Type 4: Run-time greedy  $B_{S,t}$ ,  $K_t$  with  $x_t$ 

