

# Control Systems

G V V Sharma\*

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**Abstract**—The objective of this manual is to introduce control system design at an elementary level.

Download python codes using

svn co <https://github.com/gadepall/school/trunk/control/ketan/codes>

## 1 POLAR PLOT

### 1.1 Introduction

### 1.2 Example

### 1.3 Example

### 1.4 Example

### 1.5 Example

### 1.6 Example

### 1.7 Example

## 2 BODE PLOT

### 2.1 Gain and Phase Margin

### 2.2 Example

### 2.3 Example

## 3 PID CONTROLLER

### 3.1 Introduction

## 4 NYQUIST PLOT

4.1. Using Nyquist criterion find the range of  $K$  for which closed loop system is stable.

$$G(s) = \frac{K}{s(s+6)}. \quad (4.1.1)$$

And,

$$H(s) = \frac{1}{s+9} \quad (4.1.2)$$

**Solution:** The system flow can be described as,

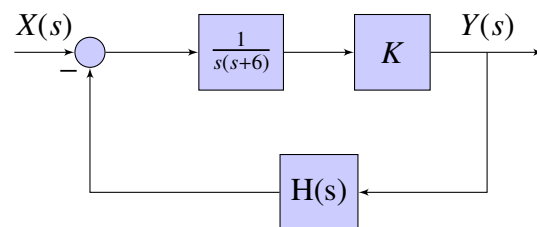


Fig. 4.1

$$G_1(s) = \frac{1}{s(s+6)}. \quad (4.1.3)$$

\*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All content in this manual is released under GNU GPL. Free and open source.

### Nyquist Stability Criterion:

$$N = Z - P \quad (4.1.4)$$

where  $Z$  is #unstable poles of closed loop transfer function,  $P$  is #unstable poles of and  $N$  is #clockwise encirclement of  $(-1/K, 0)$ .

For stable system,

$$Z = 0 \quad (4.1.5)$$

From 4.1.2 and 4.1.3,

$$P = 0 \quad (4.1.6)$$

$$\Rightarrow N = 0 \quad (4.1.7)$$

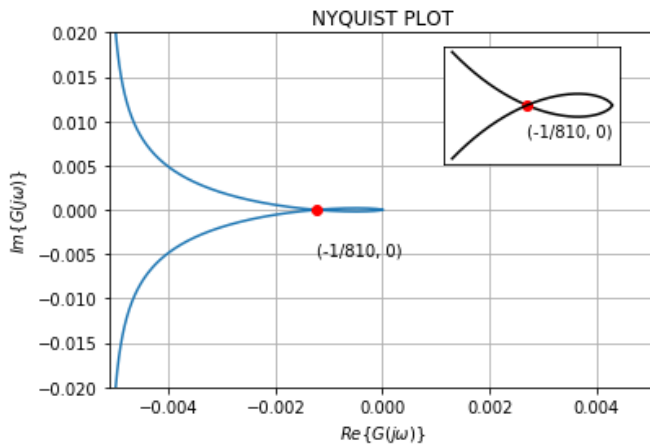


Fig. 4.1: Nyquist plot for  $G_1(s)H(s)$

Since, there is a zero at origin, an infinite radius half circle will enclose the right hand side of end points of the Nyquist plot.

$$\Rightarrow \frac{-1}{K} < \frac{-1}{810} \quad (4.1.8)$$

$$\Rightarrow K < 810 \quad (4.1.9)$$

And also,

$$K > 0 \quad (4.1.10)$$

$$\Rightarrow 0 < K < 810 \quad (4.1.11)$$

The following python code generates Fig. 4.1

codes/ee18btech11028\_1.py