Type 4: Run-time greedy $B_{S,t}$, K_t with x_t

