

Lab 1

Exercise 1:

Find two positive numbers whose sum is 300 and whose product is a maximum.

Solution:

$$Y = 300 - x$$

$$P(X) = X(300 - X) = 300X - X^2$$

Take the derivative of $P(X)$ with respect to X and set it equal to 0.

$$P'(X) = 300 - 2X = 0$$

$$X = 150$$

the two positive numbers whose sum is 300 and whose product is a maximum are:

$$x = 150 \text{ and } y = 300 - x = 150$$

So the two numbers are 150 and 150.

Exercise 2:

Let x and y be two positive numbers such that $x + 2y = 50$ and $(x + 1)(y + 2)$ is a maximum.

Solution:

$$x = 50 - 2y$$

$(x + 1)(y + 2)$ in terms of y

$$(x + 1)(y + 2) = (50 - 2y + 1)(y + 2) = (-2y^2 + 46y + 102)$$

take the derivative of this expression with respect to y and set it equal to 0.

$$(-4y + 46) = 0$$

$$y = 11.5$$

use the expression for x in terms of y to find x .

$$x = 50 - 2y = 27$$

the two positive numbers that satisfy the given conditions are:

$$x = 27 \text{ and } y = 11.5$$

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