0	
			B		

K-map for LT

			A		
	1	0	0	0	
	0	1	0	0	D
C	0	0	1	0	
	0	0	0	1	
		B			

K-map for EQ

			A		
	0	1	1	1	
	0	0	1	1	D
C	0	0	0	0	
	0	0	1	0	
		B			

K-map for GT

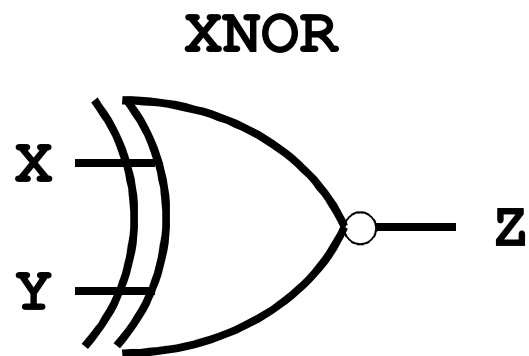
$$LT = A' B' D + A' C + B' C D$$

$$EQ = A' B' C' D' + A' B C' D + A B C D + A B' C D'$$

$$GT = B C' D' + A C' + A B D'$$

$$= (A \text{ xnor } C) \cdot (B \text{ xnor } D)$$

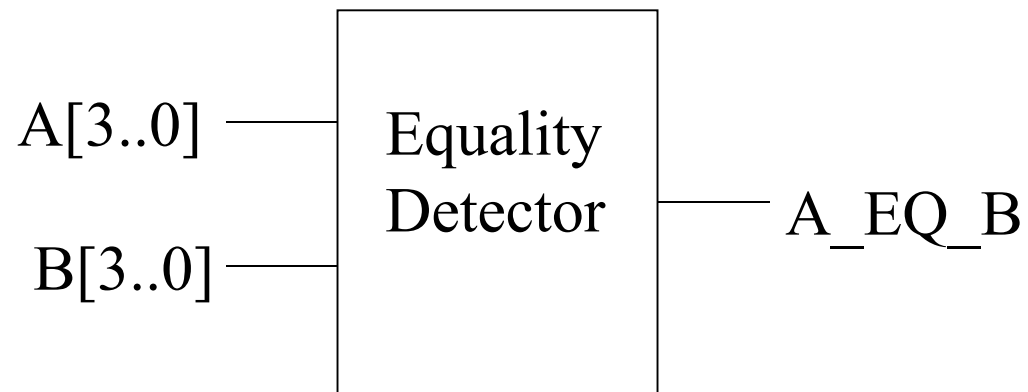
Equality Comparator



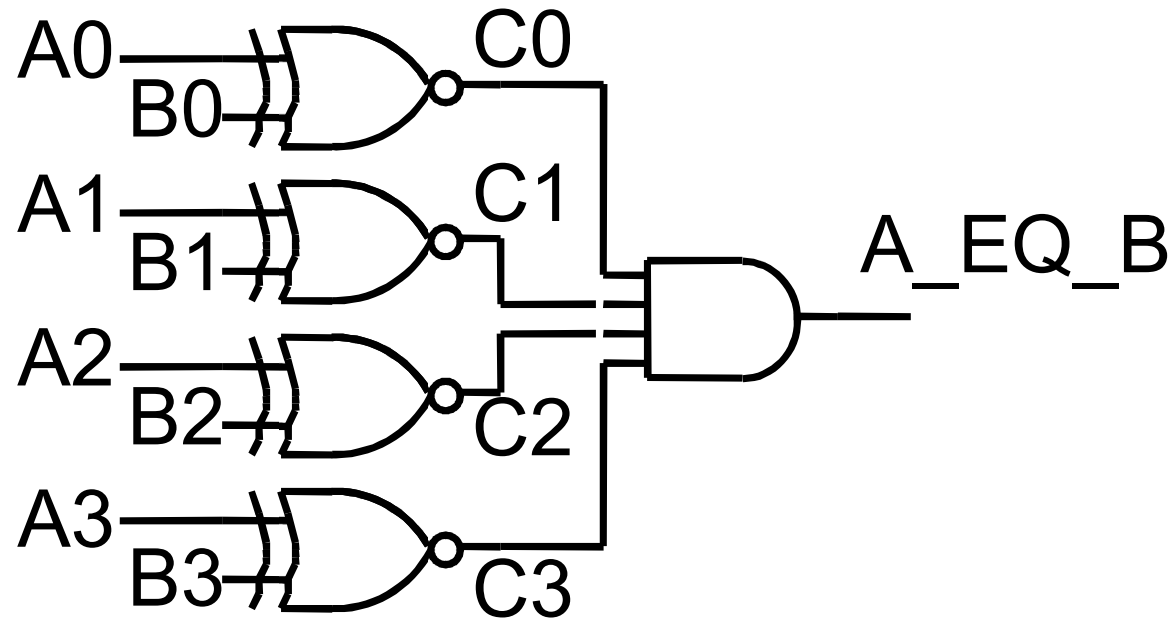
$$Z = X \text{ XNOR } Y$$

X	Y	Z
0	0	1
0	1	0
1	0	0
1	1	1

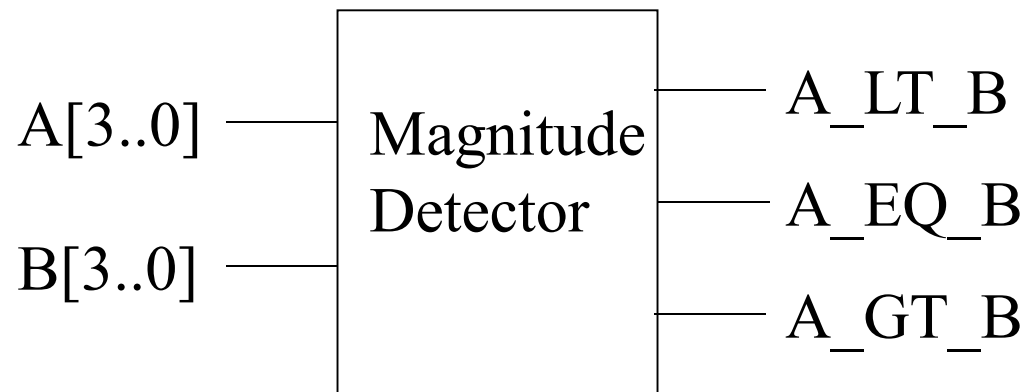
4-bit Equality Detector



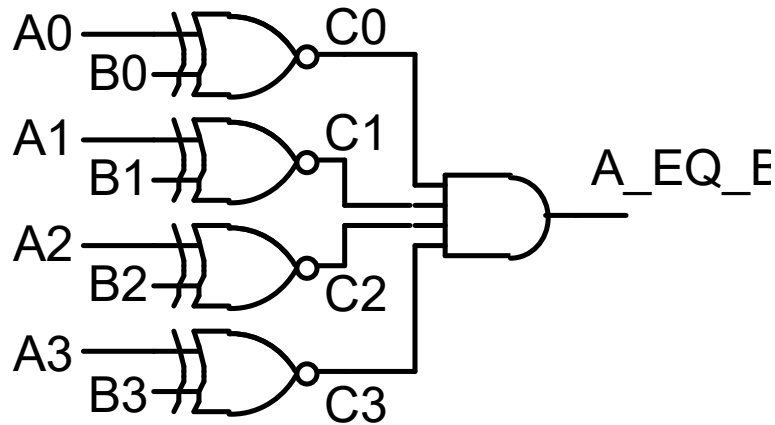
4-Bit Equality Comparator



4-bit Magnitude Comparator



Magnitude Comparator

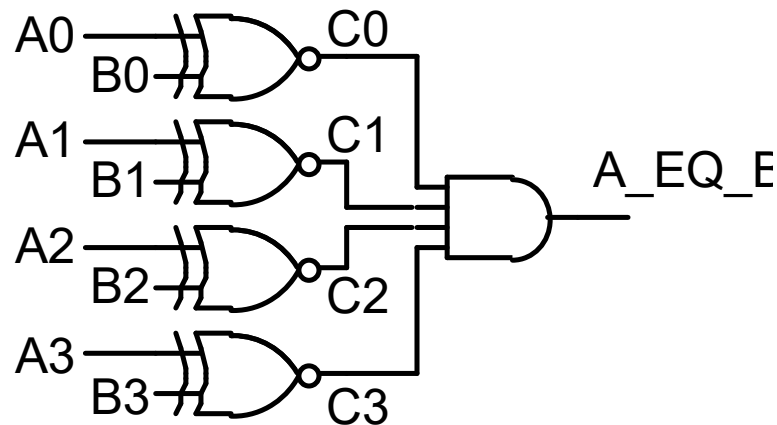


How can we find A_GT_B?

How many rows would a truth table have?

$$2^8 = 256!$$

Magnitude Comparator



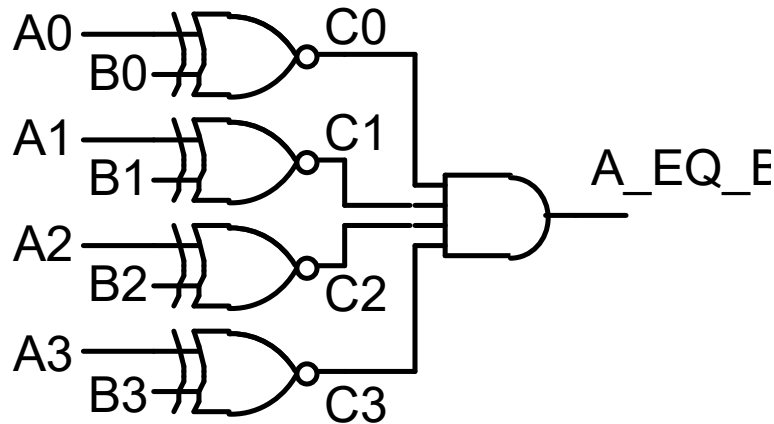
Find A_GT_B

If $A = 1001$ and
 $B = 0111$
is $A > B$?
Why?

Because $A_3 > B_3$
i.e. $A_3 \cdot B_3' = 1$

Therefore, one term in the
logic equation for A_GT_B is
 $A_3 \cdot B_3'$

Magnitude Comparator



If $A = 1101$ and
 $B = 1011$
 is $A > B$?
 Why?

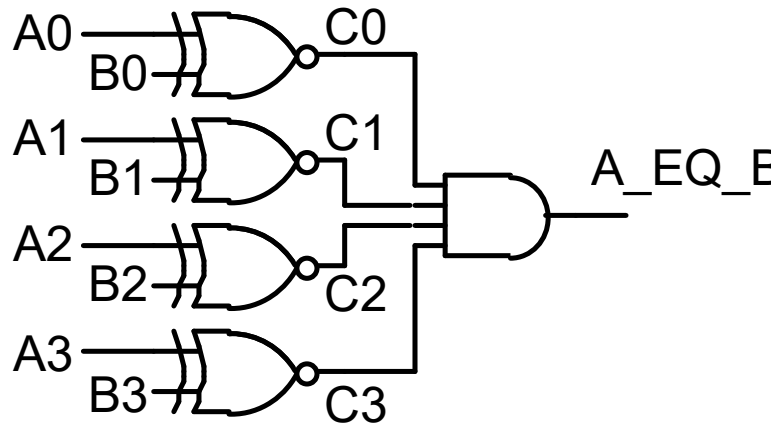
$$A_GT_B = A3 \cdot B3' \\ + \dots$$

Because $A3 = B3$ and
 $A2 > B2$

i.e. $C3 = 1$ and
 $A2 \cdot B2' = 1$

Therefore, the next term in the
 logic equation for A_GT_B is
 $C3 \cdot A2 \cdot B2'$

Magnitude Comparator



If $A = 1010$ and
 $B = 1001$
 is $A > B$?
 Why?

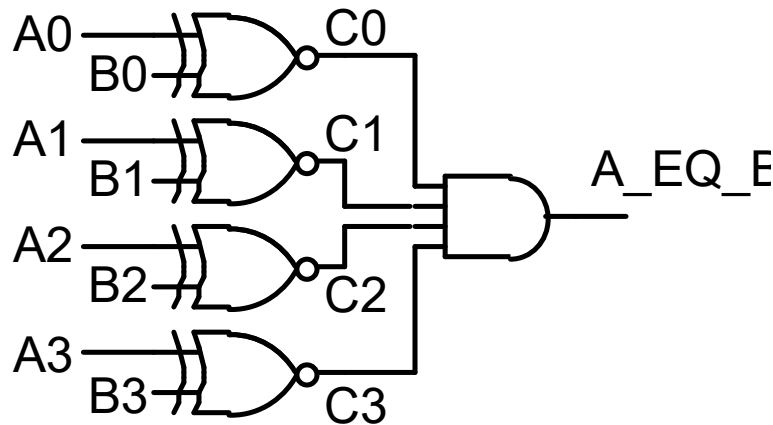
$$A_GT_B = A3 \cdot B3' \\ + C3 \cdot A2 \cdot B2' \\ + \dots$$

Because $A3 = B3$ and
 $A2 = B2$ and
 $A1 > B1$

i.e. $C3 = 1$ and $C2 = 1$ and
 $A1 \cdot B1' = 1$

Therefore, the next term in the
 logic equation for A_GT_B is
 $C3 \cdot C2 \cdot A1 \cdot B1'$

Magnitude Comparator



If $A = 1011$ and
 $B = 1010$
 is $A > B$?
 Why?

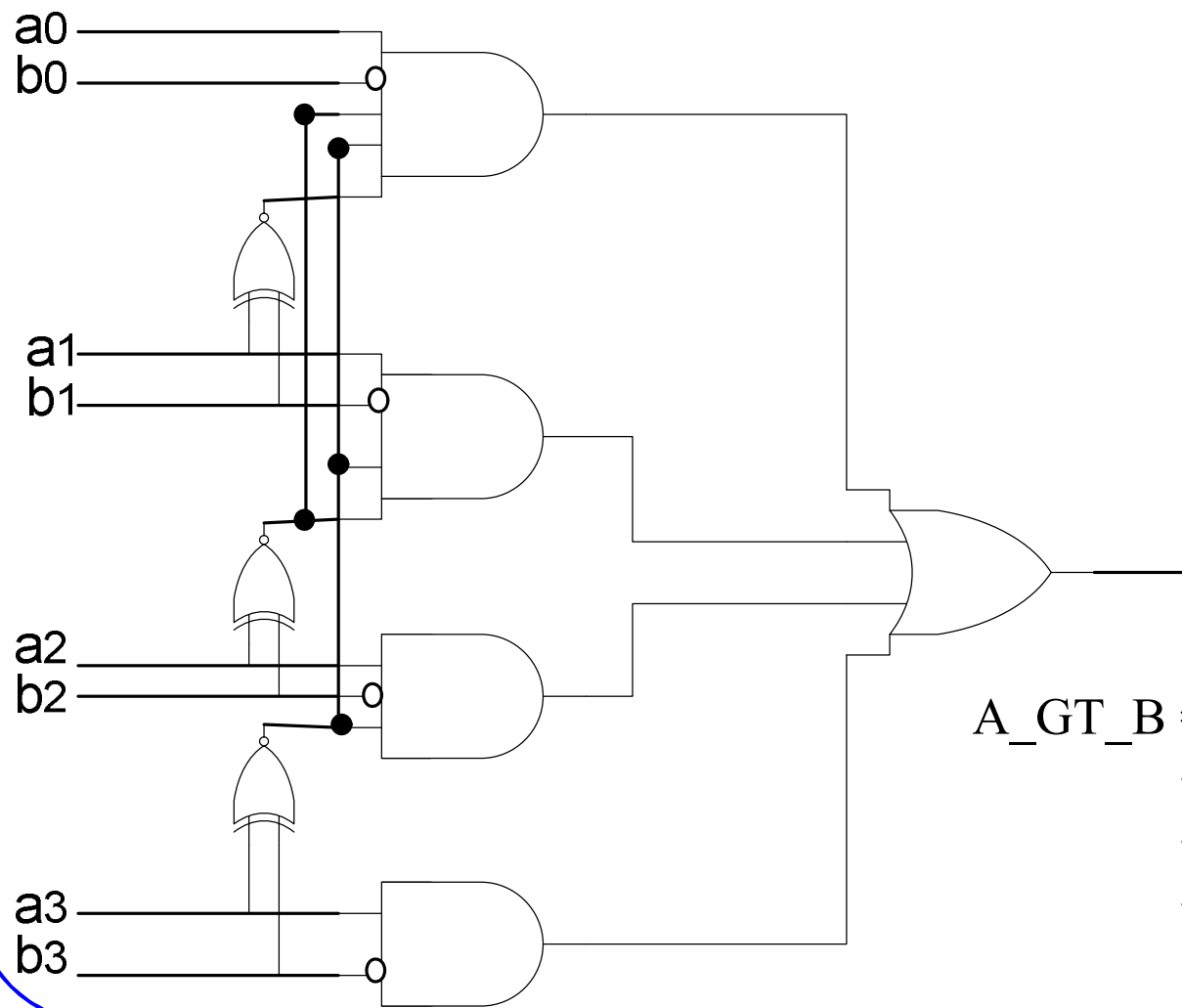
$$A_GT_B = A3 \cdot B3' \\
+ C3 \cdot A2 \cdot B2' \\
+ C3 \cdot C2 \cdot A1 \cdot B1' \\
+ \dots$$

Because $A3 = B3$ and
 $A2 = B2$ and
 $A1 = B1$ and
 $A0 > B0$

i.e. $C3 = 1$ and $C2 = 1$ and
 $C1 = 1$ and $A0 \cdot B0' = 1$

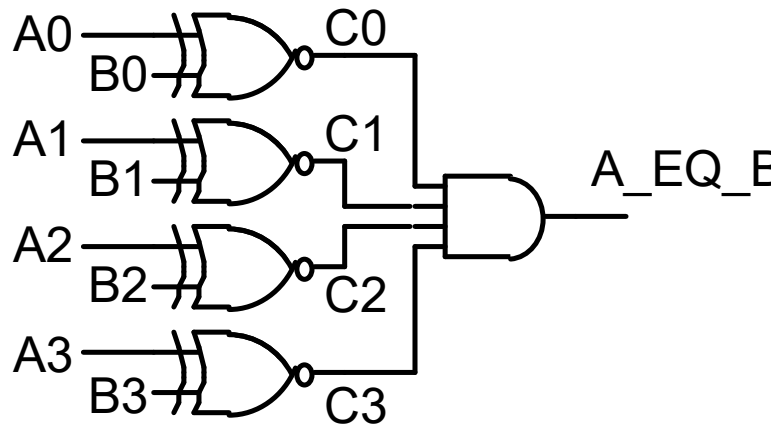
Therefore, the last term in the
 logic equation for A_GT_B is
 $C3 \cdot C2 \cdot C1 \cdot A0 \cdot B0'$

Magnitude Comparator



$$\begin{aligned}
 A_GT_B = & A3 \cdot B3' \\
 & + C3 \cdot A2 \cdot B2' \\
 & + C3 \cdot C2 \cdot A1 \cdot B1' \\
 & + C3 \cdot C2 \cdot C1 \cdot A0 \cdot B0'
 \end{aligned}$$

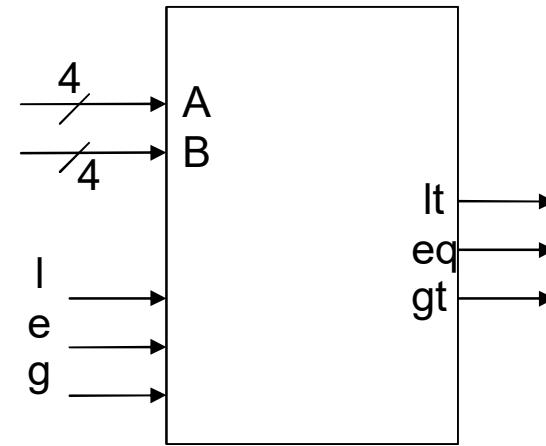
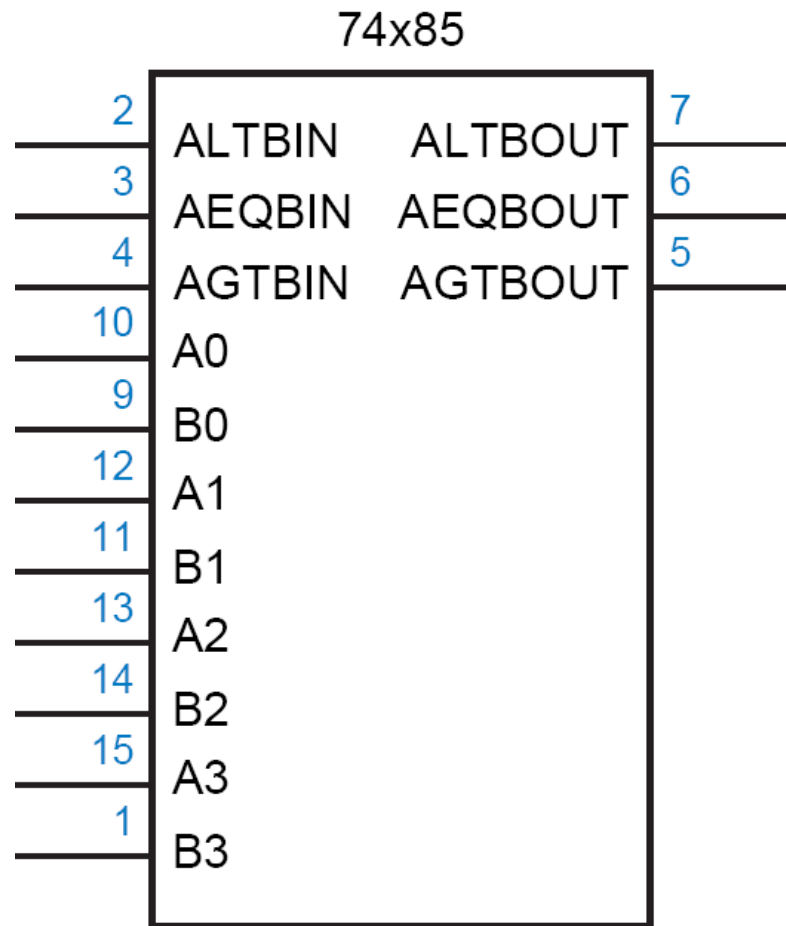
Magnitude Comparator



Find A_LT_B

$$\begin{aligned} A_LT_B = & A3' \cdot B3 \\ & + C3 \cdot A2' \cdot B2 \\ & + C3 \cdot C2 \cdot A1' \cdot B1 \\ & + C3 \cdot C2 \cdot C1 \cdot A0' \cdot B0 \end{aligned}$$

TTL 74x85

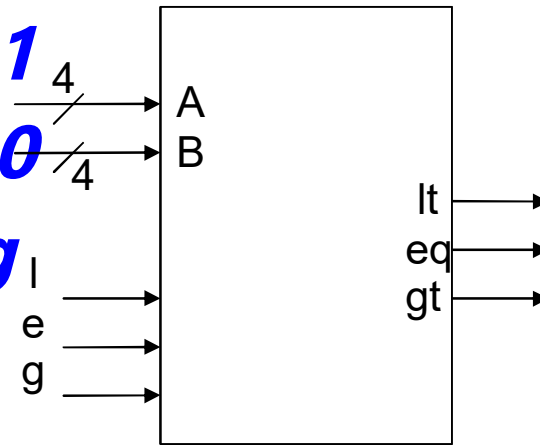


TTL 74x85

➤ *if ($A > B$)* $lt=0, eq=0, gt=1$

➤ *if ($A < B$)* $lt=1, eq=0, gt=0$

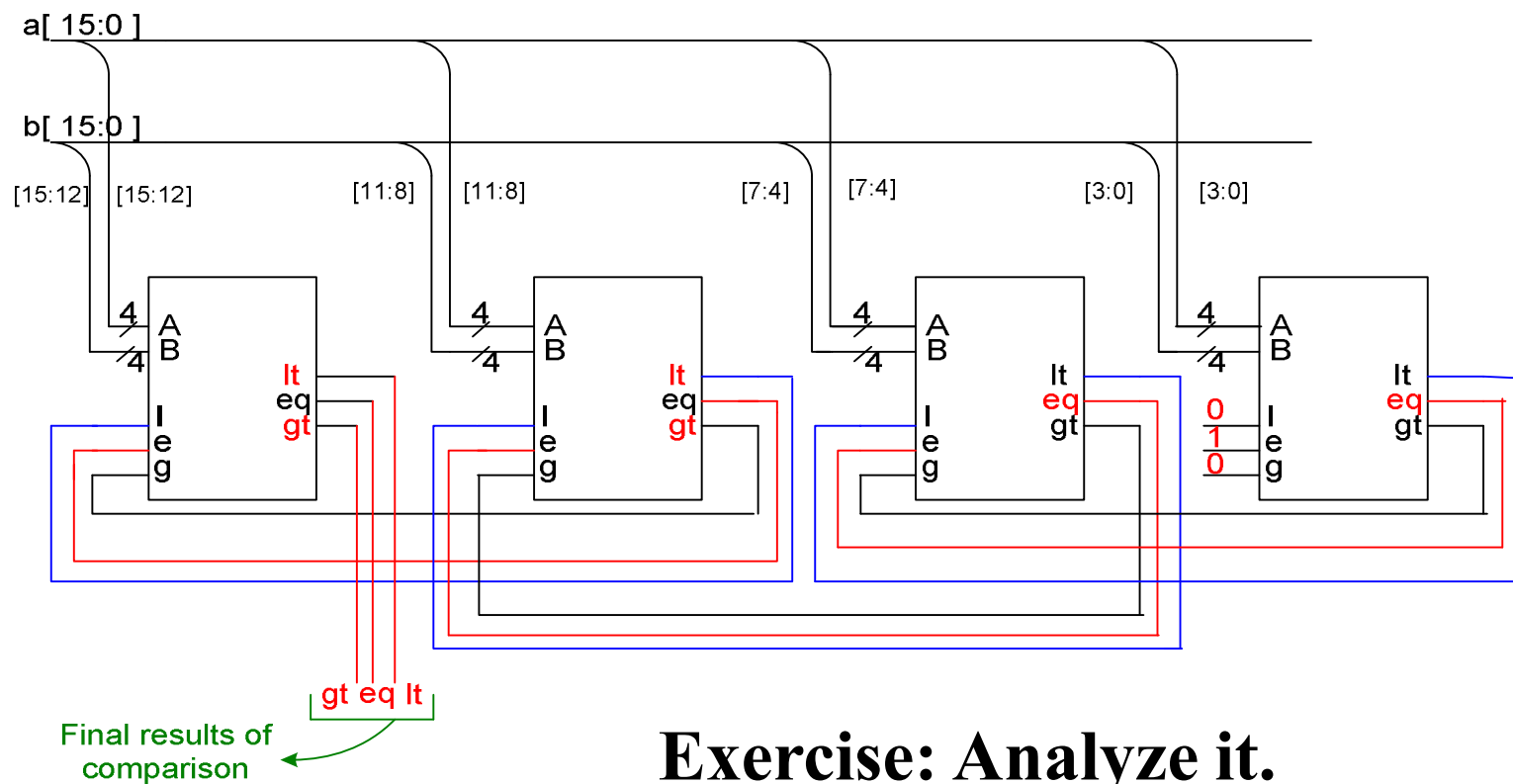
➤ *if ($A = B$)* $lt=l, eq=e, gt=g$



➤ The three l, e and g inputs are used when cascading.

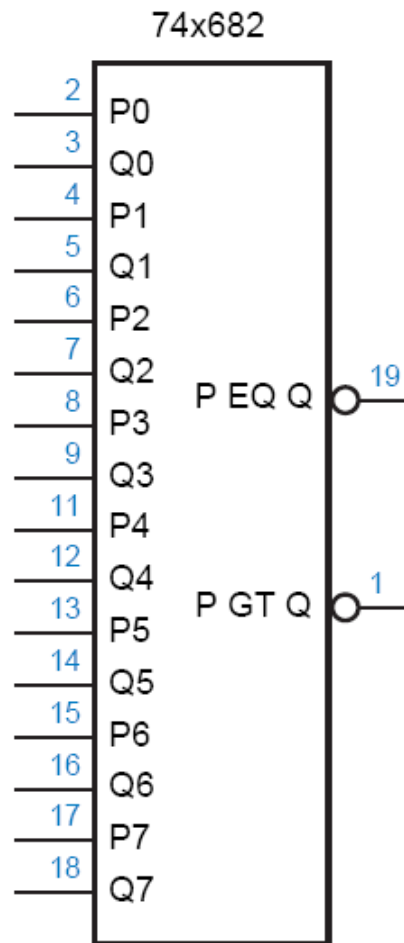
Comparator (continued...)

- Let us now cascade four of the 74x85 to construct a 16 bit comparator.

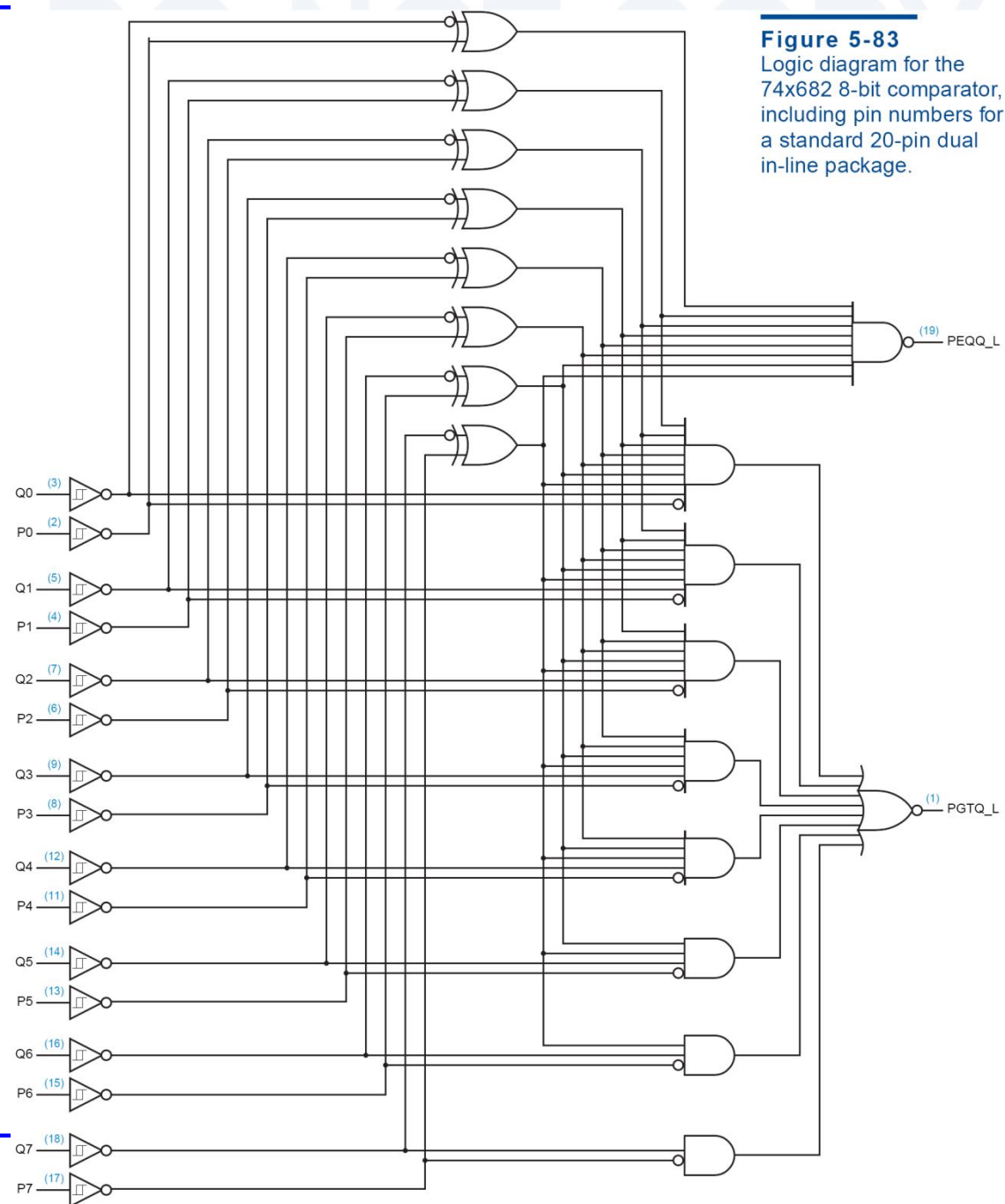


TTL 74x682

➤ 8-bit Comparator



- Arithmetic conditions derived from 74x682 outputs?
- And their circuits?



Maximum Finder

- Design a maximum finder

