Exercise-set 10. Solutions

- 1. The cut with $X = \{S, C, D, F\}$ has capacity 15.
- 2. No. Either find the max flow (of value 20), or notice that the capacity of a cut cannot be 19 (all the capacities are divisible by 3 except for 5), and use the Ford-Fulkerson theorem.
- 3. a) max m(f) = 8, min cut: $X = \{S, A, F\}$, b) max m(f) = 7, min cut: $X = \{S, B, C\}$,
 - c) max m(f) = 20, min cut: $X = \{S, A, B, C\}$,
 - d) max m(f) = 30, min cut: $X = \{S, B, C, E\}$,
 - e) max m(f) = 17, min cut: $X = \{S, B, C, D, E\}$,
 - f) max m(f) = 24, min cut: $X = \{S, A, D, G\}$,
 - g) max m(f) = 21, min cut: $X = \{S, D, F\}$,
 - h) max m(f) = 14, min cut: $X = \{S, A, B, F, I\}$,
 - i) max m(f) = 24, min cut: $X = \{S, B, D, E, F\}$.
- 4. The capacity of the cut is 19, max m(f) = 18, min cut: $X = \{S, A, B, G, H\}$.
- 5. a) max m(f) = 21, min cut: $X = \{S, A, F, G\}$,
 - b) max m(f) = 17, min cut: $X = \{S, B, D, F, G\}$,
 - c) max m(f) = 24, min cut: $X = \{S, A, C, F, G\}$.
- 6. max m(f) = 20, min cut: $X = \{S, D, E\}$.
- 7. max m(f) = 22, min cut: $X = \{S, D, E\}$.
- 8. max m(f) = 43, min cut $X = \{s, a, b, c, d\}$.