

UML State Machines

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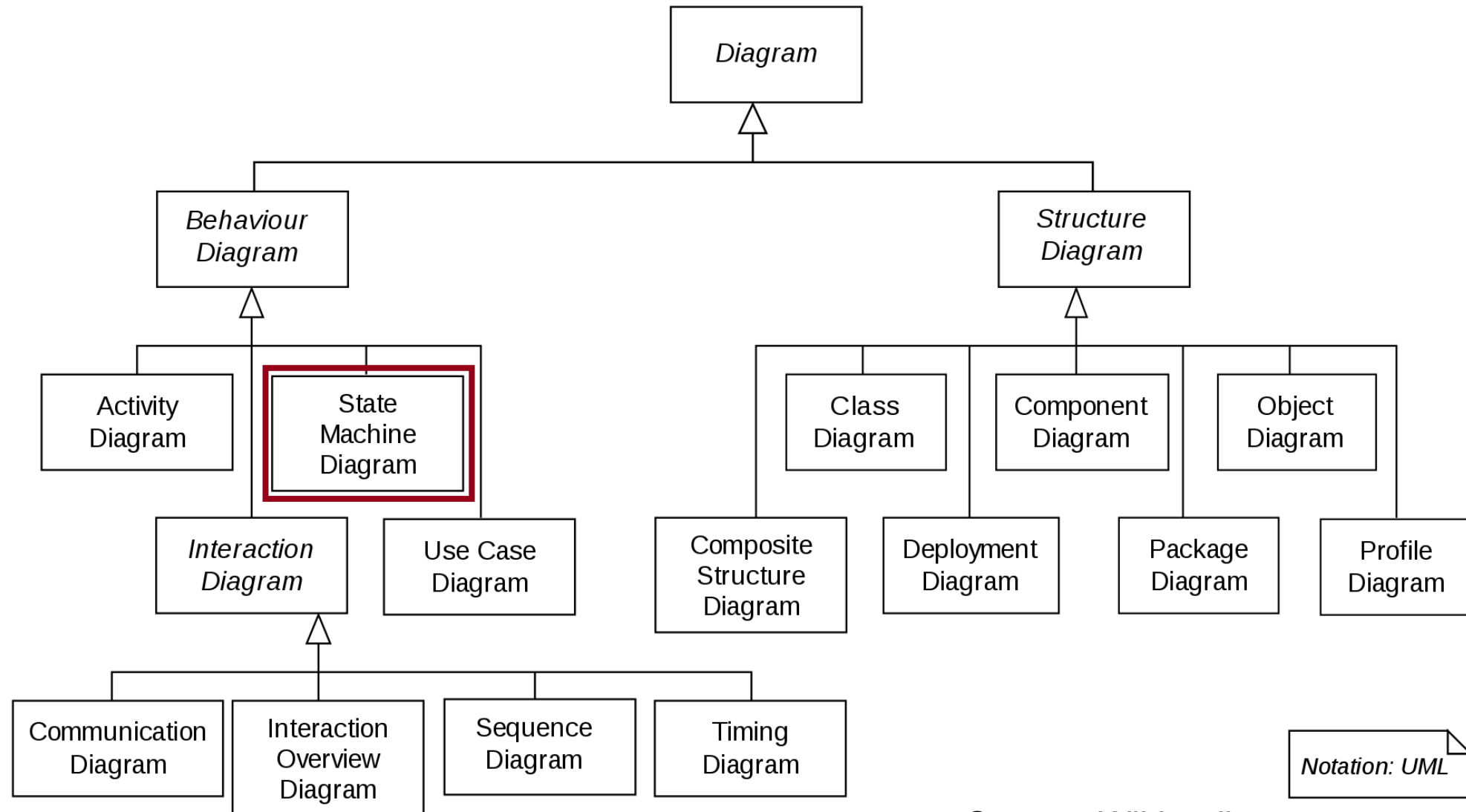


Méréstechnika és
Információs Rendszerek
Tanszék



**Critical Systems
Research Group**

UML Diagram Types



Source: Wikipedia

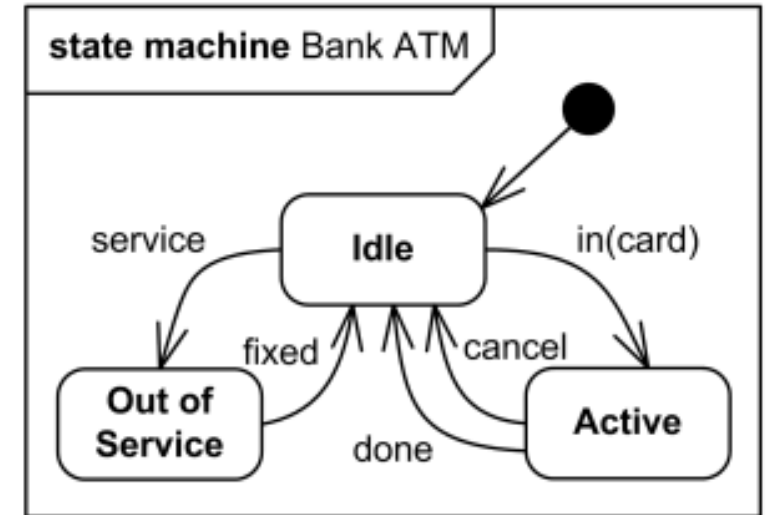
State Based Modelling

- **State**

- Distinguishable from each other
- Different behaviour in different states
- Always exactly one active state at a time

- **Reactive systems**

- Event-driven: reacting to external events
- Reaction depends on the event itself and on the history of the system
- {Waiting for events – Processing an event} loop



Background of State Machines

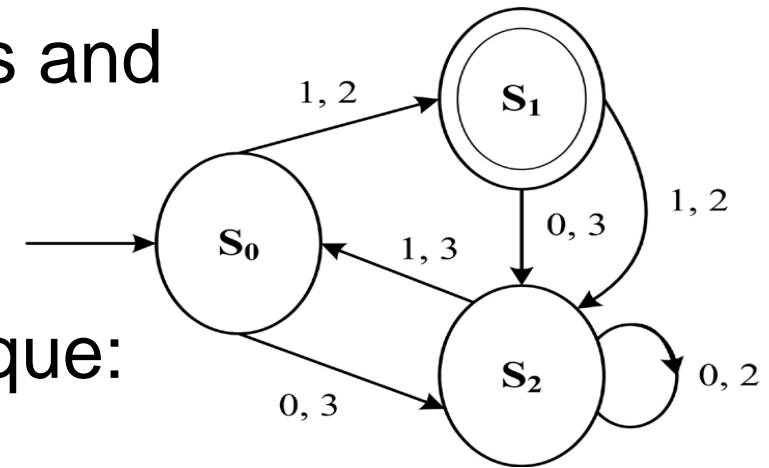
„**Finite State Machine (FSM)**: mathematical abstraction composed of a finite number of states and transitions between those states.”

- Long-standing, multipurpose description technique:

- Hardware elements (→ Digital Technique)
- Operation of programs (→ Programming 1,2,3)
- Protocols (→ Communication Networks)
- Grammars (→ Languages and Automata, MSc)
- Formal verification (→ Formal Methods, MSc)

- **In common:** states and transitions

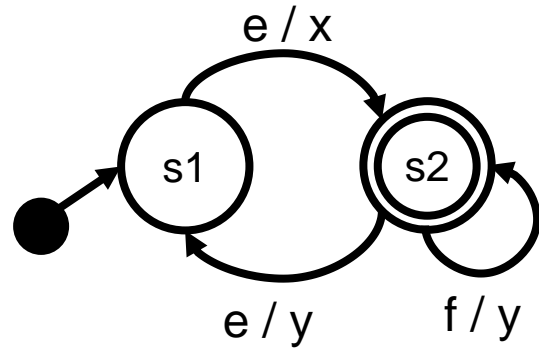
$$M = (S, I, O, f, g, s_0)$$



| Current State | Output | | State | |
|----------------|--------|---|----------------|----------------|
| | Input | | Input | |
| | 0 | 1 | 0 | 1 |
| S ₀ | 3 | 2 | S ₂ | S ₁ |
| S ₁ | 3 | 2 | S ₂ | S ₂ |
| S ₂ | 2 | 3 | S ₂ | S ₀ |

Source: SWEBOK

Behaviour Defined by the State Machine



- **Behaviour** := set of possible **traces**

– trace: series of (input, output) steps

- Example: traces of the state machine on the left

– (e, x)
– (e, x), (f, y)
– (e, x), (f, y), (f, y)
– (e, x), (e, y), (e, x)
– ...

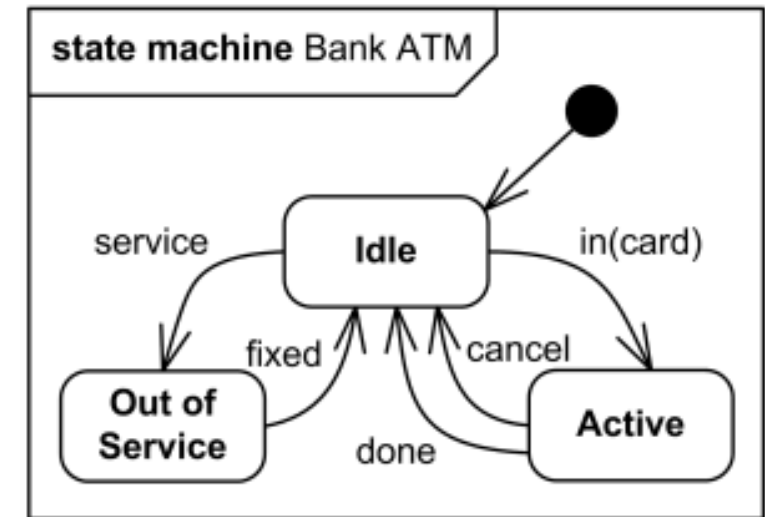
- Set of states:
 - s1, s2
- Set of events:
 - e, f
- Set of output actions:
 - x, y

What happens if in state s1 an event f occurs?

How They Can Be Used in Software Systems?

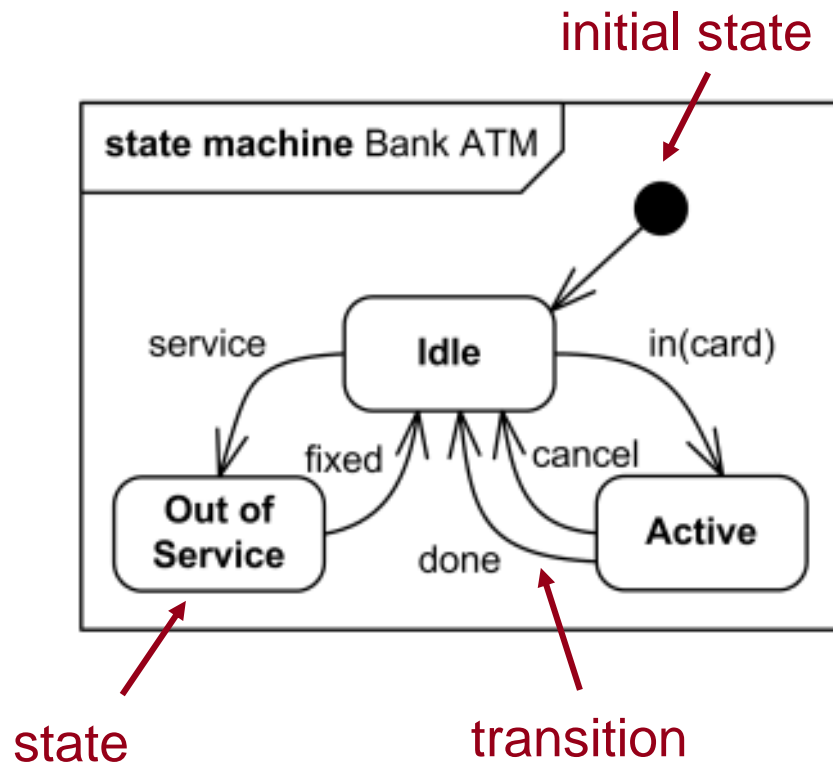
- **High-level** descriptions of behaviours
 - Description of the whole system or its main components
 - From outside visible behaviour (protocol)
 - Often abstract events and actions
- **Low-level** descriptions of behaviours
 - Specification of a complex class
 - Describing the main behaviour (classifierBehavior)
 - Events: Reception of a *Signal*, invocation of an *Operation*

Elements



State, Transition

State and Transition



- **State**

- (Implicit) invariant holds in it

- **Pseudo state**

- Transient states (see later)

- E.g. initial state

- **Transition**

- Between source and target nodes

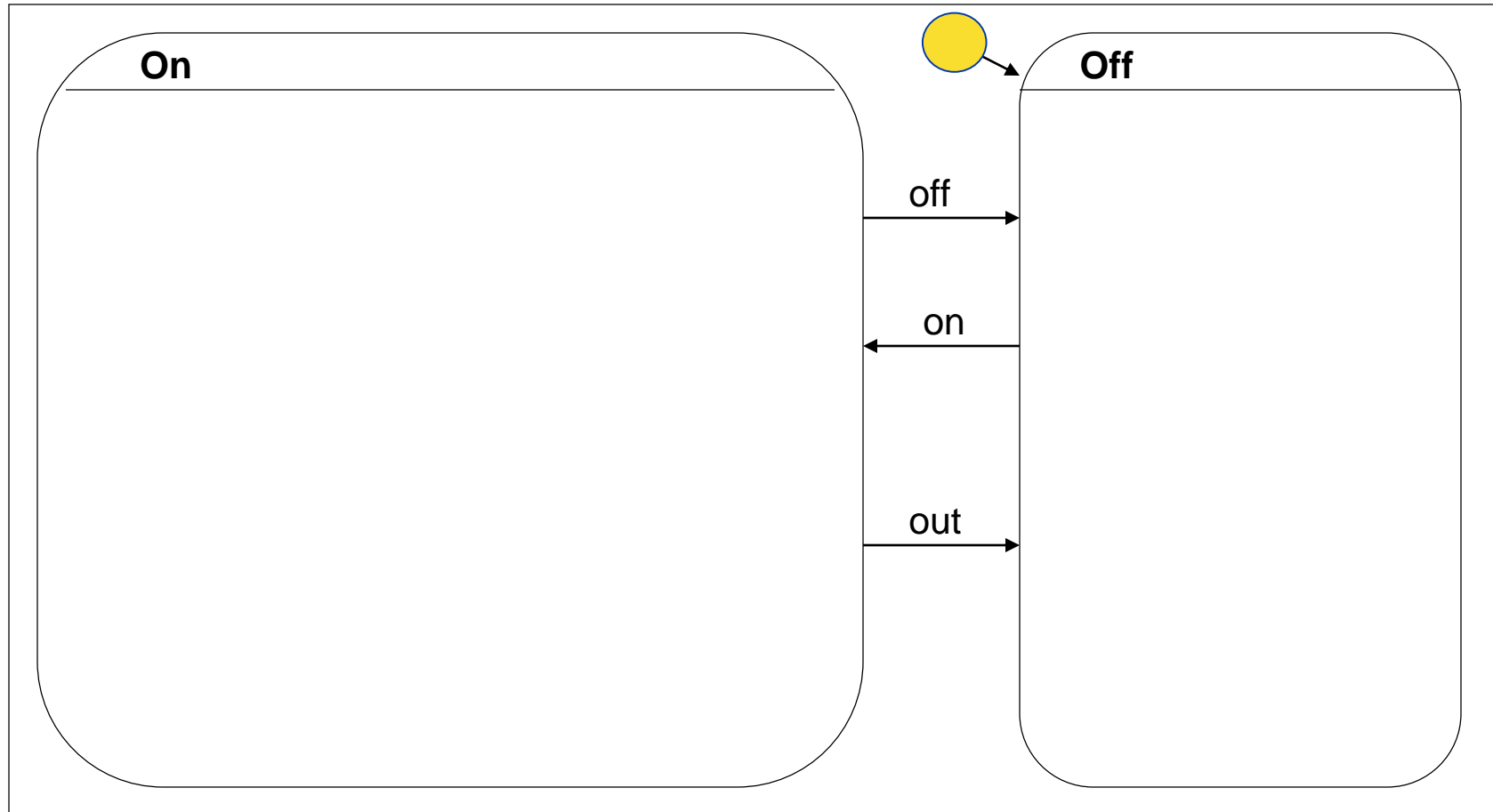
- Source and target can be the same

- trigger [guard] / effect

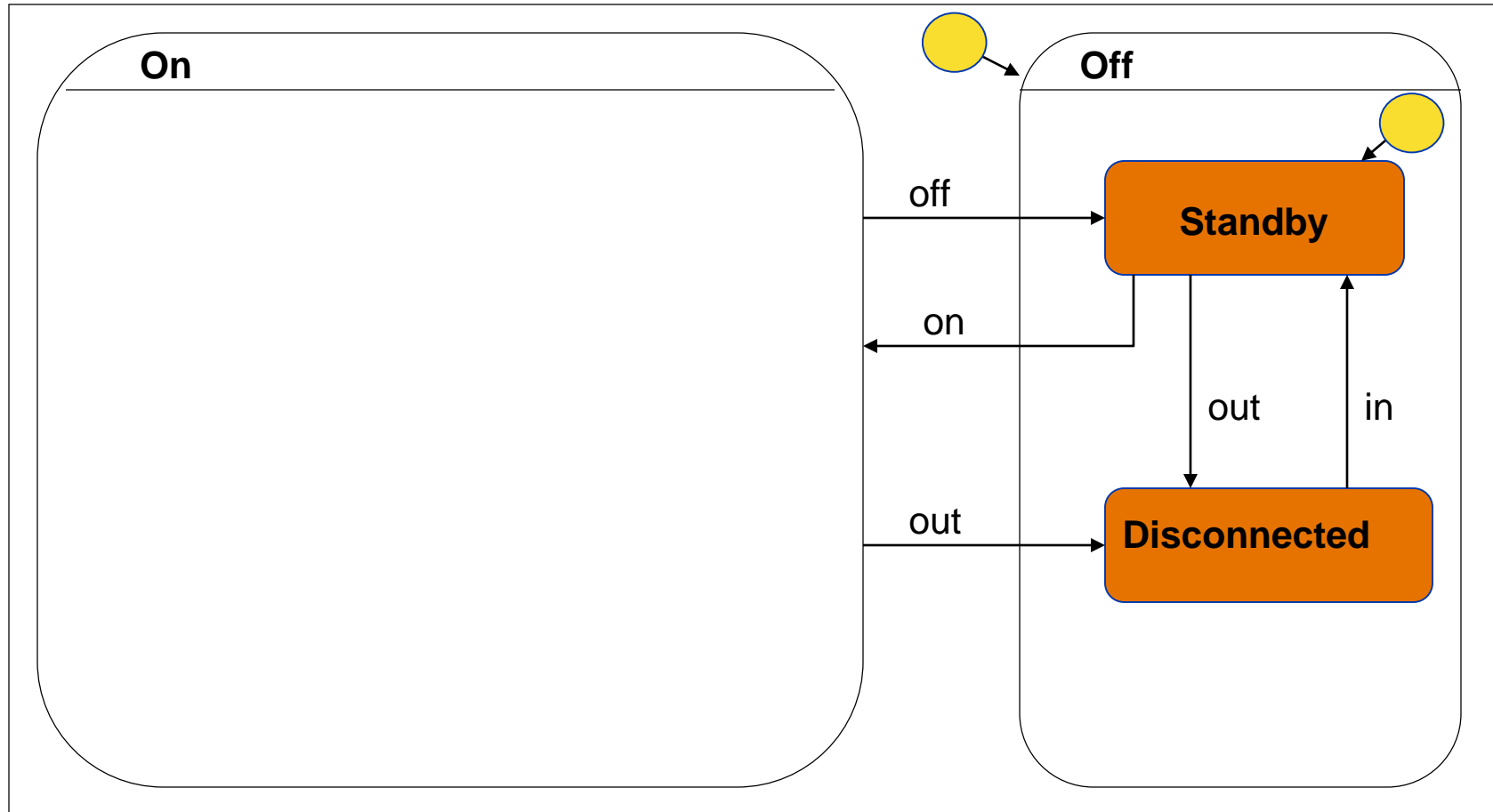
Refinement of States

- **Simple** state
 - Has no substates
- **Composite** state
 - Has at least one **region** (=container for nodes and transitions)
 - **OR-type** (hierarchic) refinement
 - Has 1 region, in it always exactly 1 state is active
 - **AND-type** (parallel) refinement
 - Has multiple orthogonal regions, in **each of them** always exactly 1 state is active
- **Submachine** refinement
 - Embedding a whole state machine

Refinement of States (Example)

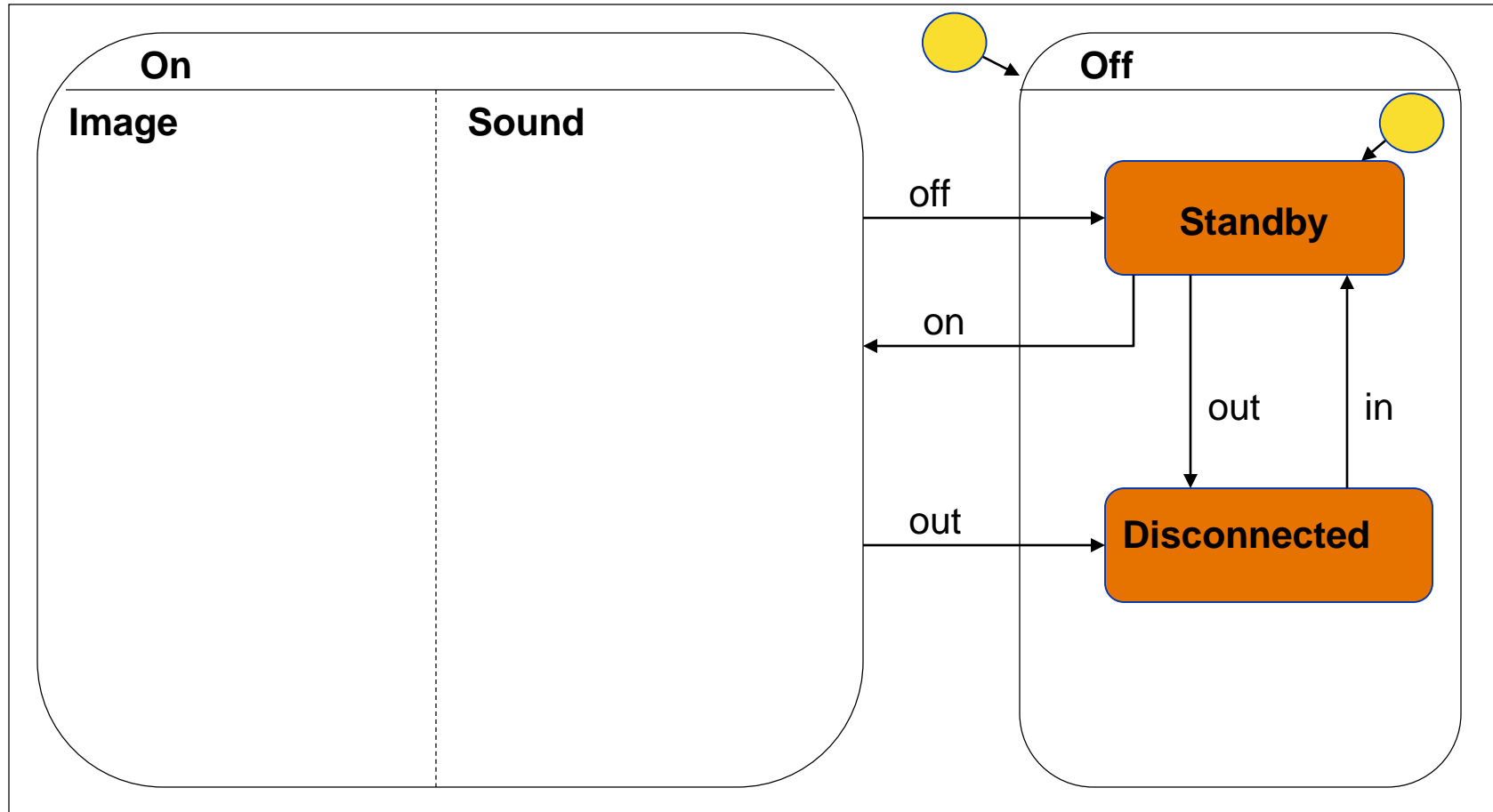


Refinement of States (Example)



OR-refinement

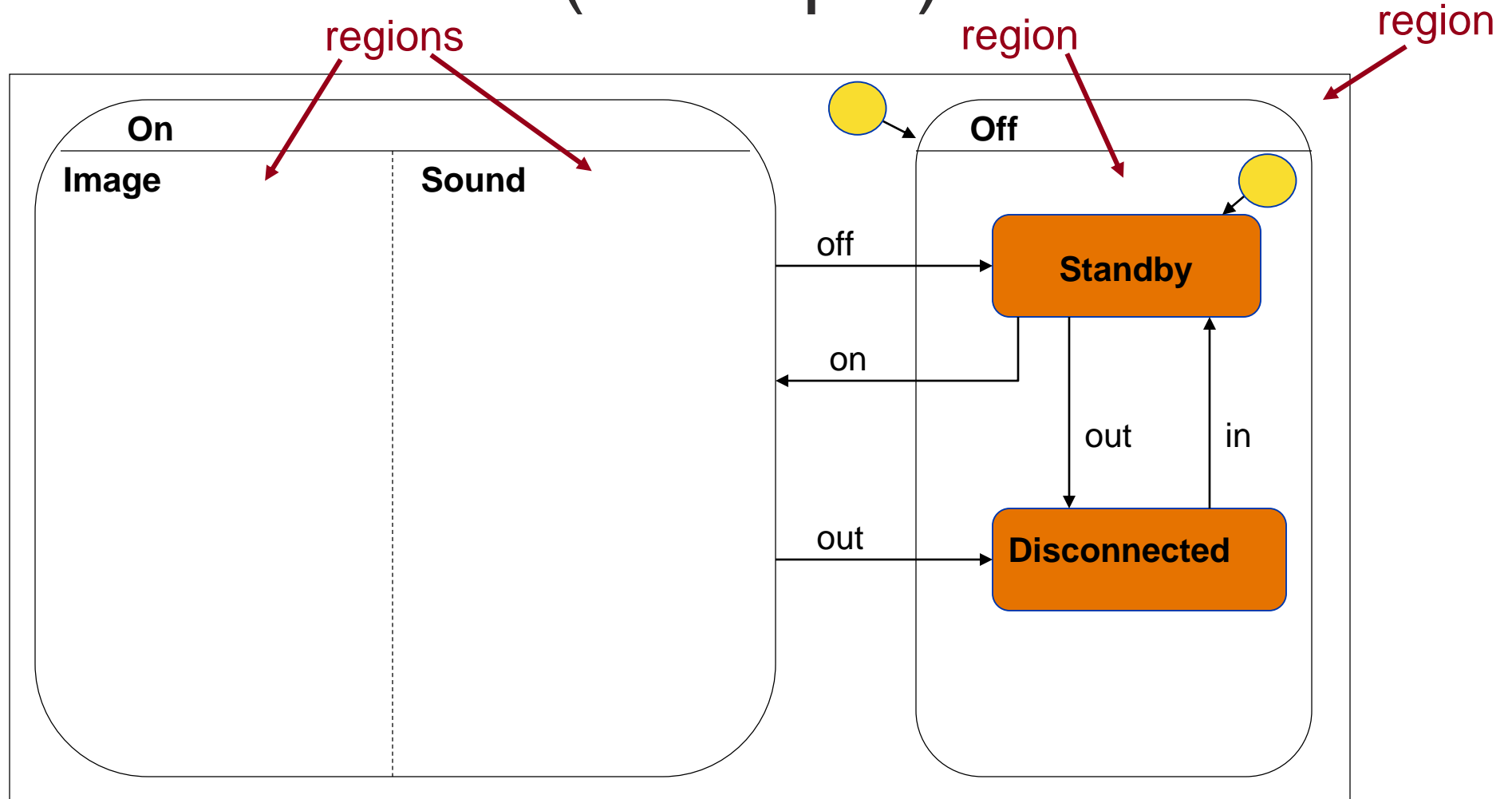
Refinement of States (Example)



AND-refinement

OR-refinement

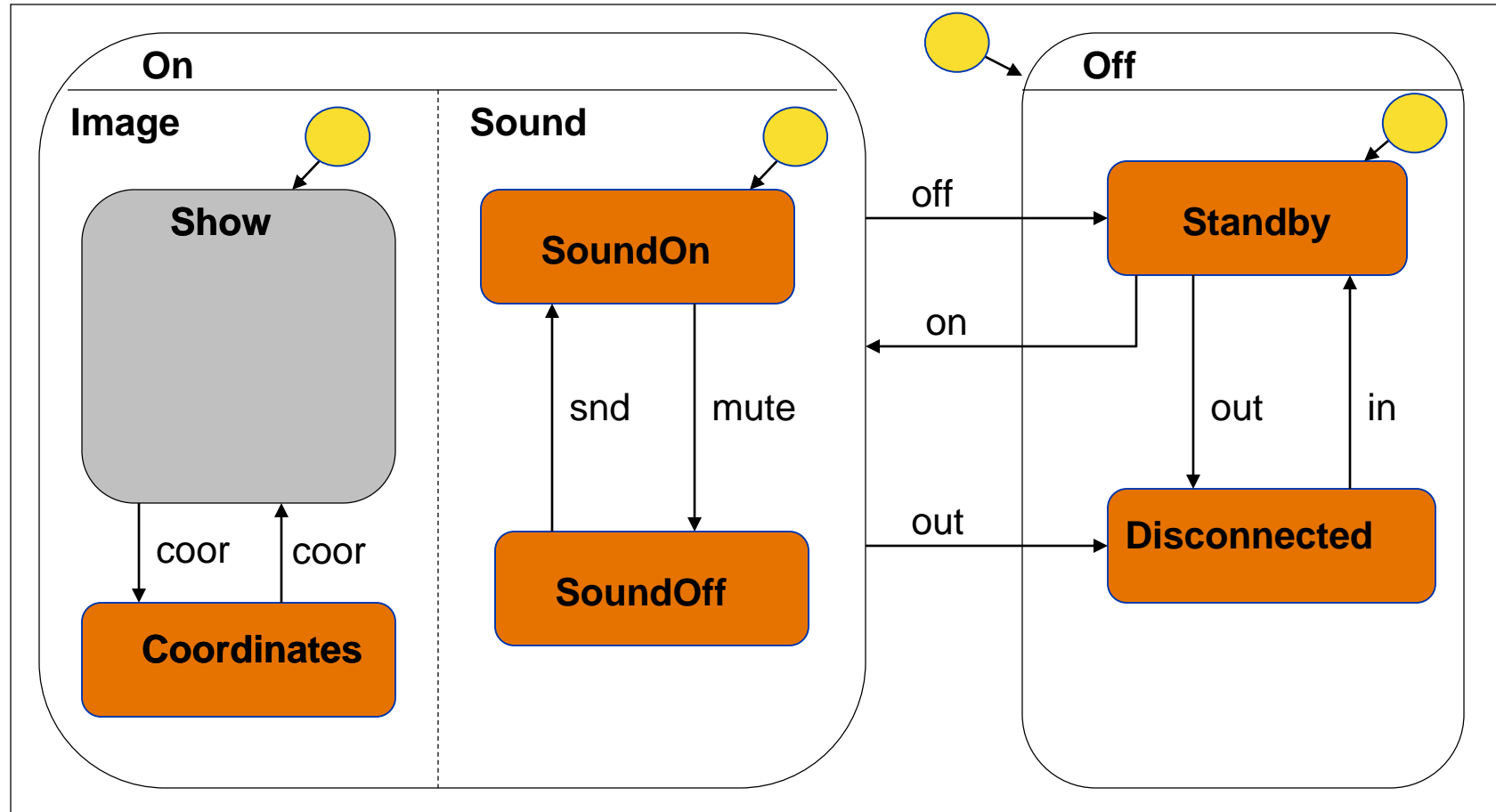
Refinement of States (Example)



AND-refinement

OR-refinement

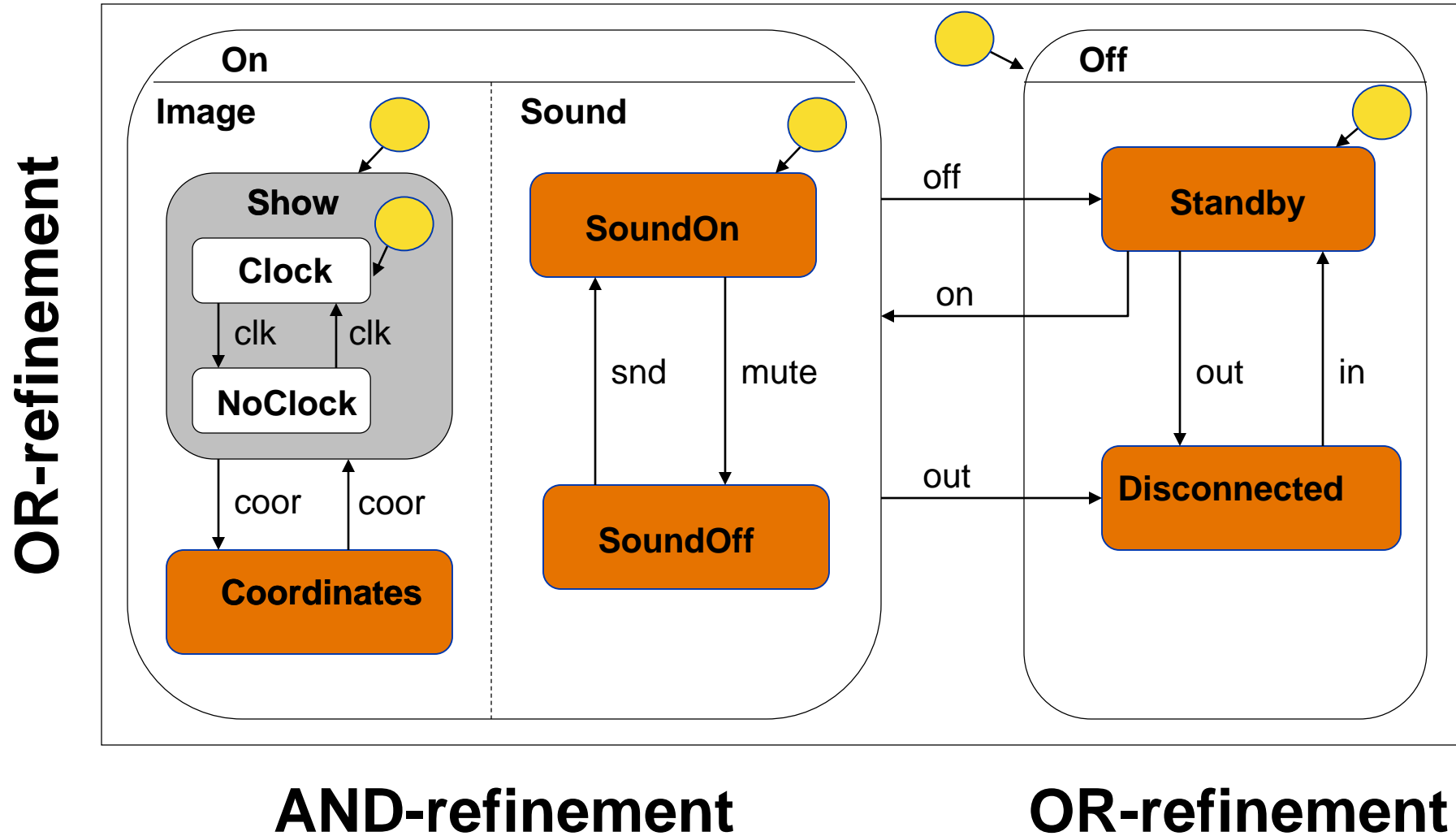
Refinement of States (Example)



AND-refinement

OR-refinement

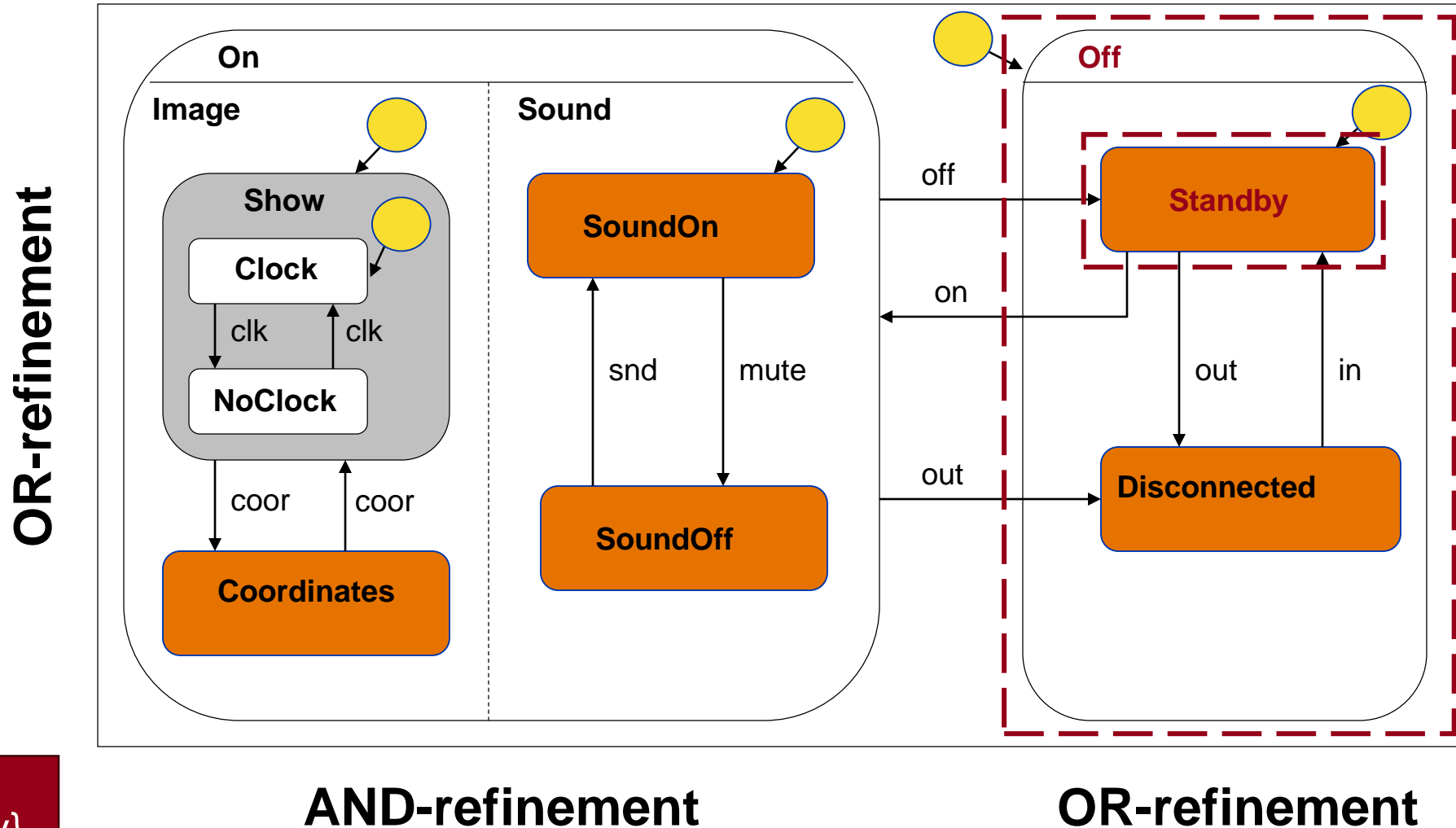
Refinement of States (Example)



States Configuration

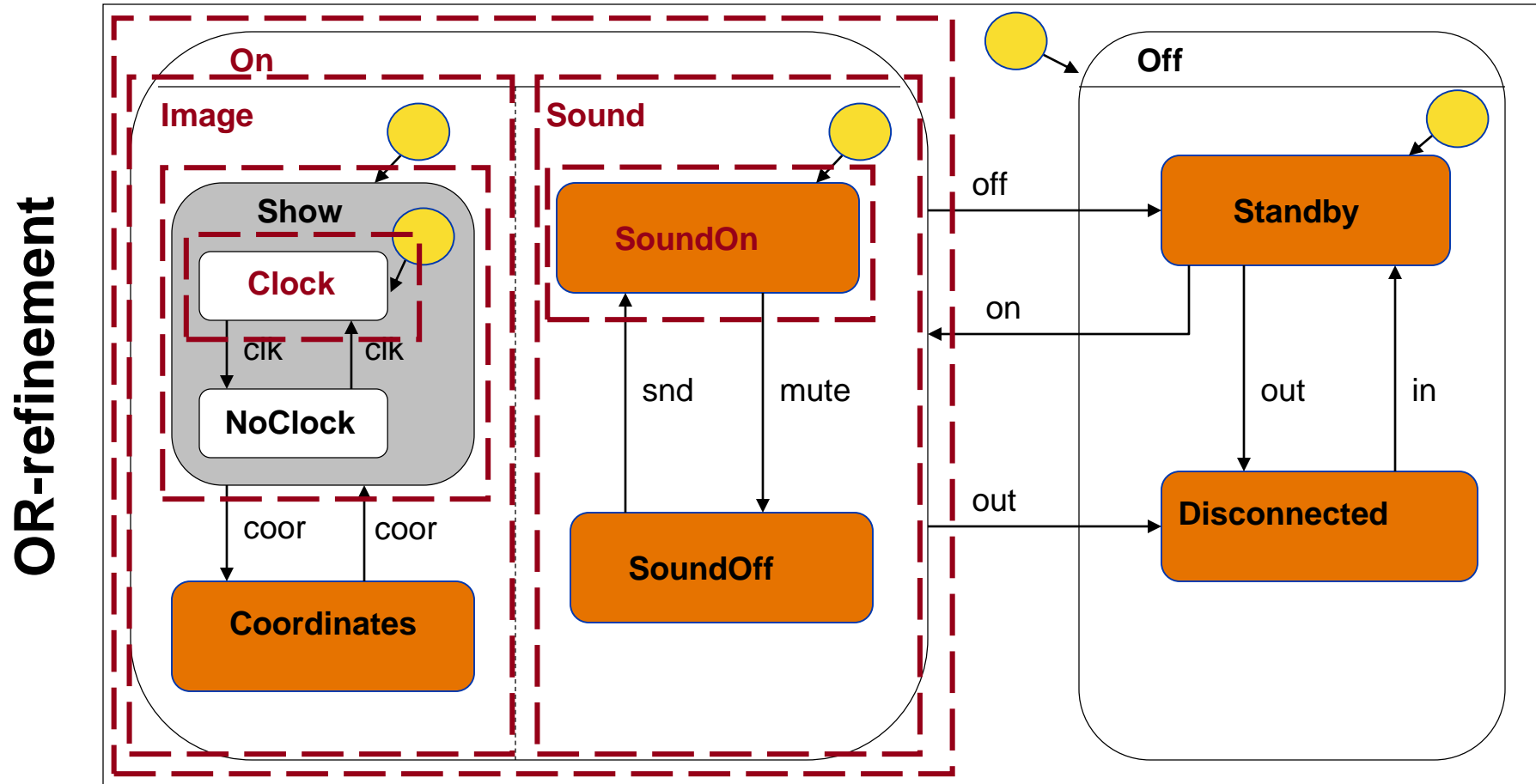
- In composite states: active **state configurations** (instead of active states)
- **Valid configuration:**
 - Top-level state machine has always exactly one active state
 - In each active OR-refined state: always exactly one active (sub)state
 - In each active AND-refined state: always exactly one active (sub)state in each region

Valid State Configuration (Example 1)



{Off, Standby}

Valid State Configuration (Example 2)



{On, SoundOn, Show, Clock}

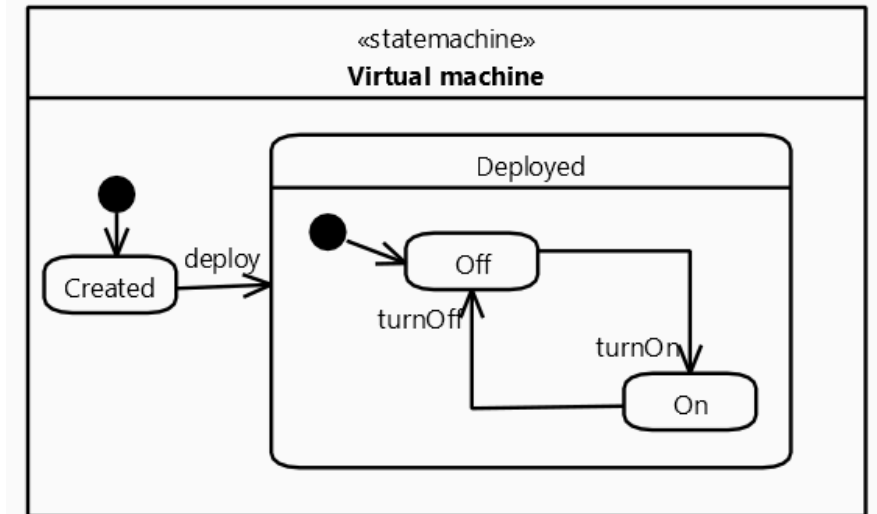
AND-refinement

OR-refinement

Entering a Region

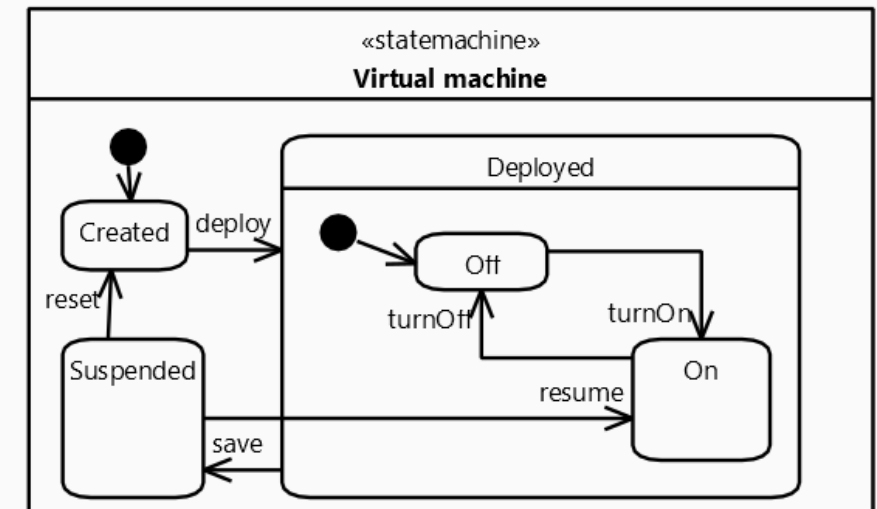
- **Default activation**

- Implicit entering: the target of the transition is the containing state
- The (contained) initial substate will be entered
- Have a initial state in each region!



- **Explicit activation**

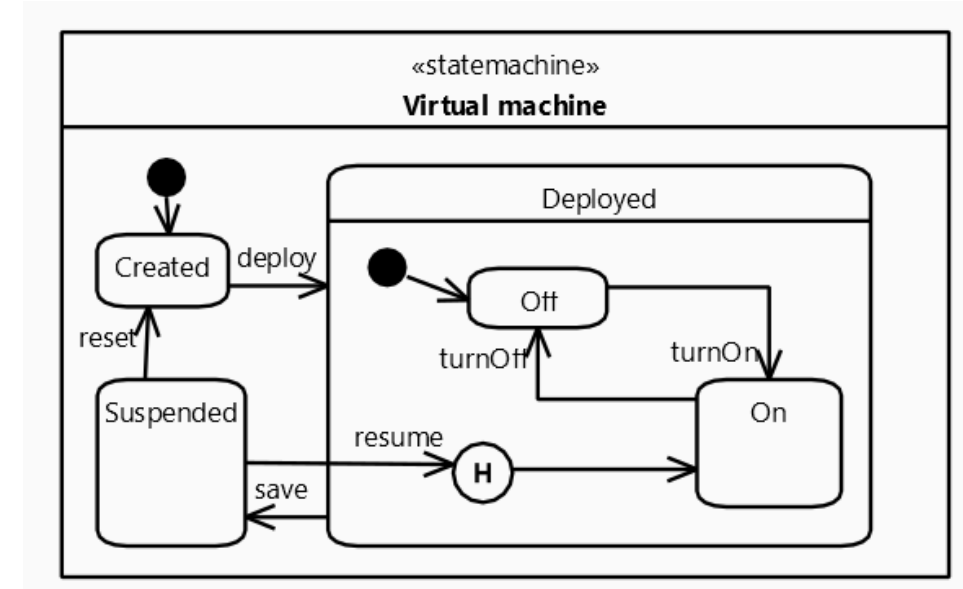
- The target of the transition is a substate
- The active state is directly specified
- Think twice before using it!



Entering a Region (2)

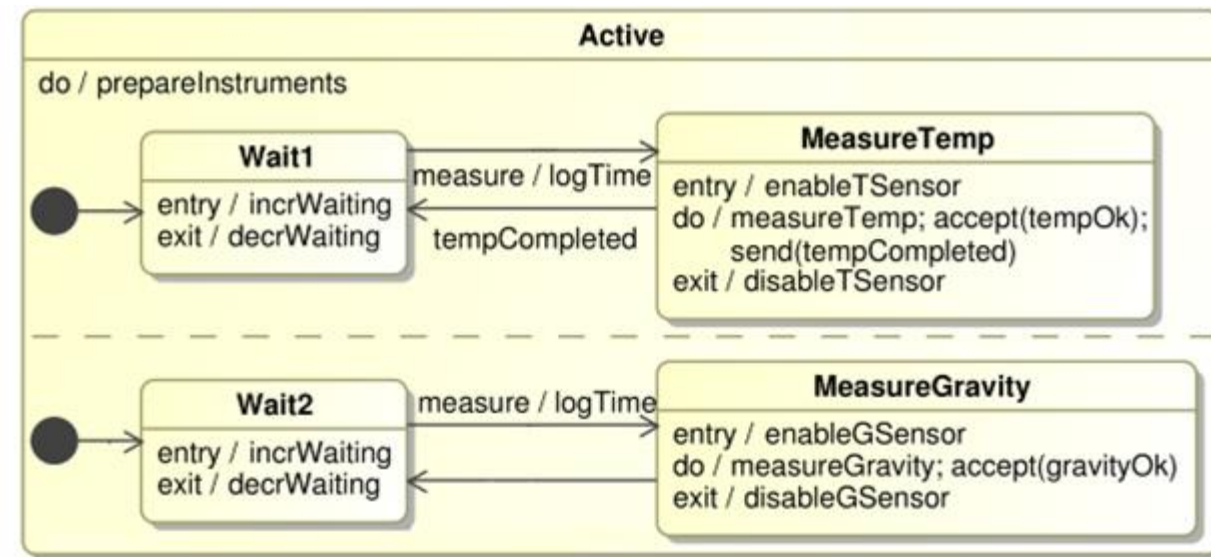
- History

- Remembers, from which substate it was left the last time
- The system can return to that (continue)
- Kinds:
 - Shallow (H): remembers the first level only
 - Deep (H*): remembers the whole hierarchy of states
- Transition from the History (optional):
default, if there was no “last time”, no previous active state

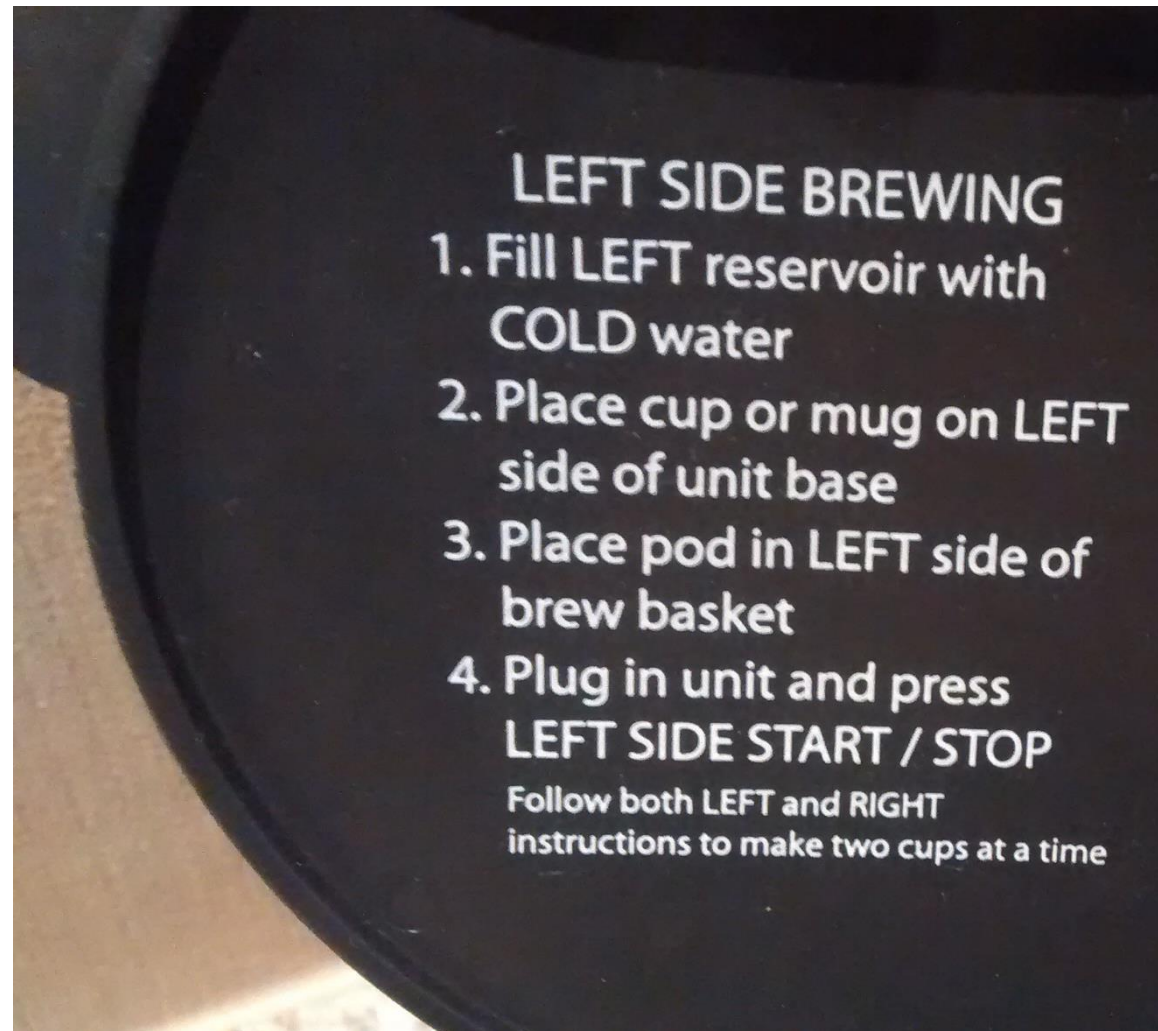


Defining Behaviours Inside the States

- **entry behavior**
 - when entering the state (from outside)
- **exit behavior**
 - when leaving the state
- **doActivity behavior**
 - starts after entering the state
 - Runs until it finishes or until the state is left
 - Parallel to everything else
 - CAUTION: complicated semantics!



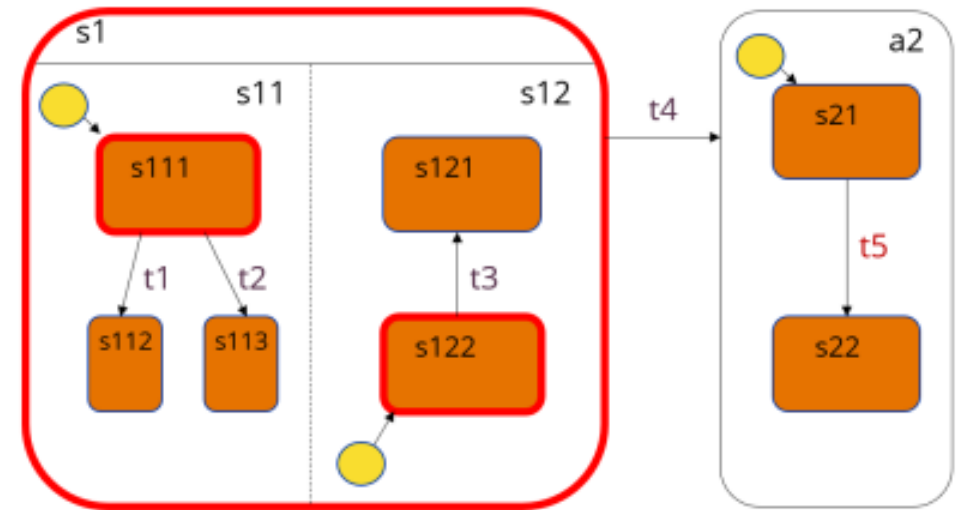
EXERCISE: Coffee Machine



Further Elements (not further specified here)

- **Completion transition:**
 - implicit trigger: Completion event (activity in source state is finished)
- **Deferred events:** event is "put off" for later
- **Transition kinds:** external / local / internal
- **Compound transition:** "chain" of transitions
- **Final state:** given region finishes
- **Further pseudo states:**
 - fork and join, choice and junction
 - entryPoint and exitPoint
 - terminate

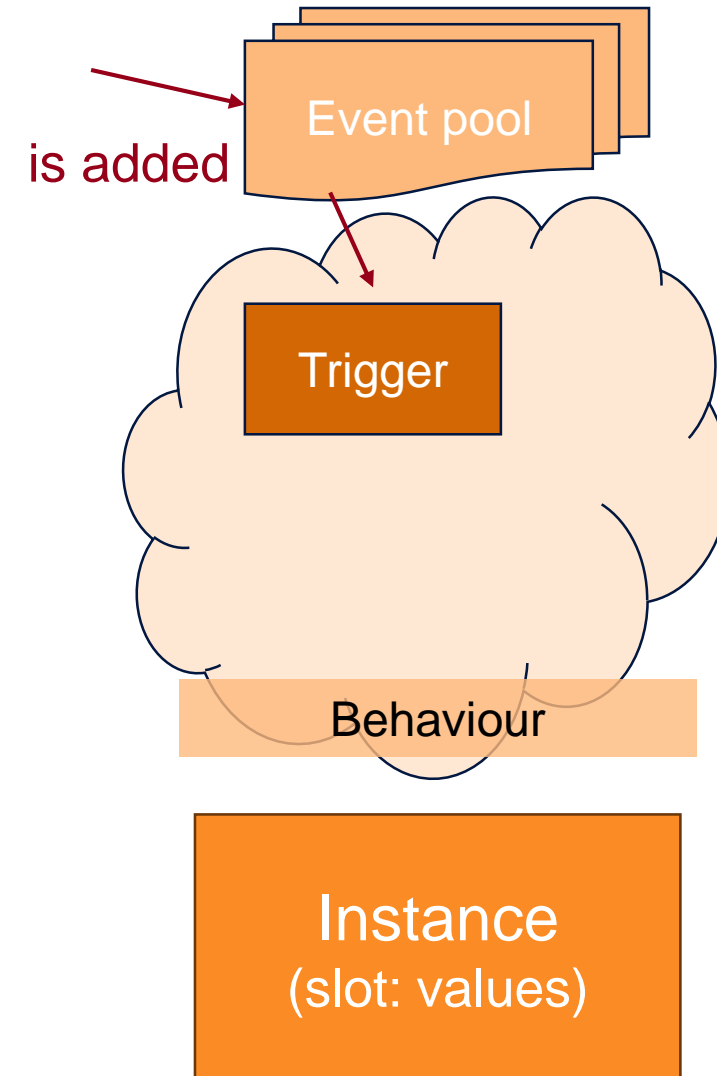
(Simplified) Semantics



Run-to-completion (RTC)

The Execution of State Machines

- Asynchronously arriving event occurrences
 - Added to the **Event pool**
 - Processing not necessarily FIFO
- Cyclical operation of the execution:
 - **Stable state configuration**: waiting
 - **Event processing step**:
 - Dispatch: selection from pool, processing
 - **„run-to-completion” (RTC)**: processing only one event at a time, it cannot take another event before it was completed
 - Reaching a new stable state configuration



Event Processing (1)

1. **Selecting** an event occurrence
2. Collecting the **enabled** transitions
 - Each source of it is active AND it is triggered by the selected event AND its guard condition evaluates to true
3. Depending on the **number** of enabled transitions:
 - If 0: event is dropped, the RTC is completed
 - If 1: that transition is fired (executed)
 - If >1:
 - Identifying the **conflicting** transitions, resolving, choosing from them
 - Conflict: the intersection of the sets of states they would exit is not empty
 - The ones in **different orthogonal** regions may fire in the same step

Event Processing (2)

4. Conflict resolution: based on priorities

- Transition originating from a substate has a higher priority than one originating from its superstate
- It is a partial solution only, it does not resolve all conflicts

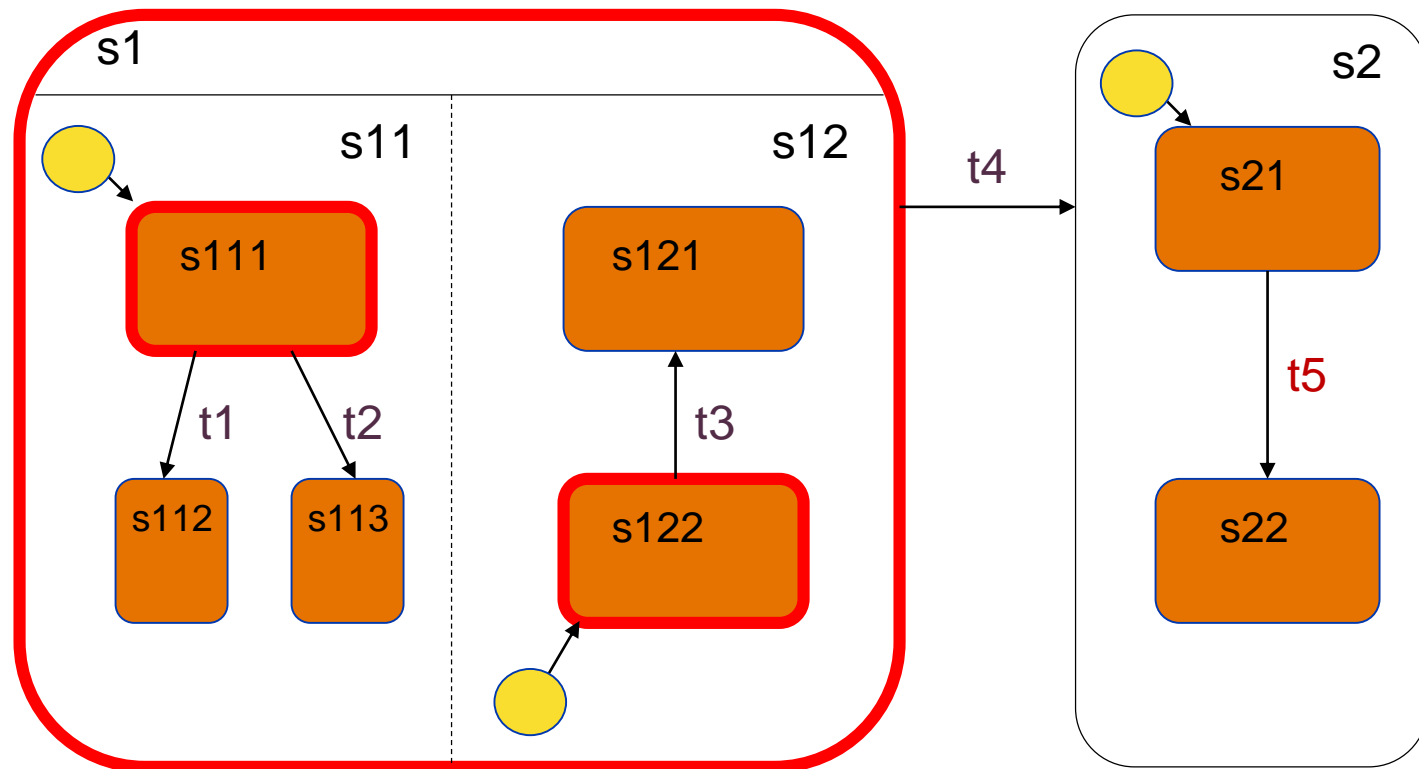
5. Selecting the transitions to be fired

- Conflict-free sets with no higher priority transitions left out
- If there are several such sets, then non-deterministic choice

6. Executing firing

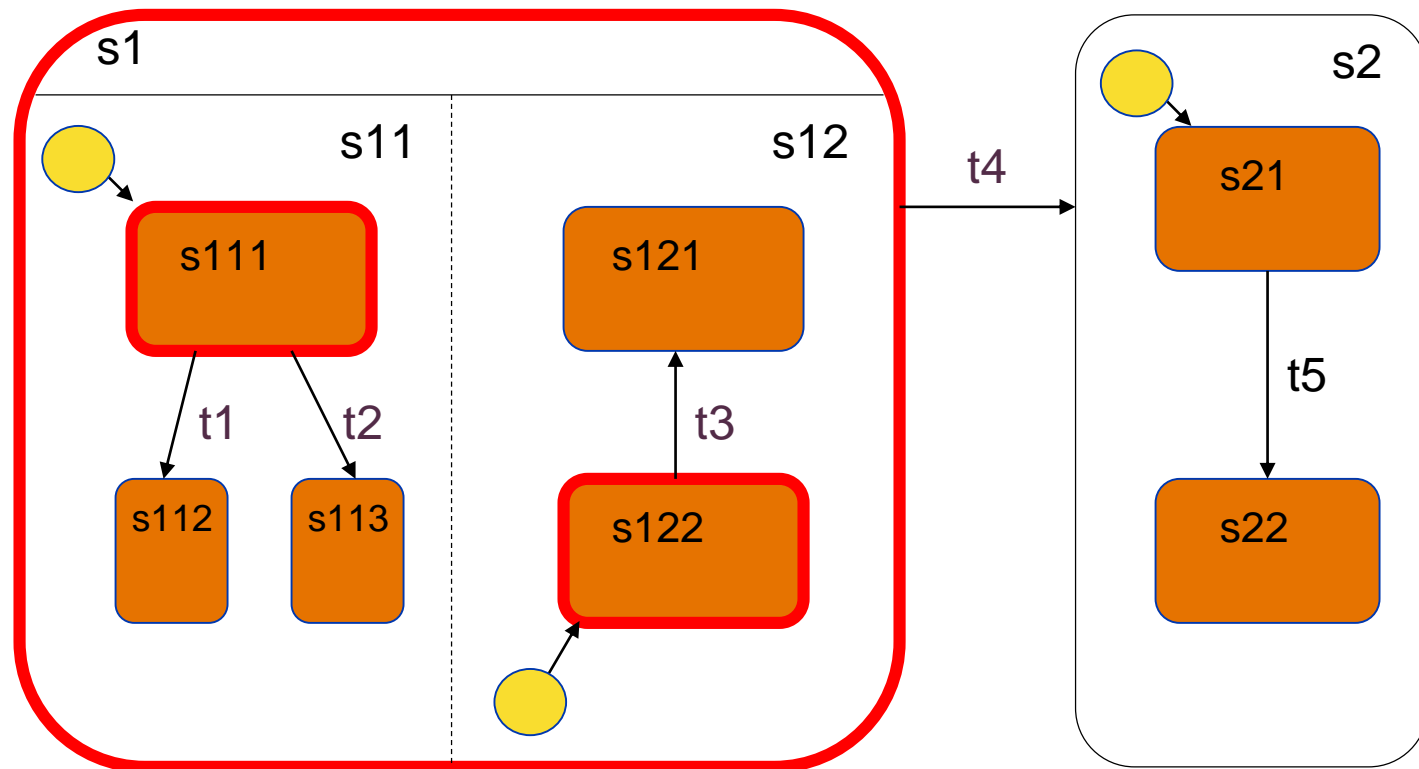
- Exiting the source states, executing the exit behaviours (from inside out)
- Executing the effects of the transition
- Entering the target states, executing the entry behaviours (from outside in)

Enabling, Priority, Selection (Example)



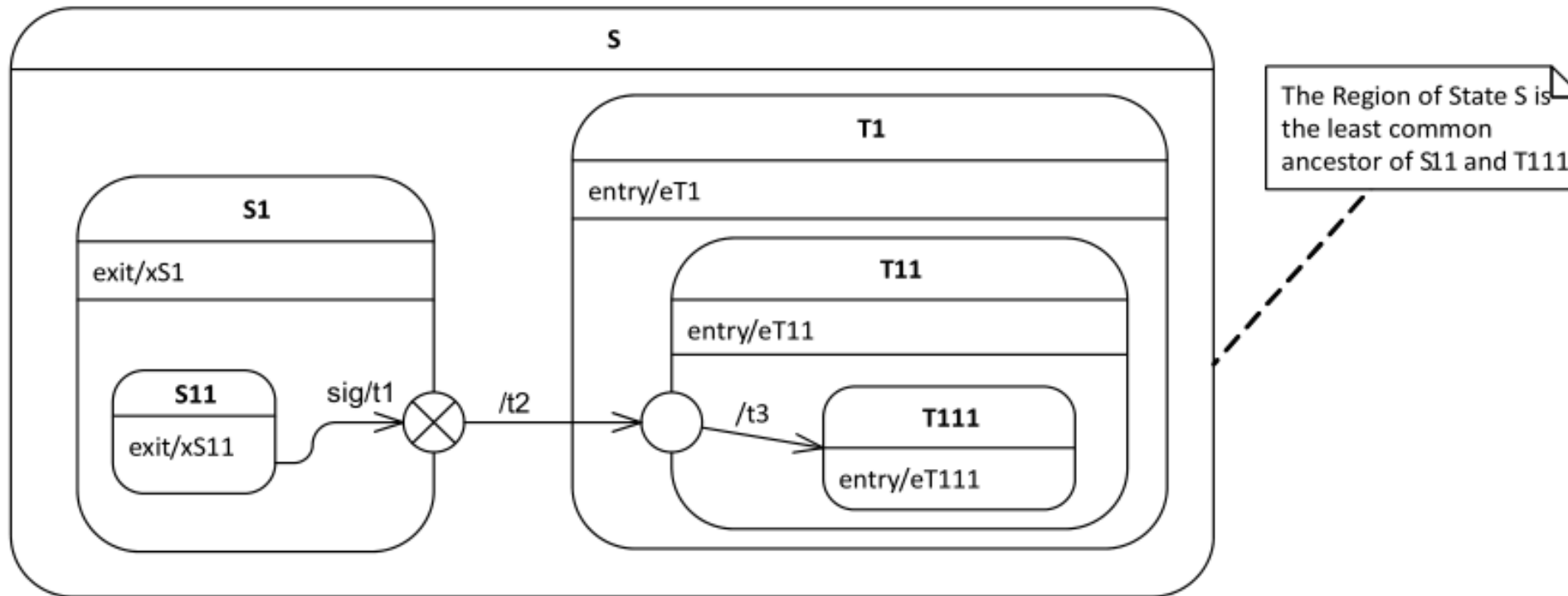
- Each t^* transition is triggered by event e
- State configuration:
 - $\{s1, s111, s122\}$
- e event dispatch
- Enabled transitions:
 - $t1, t2, t3, t4$
- Conflicting one:
 - $\{t1, t2\}; \{t1, t4\}; \{t2, t4\}; \{t3, t4\}$
- Not in conflict:
 - $\{t1, t3\}, \{t2, t3\}$

Enabling, Priority, Selection (Example)






- Priorities:
 - $t1 > t4$, $t2 > t4$, $t3 > t4$
- Fireable sets:
 - $\{t1, t3\}$
 - $\{t2, t3\}$
- One of them will be chosen

Execution of Firing (Example)



- State configuration:
 - {S, S1, S11}
- Event: sig
- Elements of the execution of firing:
 - xS11, t1, xS1, t2, eT1, eT11, t3, eT111

Good Practices

|   | fuel | abort | launch | land |
|---|-------------|--------------|---|-----------------------------|
| Ready | Fueled/- | -/- | -/- | -/- |
| Fueled | -/- | Ready/- | Flying/ ignite engine | -/- |
| Flying | -/- | -/- | -/-  | Landed/ shut down engine |
| Landed | -/- | -/- | -/- | -/- |

Advices to state machines

How to Model with State Machines?

- **Collect** the input events and output actions
- **Start** with simple states
 - What are the different operational modes?
- **Refine gradually** (OR- or AND-refinement)
 - Have an initial state in each region
 - Move the common behaviour to the containing superstate
- **Extend the transitions**
 - Add effects and other behaviours
 - Resolve the initial non-determinisms, if possible
 - Completeness: are there any state+event pairs without specified behaviour?

Completeness and Unambiguity

There is no non-specified behaviour

- **Completeness**

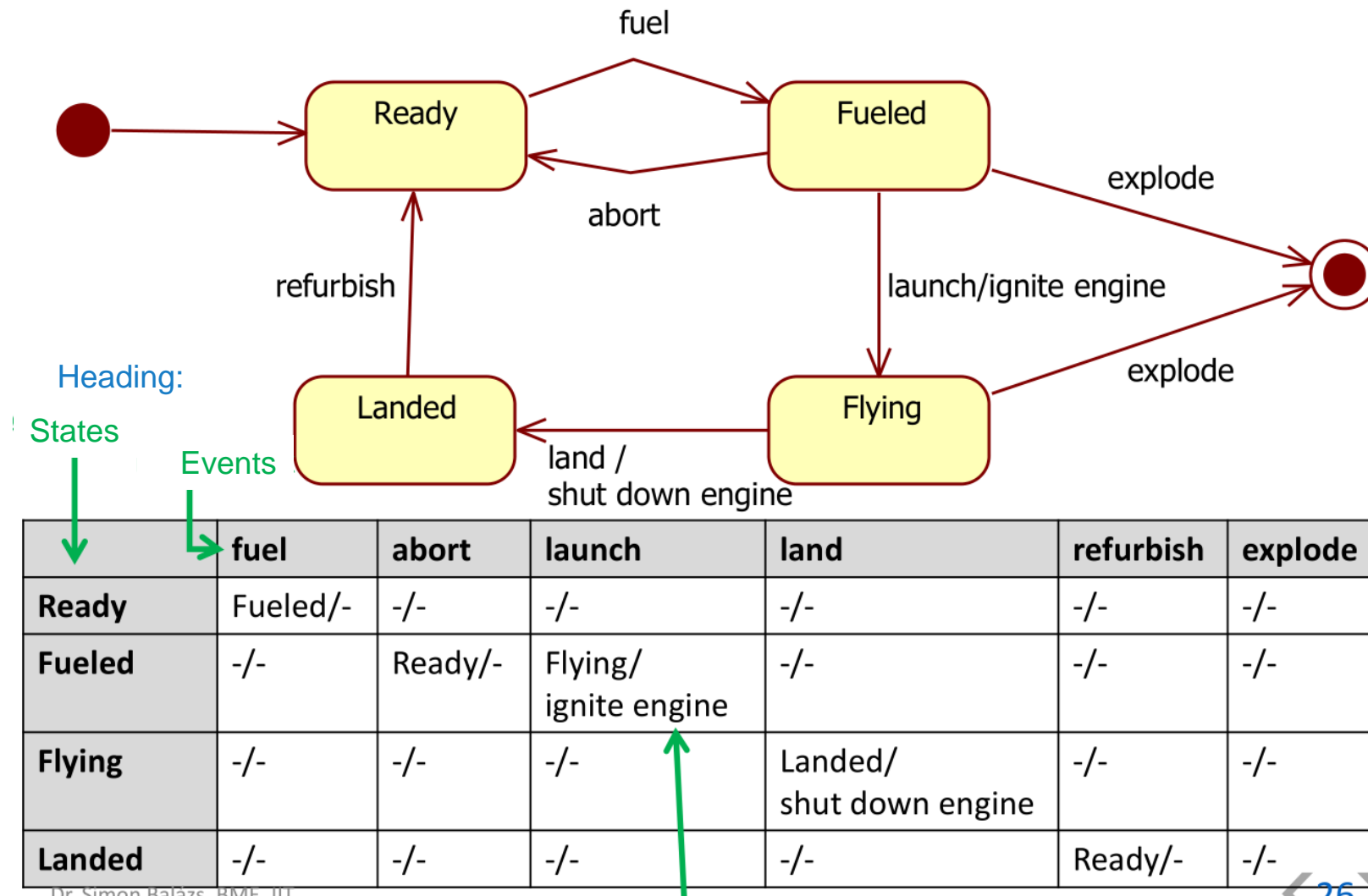
- For each <state configuration, guard evaluation, event> triplet ...
- ... there is **at least 1** behaviour defined

- **Unambiguity**

- For each <state configuration, guard evaluation, event> triplet ...
- ... there is **at most 1** behaviour defined

There is no non-deterministic behaviour

Specifying by State Table



In case of simple states, it helps checking completeness and unambiguity

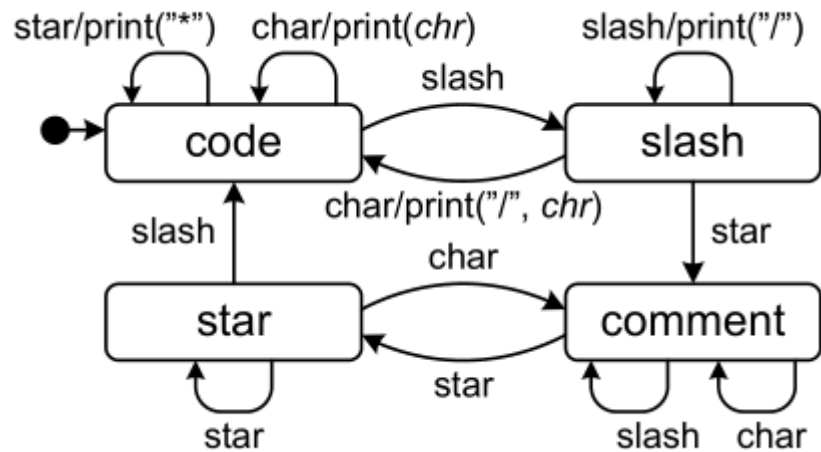
Implementing State Machines

```
public class Something {  
  
    int s = 0;  
  
    public void process(E e) {  
        if (s==0) {  
            if (e == E.N) s = 1;  
        } else if (s==1) {  
            if (e == E.S) s = 2;  
            else if (e == E.M) s = 3;  
        } else if (s==2) {  
            if (e == E.I) s = 0;  
            else if (e == E.F) s = 4;  
        } else if (s==3) {  
            if (e == E.I) s = 0;  
        }  
    }  
}
```

Implementing State Machines

- Patterns depending on the target programming language
 - Embedded code: no hierarchy, simple control, limited storage capacity
 - High-level languages: even on OO basis
- Typical patterns:
 - Mapping a simple state machine to an embedded switch
 - State table: two-dimensional array (states x events)
 - “State” design pattern
- It may be worth **generating the code!**

Example: Nested Switch Patterns

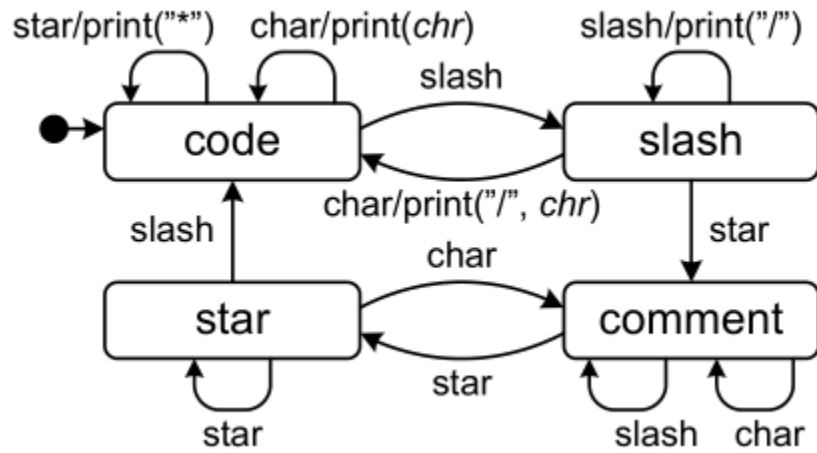


Source: Pintér Gergely. *Model based program synthesis and runtime error detection for dependable embedded systems*. [PhD thesis](#), 2007.

```
1 void
2 nested_switch_implementation(const char* input) {
3
4     const char *input_ptr;
5     state_t state = S_CODE;
6
7     for (input_ptr = input; *input_ptr != '\0'; input_ptr += 1) {
8         trigger_t trigger = translate_trigger(*input_ptr);
9
10        switch (state) {
11            case S_CODE:
12                switch (trigger) {
13                    case T_STAR: /* Output the character. */
14                        case T_CHAR:
15                            printf("%c", *input_ptr);
16                            break;
17
18                    case T_SLASH: /* Transition to state 'SLASH'. */
19                        state = S_SLASH;
20                        break;
21                }
22                break;
23
24            case S_SLASH:
25                switch (trigger) {
26                    case T_STAR: /* Transition to state 'COMMENT'. */
27                        state = S_COMMENT;
28                        break;
29
30                    case T_SLASH: /* Output a slash character. */
31                        printf("/");
32                        break;
33
34                    case T_CHAR: /* Output and transition to state 'CODE'. */
35                        printf("/%c", *input_ptr);
36                        state = S_CODE;
37                        break;
38                }
39                break;
40        }
41    }
```

Listing B.2: Implementation by the Nested Switch Pattern

Example: State Table Patterns



Source: Pintér Gergely. *Model based program synthesis and runtime error detection for dependable embedded systems*. [PhD thesis](#), 2007.

```
1  /** Pointer to activity function type. */
2  typedef void (*activity_t)(const char input_char);
3
4  /** Type of a cell in a state table. */
5  typedef struct {
6      state_t next_state;          /* The next state to be stepped to. */
7      activity_t activity;         /* The activity to be preformed. */
8  } cell_t;
9
10 void
11 state_table_implementation(const char* input) {
12
13     const char *input_ptr;
14     state_t state = S_CODE;
15
16     const cell_t table[NUM_STATE][NUM_TRIGGER] = {
17         /* State 'CODE' (triggers: star, slash, char) */
18         {{S_CODE, act_out_chr}, {S_SLASH, NULL}, {S_CODE, act_out_chr}},
19         /* State 'SLASH' (triggers: star, slash, char) */
20         {{S_COMMENT, NULL}, {S_SLASH, act_out_slash}, {S_CODE, act_out_slash_chr}},
21         /* State 'COMMENT' (triggers: star, slash, char) */
22         {{S_STAR, NULL}, {S_COMMENT, NULL}, {S_COMMENT, NULL}},
23         /* State 'STAR' (triggers: star, slash, char) */
24         {{S_STAR, NULL}, {S_CODE, NULL}, {S_COMMENT, NULL}}
25     };
26
27     for (input_ptr = input; *input_ptr != '\0'; input_ptr += 1) {
28         const cell_t *cell;
29         trigger_t trigger = translate_trigger(*input_ptr);
30
31         cell = &(table[state][trigger]);
32         if (NULL != cell -> activity)
33             (cell -> activity)(*input_ptr);
34
35         state = cell -> next_state;
36     }
37 }
```

Listing B.3: Implementation by the State Table Pattern

Summary

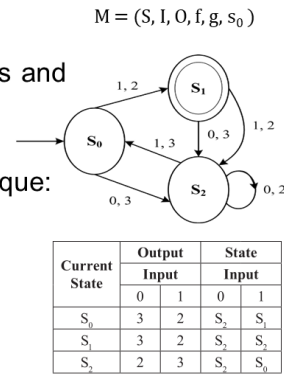
Summary

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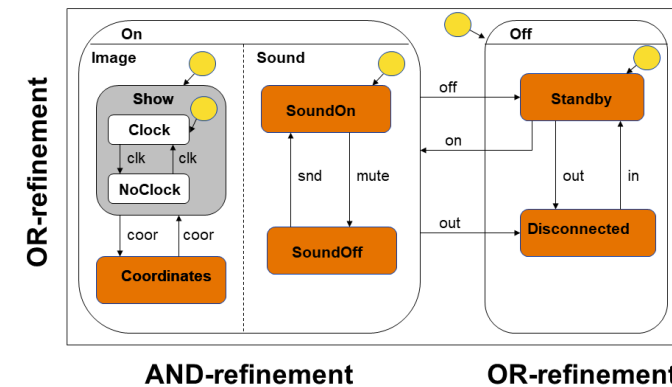
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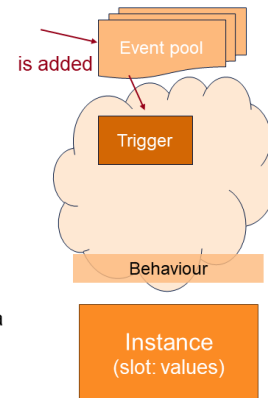
Refinement of States (Example)



Software Engineering (VIMIAB04)

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