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subject: TCS.

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Pg No: 1/6 of Q2. Sign: K. Kalani

A). we have following productions.

$S \rightarrow aB$ (Rule 1)

$S \rightarrow bA$ (Rule 2)

$A \rightarrow a$ (Rule 3)

$A \rightarrow aS$ (Rule 4)

$A \rightarrow bAA$ (Rule 5)

$B \rightarrow b$ (Rule 6)

$B \rightarrow bS$ (Rule 7)

$B \rightarrow aBB$ (Rule 8).

Let's generate leftmost derivation for string 'bbaaabbaba'

$S \rightarrow bA$ (Rule 2)

$S \rightarrow bbAA$ (Rule 5)

$S \rightarrow bbASA$ (Rule 4)

$S \rightarrow bbaaBA$ (Rule 1)

$S \rightarrow bbaaaBBA$ (Rule 8)

$S \rightarrow bbaaa bSBA$ (Rule 7)

$S \rightarrow bbaaa bbABA$ (Rule 2)

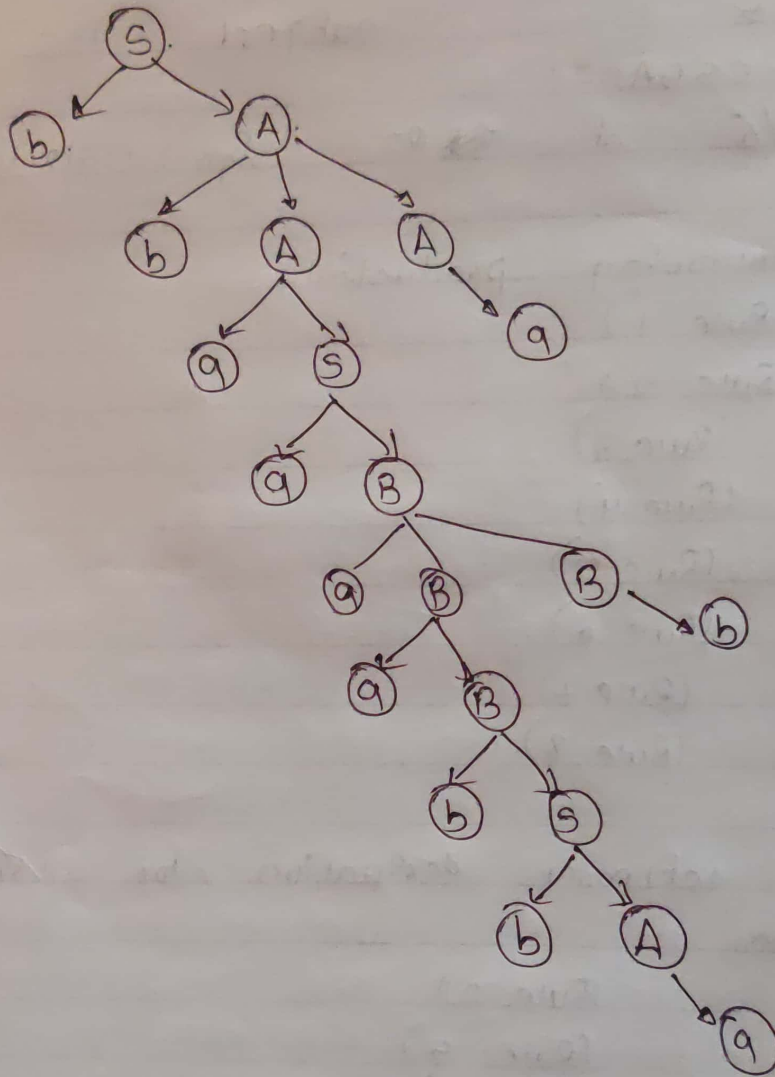
$S \rightarrow bbaaa bbaBA$ (Rule 3)

$S \rightarrow bbaaa bbabA$ (Rule 6)

$S \rightarrow bbaaa bba b a$ (Rule 3).

pg NO :- 2/6. of Q2.

Sign :- K.G. Kalanji



pg No. = 3/6 of Q2. Sign: K. G. Kalau

A). Lets generate rightmost derivation for string $bbaaaabbaba$.

$S \rightarrow bA$	(Rule 2)
$S \rightarrow bbAA$	(Rule 5)
$S \rightarrow bbAa$	(Rule 3)
$S \rightarrow bbAsa$	(Rule 4)
$S \rightarrow bbaaBa$	(Rule 1)
$S \rightarrow bbaaaB\bar{B}a$	(Rule 8)
$S \Rightarrow bbaaaBba$	(Rule 6)
$S \rightarrow bbaaabSba$	(Rule 7)
$S \Rightarrow bbaaabBaba$	(Rule 2)
$S \rightarrow bbaaabbaba$	(Rule 3)

B). The language becomes
 $L = \{abb, aabb, aaabb, aaaabb, \dots\}$

Logic:-

- i) Each 'a' is replaced by 'x' and head movement towards right till 'b'
- ii) Each 'b' is replaced by 'y' and head movement towards left till 'x'
- iii) Repeat above two steps till 'a's and 'b's are over.
- iv) For last 'b' make it blank.

Pg No :- 4/6 of Q2. Signt K.G. Karan.

B). Implementation -

let $M = \{Q, \Sigma, r, \delta, q_0, B, F\}$

where

$Q = [q_0, q_1, q_2, q_3, q_4, q_5]$

$\Sigma = [a, b]$

$r = [a, b, x, y, B]$

$q_0 = q_0$

$B = \text{Blank symbol}$

$F = [q_5]$

Working :-

q_0 :- Replace 'a' by 'x' and head moves towards right.

q_1 :- Search for 'b' and Replace it by 'y' and head moves towards left, Bypass all 'a's and 'y's

q_2 :- Bypass all 'a's and 'y's. Search for 'x' and replace it by 'x' only and head moves towards right whenever get 'a' at q_0 state repeat this cycle for all 'a' and 'b's.

q_3 :- On q_0 state if we get 'y' replace it by 'y' only and head moves towards right. Now move the head right to search for last 'b'. Bypass all 'y's

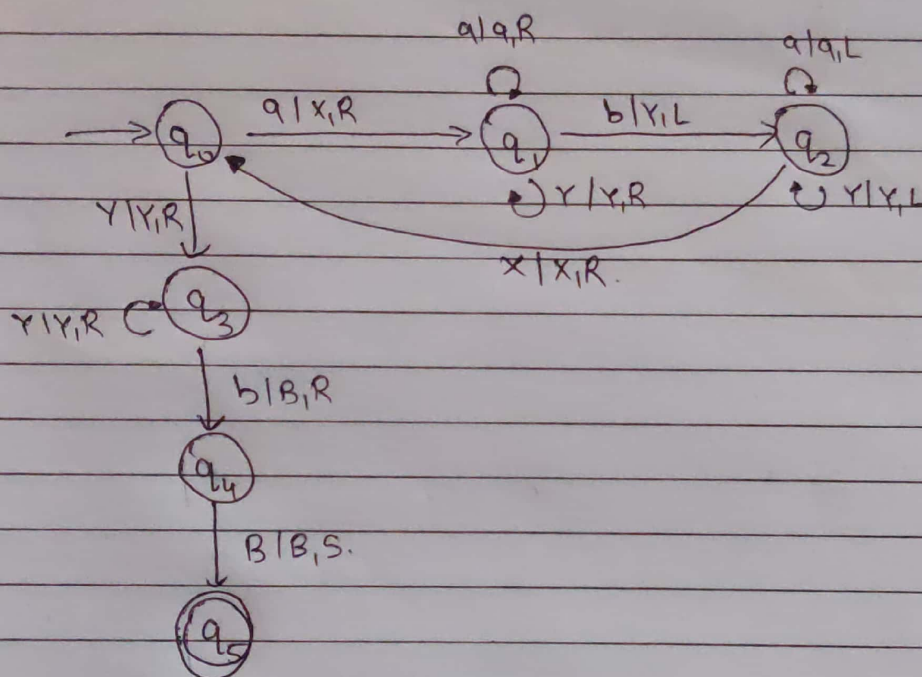
q_4 :- On q_0 state if we get 'y' replace it by 'y' only and head moves towards right. Now move the head right to search for last 'b'. Bypass all 'y's.

q_5 :- After all 'y's if we get 'b' this indicates one extra 'b' than 'a' is found.

pg No: 5/6 of Q2 sign + t. Giraburo

B). q_5 :- After the last 'b' if we get blank symbol means no more 'b's are remaining.

Transition diagram :-



Transition table :-

q \ Σ	a	b	x	y	B
$\rightarrow q_0$	(q_1, x, R)	-	-	(q_1, y, R)	-
q_1	(q_1, a, R)	(q_2, y, L)	-	(q_1, y, R)	-
q_2	(q_2, a, L)	-	(q_0, x, R)	(q_2, y, L)	-
q_3	-	(q_4, B, R)	-	(q_3, y, R)	-
q_4	-	-	-	-	(q_5, B, S)
q_5^*	-	-	-	-	-

pg No. 5/6. At Q2 sign :- K.G. Kalan

Instantaneous description:-

1 → $q_0 a b b B$	1 → $X q_0 Y b B$
1 → $X q_1 b b B$	1 → $X Y q_3 b B$
1 → $X q_2 Y b B$	1 → $X Y B q_4 B$
1 → $q_2 X Y b B$	1 → $X Y B q_5$ (Accept)