Exercise-set 1. Solutions

- 1. (a) yes, yes,
 - (b) no, no,
 - (c) no, yes,
 - (d) no, yes.
- 2. 8 (the smallest possible and also realizable degree-sequence is 0,1,2,3,4,6).
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- 4. Directed complete graph.
- 5. Only 18.
- 6. 6, 10, 15 or 30.
- 7. There are n-1 odd degrees $\implies n-1$ is even, n is odd \implies one even degree in \overline{G} .
- 8. The number of edges between the vertices of degree ≤ 7 and the vertices of degree ≥ 16 is both ≤ 70 and $\geq 70 \implies |E(G)| = 115$.
- 9. No: the number of edges between the vertices of degree 4 and 10 and the vertices of degree 16 is both ≤ 66 and ≥ 72 , a contradiction.
- 10. There are 11 of them.
- 11. There are 2 of them.
- 12. a) There are 4 such graphs,
 - b) there are 4 such graphs,
 - c) there are 2 such graphs.
- 13. a) Yes, yes, no (should have 15/2 edges).
 - b) No (should have 11 vertices and 55/2 edges).
- 14. a) no, b) yes.
- 15. a) and b) are isomorphic, and c) is not isomorphic to them.
- 16. a) and b) are isomorphic to it, c) is not.
- 17. No. The underlying graph is a cycle, and the knights cannot change their order on it.