TIPE : Propagation de rumeurs dans un réseau social Listing des programmes

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Table des matières

1	graph.ml	2
2	experiment.ml	4
3	$\operatorname{sortFirst.ml}$	6
4	$\operatorname{spread.ml}$	6
5	${\bf experiment Spreading.ml}$	7
6	${\bf experiment Spreading Random.ml}$	8
7	${\bf experiment Spreading Degree.ml}$	9
8	${\bf experiment Spreading Between.ml}$	10
9	${\bf experiment Spreading All.ml}$	11
10	${\bf draw Experiment Spreading Random Initial.py}$	11
11	${\bf draw Experiment Spreading Degree Initial.py}$	13
12	${\bf draw Experiment Spreading Between Initial.py}$	14
13	drawExperimentSpreadingAllInitial.py	16

1 graph.ml

```
open Core.Std;;
(* Builds a random graph with the Watts and Strogatz method.
Random.self_init ();;
let wattsStrogatzMatrix n k beta =
  let 1 = Array.make_matrix n n false in
  let rec wire i j = if i < 0 then wire (n+i) j
    else if i \ge n then wire (i-n) j
    else if j < 0 then wire i (n+j)
    else if j \ge n then wire i (j-n)
    else (1.(i).(j) \leftarrow true; 1.(j).(i) \leftarrow true)
  let rec unwire i j = if i < 0 then unwire (n+i) j
    else if i \ge n then unwire (i-n) j
    else if j < 0 then unwire i (n+j)
    else if j \ge n then unwire i (j-n)
    \texttt{else} \ (\texttt{l.(i).(j)} \ \texttt{\leftarrow} \ \texttt{false;l.(j).(i)} \ \texttt{\leftarrow} \ \texttt{false})
  let rec wired i j = if i < 0 then wired (n+i) j
    else if i >= n then wired (i-n) j
    else if j < 0 then wired i (n+j)</pre>
    else if j \ge n then wired i (j-n)
    else 1.(i).(j)
  in
  for i=0 to n-1 do
    for j = i-k/2 to i+k/2 do
      if j != i then wire i j
    done
  done;
  for i = 0 to n-1 do
    for j = i+1 to (i+k/2) do
      let r = Random.float 1.0 in
      if r < beta then begin
        unwire i j;
        let k = ref (Random.int n) in
        while (wired i \mid k) || (!k = i) do
           k := Random.int n
        done:
        wire i !k
      end
    done;
  done;
  1
; ;
```

```
(* Betweenness centrality of a graph via its adjacency matrix*)
let betweenness g =
  let n = Array.length g in
  let cB = Array.create n (0.0) in
  for s = 0 to n-1 do
    let stack = Stack.create() in
    let p = Array.create n ([]) in
    let sigma = Array.create n ( 0.0) in
    sigma.(s) < -1.0;
    let d = Array.create n ((-1)) in
    d.(s) <- 0;
    let q = Queue.create() in
    Queue.enqueue q s;
    while not (Queue.is_empty q) do
      let v = Queue.dequeue_exn q in
      Stack.push stack v;
      for w = 0 to (n-1) do
        let iw = g.(v).(w) in
        if iw then
          if d.(w) < 0 then begin
            Queue.enqueue q w;
            d.(w) \leftarrow d.(v) + 1;
          end:
          if d.(w) = (d.(v) + 1) then begin
            sigma.(w) <- sigma.(w) +. sigma.(v);
            p.(w) \leftarrow v::p.(w);
          end;
      done;
    done;
    let delta = Array.create n (0.0) in
    while not (Stack.is_empty stack) do
      let w = Stack.pop_exn stack in
      List.iter ~f:(fun v -> delta.(v) <-</pre>
        delta.(v) +. sigma.(v) /. sigma.(w) *. (1.0 +. delta.(w))) p.(w);
      if w \mathrel{!=} s then begin cB.(w) \mathrel{<-} cB.(w) +. delta.(w); end;
    done;
  done;
  сВ
; ;
let degree g i =
 let n = Array.length g in
 let r = ref 0 in
  for j = 0 to (n-1) do
     if g.(i).(j) then incr r
  done;
  !r
;;
```

```
let maxDegree g n = 
 let deg = degree g in
  let size = Array.length g in
 let rec loop i r = if i >= size then r else
   loop (i+1) ((deg i, i)::r)
  SortFirst.sortFirst n (loop 0 [])
;;
let maxBetweenness g n =
 let a = betweenness g in
  let size = Array.length g in
  let rec loop i r = if i >= size then r else
   loop (i+1) ((a.(i), i)::r)
  in
 SortFirst.sortFirst n (loop 0 [])
    experiment.ml
(* Structure de la table experiments:
CREATE TABLE "experiments"
("name" TEXT, "last_id" INT, "infos" TEXT DEFAULT (null))
*)
let silent = true;;
let print_return m r = if silent then () else
  Printf.printf ("%s %s") m (Sqlite3.Rc.to_string r)
;;
let load_db () =
  Sqlite3.db_open "experiments.sqlite"
; ;
let close_db db =
  Sqlite3.db_close db
let cleaner target row =
 let 1 = Array.length row in
 for i = 0 to l-1 do
   target := Some(row.(i))
  done;
;;
let get_exp_last_id db name =
```

```
let last_id = ref None in
  let get_last_id () =
   print_return "Recherche du dernier identifiant."
    (Sqlite3.exec_not_null_no_headers db ~cb:(cleaner last_id)
      ("SELECT last_id FROM experiments WHERE name=\""^name^"\";"))
  in
  get_last_id ();
  ! last_id
; ;
let get_experiment db name =
  let last_id = get_exp_last_id db name in
  let last_result = ref None in
  let create_table () =
   print_return ("Création de la table " ^ name)
    (Sqlite3.exec db ("CREATE TABLE "^name^" (id INT, value TEXT);"));
   print_return ("Enregistrement dans 'experiments' de la table "
    name) (Sqlite3.exec db
    ("INSERT INTO experiments VALUES (\""^name^"\", 0, \"\");"
   ))
  in
  let get_last_result id =
   print_return "Recherche du dernier résultat."
    (Sqlite3.exec_not_null_no_headers db ~cb:(cleaner last_result)
      ("SELECT value FROM "^name^" WHERE id=\""^id^"\";"))
  in
  let get_last_step () = match last_id with
  | None -> create_table (); !last_result
  | Some s -> get_last_result s; !last_result
  in
  get_last_step ()
;;
let add_step_id db exp id str =
  print_return (Printf.sprintf ("Ajout de l'étape %d à %s") id exp)
  (Sqlite3.exec db
    ("INSERT INTO "^exp
      ^" VALUES ("^(string_of_int id)^",\""^str^"\");"))
;;
let change last id db exp id =
  print_return (Printf.sprintf
    ("Mise à jour du dernier identifiant (%d) de %s") id exp)
  (Sqlite3.exec db
    ("UPDATE experiments SET last_id = "
      ^(string_of_int id)^" WHERE name=\""^exp^"\";"))
let add_step db exp str = let id =
  match get_exp_last_id db exp with
```

```
| None -> 0
  | Some(s) -> (1 + (int_of_string s))
  add_step_id db exp id str;
  change_last_id db exp id;
3
    sortFirst.ml
open Core.Std;;
let sortFirst n l =
  let rec sep p l left right len_l = match l with
  | [] -> left, right, len_l
  | (a,b)::tl when a > p \rightarrow sep p tl ((a,b)::left) right (len_l + 1)
  | (a,b)::tl -> sep p tl left ((a,b)::right) len_l
  in
  let rec loop n l = match l with
  | [] -> []
  | (a,b)::tl ->
    let left, right, len_l = sep a tl [] [] 0 in
    if len_l >= n then (loop n left)
    (loop n left)@[(a,b)]@(loop (n-len_l-1) right)
 List.map (loop n 1) \sim f:(fun (a,b) \rightarrow b)
; ;
   spread.ml
open Core.Std;;
  Spread the rumor and return the amount of nodes aware of it.
*)
let step_p graph a b s =
 let n = Array.length graph in
  let p_{lim} = b /. (a +. b) in
  let nb = ref 0 in
  for i = 0 to n-1 do
    if not s.(i) then begin
      let aware = ref 0 in
      let d = ref 0 in
      for j = 0 to n-1 do
        \quad \text{if $\tt graph.(i).(j)$ then(} \\
          incr d;
          if s.(j) then incr aware;
```

```
done;
  done;
  let p = (float_of_int !aware) /. (float_of_int !d) in
  if p > p_lim then (s.(i) <- true; incr nb)
  end
  else incr nb
  done;
!nb
;;</pre>
```

5 experimentSpreading.ml

```
open Core.Std;;
open Yojson.Basic.Util;;
type exp_stat = {
  graph_no:int;
  prop_spread:float array;
};;
let json_of_exp_stat e =
  `Assoc [
  ("graph_no", `Int e.graph_no);
  ("prop_spread",
    `List (List.map (Array.to_list e.prop_spread)
      \  \  \, \text{`f:}(\texttt{fun}\ x\ -\text{``Float}\ x)))
];;
let exp_stat_of_json json =
  {
    graph_no = json |> member "graph_no" |> to_int;
    prop_spread = json |> member "prop_spread" |> to_list
    |> List.map ~f:(fun x -> x |> to_float) |> Array.of_list
;;
let escape_double_quotes s =
  let exp = Str.regexp "\"" in
  Str.global_replace exp "\"\"" s
let save_step db e exp_name=
  json_of_exp_stat e
  |> Yojson.Basic.to_string
  |> escape_double_quotes
```

```
|> Experiment.add_step_id db exp_name e.graph_no;
  Experiment.change_last_id db exp_name e.graph_no
;;
let process ?(max=99) db graph_size nb_gen
k beta max_spread_step a b choose_spread name=
  let step i init=
   let g = Graph.wattsStrogatzMatrix graph_size k beta in
   let prop_spread = Array.create max_spread_step 0.0 in
   let spread = choose_spread g init in
   let j = ref 0 in
   let p = ref(-1.0) in
   while !j \le (max\_spread\_step-1) \&\& prop\_spread.(!j) != !p do
      prop_spread.(!j) <-</pre>
      (float_of_int (Spread.step_p g a b spread))
        /. (float_of_int graph_size);
      if !j > 0 then (p := prop\_spread.(!j-1));
      incr j;
   done;
    {graph_no=i; prop_spread=prop_spread}
  in
  let experiment init db=
   let exp_name = Printf.sprintf
      ("r_spreading_%s_%d_%d_%d_%d_%d_%d_%d")
      name graph_size (int_of_float (beta*.100.0))
      k nb_gen init max_spread_step (int_of_float a)
        (int_of_float b) in
    print_endline ("Nom de l'expérience : "^exp_name);
   let cur_step = ref (match Experiment.get_experiment db exp_name
   with
    | None -> {graph_no= (-1);prop_spread=[||]}
    | Some(s) -> s |> Yojson.Basic.from_string |> exp_stat_of_json
   ) in
   let beg = !cur_step.graph_no + 1 in
   for i = beg to nb_gen - 1 do
      cur_step := step i ((float_of_int init)/.100.0);
      save_step db !cur_step exp_name
   done;
  in
  for i = 1 to max do
   experiment i db;
  done
; ;
```

6 experimentSpreadingRandom.ml

```
open Core.Std;;
```

```
let graph_size = 500;;
let nb_gen = 100;;
let max_spread_step = 500;;
let choose_spread _ init =
  let s = Array.create graph_size false in
  let k = ref 0 in
 let n = int_of_float ((float_of_int graph_size) *. init) in
  while !k <= n do
   let i = Random.int graph_size in
   if not s.(i) then (incr k; s.(i) \leftarrow true)
  done;
;;
let () =
 print_endline "Initialisation de Random.";
 Random.self_init ();
  print_endline "Ouverture de la base de données.";
  let db = Experiment.load_db () in
  for b = 0 to 4 do
   ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 1.0 1.0
      choose_spread "random";
    ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 3.0 1.0
      choose_spread "random";
   ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 1.0 3.0
      choose_spread "random";
  done;
  print_endline "Fermeture de la base de données.";
  if (Experiment.close_db db) then
   print_endline "Fermeture réussie."
  else
   print_endline "Echec de la fermeture."
```

7 experimentSpreadingDegree.ml

```
open Core.Std;;
let graph_size = 500;;
let nb_gen = 100;;
let max_spread_step = 500;;
let choose_spread g init =
```

```
let s = Array.create graph_size false in
  let n = int_of_float ((float_of_int graph_size) *. init) in
  let rec loop 1 = match 1 with
  | [] -> ()
  | hd::tl -> s.(hd) <- true; loop tl
  loop (Graph.maxDegree g n); s
let () =
  print_endline "Initialisation de Random.";
  Random.self_init ();
  print_endline "Ouverture de la base de données.";
  let db = Experiment.load_db () in
  for b = 0 to 4 do
   ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 1.0 1.0 choose_spread "degree";
   ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 3.0 1.0 choose_spread "degree";
   ExperimentSpreading.process db graph_size nb_gen 50
      ((float_of_int b) *. 0.25) max_spread_step 1.0 3.0 choose_spread "degree";
  done;
  print_endline "Fermeture de la base de données.";
  if (Experiment.close_db db) then
   print_endline "Fermeture réussie."
  else
   print_endline "Echec de la fermeture."
```

8 experimentSpreadingBetween.ml

```
open Core.Std;;
let graph_size = 500;;
let nb_gen = 100;;
let max_spread_step = 500;;

let choose_spread g init =
    let s = Array.create graph_size false in
    let n = int_of_float ((float_of_int graph_size) *. init) in
    let rec loop l = match l with
    | [] -> ()
    | hd::tl -> s.(hd) <- true; loop tl
    in
    loop (Graph.maxBetweenness g n); s

;;

let () =
    print_endline "Initialisation de Random.";</pre>
```

```
Random.self_init ();
print_endline "Ouverture de la base de données.";
let db = Experiment.load db () in
for b = 0 to 4 do
 ExperimentSpreading.process db graph_size nb_gen 50
    ((float_of_int b) *. 0.25) max_spread_step 1.0 1.0 choose_spread "between";
  ExperimentSpreading.process db graph_size nb_gen 50
    ((float_of_int b) *. 0.25) max_spread_step 3.0 1.0 choose_spread "between";
 ExperimentSpreading.process db graph_size nb_gen 50
    ((float_of_int b) *. 0.25) max_spread_step 1.0 3.0 choose_spread "between";
done;
print_endline "Fermeture de la base de données.";
if (Experiment.close_db db) then
  print_endline "Fermeture réussie."
else
  print_endline "Echec de la fermeture."
```

experimentSpreadingAll.ml

```
let graph_size = 500;;
let nb_gen = 50;;
let max_spread_step = 500;;
let b = 0.5;;
let () =
  print_endline "Initialisation de Random.";
  Random.self init ();
  print_endline "Ouverture de la base de données.";
  let db = Experiment.load_db () in
  ExperimentSpreading.process ~max:50 db graph_size nb_gen 50
   b max_spread_step 2.0 1.0 ExperimentSpreadingRandom.choose_spread "random";
  ExperimentSpreading.process ~max:50 db graph_size nb_gen 50
   b max_spread_step 2.0 1.0 ExperimentSpreadingDegree.choose_spread "degree";
  ExperimentSpreading.process ~max:50 db graph_size nb_gen 50
   b max_spread_step 2.0 1.0 ExperimentSpreadingBetween.choose_spread "between";
  print_endline "Fermeture de la base de données.";
  if (Experiment.close_db db) then
   print_endline "Fermeture réussie."
  else
   print_endline "Echec de la fermeture."
```

drawExperimentSpreadingRandomInitial.py 10

```
import matplotlib.pyplot as pl
from matplotlib2tikz import save as tikz_save
import numpy as np
import sqlite3
```

```
import json
graph_size = 500
nb_gen = 100
k = 50
max\_spread\_step = 500
conn = sqlite3.connect('experiments.sqlite')
for a,b in [(1,1), (1,3), (3,1)]:
  for beta in [0,25,50,75,100]:
    X = np.arange(1,100)
    pl.close('all')
    fig = pl.figure()
    ax = fig.add_subplot(111)
    ax.set_title('Taille du graphe={} Taille de l\'échantillon={}'
      +' K=\{\}, q=\{\}, Beta =\{\}\\''
      .format(graph_size,nb_gen,k,b/(a+b),beta))
    ax.set_ylabel("Proportion finale")
    ax.set_xlabel("Proportion initiale (\\%)")
    Y = np.zeros(100)
    Y_high = np.zeros(100)
    Y_low = np.zeros(100)
    x_50 = 0
    for x in X:
      cursor = conn.execute(
        "SELECT value FROM r_spreading_random_"+
        \label{lem:condition} $$ "\{graph_size\}_{k}_{nb_gen}_{x}_{max\_spread\_step}_{a}_{b}" $$
        .format(**locals()))
      rows = cursor.fetchall()
      v = 0
      n = len(rows)
      for row in rows:
        v += json.loads(row[0])['prop_spread'][-1]
      Y[x] = v/n
      if abs(0.5-Y[x]) < abs(Y[x_50]-0.5):
        x 50 = x
      v = 0
      for row in rows:
        v += (Y[x] - json.loads(row[0])['prop_spread'][-1])**2
      v = (v/n)**(1/2)
      Y_high[x] = Y[x] + v
      Y_low[x] = Y[x] - v
    pl.grid()
```

11 drawExperimentSpreadingDegreeInitial.py

```
import matplotlib.pyplot as pl
from matplotlib2tikz import save as tikz_save
import numpy as np
import sqlite3
import json
graph_size = 500
nb_gen = 100
k = 50
max\_spread\_step = 500
conn = sqlite3.connect('experiments.sqlite')
for a,b in [(1,1), (1,3), (3,1)]:
    for beta in [0,25,50,75,100]:
        X = np.arange(1,100)
        pl.close('all')
        fig = pl.figure()
        ax = fig.add_subplot(111)
        ax.set_title('Taille du graphe={} Nb gen={} K={}, q={}, Beta ={}\\%'
             .format(graph_size,nb_gen,k,b/(a+b),beta))
        ax.set_ylabel("Proportion finale")
        ax.set_xlabel("Proportion initiale (\\%)")
        Y = np.zeros(100)
        Y \text{ high} = np.zeros(100)
        Y_{low} = np.zeros(100)
```

x 50 = 0

```
for x in X:
           cursor = conn.execute(
               "SELECT value FROM r_spreading_degree_"+
                \label{lem:condition} $$ "\{graph_size\}_{k}_{nb_gen}_{x}_{max\_spread\_step}_{a}_{b}" $$
                .format(**locals()))
           rows = cursor.fetchall()
           v = 0
           n = len(rows)
           for row in rows:
               v += json.loads(row[0])['prop_spread'][-1]
           Y[x] = v/n
            if abs(0.5-Y[x]) < abs(Y[x_50]-0.5):
               x_50 = x
           v = 0
           for row in rows:
               v += (Y[x] - json.loads(row[0])['prop_spread'][-1])**2
           v = (v/n)**(1/2)
           Y_high[x] = Y[x] + v
           Y_low[x] = Y[x] - v
       pl.plot(X,Y[1:], 'b', label="Propagation finale", lw=2.5)
       pl.plot(X,X/100, 'g--', label="Identité", lw=2.5)
       pl.plot(X, Y_high[1:], 'r--', label="Écart-type", lw=2.5)
       pl.plot(X, Y_low[1:], 'r--')
       pl.axvline(x_50, c='orange', lw=2.5)
       pl.axhline(0.5, xmin=0, xmax=100, c='orange', lw=2.5)
       bbox=dict(facecolor='orange', alpha=0.95),
           size="large",
           color="white",
           fontweight="bold")
       pl.legend(loc="lower right")
       pl.grid()
       tikz_save("resultats/degree_finale_f_initiale_q{}_Beta{}_ec.tex"
            format(int(b/(a+b)*100), beta))
conn.close()
```

12 drawExperimentSpreadingBetweenInitial.py

```
import matplotlib.pyplot as pl
from matplotlib2tikz import save as tikz_save
```

```
import numpy as np
import sqlite3
import json
graph_size = 500
nb_gen = 100
k = 50
max\_spread\_step = 500
conn = sqlite3.connect('experiments.sqlite')
for a,b in [(1,1), (1,3), (3,1)]:
    for beta in [0,25,50,75,100]:
        X = np.arange(1,100)
        pl.close('all')
        fig = pl.figure()
        ax = fig.add_subplot(111)
        ax.set\_title('Taille du graphe={} Nb gen={} K={}, q={}, Beta ={}\\%'
            .format(graph_size,nb_gen,k,b/(a+b),beta))
        ax.set_ylabel("Proportion finale")
        ax.set_xlabel("Proportion initiale (\\%)")
        Y = np.zeros(100)
        Y_high = np.zeros(100)
        Y_{low} = np.zeros(100)
        x_50 = 0
        for x in X:
            cursor = conn.execute(
                "SELECT value FROM r_spreading_between_"+
                "{graph_size}_{beta}_{k}_{nb_gen}_{x}_{max_spread_step}_{a}_{b}"
                 .format(**locals()))
            rows = cursor.fetchall()
            \Delta = 0
            n = len(rows)
            for row in rows:
                v += json.loads(row[0])['prop_spread'][-1]
            Y[x] = v/n
            if abs(0.5-Y[x]) < abs(Y[x_50]-0.5):
                x_50 = x
            v = 0
            for row in rows:
                v \leftarrow (Y[x] - json.loads(row[0])['prop_spread'][-1])**2
            v = (v/n)**(1/2)
            Y_high[x] = Y[x] + v
            Y_low[x] = Y[x] - v
```

```
pl.grid()
      pl.plot(X,Y[1:], 'b', label="Propagation finale", lw=2.5)
      {\tt pl.plot(X,X/100, 'g--', label="Identit\'e", lw=2.5)}
      pl.plot(X, Y_high[1:], 'r--', label="Écart-type", lw=2.5)
      pl.plot(X, Y_low[1:], 'r--', lw=2.5)
      pl.axvline(x_50, c='orange', lw=2.5)
      pl.axhline(0.5, xmin=0, xmax=100, c='orange', lw=2.5)
      bbox=dict(facecolor='orange', alpha=0.95),
          size="large",
          color="white",
          fontweight="bold")
      pl.legend(loc="lower right")
      .format(int(b/(a+b)*100), beta))
      pl.plot()
      pl.show()
conn.close()
```

13 drawExperimentSpreadingAllInitial.py

```
import matplotlib.pyplot as pl
from matplotlib2tikz import save as tikz_save
import numpy as np
import sqlite3
import json
graph_size = 500
nb_gen = 100
k = 50
max_spread_step = 500
conn = sqlite3.connect('experiments.sqlite')
size = 100
1 = [(1,1), (1,3), (3,1)]
\# size = 50
# l = [(2,1)]
X = np.arange(1,size)
n = 4
Y = [np.zeros(size) for _ in range(n)]
Y_high = [np.zeros(size) for _ in range(n)]
Y_low = [np.zeros(size) for _ in range(n)]
corres = [
    (50, "degree", "Degré", "red"),
```

1

```
(50, "random", "Aléatoire", "green"),
    (25, "between", "Centralité \frac{1}{4}", "m"),
    (75, "between", "Centralité $\\beta=\\frac{3}{4}$", "b"),
def affiche(a, b):
   pl.close('all')
   fig = pl.figure()
   ax = fig.add_subplot(111)
    ax.set_title('Taille du graphe:{} Échantillon:{} K={}, q=$\\frac'
        .format(graph_size,nb_gen,k)+'\{'+str(b)+'\}\{'+str(a+b)+'\}\}')
   ax.set_ylabel("Proportion finale")
   ax.set_xlabel("Proportion initiale")
   pl.grid()
   pl.plot(X/100,X/100, '--', color="gray", label="Identité", lw=2.5)
   for i,(beta, name, label, color) in enumerate(corres):
        for x in X:
            cursor = conn.execute(
                "SELECT value FROM r_spreading_{}_".format(name)+
                .format(graph_size, beta, k, nb_gen, x, max_spread_step, a, b))
           rows = cursor.fetchall()
           \Delta = 0
           n = len(rows)
            for row in rows:
               v += json.loads(row[0])['prop_spread'][-1]
           Y[i][x] = v/n
           v = 0
           for row in rows:
               v += (Y[i][x] - json.loads(row[0])['prop_spread'][-1])**2
            v = (v/n)**(1/2)
           Y_high[i][x] = Y[i][x] + v
           Y_low[i][x] = Y[i][x] - v
        pl.plot(X/100,Y[i][1:], label="{}".format(label), lw=2.5, color=color)
    # for i in range(3):
        # pl.plot(X, Y_high[i][1:], 'r--', lw=2)
        # pl.plot(X, Y_low[i][1:], 'r--', lw=2)
    # pl.axhline(0.5, xmin=0, xmax=100, c='orange', lw=2.5)
   pl.legend(loc="lower right")
   tikz_save("resultats/all_finale_f_initiale_q{}.tex"
        .format(int(b/(a+b)*100), beta),
        figurewidth="\\textwidth",
       figureheight=".33\\textheight")
    # pl.show()
for a,b in 1:
   affiche(a,b)
```

conn.close()