1 Perceptron Theory

Perceptron is also known as a single neuron. It is used as a binary classifier, and is a type of supervised learning. After training on data, it is able to classify a given input to one of two classes.

It was introduced in 1943 by Warren McCulloch and Walter Pitts. They released a paper in 1958 with all the details of the perceptron https://psycnet.apa.org/doiLanding?doi=10.1037%2Fh0042519.

1.1 Requirements

There is limitation for using the perceptron:

- Binary classification only i.e only two classes in the dataset.
- Training data must be labeled.
- Data has to be linearly separable.

1.2 Definition

The perceptron can be defined as a function $f(\vec{x})$, that take a feature vector \vec{x} :

$$f(\vec{x}) = h(\vec{w} \cdot \vec{x} + b) \tag{1}$$

$$= h(w_1 \cdot x_1 + w_2 \cdot x_2 + b) \tag{2}$$

Where \vec{w} is the weight vector with the two weights for the perceptron and b is the bias of the network.

Note that we use a activation function called *Heaviside step function*. The output of the activation function is either 0 or 1.

1.3 Why do we need a bias?

The bias is important to improve the flexibility of the model. Without a bias, the model will always go through origin. When we introduce a bias, it allows the model to pass thought the x-axis at different points.

1.4 Training

- 1. Initialize weights.
- 2. Loop over each training instance until some criteria is met.
- 3. Calculate the output of the training instance, y.
- 4. Compare the target value, t to the output y.
- 5. If t = y, then continue. If not, we need to change all the weights.

- (a) If t = 0, y = 1, we need increase the weights: $w_i = w_i + \eta(t y)x_i$
- (b) If t=1,y=0, we need to decrease the weight: $w_i=w_i-\eta(y-t)x_i$

1.5 Perceptron Convergence Theorem

If the dataset is linearly separable, then the perceptron will eventually find a solution for the binary classification. Unless the training rate η is to high. It is important to note that there could be more than one solution.